GLM for Landslide Occurance Prediction

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```
landslide.train=read.csv("landslide_training_data.csv",header = T)
landslide.validation=read.csv("landslide_validation_data.csv",header = T)
landslide.test=read.csv("landslide_test_data.csv",header = T)
load(file = "landslide_raster_stack")
```

1. Data Exploration and tidying

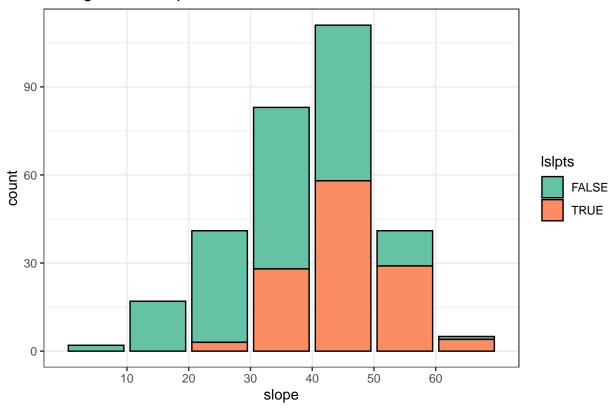
1.a Data Exploration

- Develop histograms of the five different predictor variables in the training set
- Develop a correlation plot of the predictor variables

```
# slope
slope.plot <- ggplot(data=landslide.train, aes(slope,fill = lslpts)) +</pre>
  geom_bar(colour = "black", position = "stack") +
  scale_x_binned()+
  scale_fill_brewer(palette = "Set2")+
  labs(title = "Histogram for Slope")+
 theme bw()
# cplan
cplan.plot <- ggplot(data=landslide.train, aes(cplan,fill = lslpts)) +</pre>
  geom_bar(colour = "black", position = "stack") +
  scale_x_binned()+
  scale_fill_brewer(palette = "Set3")+
  labs(title = "Histogram for Plan Curvature")+
  theme_bw()
# cprof
cprof.plot <- ggplot(data=landslide.train, aes(cprof,fill = lslpts)) +</pre>
  geom_bar(colour = "black", position = "stack") +
  scale_x_binned(breaks = c(-0.10, -0.06, -0.04, -0.02, 0, 0.02, 0.04)) +
  scale_fill_brewer(palette = "Pastel2")+
 labs(title = "Histogram for Profile Curvature")+
 theme_bw()
elev.plot <- ggplot(data=landslide.train, aes(elev,fill = lslpts)) +</pre>
  geom_bar(colour = "black") +
```

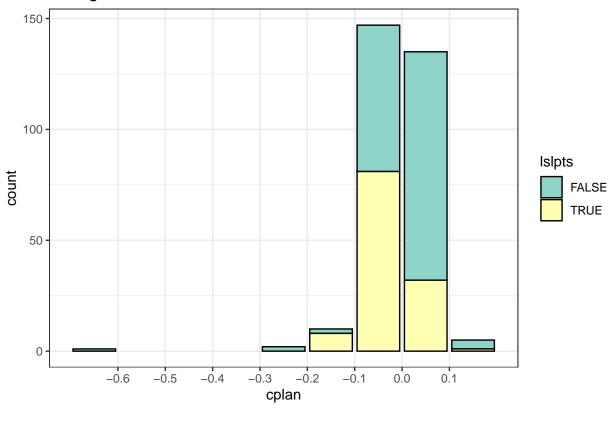
```
scale_x_binned(breaks = c(1800,2000,2200,2400,2600,2800,3000))+
  scale_fill_brewer(palette = "Pastel1")+
  labs(title = "Histogram for Elevation ")+
  theme_bw()
# log10 carea
log10_carea.plot <- ggplot(data=landslide.train, aes(log10_carea,fill = lslpts)) +</pre>
  geom_bar(colour = "black", position = "stack") +
  scale_x_binned()+
  scale_fill_brewer(palette = "Accent")+
  labs(title = "Histogram for Catchment Area")+
  theme_bw()
train.variable <- data.frame(landslide.train $slope) %>%
  cbind(data.frame(landslide.train$cplan)) %>%
  cbind(data.frame(landslide.train$cprof)) %>%
  cbind(data.frame(landslide.train$elev)) %>%
  cbind(data.frame(landslide.train$log10_carea))
colnames(train.variable) <- c("slope","cplan","cprof","elev","log10_carea")</pre>
# correlation
cor_plot <- ggcorr(train.variable,label = TRUE,label_size = 3, hjust = 0.75,</pre>
                   size = 5, color = "grey40",
       low = "#3399FF", mid = "#FFFF66", high = "#CC0033", method = c("pairwise", "spearman"))+
  theme(legend.title = element_text(size = 11))
slope.plot
```

Histogram for Slope



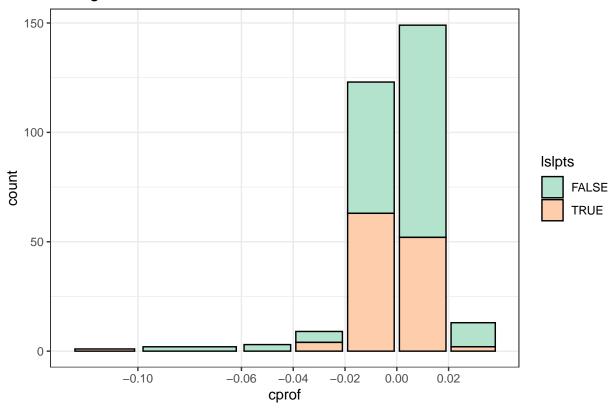
cplan.plot

Histogram for Plan Curvature



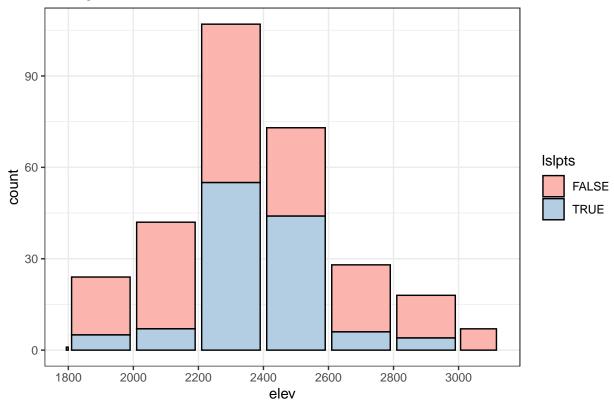
cprof.plot

Histogram for Profile Curvature



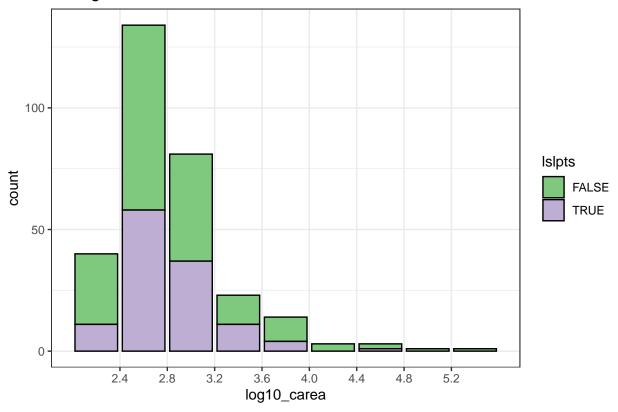
elev.plot

Histogram for Elevation

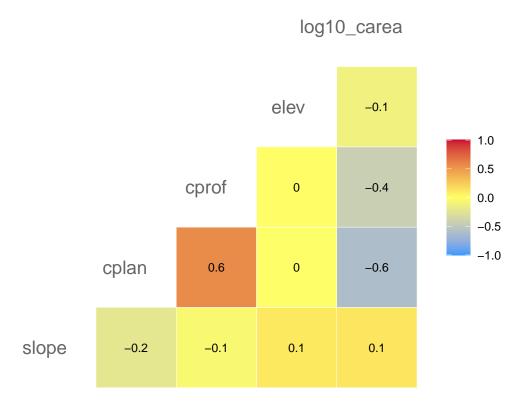


log10_carea.plot

Histogram for Catchment Area



cor_plot



The slope degree ranges from close 0 to more than 60, but most of them lie between 20 to 50, and the data points at the far left end of the x-axis can be considered of the outliers;

The plan curvature ranges from less than -0.6 to greater than 0.1, but most of them lie between -0.1 to 0.1, and the data points at the far right end of the x-axis can be considered of the outliers;

The profile curvature ranges from less than -0.12 to greater than 0.02, but most of them lie between -0.02 to 0.02, the data points at the far right and left end of the x-axis can be considered of the outliers;

The elevation ranges less than 1800 to greater than 3100, but most of them lie between 2300 to 2500, the data points at the far right end of the x-axis can be considered of the outliers; The catchment Area ranges from less than 24 to greater than 5.2, but most of them lie between 2.4 to 3.2, the data points at the far left end of the x-axis can be considered of the outliers; All the parameters are normalized-like distribution.

1.b Outliers

• Sometimes outliers can indicate errors in measurements or other glitch in our data-collection or processing. In the context of modelling and prediction, outliers sometimes drastically impact the fit / bias of the model. Note that loss functions related to squared errors are highly sensitive to outliers.

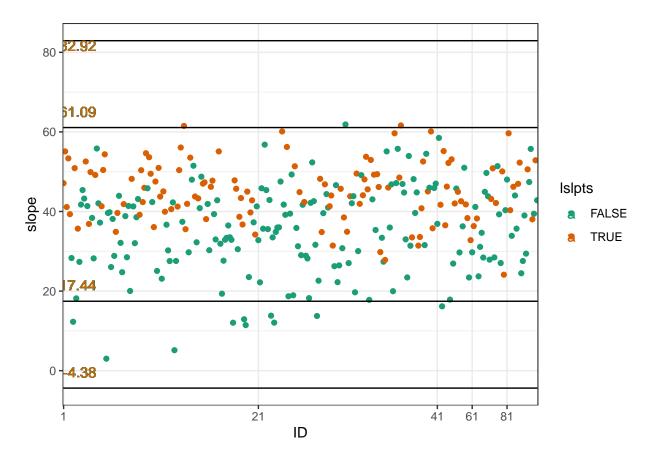
```
# slope
train.slope <- data.frame(landslide.train$slope,landslide.train$lslpts)</pre>
```

