

Neural Networks and Deep Learning

CS5242

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Concepts

• AI

- 1950's
- "Human intelligence exhibited by machines"
- Narrow AI: image recognition, machine translation

Machine learning

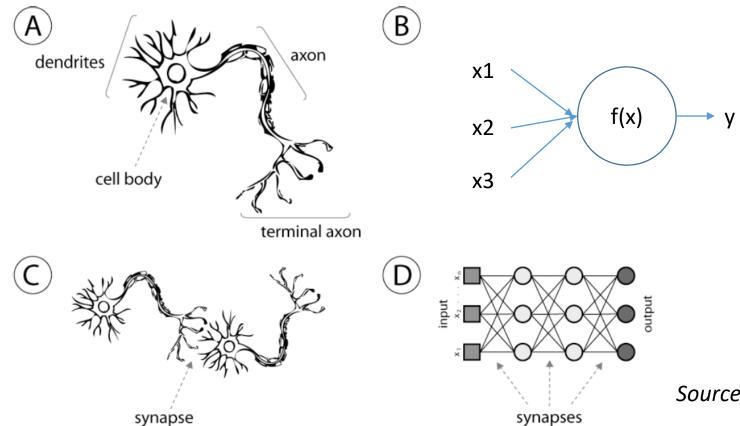
- 1980's
- "An approach to achieve AI through systems that can learn from experience to find patterns in that data"

Neural networks and Deep learning

- 2010's
- A class of machine learning algorithm that use a cascade of multiple layers of nonlinear processing units for feature extraction and transformation---Wikipedia

Neural networks (NN)

Artificial neural networks



Source from Hwee Kuan Lee

Neural networks (NN)

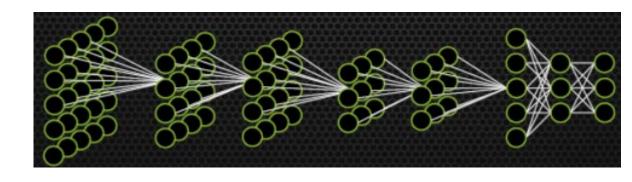
Shallow to deep



Source from Hwee Kuan Lee

Neural networks (NN)

- Multi-layer perceptron (MLP)
- Convolutional neural network (CNN)
- Recurrent neural networks (RNN)
- (Restricted) Boltzmann machine
- Deep belief network
- Spike neural network
- Radial basis function neural network
- Hopfield networks



Source from [3]

Deep Learning

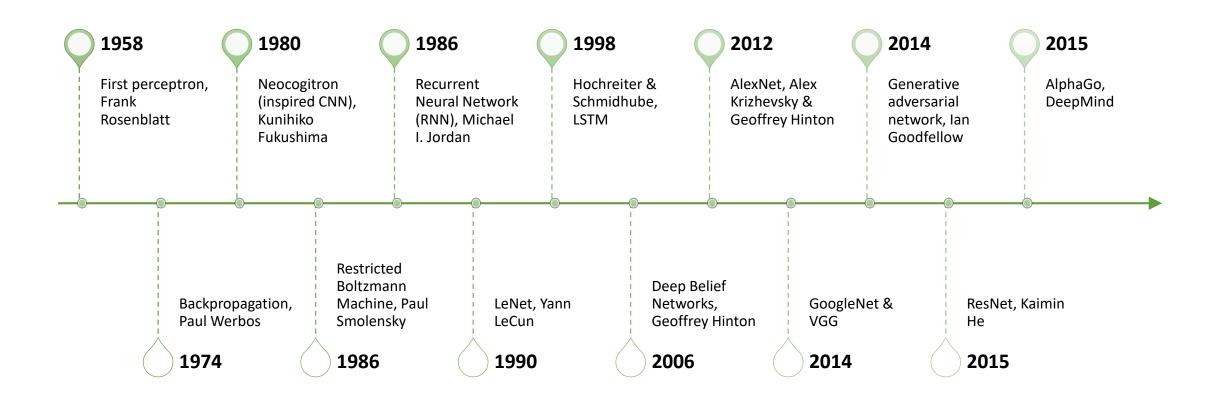
Rebrand/resurgence of neural networks

- Big data (new oil/electricity)
- New models and training algorithms
- Powerful machines, e.g. GPU

