

PyCSP v1.0



Software documentation

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1 Introduction

PyCSP is a collection of libraries for the analysis, model reduction and ODE integration of reacting systems using the computational singular perturbation (CSP) method and its extensions, including the Tangential Stretching Rate.

1.1 Copyright

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1.2 Contacts

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1.3 Folder structure

2.1 Prerequisites

PyCSP relies on Cantera 2.4.0, numpy and matplotlib. The current version of PyCSP has been tested with Python 3.6.10. The Python version must comply with Cantera. Presently, versions higher than 3.6.10 are not supported by Cantera 2.4.0. In February 2021, Cantera's authors released thier version 2.5.0. PyCSP compliance with such version will be part of a future release.

2.2 Installation

Installation using Anaconda is recommended. In such case, proceed as follows via command line:

```
$ git clone https://github.com/rmalpica/PyCSP.git
$ cd $PATH_TO_PyCSP_MAIN_FOLDER
$ conda create --name py36 python=3.6 anaconda --file requirements.txt --channel
default --channel anaconda --channel cantera
$ conda activate py36
$ pip install $PATH_TO_PyCSP_MAIN_FOLDER (e.g. /Users/rmalpica/PyCSP)
```

Alternatively, once the prerequisite libraries are installed, the installation may be performed via command line as follows:

```
$ git clone https://github.com/rmalpica/PyCSP.git
$ pip install $PATH_TO_PyCSP_MAIN_FOLDER (e.g. /Users/rmalpica/PyCSP)
```

2.3 Testing

To test the installation, proceed as follows via command line:

```
$ cd tests
$ python test_kernel.py
```

The test should outcome two images: first, the time evolution of temperature, OH, H and H₂ in a constant pressure reactor run with Cantera, second, the time evolution of the system's eigenvalues.

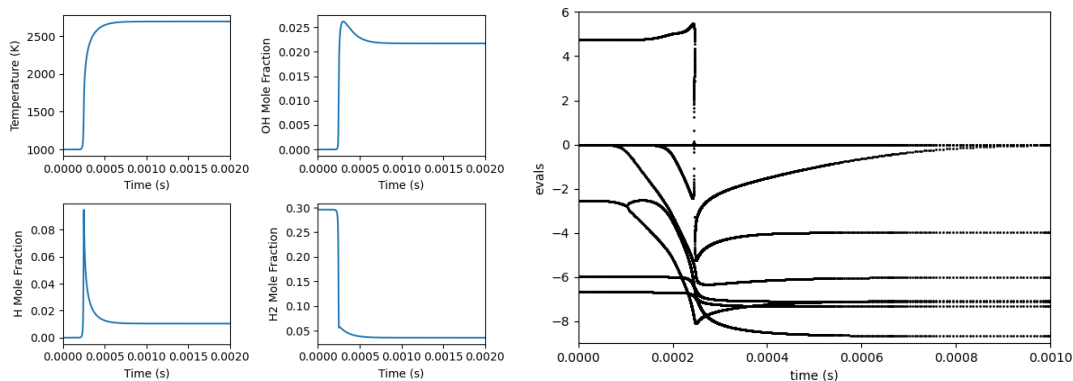


Figure 1: Testing outcomes

3 Classes, attributes and methods

3.1 ThermoKinetics.py

3.1.1 class CanteraThermoKinetics

This class inherits attributes and methods from Cantera's `Solution` class and extends its capabilities by adding thermodynamics and kinetics-related class methods. Hence, the constructor for this class is equivalent to the constructor of Cantera's `Solution` class. The proper way to instantiate `CanteraThermoKinetics` objects is by using species and reactions defined in an input file, e.g. `hydrogen.cti`:

```
1 import PyCSP.ThermoKinetics as csp
2 gas = csp.CanteraThermoKinetics('hydrogen.cti')
```

Different formulations exist for the majority of this class methods depending on whether the reactor is considered having a constant pressure or a constant volume (density). Hence, it is mandatory to choose between constant pressure and constant density after instantiating an object of the `CanteraThermoKinetics` class and before accessing its attributes. The choice is made by defining either the pressure value or the density value through the attributes `constP` or `constRho` (see below). A lack of this choice will raise an exception when accessing the class attributes having multiple formulations.

Instance attributes:

- `constP`
Type (*float*).
Set/get the thermodynamic pressure [Pa] and activates the constant pressure version of all the class methods (`problemtype == const_p`).