```
train.slope <- train.slope %>% mutate(rownames(train.slope))
colnames(train.slope) <- c("slope","lslpts","ID")</pre>
train.slope_plot<-ggplot(train.slope,aes(x = ID, y = slope, color = lslpts))+
  geom_point()+
  scale_x_discrete(breaks=seq(1, 100, by = 20))+
  geom_hline(yintercept = mean(train.slope$slope)+ 2*sd(train.slope$slope))+
  geom text(aes(10,61.09,label = 61.09, vjust = -1))+
  geom hline(yintercept = mean(train.slope$slope)-
               2*sd(train.slope$slope))+
  geom_text(aes(10,17.44,label = 17.44, vjust = -1))+
  geom_hline(yintercept = mean(train.slope$slope)+
               4*sd(train.slope$slope))+
  geom_text(aes(10,82.92,label = 82.92, vjust = 1))+
  geom_hline(yintercept = mean(train.slope$slope)-
               4*sd(train.slope$slope))+
  geom_text(aes(10, -4.38, label = -4.38, vjust = -1))+
  theme_bw()+
  scale_color_brewer(palette = "Dark2")
# cplan
train.cplan <- data.frame(landslide.train$cplan,landslide.train$lslpts)</pre>
train.cplan <- train.cplan %>% mutate(rownames(train.cplan))
colnames(train.cplan) <- c("cplan","lslpts","ID")</pre>
train.cplan_plot < -ggplot(train.cplan, aes(x = ID, y = cplan, color = lslpts))+
  geom point()+
  scale_x_discrete(breaks=seq(1, 100, by = 20))+
        geom_hline(yintercept = mean(train.cplan$cplan)+
               2*sd(train.cplan$cplan))+
  geom_hline(yintercept = mean(train.cplan$cplan)-
               2*sd(train.cplan$cplan))+
  geom_hline(yintercept = mean(train.cplan$cplan)+
               4*sd(train.cplan$cplan))+
  geom_hline(yintercept = mean(train.cplan$cplan)-
               4*sd(train.cplan$cplan))+
  geom_text(aes(10,0.012,label = 0.012, vjust = -2))+
  geom_text(aes(10, -0.13, label = -0.13, vjust = 1))+
  geom_text(aes(10,0.24,label = 0.24, vjust = 1))+
  geom_text(aes(10,-0.26,label = -0.26, vjust = 1))+
  theme_bw()+
  scale_color_brewer(palette = "Set2")
# cprof
train.cprof <- data.frame(landslide.train$cprof,landslide.train$lslpts)</pre>
train.cprof <- train.cprof %>% mutate(rownames(train.cprof))
colnames(train.cprof) <- c("cprof","lslpts","ID")</pre>
train.cprof_plot<-ggplot(train.cprof,aes(x = ID, y = cprof, color = lslpts))+</pre>
  geom_point()+
  scale_x_discrete(breaks=seq(1, 100, by = 20))+
      geom_hline(yintercept = mean(train.cprof$cprof)+
               2*sd(train.cprof$cprof))+
```

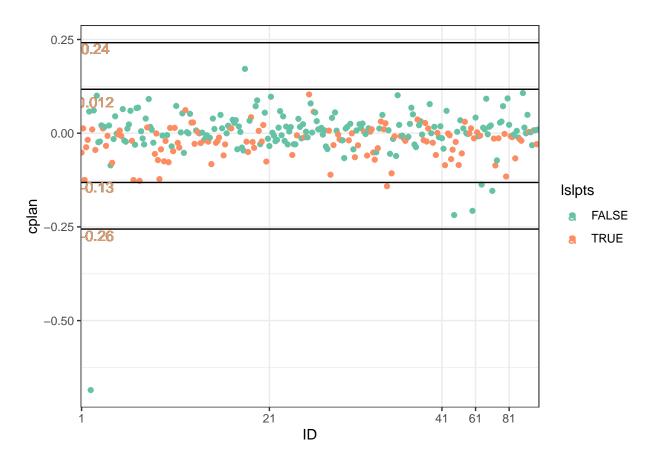
```
geom_hline(yintercept = mean(train.cprof$cprof)-
               2*sd(train.cprof$cprof))+
  geom_hline(yintercept = mean(train.cprof$cprof)+
               4*sd(train.cprof$cprof))+
  geom_hline(yintercept = mean(train.cprof$cprof)-
               4*sd(train.cprof$cprof))+
  geom_text(aes(10,0.03,label = 0.03, vjust = -1))+
  geom text(aes(10,-0.03, label = -0.03, vjust = -1))+
  geom_text(aes(10,0.06,label = 0.06, vjust = 1))+
  geom_text(aes(10,-0.06,label = -0.06, vjust = -1))+
  theme bw()+
  scale_color_brewer(palette = "Set1")
# elev
train.elev <- data.frame(landslide.train$elev,landslide.train$lslpts)</pre>
train.elev <- train.elev %>% mutate(rownames(train.elev))
colnames(train.elev) <- c("elev","lslpts","ID")</pre>
train.elev_plot<-ggplot(train.elev,aes(x = ID, y = elev, color = lslpts))+
  geom_point()+
  scale_x_discrete(breaks=seq(1, 100, by = 20))+
    geom_hline(yintercept = mean(train.elev$elev)+
               2*sd(train.elev$elev))+
  geom_hline(yintercept = mean(train.elev$elev)-
               2*sd(train.elev$elev))+
  geom hline(yintercept = mean(train.elev$elev)+
               4*sd(train.elev$elev))+
  geom_hline(yintercept = mean(train.elev$elev)-
               4*sd(train.elev$elev))+
  geom_text(aes(10,2914,label = 2914, vjust = -1))+
  geom_text(aes(10,1842,label = 1842, vjust = -1))+
  geom_text(aes(10,3450,label = 3450, vjust = 1))+
  geom_text(aes(10,1306,label = 1306, vjust = -1))+
  theme bw()+
  scale_color_brewer(palette = "Accent")
# log10_carea
train.log10_carea <- data.frame(landslide.train$log10_carea,landslide.train$lslpts)
train.log10_carea <- train.log10_carea %>% mutate(rownames(train.log10_carea))
colnames(train.log10_carea) <- c("log10_carea","lslpts","ID")</pre>
train.log_plot<-ggplot(train.log10_carea, aes(x = ID, y = log10_carea, color = lslpts))+
  geom point()+
  scale_x_discrete(breaks=seq(1, 100, by = 20))+
  geom_hline(yintercept = mean(train.log10_carea$log10_carea)+
               2*sd(train.log10_carea$log10_carea))+
  geom_hline(yintercept = mean(train.log10_carea$log10_carea)-
               2*sd(train.log10_carea$log10_carea))+
  geom_hline(yintercept = mean(train.log10_carea$log10_carea)+
               4*sd(train.log10_carea$log10_carea))+
  geom_hline(yintercept = mean(train.log10_carea$log10_carea)-
               4*sd(train.log10_carea$log10_carea))+
  geom_text(aes(10,3.79,label = 3.79, vjust = -1))+
```