Feature learning

- Not only neural networks
- Distributed representation of words, e.g. word

History [2]



- Vision
 - Image classification
 - Object detection and tracking
 - Scene text recognition







- Natural language processing
 - Question answering
 - Machine translation

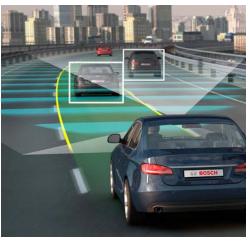


- Speech
 - Speech recognition, e.g. <u>Amazon Echo</u>



- And more?
 - Health-care
 - Agriculture
 - Environment
 - Fin-tech
 - Autonomous vehicle
 - Manufacture







Similar online courses

Neural Networks and Deep Learning

- Andrew Ng
- https://www.coursera.org/learn/neural-networks-deep-learning

CS231n: Convolutional Neural Networks for Visual Recognition

- Fei-Fei Li, Justin Johnson, Serena Yeung
- http://cs231n.stanford.edu/

CS224d: Deep Learning for Natural Language Processing

- Richard Socher
- http://cs224d.stanford.edu/

CSC 321: Intro to Neural Networks and Machine Learning

- Roger Grosse
- http://www.cs.toronto.edu/~rgrosse/courses/csc321 2017/

Neural Networks for Machine Learning

- Geoffrey Hinton
- https://www.coursera.org/learn/neural-networks

Schedule (Check IVLE for latest plan)

- Part I: Basics of training neural networks
 - Week 1: Introduction
 - History, applications and administrative
 - Linear regression
 - Week 2: Training tricks
 - Data normalization
 - Bias and variance
 - Regularization
 - SGD
 - Week 3: Deep neural networks
 - Loss function, BP
 - Initialization
 - Activation
 - Dropout
 - Batch-Normalization

Schedule (Check IVLE for latest plan)

- Part II: Convolutional neural networks
 - Week 4: Layers
 - Convolution, pooling
 - Week 5: Architecture comparison
 - AlexNet, VGG, ResNet, InceptionNet
 - Week 6: Applications
 - Image classification, object detection, image segmentation
 - Week 7: Practice session
- Part III: Recurrent neural networks
 - Week 8: Layer and architecture
 - Vanilla RNN, LSTM, GRU, Bi-directional RNN
 - Week 9: Training and prediction & Quiz
 - Greedy search VS Beam search
 - Week 10: Applications
 - Machine translation, question answering
 - Week 11: Practice session
- Part IV: Advanced topics (TBD)
 - Week 12: Generative adversarial network
 - Week 13: Distributed deep learning

Intended learning outcomes

1

Explain the logics (intuitions) of the operations of different layers and training algorithms

2

Compare different neural network architectures in terms of their characteristics 3

Implement popular neural networks

4

Solve real problems using neural networks and deep learning techniques

Pre-requisite

Course

- Machine Learning (CS3244)
 - Or https://www.coursera.org/learn/machine-learning
- Linear Algebra (MA1101R)
 - Or https://ocw.mit.edu/courses/mathematics/18-06-linear-algebra-spring-2010/
- Calculus (MA1521)
- Probability (ST2334)

Coding

- Python (ONLY, version 3.x is recommended)
 - Numpy
 - Keras, TensorFlow, PyTorch, MxNet, Caffe, SINGA
- Jupyter notebook

Grading policy

Weightage:

- Assignment 1 20%
- Assignment 2 20%
- Quiz 30%
- Closed book with one page cheat sheet
- Project 30%
- Register the group information on IVLE

Late submission

• 15% off per day late (17:01 is the start of one day)