- **constRho**
Type (*float*).
Set/get the thermodynamic density [Kg/m³] and activates the constant volume version of all the class methods (`problemtype == const_v`).
- **problemtype**
Type (*string, read-only*).
Get the active definition of `problemtype`, either `const_p` or `const_v`.
- **nv**
Type (*int*).
Set/get the number of variables. Defaults to `n_species + 1`. The only alternative value is `n_species`, e.g., to exclude temperature from the list of variables and get appropriately sized objects from the class methods.
- **source**
Type (*[N_s+1] array of float, read-only*).
Get the chemical source term [$\dot{\omega}_1, \dot{\omega}_2, \dots, \dot{\omega}_{N_s}, \dot{\omega}_T$] for the species mass fractions and temperature, based on either the constant pressure or constant volume formulation. Depending on the value of `nv`, the last component (temperature source term) is returned or not.
- **jacobian**
Type (*[N_s+1 × N_s+1] array of float, read-only*).
Get the numerical Jacobian of the chemical source term, based on either the constant pressure or constant volume formulation.
- **generalized_Stoich_matrix**
Type (*[N_v × 2N_r] array of float, read-only*).
Get the generalized stoichiometric matrix, based on either the constant pressure or constant volume formulation. Depending on the value of `nv`, the last row (temperature coefficients) is returned or not.
- **R_vector**
Type (*[2N_r] array of float, read-only*).
Get the reaction rates vector.

Class methods:

- **set_stateYT(state)**.
Set the thermochemical state of the mixture. This is an alternative to separately setting Cantera's attributes `Y` and either `TP` or `TD`. Pressure and density are automatically set based on the values of `constP` or `constRho`.
Input:
 state (array of float). Array containing the mass fractions Y_i of all the species and the temperature: [Y_1, Y_2, \dots, Y_N, T]. The order of the Y_i values must comply with the species ordering set at the class instantiation. This can be retrieved with the method `species()`.
- **stateYT()**.
Returns the thermochemical state of the mixture [Y_1, Y_2, \dots, Y_N, T].
- **rhs_const_p()**.
Returns the constant-pressure chemical source term of the mixture [$\dot{\omega}_1, \dot{\omega}_2, \dots, \dot{\omega}_{N_s}, \dot{\omega}_T$]_P, where:

$$\dot{\omega}_i = \frac{W_i}{\rho} \sum_{k=1}^{2N_r} \nu_{ik} r^k \quad i = 1, \dots, N_s$$

$$\dot{\omega}_T = -\frac{1}{c_p} \sum_{i=1}^{N_s} \dot{\omega}_i h_i$$

where W_i is the molecular mass of species i , ρ is the mixture density, ν_{ik} is the molar stoichiometric coefficient of species i in reaction k , r^k is the molar rate of progress of reaction k , c_p is the mixture constant pressure specific heat and h_i is the molar enthalpy of species i .

- **rhs_const_v()**.

Returns the constant-volume chemical source term of the mixture $[\dot{\omega}_1, \dot{\omega}_2, \dots, \dot{\omega}_{N_s}, \dot{\omega}_T]_v$, where:

$$\dot{\omega}_i = \frac{W_i}{\rho} \sum_{k=1}^{2N_r} \nu_{ik} r^k \quad i = 1, \dots, N_s$$

$$\dot{\omega}_T = -\frac{1}{c_v} \sum_{i=1}^{N_s} \dot{\omega}_i h_i + \frac{RT}{c_v} \sum_{i=1}^{N_s} \dot{\omega}_i$$

- **generalized_Stoich_matrix_const_p()**.

Returns the constant-pressure generalized stoichiometric matrix \mathcal{S} , defined as:

$$\mathcal{S}_{i,k} = \frac{W_i}{\rho} \nu_{ik} \quad i = 1, \dots, N_s \quad k = 1, \dots, 2N_r$$

$$\mathcal{S}_{N_s+1,k} = -\frac{1}{\rho c_p} \sum_{i=1}^{N_s} W_i \nu_{ik} h_i \quad k = 1, \dots, 2N_r$$

- **generalized_Stoich_matrix_const_v()**.

Returns the constant-volume generalized stoichiometric matrix \mathcal{S} , defined as:

$$\mathcal{S}_{i,k} = \frac{W_i}{\rho} \nu_{ik} \quad i = 1, \dots, N_s \quad k = 1, \dots, 2N_r$$

$$\mathcal{S}_{N_s+1,k} = -\frac{1}{\rho c_v} \sum_{i=1}^{N_s} W_i \nu_{ik} h_i + \frac{RT}{\rho c_v} \sum_{i=1}^{N_s} W_i \nu_{ik} \quad k = 1, \dots, 2N_r$$

- **Rates_vector()**.

Returns the molar rates of progress r^k vector of the mixture.

- **jacobian_const_p()**.