```
geom_text(aes(10,1.86,label = 1.86, vjust = -1))+
geom_text(aes(10,4.76,label = 4.76, vjust = 1))+
geom_text(aes(10,0.89,label = 0.89, vjust = -1))+
theme_bw()+
scale_color_brewer(palette = "Dark2")

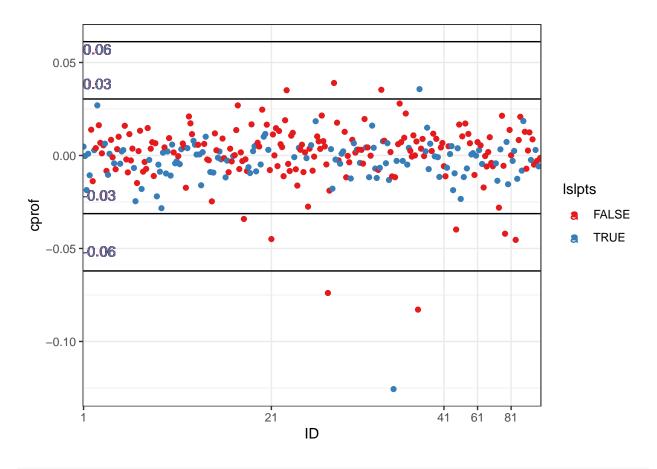
train.slope_plot
```



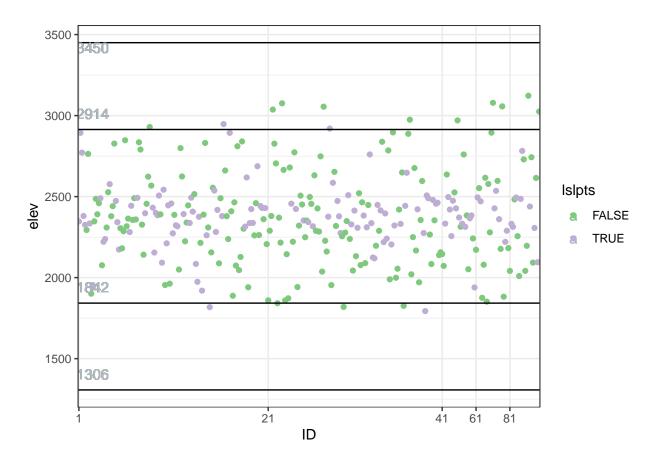
train.cplan_plot



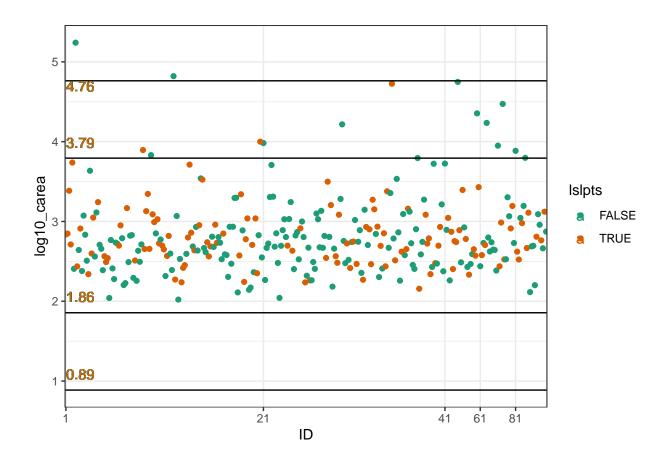
train.cprof_plot



train.elev_plot



train.log_plot



Here we firstly use two standard deviations from the mean which means that 95% values fall inside the of 2 standard deviations, and the values that fall outside are still part of the distribution, but they are unlikely or rare events – outliers.

Then we use four standard deviations from the mean which means that 99.9% values fall inside the of 4 standard deviations, and the values that fall outside are the outliers.

Inputation and capping are different approaches of treating outliers which the former one is replacing the outliers with the mean / median / mode while the later one is replacing the outliers that outside the lower limit with the value of 5th %Inter Quartile Range and those that lie above the upper limit, with the value of 95th %Inter Quartile Range.

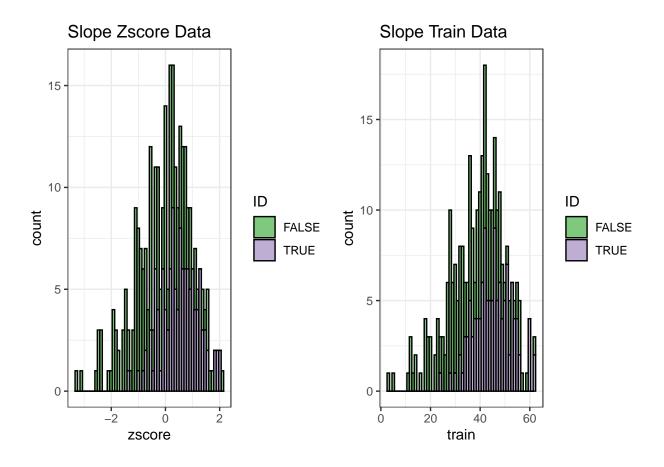
1.c. Normalization and Standardization