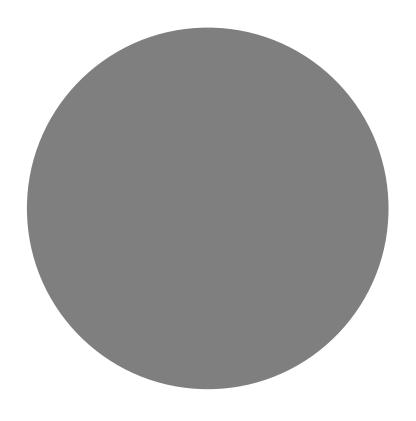
Collaboration

- Every assignment is an individual task (no discussion)
- The project is a group-based task (should discuss)
- Avoid academic offence (cheating, plagiarism)

Contacts

- IVLE forum
 - For all issues
- Email: cs5242@comp.nus.edu.sg
 - For private/personal issues
- Consultation (make appointments on IVLE)
 - Teacher
 - Wei WANG, <u>wangwei@comp.nus.edu.sg</u>
 - Wed, 11:00-12:00 (Except 24 Jan), COM2-04-09
 - Teaching Assistants
 - Yaqi Xie, <u>e0205023@u.nus.edu</u>
 - Friday 11:00-12:00, Week 1-6 (Except 23 Feb)
 - Xindi SHANG, shangxin@comp.nus.edu.sg
 - Fridy 11:00-12:00, Week 7-13
 - Yao SHU, shuyao95@u.nus.edu

Machine learning basics



Model/task categorization

- Supervised learning
 - Input --- Output
 - Learning the pattern from labeled training data
 - Image classification
- Unsupervised learning
 - Learning to differentiate/cluster unlabeled data
 - Clustering of images
- Reinforcement learning
 - Learning from trail-and-error through rewards
 - CS4246

House price prediction

- Problem definition
 - Given the **information** of a house, predict its **price**.
- Data
 - Input
 - A house: size, number of floors, distance to CBD, etc
 - Output
 - Price

Data preparation

- Collect data
 - From websites, e.g. <u>kaggle</u>, <u>property guru</u>
 - From data sellers
- Clean data
 - Extract useful fields, size, distance to CBD, height, etc.
 - Handle missing values
- Partition data
 - Training
 - Validation
 - Testing

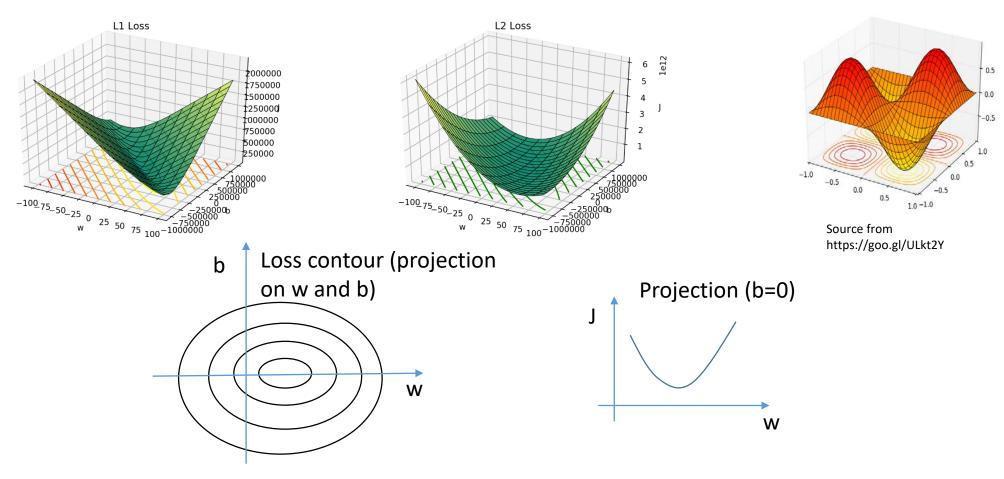
Modeling with a single feature

- Model
 - How to represent the input samples, i.e. features/attributes?
 - How to map the input to the output?
- Formalize the input and output
 - Represent the house by its size, denoted as $x \in R$
 - x is called the **feature** of **a data sample** (i.e. one house)
 - Denote the price by $y \in R^+$, called the ground truth (label)
- Map from input to output by linear regression
 - $\tilde{y} = xw + b, w \in R$, $b \in R$
 - \tilde{y} is called the **prediction**