Returns the constant-pressure numerically-evaluated Jacobian of the chemical source term of the mixture:

$$J_{\dot{\omega}} = \begin{bmatrix} \left. \frac{\partial \dot{\omega}_1}{\partial Y_1} \right|_P & \left. \frac{\partial \dot{\omega}_1}{\partial Y_2} \right|_P & \cdots & \left. \frac{\partial \dot{\omega}_1}{\partial Y_{N_s}} \right|_P & \left. \frac{\partial \dot{\omega}_1}{\partial T} \right|_P \\ \vdots & \ddots & & & \\ \vdots & & \ddots & & \\ \vdots & & & \ddots & \\ \left. \frac{\partial \dot{\omega}_{N_s}}{\partial Y_1} \right|_P & & & & \\ \left. \frac{\partial \dot{\omega}_T}{\partial Y_1} \right|_P & \cdots & \cdots & \cdots & \left. \frac{\partial \dot{\omega}_T}{\partial T} \right|_P \end{bmatrix}$$

- **jacobian_const_v()**.

Returns the constant-volume numerically-evaluated Jacobian of the chemical source term of the mixture:

$$J_{\dot{\omega}} = \begin{bmatrix} \left. \frac{\partial \dot{\omega}_1}{\partial Y_1} \right|_v & \left. \frac{\partial \dot{\omega}_1}{\partial Y_2} \right|_v & \cdots & \left. \frac{\partial \dot{\omega}_1}{\partial Y_{N_s}} \right|_v & \left. \frac{\partial \dot{\omega}_1}{\partial T} \right|_v \\ \vdots & \ddots & & & \\ \vdots & & \ddots & & \\ \vdots & & & \ddots & \\ \left. \frac{\partial \dot{\omega}_{N_s}}{\partial Y_1} \right|_v & & & & \\ \left. \frac{\partial \dot{\omega}_T}{\partial Y_1} \right|_v & \cdots & \cdots & \cdots & \left. \frac{\partial \dot{\omega}_T}{\partial T} \right|_v \end{bmatrix}$$

- `jac_contribution()`.
Returns a $2N_r$ -long array of $[N_v \times N_v]$ Jacobian matrices, each one representing the contribution of reaction k to the Jacobian:

$$J_{\dot{\omega}_k} = \frac{\partial \mathcal{S}_{ik} r^k}{\partial Y_j} \quad i = 1, \dots, N_s \quad j = 1, \dots, N_s$$

- `jacKinetic()`.
Returns the $N_s \times N_s$ Jacobian, excluding the temperature row/column.
- `reaction_names()`.
Returns the names of the chemical reactions (forward + backward).

3.2 Functions.py

3.2.1 class CanteraCSP

This class inherits attributes and methods from the `CanteraThermoKinetics` class, which is in turn a derived class of Cantera's `Solution` class (multilevel inheritance) and extends their capabilities by adding computational singular perturbation (CSP)-related class methods. Hence, the constructor for this class is equivalent to the constructor of Cantera's `Solution` class. The proper way to instantiate `CanteraCSP` objects is by using species and reactions defined in an input file, e.g. `hydrogen.cti`:

```
1 import PyCSP.Functions as csp
2 gas = csp.CanteraCSP('hydrogen.cti')
```

Instance attributes:

- `jacobianteype`
Type (*string*).
Set/get the Jacobian type. Available choices are: `full`, `kinetic`. Defaults to `full`. Note that this choice affects the dimension of the system ($N_v = N_s + 1$ or N_s), and in turn the dimension of the CSP-related attributes (eigenvalues, eigenvectors, timescales, amplitudes).
- `rtol`
Type (*float*).
Set/get the CSP relative tolerance for the exhausted modes calculation. Defaults to `1.0e-2`.
- `atol`
Type (*float*).
Set/get the CSP absolute tolerance for the exhausted modes calculation. Defaults to `1.0e-8`.
- `rhs`
Type ($[N_v]$ *array of float, read-only*).
Get the chemical source term used for the CSP calculations.
- `jac`
Type ($[N_v \times N_v]$ *array of float, read-only*).
Get the Jacobian of the chemical source term used for the CSP calculations.
- `evals`
Type ($[N_v]$ *array of complex, read-only*).
Get the Jacobian eigenvalues.
- `Revec`
Type ($[N_v \times N_v]$ *array of float, read-only*).
Get the matrix of the Jacobian right eigenvectors. The eigenvectors are assembled as row vectors, hence the i -th eigenvector can be accessed using `Revec[i]`. Note that the properly defined right eigenvectors matrix is the transpose of `Revec`.

- **Levec**
Type ($[N_v \times N_v]$ array of float, read-only).
Get the matrix of the Jacobian left eigenvectors, obtained by inversion of the right eigenvectors matrix. The eigenvectors are assembled as row vectors, hence the i-th eigenvector can be accessed using `Levec[i]`.
- **f**
Type ($[N_v]$ array of positive float, read-only).
Get the CSP mode amplitudes.
- **tau**
Type ($[N_v]$ array of float, read-only).
Get the modes timescales.
- **nUpdates**
Type (*int*, read-only).
Get the number of kernel updates, starting from the instantiation of the object.