```
z_sd = function(x){
  z = c()
  for (i in 1:300) {
    z[i] = (x[i] - mean(x))/sd(x)
  }
  return(z)
}
z.slope <- data.frame(z_sd(landslide.train$slope))
```

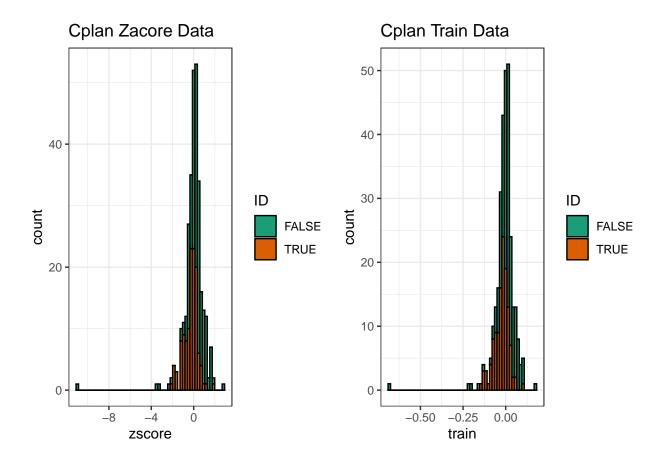
```
z.cplan <- data.frame(z_sd(landslide.train$cplan))</pre>
z.cprof <- data.frame(z_sd(landslide.train$cprof))</pre>
z.elev <- data.frame(z_sd(landslide.train$elev))</pre>
z.log10_carea <- data.frame(z_sd(landslide.train$log10_carea))</pre>
landslide.train.standard <-z.slope %>%
  cbind(z.cplan) %>%
  cbind(z.cprof) %>%
  cbind(z.elev) %>%
  cbind(z.log10 carea)%>%
  cbind(landslide.train$lslpts)
colnames(landslide.train.standard) <-</pre>
  c("z.slope","z.cplan","z.cprof",
    "z.elev", "z.log10_carea", "lslpts")
# tran.slope
train_slope <- data.frame(landslide.train$slope)</pre>
tran.slope <- train_slope %>%
  cbind(z.slope) %>%
  cbind(landslide.train$lslpts)
colnames(tran.slope) <- c("train", "zscore", "ID")</pre>
train.slope.plot <-
  ggplot(data=tran.slope, aes(x = train,fill = ID)) +
  geom_histogram(bins=60,colour = "black", position = "stack") +
  ggtitle("Slope Train Data")+
  scale fill brewer(palette = "Accent")+
  theme bw()
zscore.slope.plot <-
  ggplot(data=tran.slope, aes(x = zscore,fill = ID)) +
  geom_histogram(bins=60,colour = "black", position = "stack") +
  ggtitle("Slope Zscore Data")+
  scale_fill_brewer(palette = "Accent")+
  theme_bw()
# tran.cplan
train_cplan <- data.frame(landslide.train$cplan)</pre>
tran.cplan <- train_cplan %>%
  cbind(z.cplan) %>%
  cbind(landslide.train$lslpts)
colnames(tran.cplan) <- c("train", "zscore", "ID")</pre>
train.cplan.plot <-ggplot(data=tran.cplan, aes(x = train,fill = ID)) +</pre>
  geom_histogram(bins=60,colour = "black", position = "stack") +
  ggtitle("Cplan Train Data") +
  scale_fill_brewer(palette = "Dark2")+
  theme_bw()
zscore.cplan.plot <-ggplot(data=tran.cplan, aes(x = zscore,fill = ID)) +</pre>
  geom_histogram(bins=60,colour = "black", position = "stack") +
  ggtitle("Cplan Zacore Data") +
```