Loss function

- Define the training objective, i.e. loss function
 - $J(w,b) = \sum_{\langle x,y \rangle \in S_{train}} L(x,y|w,b) / |S_{train}|$
 - $L_1(x, y|w, b) = |\tilde{y} y|$
 - Not smooth. No gradient at some positions
 - $L_2(x, y|w, b) = |\tilde{y} y|^2$
 - Smooth. Has gradient at all positions.

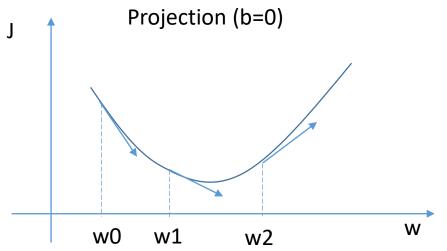
Loss contour



Training by gradient descent

Gradient descent (GD) algorithm for optimization

α



is called the learning rate, which controls the moving step length. It important for convergence. If it is large, w would oscillate around the optimal position. If it is small, it would take many iterations to reach the optimal position.

Initialize w as w0 Compute $\frac{\partial J}{\partial w0}$, negative; Move w from w0 to the right by

 $w1 = w0 - \alpha \frac{\partial J}{\partial w0}$

Compute $\frac{\partial J}{\partial w^1}$, negative;

Move w from w1 to the right by

$$w2 = w1 - \alpha \frac{\partial J}{\partial w1}$$

Compute $\frac{\partial J}{\partial w^2}$, positive Move w from w2 to the left by

$$w3 = w2 - \alpha \frac{\partial J}{\partial w^2}$$

Gradually decrease J and move w to the optimal position

Training by gradient descent

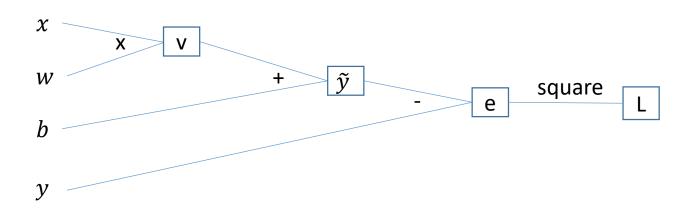
- Gradient descent algorithm for optimization
- Set w = 1, b = 0
- Repeat
 - For each data sample, compute $\tilde{y} = xw + b$
 - Compute the average loss, $\sum_{\langle x,y \rangle \in S_{train}} L(x,y|w,b) / |S_{train}|$
 - Compute partial derivative $\frac{\partial J}{\partial w}$, $\frac{\partial J}{\partial b}$
 - Update $\mathbf{w} = \mathbf{w} \alpha \frac{\partial J}{\partial w}$, $\mathbf{b} = \mathbf{b} \alpha \frac{\partial J}{\partial b}$

Back-propagation (BP) for computing derivatives

- $\tilde{y} = xw + b$
- $L(x, y|w, b) = |\tilde{y} y|^2$

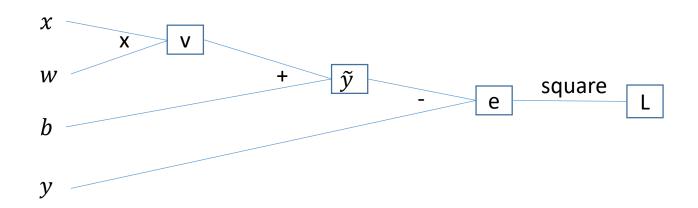
•
$$\frac{\partial J}{\partial w} = \sum_{\langle x,y \rangle \in S_{train}} \frac{\partial L(x,y|w,b)}{\partial w}$$