Class methods:

- **update_kernel()**.
Updates the CSP kernel (`evals`, `Revec`, `Levec`, `f`, `tau`), based on the current thermochemical state, employing the Jacobian formulation specified by setting either `constP` or `constRho`, and the Jacobian type specified with `jacobyantype`. Does not return any output.
- **get_kernel()**.
Returns the content of the `[evals, Revec, Levec, f]` attributes. If any attributes of the instance are changed with respect to the previous kernel calculation, the kernel is recomputed and returned.
- **calc_exhausted_modes()**.
Computes and returns the number of exhausted modes (*int*).
Optional keyword arguments:
 `rtol = float`. Relative tolerance. If not specified, instance attribute is employed.
 `atol = float`. Absolute tolerance. If not specified, instance attribute is employed.
- **calc_TSR()**.
Computes number of exhausted modes and Tangential Stretching Rate. Returns the Tangential Stretching Rate (*float*).
Optional keyword arguments:
 `rtol = float`. Relative tolerance for the exhausted modes calculation. If not specified, instance attribute is employed.
 `atol = float`. Absolute tolerance for the exhausted modes calculation. If not specified, instance attribute is employed.
 `getM = boolean`. If `True`, the number of exhausted modes is returned as well.
- **calc_CSPindices()**.
Computes number of exhausted modes and returns the CSP amplitude (API), timescale (TPI) participation indices, the CSP fast importance indices, slow importance indices, the species classification (fast/slow/trace): `[API, TPI, Ifast, Islow, species_type]` ($[N_v \times 2N_r]$ array of float, $[N_v \times 2N_r]$ array of float, $[N_v \times 2N_r]$ array of float, $[N_v \times 2N_r]$ array of float, $[N_v]$ array of strings)
Optional keyword arguments:
 `rtol = float`. Relative tolerance for the exhausted modes calculation.
 `atol = float`. Absolute tolerance for the exhausted modes calculation.
 `getM = boolean`. If `True`, the number of exhausted modes is returned as well.
 `getAPI = boolean`. If `False`, does not calculate the API.

- `getTPI` = *boolean*. If **False**, does not calculate the TPI.
- `getImpo` = *boolean*. If **False**, does not calculate the Importance indices.
- `getspeciestype` = *boolean*. If **False**, does not calculate the species classification.
- `calc_TSRindices()`.
Computes number of exhausted modes, the Tangential Stretching Rate and returns the Tangential Stretching Rate amplitude (TSR-API) or timescale participation indices (TSR-TPI) ($[2N_r]$ array of float).
Optional keyword arguments:
 - `rtol` = *float*. Relative tolerance for the exhausted modes calculation.
 - `atol` = *float*. Absolute tolerance for the exhausted modes calculation.
 - `type` = *'string'*. If **amplitude**, the TSR-API are returned. If **timescale**, the TSR-TPI are returned. Defaults to TSR-API.

3.3 Solver.py

3.3.1 class CSPsolver

This class is an ODE system integrator class based on the CSP solver. The class takes as input an instance of the `CanteraThermoKinetics` class.

Instance attributes:

- `jacobiantype`
Type (*string*).
Set/get the Jacobian type. Available choices are: **full**. Defaults to **full**.
- `csprtol`
Type (*float*).
Set/get the CSP relative tolerance for the exhausted modes calculation. Defaults to **1.0e-2**.
- `cspatol`
Type (*float*).
Set/get the CSP absolute tolerance for the exhausted modes calculation. Defaults to **1.0e-8**.
- `factor`
Type (*float*).
Set/get the timestep safety factor. Defaults to **0.2**.
- `M`
Type (*int, read-only*).
Get the current number of exhausted modes.
- `y`
Type (*array of float, read-only*).
Get the current system state in the form $[Y_1, \dots, Y_{N_s}, T]$.
- `t`
Type (*float, read-only*).
Get the current system time.
- `dt`
Type (*float, read-only*).
Get the current system timestep size.
- `Qs`
Type ($[N_s + 1 \times N_s + 1]$ *float, read-only*).
Get the current projection matrix.

- `Rc`
Type ($[N_s + 1]$ *float, read-only*).
Get the current radical correction vector.