```
scale_fill_brewer(palette = "Dark2")+
  theme_bw()
# tran.cprof
train_cprof <- data.frame(landslide.train$cprof)</pre>
tran.cprof <- train_cprof %>%
  cbind(z.cprof) %>%
  cbind(landslide.train$lslpts)
colnames(tran.cprof) <- c("train", "zscore", "ID")</pre>
train.cprof.plot <-</pre>
  ggplot(data=tran.cprof, aes(x = train,fill = ID)) +
  geom_histogram(bins=40,colour = "black", position = "stack") +
  ggtitle("Cprof Zscore Data") +
  scale_fill_brewer(palette = "Pastel2")+
  theme_bw()
zscore.cprof.plot <-
  ggplot(data=tran.cprof, aes(x = zscore,fill = ID)) +
  geom_histogram(bins=40,colour = "black", position = "stack") +
  ggtitle("Cprof Train Data") +
  scale_fill_brewer(palette = "Pastel2")+
 theme_bw()
# tran.elev
train_elev <- data.frame(landslide.train$elev)</pre>
colnames(z.elev) <- c("zscore")</pre>
colnames(train_elev) <- c("train")</pre>
tran.elev <- train_elev %>%
  cbind(z.elev)%>%
  cbind(landslide.train$lslpts)
colnames(tran.elev) <- c("train", "zscore", "ID")</pre>
zscore.elev.plot <-
  ggplot(data=tran.elev, aes(x = zscore,fill = ID)) +
  geom_bar(colour = "black") +
  scale_x_binned()+
  ggtitle("Elev Zscore Data") +
  scale_fill_brewer(palette = "Set2")+
 theme_bw()
train.elev.plot <-</pre>
  ggplot(data=tran.elev, aes(x = train,fill = ID)) +
  geom_bar(colour = "black") +
  scale_x_binned()+
  ggtitle("Elev Train Data") +
  scale_fill_brewer(palette = "Set2")+
  theme_bw()
# tran.log10_carea
```

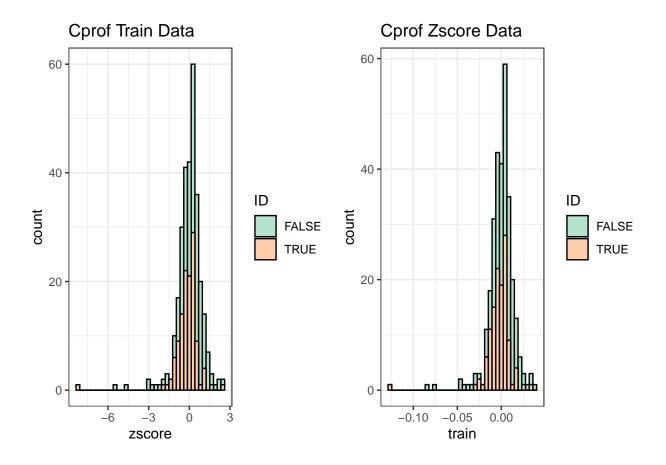
```
train_log10_carea <- data.frame(landslide.train$log10_carea)</pre>
tran.log10_carea <- train_log10_carea %>%
  cbind(z.log10_carea) %>%
  cbind(landslide.train$lslpts)
colnames(tran.log10_carea) <- c("train", "zscore", "ID")</pre>
train.log10 carea.plot <-
  ggplot(data=tran.log10_carea, aes(x = train,fill = ID)) +
  geom_histogram(bins=40,colour = "black", position = "stack") +
  ggtitle("Log10_carea Train Data") +
  scale_fill_brewer(palette = "Set1")+
  theme_bw()
zscore.log10_carea.plot <-
  ggplot(data=tran.log10_carea, aes(x = zscore,fill = ID)) +
  geom_histogram(bins=40,colour = "black", position = "stack") +
  ggtitle("Log10_carea Zscore Data") +
  scale_fill_brewer(palette = "Set1")+
  theme_bw()
# correlation
cor_z_data <- z.slope %>%
  cbind(z.cplan) %>%
  cbind(z.cprof) %>%
  cbind(z.elev) %>%
  cbind(z.log10_carea)
colnames(cor_z_data) <-</pre>
  c("z.slope","z.cplan","z.cprof",
    "z.elev", "z.log10_carea")
cor_z_plot<- ggcorr(cor_z_data,</pre>
                    label = TRUE, label_size = 3, hjust = 0.75, size = 5, color = "grey40",
       low = "#3399FF", mid = "#FFFF66", high = "#CC0033",
       method = c("pairwise", "spearman"))+
  theme(legend.title = element_text(size = 11))
grid.arrange(zscore.slope.plot,train.slope.plot,ncol=2)
```



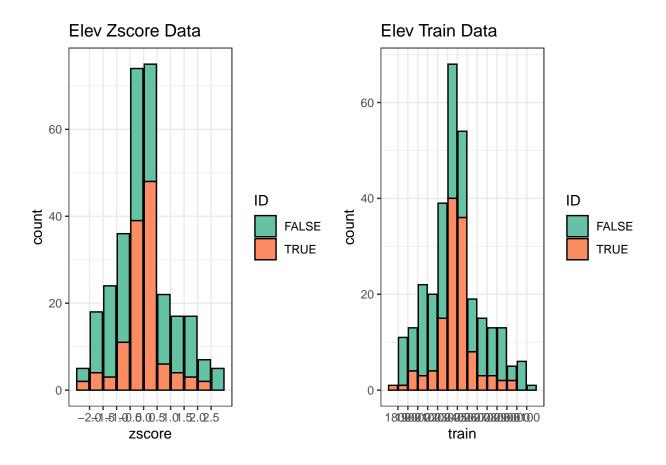
grid.arrange(zscore.cplan.plot,train.cplan.plot,ncol=2)



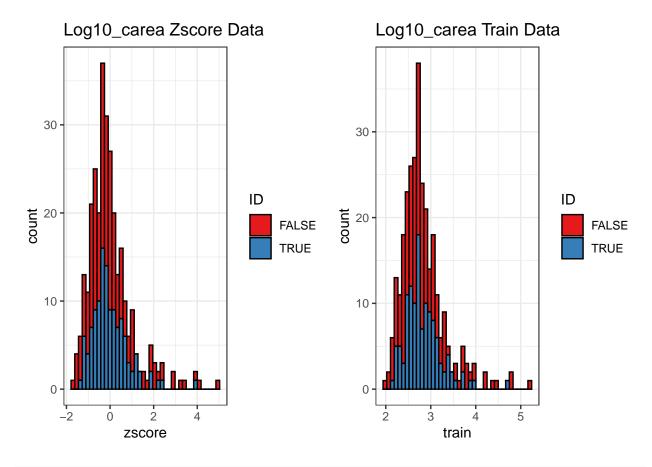
grid.arrange(zscore.cprof.plot,train.cprof.plot,ncol=2)



grid.arrange(zscore.elev.plot,train.elev.plot,ncol=2)



grid.arrange(zscore.log10_carea.plot,train.log10_carea.plot,ncol=2)



cor_z_plot





The data are transformed by Z score standardization which rescales and centers the data so that it has mean value of zero and standard deviation of one. The standardized data represent the distance between that raw data and the population mean in units of the standard deviation. The correlation plot here is the same as the un-normalized one since the correlation of the z-scores is the covariance of the z-scores, which is the covariance of the z-scores, which is just the correlation of the original scores.

2. Model Development - Logistic Regression Prediction

2.a. Original data