Computation graph



Back-propagation for a single sample

- Forward (w=1, b=0)
 - Given x=1.5, y=2
 - v=x*w=1.5x1=1.5
 - \tilde{y} =v + b=1.5+0=1.5
 - e= \tilde{y} -y=1.5-2=-0.5
 - L=(-0.5)x(-0.5)=0.25



Back-propagation

- Forward (w=1, b=0)
 - x=1.5, y=2
 - v=x*w=1.5x1=1.5
 - \tilde{y} =v + b=1.5+0=1.5
 - e= \tilde{y} -y=1.5-2=-0.5
 - L=(-0.5)x(-0.5)=0.25
- Backward

•
$$\frac{\partial L}{\partial e} = 2e = 2 \times (-0.5) = -1$$

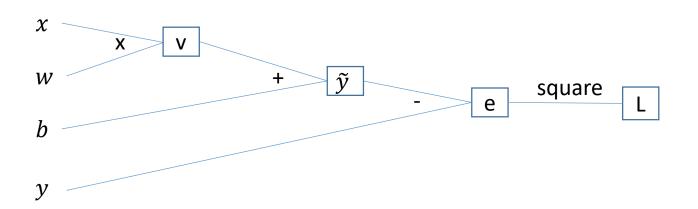
•
$$\frac{\partial L}{\partial e} = 2e = 2 \times (-0.5) = -1$$

• $\frac{\partial L}{\partial \tilde{y}} = \frac{\partial L}{\partial e} \times \frac{\partial e}{\partial \tilde{y}} = -1 \times 1 = -1$

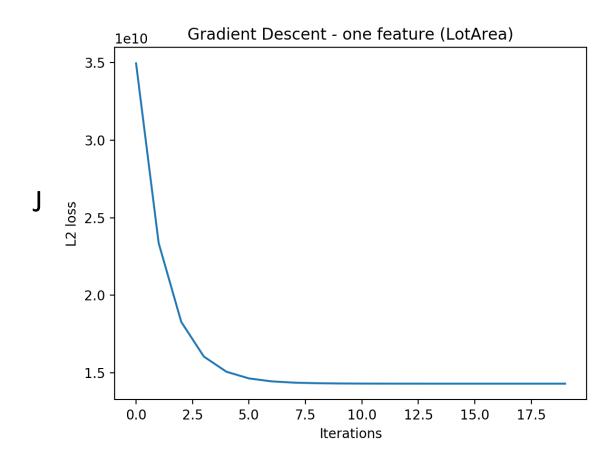
•
$$\frac{\partial L}{\partial b} = \frac{\partial L}{\partial \tilde{v}} \times \frac{\partial \tilde{v}}{\partial b} = -1 \times 1 = -1$$

•
$$\frac{\partial L}{\partial v} = \frac{\partial L}{\partial \tilde{y}} \times \frac{\partial \tilde{y}}{\partial v} = -1 \times 1 = -1$$

•
$$\frac{\partial L}{\partial w} = \frac{\partial L}{\partial v} \times \frac{\partial v}{\partial w} = -1 \times x = -1.5$$



Training loss



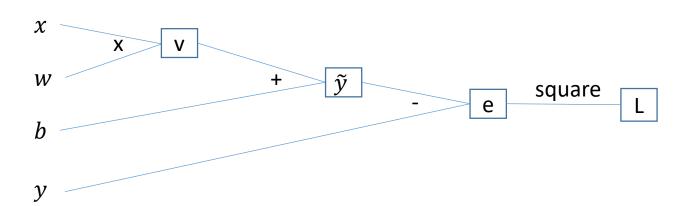
Modeling with multiple features

- Consider more features
 - Distance to CBD, number of floors, etc.
 - $x \in \mathbb{R}^m$, $y \in \mathbb{R}^+$, x_i for the i-th feature (attribute)
- Map from input to output
 - $\tilde{y} = w^T x + b, w \in R^m, b \in R$, w_i for the i-th co-efficient $= \sum_{i=1}^d x_i \times w_i + b$
- $L(x, y|w, b) = |\tilde{y} y|^2$
- $J(w,b) = \frac{\sum_{\langle x,y \rangle \in S_{train}} L(x,y|w,b)}{|S_{train}|}$