Class methods:

- `set_integrator()`.
Set the integrator parameters. Does not return any output.
Optional keyword arguments:
 `cspRtol` = *float*. Relative tolerance for the exhausted modes calculation.
 `cspAtol` = *float*. Absolute tolerance for the exhausted modes calculation.
 `factor` = *float*. Timestep safety factor.
 `jacobinatype` = *'string'*. Jacobian type.
- `set_initial_value(y0,t0)`.
Set the integrator initial condition. Does not return any output.
Mandatory positional arguments:
 `y0` ($[N_s + 1]$ *array of float*). Initial state in the form $[Y_1, \dots, Y_{N_s}, T]$.
 `t0` (*float*). Initial time.
- `integrate()`.
Advance in time by one timestep. The timestep is calculated according to the $M + 1$ -th eigenvalue, with a safety factor of `factor`.

3.4 Simplify.py

3.4.1 class CSPsimplify

This class is simplified kinetic mechanism generation class based on CSP. The class takes as input an instance of the `CanteraThermoKinetics` class and a dataset. The instance should be initialized with the detailed mechanism. The dataset must be a 2D array, each row containing species mass fractions (in the order of the detailed mechanism), temperature and pressure: `dataset=[Y1, Y2, ..., YN, T, P]`.

Instance attributes:

- `cspRtol`
Type (*float*).
Set/get the CSP relative tolerance for the exhausted modes calculation. Defaults to `1.0e-2`.
- `cspAtol`
Type (*float*).
Set/get the CSP absolute tolerance for the exhausted modes calculation. Defaults to `1.0e-8`.
- `scaled`
Type (*boolean*).
Set/get the *scaled* option for the importance indexes. When active, indexes are normalized with respect to their maximum value. Defaults to `True`.
- `targetset`
Type (*string, dictionary*).
Set/Get the list of target species. Example: `{ 'CH4', 'H2O', 'CO2' }`.
- `TSRtargetset`
Type (*boolean*).
Set/get the *TSRtargetset* option for the target set. When active, the user-defined `targetset`, which may also be empty, is augmented with the local TSR-relevant species (each state will have its own set of targets based on TSR-API indexes). Defaults to `False`.

- `tsrtol`
Type (*float*).
Set/get the TSR-API tolerance for including species in the `TSRtargetset`. A species is included if it is involved in a reaction which is part of the subset of reactions contributing to the `tsrtol`.100% of the cumulative participation to the TSR. The higher the value of `tsrtol`, the more species will be included. Defaults to 0.5.
- `y`
Type (*problemtype*).
Type (*string*).
Set/Get the problem type, among `constP` and `constRho`.

Class methods:

- `dataset_info()`.
Outputs info on `dataset`.
- `process_dataset()`.
Computes the fast/slow importance indexes and the species fast/slow classification for each state in `dataset`.
- `simplify_mechanism(threshold)`.
Returns the sets of retained species and reactions, based on the value of `threshold`, which must be between 0 and 1.

4 Examples

Several examples are available in the `examples` folder to exploit the functionalities related to:

- exhausted modes (M)
- tangential stretching rate (TSR)
- CSP and TSR indices (importance indices, amplitude and timescale participation indices, TSR amplitude/timescale participation indices)
- CSP solver
- CSP simplify

4.1 CSP analysis

It is hereby reported an example of how to analyze with PyCSP a set of thermochemical data stored in an external file called `testdata.dat`, containing N lines, each one being a full thermochemical state of the kind $[T, P, Y_1, \dots, Y_{N_s}]$. The kinetic mechanism is `hydrigen.cti`, containing 9 species and 19 reversible reactions. The dataset is the time evolution of a stoichiometric H-2/Air constant pressure homogeneous reactor, with initial temperature of 1000 K and pressure of one atmosphere.

```

1 import numpy as np
2 import PyCSP.Functions as csp
3 import PyCSP.utils as utils
4 import matplotlib.pyplot as plt
5
6 #import dataset
7 data = np.loadtxt('testdata.dat')
8 time = data[:,0]
9 Temp = data[:,1]
10 Pressure = data[:,2]
11 Y = data[:,3:]
12
```

```

13 #create an instance of the CanteraCSP class
14 gas = csp.CanteraCSP('hydrogen.cti')
15
16 #set jacobiantype
17 gas.jacobiantype = 'full'
18
19 #set CSP tolerances
20 gas.rtol = 1.0e-2
21 gas.atol = 1.0e-8
22
23 evals = []
24 Revec = []
25 Levec = []
26 fvec = []
27 M = []
28
29 for step in range(len(time)):
30     gas.constP = Pressure[step]
31     state = np.append(Y[step], Temp[step])
32     gas.set_stateYT(state)
33     lam, R, L, f = gas.get_kernel()
34     NofDM = gas.calc_exhausted_modes()
35
36     evals.append(lam)
37     Revec.append(R)
38     Levec.append(L)
39     fvec.append(f)
40     M.append(NofDM)
41
42 evals = np.array(evals)
43 Revec = np.array(Revec)
44 Levec = np.array(Levec)
45 fvec = np.array(fvec)
46 M = np.array(M)
47
48 #plot eigenvalues and lambda_M+1
49 evalM = utils.select_eval(evals, M)
50 logevals = np.clip(np.log10(1.0+np.abs(evals)), 0, 100)*np.sign(evals.real)
51 logevalM = np.clip(np.log10(1.0+np.abs(evalM)), 0, 100)*np.sign(evalM.real)
52 fig, ax = plt.subplots(figsize=(6,4))
53 for idx in range(evals.shape[1]):
54     ax.plot(states.t, logevals[:,idx], color='black', marker='.', markersize = 5,
55            linestyle = 'None')
56 ax.plot(states.t, logevalM, color='orange', marker='.', markersize = 4, linestyle =
57        'None', label='lam(M+1) rtol e-2; atol e-8')
58 ax.set_xlabel('time (s)')
59 ax.set_ylabel('evals')
60 ax.set_ylim([-9, 6])
61 ax.set_xlim([0., 0.001])
62 ax.grid(False)
63 ax.legend()
64 plt.show()
65
66 #plot exhausted modes
67 print('plotting exhausted modes...')
68 fig, ax = plt.subplots(figsize=(6,4))
69 #ax.plot(states.t, M, color='black')
70 ax.plot(M, color='orange', label='rtol e-2; atol e-8')
71 #ax.set_xlabel('time (s)')
72 ax.set_xlabel('# timestep')
73 ax.set_ylabel('M')
74 ax.set_ylim([0,10])
75 #ax.set_xlim([0., 0.001])
76 ax.grid(False)
77 ax.legend()
78 plt.show()