```
##
## Call:
## glm(formula = lslpts ~ slope + cplan + cprof + elev + log10_carea,
```

```
##
       family = binomial("logit"), data = landslide.train)
##
  Deviance Residuals:
##
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
##
   -2.6913
           -0.7950 -0.3542
                               0.8372
                                        2.1973
##
## Coefficients:
##
                  Estimate Std. Error z value
                                                        Pr(>|z|)
## (Intercept)
                 1.4683397
                             2.0709912
                                        0.709
                                                         0.47832
## slope
                 0.1206115
                             0.0176921
                                         6.817 0.00000000000928 ***
## cplan
               -17.3536836
                             4.1864977
                                        -4.145 0.00003395832741 ***
## cprof
               -30.1095279
                            10.6154965
                                        -2.836
                                                        0.00456 **
                -0.0007206
                             0.0005725
                                        -1.259
                                                        0.20816
## elev
## log10_carea -1.8460903
                             0.4716705
                                       -3.914 0.00009080195073 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 405.37
                             on 299
                                      degrees of freedom
## Residual deviance: 297.89 on 294 degrees of freedom
## AIC: 309.89
##
## Number of Fisher Scoring iterations: 5
exp(fit.model.train$coefficients)
##
              (Intercept)
                                           slope
                                                                   cplan
## 4.34202010476675326345 1.12818657851853343388 0.00000002906638310999
##
                    cprof
                                            elev
                                                             log10_carea
## 0.0000000000008386837 0.99927965706515098354 0.15785312757486893998
RMSE = function (error) {
  sqrt(mean(error^2)) }
RMSE(fit.model.train$residuals)
## [1] 3.556733
```

The coefficient for slope = 0.1206115, cplan = -17.3536836, cprof = -30.109527, elev = -0.0007206, log10_carea = 1.8460903 which can be interpreted as the expected change in log odds for a one-unit increase in the slope degree/plan curvature/profile curvature/elevation/the decadic logarithm of the catchment area(normalized).

The odds ratio can be calculated by exponentiating these values respectively to get about 1.128, 0.000000029, 0.0000000000000000, 0.999, 0.1579 which means we expect to see

- 1. For every unit change in slope degree, the odds of landslides increase by 1.128,
- 2. For every unit change in plan curvature, the odds of landslides increase by 0.2537602,
- 3. For every unit change in profile curvature, the odds of landslides increase by 0.000000029,
- 4. For every unit change in elevation, the odds of landslides increase by 0.999,
- 5. For every unit change in the decadic logarithm of the catchment area, the odds of landslides increase by 0.1579.

 $odds = probability \ of \ event \ occurence/(1-probability \ of \ event \ occurence)$

2.b. Standardized data

```
fit.model.train.std =glm(formula = lslpts ~ z.slope +
                      z.cplan + z.cprof + z.elev + z.log10_carea,
                    family = binomial('logit'), data = landslide.train.standard)
RMSE = function (error) {
 sqrt(mean(error^2)) }
summary(fit.model.train.std)
##
## Call:
## glm(formula = lslpts ~ z.slope + z.cplan + z.cprof + z.elev +
      z.log10_carea, family = binomial("logit"), data = landslide.train.standard)
##
## Deviance Residuals:
      Min
           1Q
                    Median
                                  3Q
                                          Max
## -2.6913 -0.7950 -0.3542 0.8372
                                       2.1973
## Coefficients:
                Estimate Std. Error z value
                                                    Pr(>|z|)
                          0.1497 -3.919 0.00008887881111 ***
## (Intercept)
                 -0.5865
                             0.1931 6.817 0.00000000000928 ***
## z.slope
                 1.3163
## z.cplan
                 -1.0787
                             0.2602 -4.145 0.00003395832741 ***
## z.cprof
                 -0.4639
                             0.1636 - 2.836
                                                     0.00456 **
                             0.1534 -1.259
## z.elev
                 -0.1930
                                                     0.20816
## z.log10_carea -0.8943
                             0.2285 -3.914 0.00009080195073 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 405.37 on 299 degrees of freedom
## Residual deviance: 297.89 on 294 degrees of freedom
## AIC: 309.89
## Number of Fisher Scoring iterations: 5
RMSE(fit.model.train.std$residuals)
## [1] 3.556733
exp(fit.model.train.std$coefficients)
##
     (Intercept)
                      z.slope
                                    z.cplan
                                                  z.cprof
                                                                 z.elev
##
      0.5562463
                    3.7294812
                                  0.3400519
                                                0.6287955
                                                              0.8244431
## z.log10 carea
      0.4088834
##
```

The coefficient for z.slope = 1.3163, z.plan = -1.0787, z.cprof = -0.4639, z.elev = -0.193, z.log10_carea = -0.8943 which can be interpreted as the expected change in log odds for a one-unit increase in the standardized slope degree/plan curvature/profile curvature/elevation/the decadic logarithm of the catchment area(normalized).

The odds ratio can be calculated by exponentiating these values respectively to get 3.729596, 0.3400519, 0.6287955, 0.8244431, 0.4088834 which means we expect to see

- 1. For every unit change in standardized slope degree, the odds of landslides increase by about 372.95%,
- 2. For every unit change in standardized plan curvature, the odds of landslides increase by 25.37%,
- 3. For every unit change in standardized profile curvature, the odds of lands lides increase by 38.60%,
- 4. For every unit change in standardized elevation, the odds of landslides increase by 45.18%,
- 5. For every unit change in the standardized decadic logarithm of the catchment area, the odds of lands lides increase by 29.02%.

Compare the model fitted with origincal data and the model fitted with standardized data, the RMSE for them are the same.

3. Model Prediction

- Use the logistic model (the one fit to non-normalized data) to predict outcomes on the land-slide.validation data
- Develop a confusion table for landslide occurance, using a threshold of 0.5

```
2
                                       3
                                                    4
                                                                 5
                                                                              6
##
             1
## 0.015205399 0.642192830 0.626146973 0.847935472 0.128946606 0.190975074
##
             7
                          8
                                       9
                                                   10
                                                                11
## 0.004192568 0.132859911 0.914665894 0.470010157 0.301845507 0.821955367
##
            13
                         14
                                      15
                                                   16
                                                                17
                                                                             18
## 0.212911296 0.097767229 0.894608530 0.094267817 0.405685660 0.771971407
##
            19
                         20
                                      21
                                                   22
                                                                23
                                                                             24
```