Back-propagation

Forward

- Given
 - $w=[1,1,1]^T$, b=0
 - $x=[0.5,1,1.5]^T$
 - y=2
- $v = w^T x = 1x0.5 + 1x1 + 1x1.5 = 3$
- \tilde{y} = 3+0 = 3
- e=3-2=1
- L=1x1=1



Back-propagation

Backward

$$\bullet \frac{\partial L}{\partial e} = 2e = 2 \times 1 = 2$$

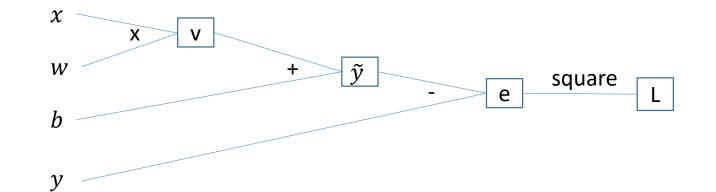
•
$$\frac{\partial L}{\partial \tilde{y}} = \frac{\partial L}{\partial e} \times \frac{\partial e}{\partial \tilde{y}} = 2 \times 1 = 2$$

$$\bullet \frac{\partial L}{\partial b} = \frac{\partial L}{\partial \tilde{y}} \times \frac{\partial \tilde{y}}{\partial b} = 2 \times 1 = 2$$

•
$$\frac{\partial L}{\partial v} = \frac{\partial L}{\partial \tilde{v}} \times \frac{\partial \tilde{v}}{\partial v} = 2 \times 1 = 2$$

•
$$\frac{\partial L}{\partial w} = \frac{\partial L}{\partial v} \times \frac{\partial v}{\partial w} = 2 \times x^T = 2 \times [0.5, 1, 1.5]^T = [1, 2, 3]^T$$

• Shape check: w and $\frac{\partial L}{\partial w}$, b and $\frac{\partial L}{\partial b}$



Vectorization

The notation m and n are different to those introduced in the lecture. We will use m for the number of features (attributes) and n for the number of samples for the next lectures.

Back-propagation over all samples

•
$$J(w,b) = \frac{\sum_{\langle x,y \rangle \in S_{train}} L(x,y|w,b)}{|S_{train}|} = \frac{\sum_{i=1}^{n} L(x^{(i)},y^{(i)}|w,b)}{n}$$

- n=| S_{train} |, $x^{(i)} \in R^m$ and $y^{(i)} \in R^+$ for the i-th sample (i.e. i-th house)
- Put all sample features into a matrix (one column per sample)

•
$$X = [x^{(0)}, x^{(1)}, ..., x^{(n)}], \in \mathbb{R}^{m * n}$$

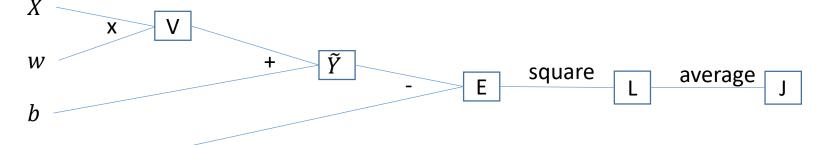
Put all labels (price) into a matrix

•
$$Y = [y^{(0)}, y^{(1)}, ..., y^{(n)}], \in R^{1*n}$$

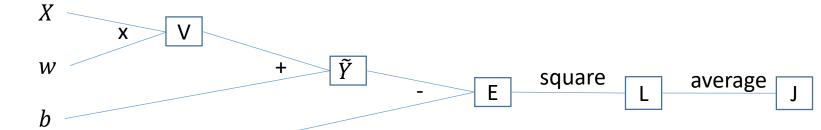
Vectorization

- Forward
- $V = w^T X$, $\in R^{1*n}$
- $\tilde{Y} = V + b$, $\in R^{1*n}$
- $E = \tilde{Y} Y \in \mathbb{R}^{1*n}$
- $L = E^2$, $\in R^{1*n}$
- $J = numpy.average(L) \in R^+$

Correction: The shapes of the variables are wrong in the handwriting notes. Please ignore the handwriting notes and use this slide.