```

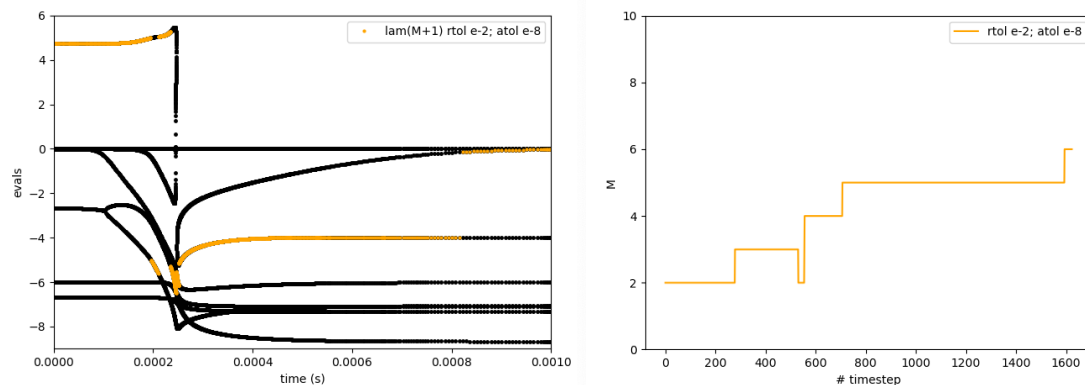


Figure 2: Example outcomes. Left: eigenvalues (black) and M+1-th eigenvalue (orange). Right: number of exhausted modes.

4.2 CSP solver

This example shows how to integrate a constant volume homogeneous reactor with the CSPsolver class.

```

1 import PyCSP.Functions as cspF
2 import PyCSP.Solver as cspS
3
4 #create an instance of the CanteraCSP class
5 gas = cspF.CanteraCSP('hydrogen.cti')
6
7 #set the gas state using Cantera's methods ( as an alternative to set_stateYT() )
8 T = 1000
9 P = ct.one_atm
10 gas.TP = T, P
11 gas.set_equivalence_ratio(1.0, 'H2', 'O2:1, N2:3.76')
12
13 #push density
14 rho = gas.density
15 gas.constRho = rho
16
17 #initial condition
18 y0 = np.hstack((gas.Y,gas.T))
19 t0 = 0.0
20
21 t_end = 1e-2
22
23 #create an instance of CSPsolver
24 solver = cspS.CSPsolver(gas)
25 solver.set_integrator(cspRtol=1e-2, cspAtol=1e-8, factor=0.2, jacobiantype='full')
26 solver.set_initial_value(y0,t0)
27
28 states = ct.SolutionArray(gas, 1, extra={'t': [0.0], 'M': 0})
29
30 #integrate ODE with CSP solver
31 while solver.t < t_end:
32     solver.integrate()
33     states.append(gas.state, t=solver.t, M=solver.M)
34     print('%10.3e %10.3f %10.3e %10.3e %10.3e %2i' % (solver.t, solver.y[-1],
35         solver.dt, gas.P, gas.density, solver.M))

```

4.3 CSP simplify

This example shows how to generate a set of simplified kinetic mechanisms, based on a dataset produced with a detailed mechanism, with the CSPsimplify class.

```

1 #-----CREATE DATASET-----