```
## 0.082682016 0.461349120 0.809469486 0.479803394 0.087846559 0.831491446
##
             25
                          26
                                       27
                                                     28
                                                                  29
                                                                               30
   0.245039974 0.825879134 0.667556821 0.327284088 0.517999876 0.014121483
                          32
                                       33
                                                     34
                                                                  35
##
             31
##
   0.685109275
                0.022388021 0.104502309
                                          0.008182808 0.359755950 0.076519496
                          38
                                       39
##
             37
                                                     40
                                                                  41
   0.637386455 0.053120822 0.726267236 0.673784893 0.051385448 0.296191044
##
             43
                          44
                                       45
                                                     46
                                                                  47
                                                                               48
##
   0.705789069 \ 0.519445405 \ 0.675967340 \ 0.337959417 \ 0.379665044 \ 0.890869448
##
             49
                          50
                                       51
                                                     52
                                                                  53
                                                                               54
                0.457026871 0.136608703 0.587535400 0.585567188
##
   0.765333394
                                                                     0.767548423
             55
                          56
                                       57
                                                     58
                                                                  59
##
                                                                               60
##
   0.359755950 0.727064855 0.670576397 0.220196019 0.807006303 0.742312118
##
                          62
                                       63
                                                     64
                                                                  65
   0.748700399 \ 0.359928023 \ 0.057629760 \ 0.083036269 \ 0.212143107 \ 0.847956137
##
             67
                          68
                                       69
                                                     70
                                                                  71
   0.301845507 \ \ 0.132598708 \ \ 0.481907707 \ \ 0.725289039 \ \ 0.310322716 \ \ 0.442447807 
             73
                          74
                                       75
                                                     76
                                                                  77
                                                                               78
   0.958397958 0.799189864 0.432176386
                                          0.048115719 0.890925017 0.246257746
##
##
             79
                          80
                                       81
                                                     82
                                                                  83
##
   0.858929467 0.398813265 0.618705078 0.521543955 0.361152568 0.089118054
             85
                                                                  89
##
   0.284202556 \ 0.802651580 \ 0.771224586 \ 0.237831971 \ 0.658221510 \ 0.020316410
##
                          92
                                       93
                                                     94
                                                                  95
   0.380753338 0.874128100 0.461909958 0.846559405 0.339320176 0.834511311
                          98
                                       99
                                                    100
## 0.060001336 0.561791709 0.641563173 0.707668405
```

```
confusion.table
```

```
##
##
         0
           1
     0 43 11
##
        8 38
```

```
print("Model accuracy = correct prediction/all prediction = 81%")
```

```
## [1] "Model accuracy = correct prediction/all prediction = 81%"
```

4. Model Selection

- Trial an alternative model, in this case the logistic model with fewer predictor variables has been used since sometimes the model might be overfitting the training data
- Fit the alternative new model to the training data set and predict the response on the validation data-set

```
new.model.train <- data.frame(landslide.train$slope) %>%
  cbind(landslide.train$cplan) %>%
  cbind(landslide.train$cprof) %>%
  cbind(landslide.train$lslpts)
```

```
colnames(new.model.train) <- c("slope","cplan","cprof","lslpts")</pre>
fit.new.model.train = glm(formula = lslpts ~ slope + cplan + cprof,
                          family = binomial('logit'),
                          data = new.model.train)
summary(fit.new.model.train)
##
## Call:
  glm(formula = lslpts ~ slope + cplan + cprof, family = binomial("logit"),
       data = new.model.train)
##
## Deviance Residuals:
##
       Min
                1Q
                     Median
                                   3Q
                                           Max
## -2.2447 -0.8825 -0.3564
                               0.9067
                                        2.1837
##
## Coefficients:
##
               Estimate Std. Error z value
                                                     Pr(>|z|)
## (Intercept) -5.45577
                           0.74988 -7.276 0.00000000000345 ***
## slope
                0.12198
                            0.01746 6.986 0.000000000002828 ***
## cplan
                -8.59963
                            2.88629 -2.979
                                                      0.00289 **
## cprof
               -16.91731 10.07036 -1.680
                                                      0.09297 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 405.37 on 299 degrees of freedom
## Residual deviance: 316.37 on 296 degrees of freedom
## AIC: 324.37
##
## Number of Fisher Scoring iterations: 5
new.model.validation <- data.frame(landslide.validation$slope) %>%
  cbind(landslide.validation$cplan) %>%
  cbind(landslide.validation$cprof) %>%
  cbind(landslide.validation$lslpts)
colnames(new.model.validation) <- c("slope", "cplan",</pre>
                                    "cprof", "lslpts")
pred.landslide.new = predict(fit.new.model.train, newdata=new.model.validation, type="response")
thr.val.new <- ifelse(pred.landslide.new >= 0.5, 1, 0)
table(factor(t(thr.val.new),
             levels =min(new.model.validation$lslpts):
               max(new.model.validation$lslpts)),
      factor(as.numeric(new.model.validation$lslpts),
             levels=min(new.model.validation$lslpts):
               max(new.model.validation$lslpts)))
```

```
## 0 1
## 0 42 15
## 1 9 34
```

```
print("Model accuracy = correct prediction/all prediction = 76%")
```

```
## [1] "Model accuracy = correct prediction/all prediction = 76%"
```

Compared to the previous logistic model using more predictor variables, whose model accuracy is 81%, model precision is 77.5%, model recall is 82.6% and model F1-score is 90.5%, the new alternative model's accuracy, precision, recall and F1-score performances are 76%, 69.39%, 79% and 88.24% respectively, which are all worse than the model from previous problem.

5. Model Evaluation

5.a. Model skill metrics

```
## ## 0 1
## 0 42 15
## 1 9 34

print("Model accuracy = correct prediction/all prediction = 76%")

## [1] "Model accuracy = correct prediction/all prediction = 76%"

print("Model precision = true positives/(true positives + false positives) = 69.39%")

## [1] "Model precision = true positives/(true positives + false positives) = 69.39%")
```

```
print("Model recall = true positives/(true positives + false negatives) = 79%")

## [1] "Model recall = true positives/(true positives + false negatives) = 79%"

print("Model F1-score = (1+1^2)*(precision * recall)/((1^2 * precision) + recall) = 88.24% ")

## [1] "Model F1-score = (1+1^2)*(precision * recall)/((1^2 * precision) + recall) = 88.24% "
```

5.b. Brier Score

• The Brier Score is useful for assessing model performance when predictions are probabilistic.