Vectorization



Backward

•
$$\frac{\partial J}{\partial L} = \left[\frac{1}{n}, \frac{1}{n}, \frac{1}{n}, \dots\right]$$
 , $\in R^{1*n}$ × : element-wise multiplication

•
$$\frac{\partial J}{\partial E} = \frac{\partial J}{\partial L} \times \frac{\partial L}{\partial E} = \frac{\partial J}{\partial L} \times 2E = 2E/n, \in R^{1*n}$$

•
$$\frac{\partial J}{\partial \tilde{Y}} = \frac{\partial J}{\partial E} \times \frac{\partial E}{\partial \tilde{Y}} = \frac{\partial J}{\partial E} \times [1,1,1,\dots] = 2E/n , \in R^{1*n}$$

•
$$\frac{\partial I}{\partial b} = \frac{\partial E}{\partial \tilde{Y}} \cdot \frac{\partial \tilde{Y}}{\partial b} = \frac{\partial J}{\partial \tilde{Y}} \cdot [1,1,1,\dots]$$
 , $\in R$ (dot product)

•
$$\frac{\partial J}{\partial V} = \frac{\partial J}{\partial \tilde{Y}} \times \frac{\partial \tilde{Y}}{\partial V} = \frac{\partial J}{\partial \tilde{Y}} \times [1,1,1,\dots] = 2E/n, \in R^{1*n}$$

•
$$\frac{\partial J}{\partial w} = \left(\frac{\partial J}{\partial V}\frac{\partial V}{\partial w}\right)^T = X\left(\frac{\partial J}{\partial V}\right)^{T} \in \mathbb{R}^m$$
 (matrix-matrix product)

Element-wise multiplication? dot product? matrix product? transpose?



Shape check: for every node in the graph, its shape should be the same during forward and backward.

Assignment 0 (0 marks) --- GPU machines

- NSCC (National Super-Computing Center)
 - Free for NUS students
 - 128 GPU nodes, each with a NVIDIA Tesla K40 (12 GB)
 - Follow the manual and test program on IVLE Assignments/assignment0 to get yourself familiar with it.
 - Check the versions of the software
- SoC GPU Cluster
 - https://docs.comp.nus.edu.sg/node/1814
- Google Cloud Platform
 - 300 USD credit for new register
 - NVIDIA Tesla K80 (2x12GB) is available for Region Taiwan
- Amazon EC2 (g2.8xlarge)
 - 100 USD credit for students
 - NVIDIA Grid GPU, 1536 CUDA cores, 4GB memory
 - Available for Singapore region
- Alibaba cloud
- Tips:
 - STOP/TERMINATE the instance immediately after your program terminates
 - Check the usage status frequently to avoid high outstanding bills
 - Use Amazon or Google cloud platform for debugging and use NSCC for actual training and tuning

References

- [1] Goodfellow Ian, Bengio Yoshua, Courville Aaron. Deep learning. MIT Press. http://www.deeplearningbook.org
- [2] Haohan Wang, Bhiksha Raj. On the Origin of Deep Learning. 2017 https://arxiv.org/abs/1702.07800
- [3] H. Lee, R. Grosse, R. Ranganath, and A. Y. Ng. "Convolutional deep belief networks for scalable unsupervised learning of hierarchical representations." In ICML 2009
- http://neuralnetworksanddeeplearning.com/chap1.html
- https://www.analyticsvidhya.com/blog/2017/06/a-comprehensiveguide-for-linear-ridge-and-lasso-regression/