```

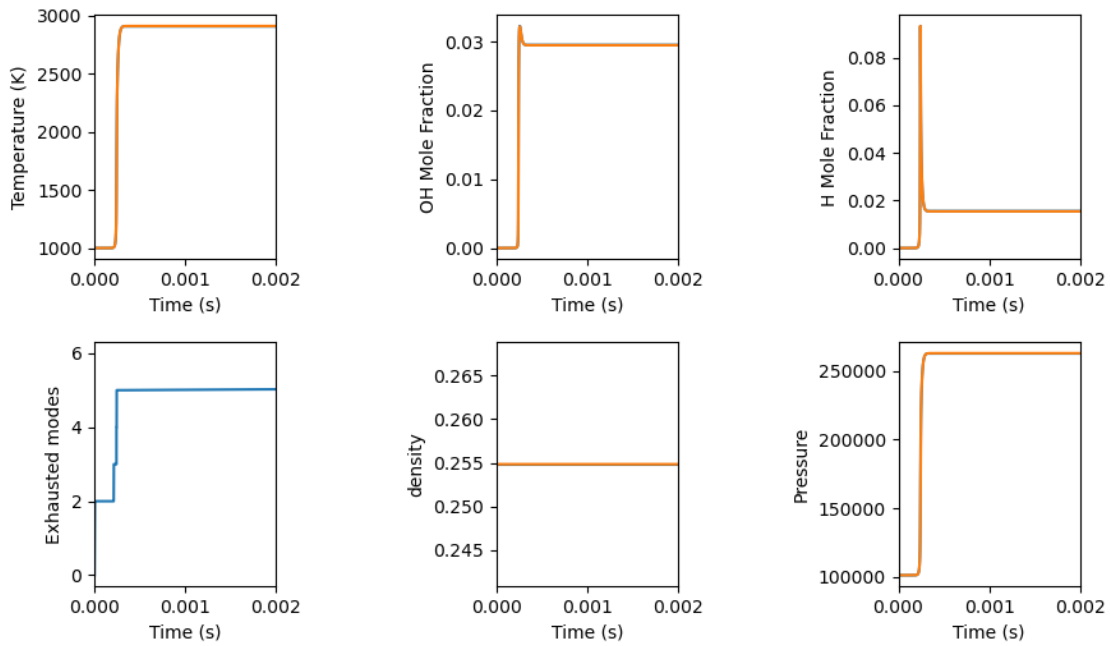


Figure 3: Example outcomes.

```

2 #create gas from original mechanism file hydrogen.cti
3 dtl_mech = csp.CanteraCSP('gri30.cti')
4
5 #set the gas state
6 T = 1000
7 P = ct.one_atm
8 dtl_mech.TP = T, P
9 dtl_mech.constP = P
10 dtl_mech.set_equivalence_ratio(1.0, 'CH4', 'O2:1, N2:3.76')
11
12
13 #integrate ODE with detailed mech
14 r = ct.IdealGasConstPressureReactor(dtl_mech)
15 sim = ct.ReactorNet([r])
16 states = ct.SolutionArray(dtl_mech, 1, extra={'t': [0.0], 'rhsT': [0.0]})
17
18 sim.set_initial_time(0.0)
19 while sim.time < 1000:
20     sim.step()
21     states.append(r.thermo.state, t=sim.time, rhsT=dtl_mech.source[-1])
22
23 dataset = np.concatenate((states.Y, states.T[:, np.newaxis], states.P[:, np.newaxis]),
24                             axis=1)
25 print('Dataset created, start processing...')
26
27 #coarsen dataset (to speed up)
28 dataset = dataset[::64]
29
30 #-----SIMPLIFY-----
31 #init simplifier
32 simplifier = simp.CSPsimplify(dtl_mech, dataset)
33
34 #simplifier settings
35 simplifier.targetset = {'CH4', 'O2', 'N2', 'HCO', 'H2O', 'CO2'}
36 simplifier.problemtypes = 'constP'
37 simplifier.scaled = True
38 simplifier.csprt看 = 1.0e-2
39 simplifier.cspatol = 1.0e-8

```

```

40 #process dataset
41 simplifier.process_dataset()
42
43 print('Done processing')
44
45 print('Start pruning...may take a while')
46 #loop over thresholds
47 thr = np.arange(0.01, 1, 0.01)
48
49 simp_mech = []
50 prev_species = dtl_mech.species_names
51 for i in range(len(thr)):
52     species, reactions = simplifier.simplify_mechanism(thr[i])
53     simp = csp.CanteraCSP(thermo='IdealGas', kinetics='GasKinetics', species=
54         species, reactions=reactions)
55     if simp.species_names != prev_species: #append only if different from previous
56         one
57         simp_mech.append(simp)
58         prev_species = simp.species_names
59
60 nmech = len(simp_mech)
61 print('%i mechanisms found' % (nmech))
62
63 #-----RE-RUN-----
64 # Re-run the ignition problem with the simplified mechanisms
65 all_states_simp = []
66 for i in range(nmech):
67     simp_mech[i].TP = T,P
68     simp_mech[i].constP = P
69     simp_mech[i].set_equivalence_ratio(1.0, 'CH4', 'O2:1, N2:3.76')
70     r = ct.IdealGasConstPressureReactor(simp_mech[i])
71     sim = ct.ReactorNet([r])
72     states_simp = ct.SolutionArray(simp_mech[i], 1, extra={'t': [0.0], 'rhsT':
73         [0.0]})
74
75     sim.set_initial_time(0.0)
76     while sim.time < 1000:
77         sim.step()
78         states_simp.append(r.thermo.state, t=sim.time, rhsT=simp_mech[i].source
79             [-1])
80     all_states_simp.append(states_simp)
81
82 #-----ERRORS-----
83 dtl_idt = states.t[states.rhsT.argmax()]
84 simp_idt = [all_states_simp[i].t[all_states_simp[i].rhsT.argmax()] for i in range(
85     nmech)]
86 err_idt = abs((simp_idt-dtl_idt)/dtl_idt)*100
87
88 fig, ax = plt.subplots(figsize=(6,4))
89 ax.plot([simp_mech[i].n_species for i in range(nmech)], err_idt, color='red',
90     marker='.')
91 ax.set_xlabel('# of species')
92 ax.set_ylabel('ignition delay time relative Error [%]')
93 ax.set_yscale('log')
94 ax.set_ylim([1e-3, 1e2])
95 plt.savefig('ign_delay_error.png', dpi=800, transparent=False)

```

Figure 4 shows the percent relative error on the ignition delay time versus the number of retained species. A significant improvement is given by the TSR kernel set, which replaces the user-specified target species set. With the following settings:

```

1 simplifier.TSRtargetset = True
2 simplifier.TSRtol = 0.5
3 simplifier.targetset = {'N2'}

```

the previous example delivers the ignition delay relative errors shown in Fig.5. The manual addition of N_2 to the TSR kernel set is needed to force the presence of N_2 in the skeletal mechanisms.

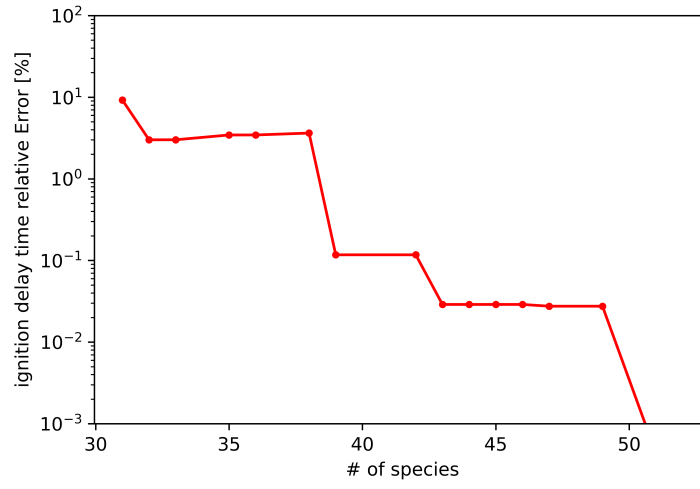


Figure 4: Example outcomes of the mechanism simplification.

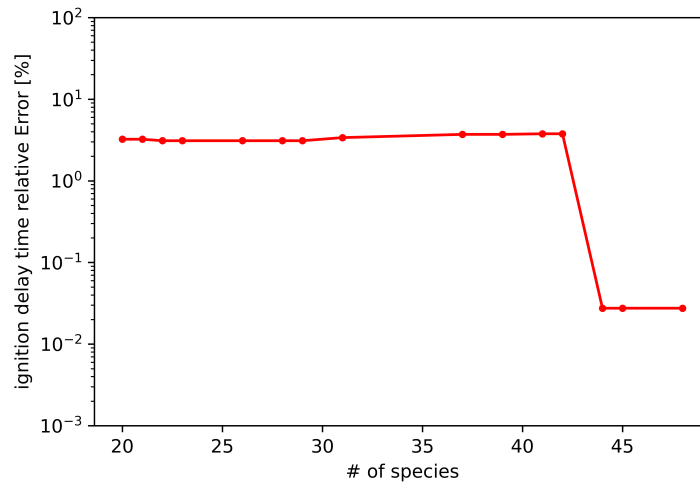


Figure 5: Example outcomes of the mechanism simplification with TSR kernel set.