```
pred.new <-data.frame(pred.landslide.new)
val.new <- data.frame(as.numeric(new.model.validation$lslpts))

B_Score = function(){
   Ts = c()
   for (i in 1:100) {
      Ts[i] = ((pred.new[i,]- val.new[i,]))^2
   }
   Bs = sum(Ts)/100
   return(Bs)
}
B_Score()</pre>
```

[1] 0.1682691

Comments:

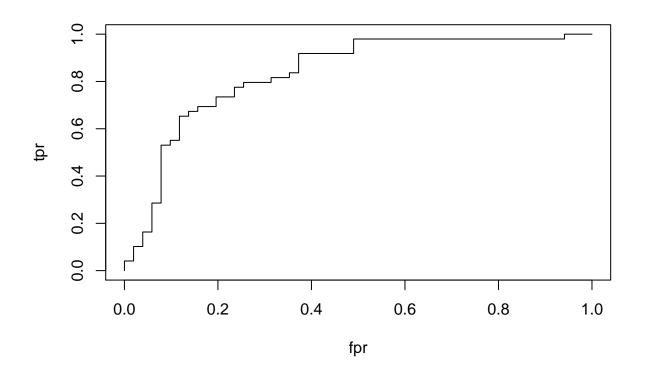
Although smaller scores (closer to zero) in Brier score indicate better forecasts, when model scores in the middle (e.g. 0.44, 0.69) it can be hard to interpret as "good" or "bad". Also, The Brier score becomes inadequate for very rare (or very frequent) events, because it does not sufficiently discriminate between small changes in forecast that are significant for rare events. But, apart from its limitation, the Brier score is still an efficient measure of model skills for our probability forcast model with binary outcomes.

5.c. ROC and AUC

- The ROC curve (receiver operating characteristic curve) is a plot showing the performance of the classification model at all classification thresholds. It is the plot of True Positive Rate (TPR) vs False Positive Rate (FPR) for all thresholds.
- Based on the ROC curve, the Area Under the ROC Curve (AUC) can be calculated. It is a single value which provides an aggregate measure of the performance of the classification model accross all possible classification threshold.

```
[,2]
##
                 [,1]
                                      [,3]
                                                 [,4]
                                                           [,5]
                                                                     [,6]
                                                                                [,7]
## threshold
                    0 0.0100000 0.0200000 0.0300000 0.0400000 0.0500000 0.0600000
                    1 1.0000000 1.0000000 0.9795918 0.9795918 0.9795918 0.9795918
## sensitivity
## 1-specificity
                    1 0.9607843 0.9411765 0.9215686 0.9019608 0.9019608 0.8627451
##
                                 [.9]
                                          [,10]
                                                     [,11]
                                                               [,12]
                 0.0700000 0.0800000 0.0900000 0.1000000 0.1100000 0.1200000
## threshold
## sensitivity
                 0.9795918 0.9795918 0.9795918 0.9795918 0.9795918 0.9795918
  1-specificity 0.8431373 0.8039216 0.7647059 0.7647059 0.7450980 0.6862745
##
                      [,14]
                                [,15]
                                          [,16]
                                                     [,17]
                                                               [,18]
                 0.1300000 0.1400000 0.1500000 0.1600000 0.1700000 0.1800000
## threshold
                 0.9795918 0.9795918 0.9795918 0.9795918 0.9795918 0.9795918
  sensitivity
  1-specificity 0.6470588 0.6470588 0.6470588 0.6274510 0.6274510 0.5882353
##
                      [,20]
                                [,21]
                                          [,22]
                                                     [,23]
                                                               [,24]
                 0.1900000 0.2000000 0.2100000 0.2200000 0.2300000 0.2400000
## threshold
                 0.9795918 0.9795918 0.9795918 0.9591837 0.9591837 0.9591837
   sensitivity
   1-specificity 0.5490196 0.5490196 0.5098039 0.4901961 0.4901961 0.4901961
                      [.26]
                                [,27]
                                          [,28]
                                                     [,29]
## threshold
                 0.2500000 0.2600000 0.2700000 0.2800000 0.2900000 0.3000000
## sensitivity
                 0.9183673 0.9183673 0.9183673 0.9183673 0.9183673 0.9183673
## 1-specificity 0.4901961 0.4509804 0.4313725 0.4313725 0.4313725 0.4313725
##
                      [,32]
                                [,33]
                                          [,34]
                                                     [,35]
                                                               [,36]
                 0.3100000 0.3200000 0.3300000 0.3400000 0.3500000 0.3600000
## threshold
## sensitivity
                 0.9183673 0.9183673 0.8571429 0.8367347 0.8367347 0.8163265
## 1-specificity 0.3921569 0.3725490 0.3725490 0.3529412 0.3529412 0.3529412
##
                      [,38]
                                [,39]
                                          [,40]
                                                     [,41]
                                                               [,42]
                                                                         [,43]
                 0.3700000 0.3800000 0.3900000 0.4000000 0.4100000 0.4200000
## threshold
                 0.8163265 0.8163265 0.7959184 0.7959184 0.7959184 0.7959184
   sensitivity
   1-specificity 0.3333333 0.3137255 0.2745098 0.2745098 0.2745098 0.2549020
##
                      [,44]
                                [,45]
                                          [,46]
                                                     [,47]
                                                               [,48]
  threshold
                 0.4300000 0.4400000 0.4500000 0.4600000 0.4700000 0.4800000
  sensitivity
                 0.7755102 0.7551020 0.7346939 0.7346939 0.7346939 0.7346939
  1-specificity 0.2352941 0.2352941 0.2352941 0.2156863 0.2156863 0.1960784
##
                      [.50]
                                [,51]
                                          [,52]
                                                     [,53]
                                                               [,54]
## threshold
                 0.4900000 0.5000000 0.5100000 0.5200000 0.5300000 0.5400000
## sensitivity
                 0.6938776 0.6938776 0.6734694 0.6734694 0.6734694 0.6530612
## 1-specificity 0.1764706 0.1764706 0.1568627 0.1568627 0.1372549 0.1372549
                      [,56]
                                [,57]
                                                     [,59]
                                                               [,60]
##
                                          [,58]
                                                                          [,61]
## threshold
                 0.5500000 0.5600000 0.5700000 0.5800000 0.5900000 0.6000000
## sensitivity
                 0.6530612 0.6326531 0.6326531 0.6122449 0.6122449 0.6122449
## 1-specificity 0.1176471 0.1176471 0.1176471 0.1176471 0.1176471 0.1176471
                                                                             [,67]
##
                      [,62]
                                [,63]
                                          [,64]
                                                      [,65]
                                                                 [,66]
                 0.6100000 0.6200000 0.6300000 0.64000000 0.65000000 0.66000000
## threshold
```

```
## sensitivity 0.5918367 0.5510204 0.5510204 0.55102041 0.51020408 0.46938776
## 1-specificity 0.1176471 0.1176471 0.1176471 0.09803922 0.07843137 0.07843137
##
                     [,68]
                                [,69]
                                           [,70]
                                                     [,71]
                0.67000000 0.68000000 0.69000000 0.70000000 0.71000000 0.72000000
## threshold
## sensitivity
                0.40816327 0.38775510 0.34693878 0.32653061 0.32653061 0.28571429
## 1-specificity 0.07843137 0.07843137 0.07843137 0.07843137 0.07843137 0.07843137
                     Γ.74]
                                [.75]
                                           [,76]
                                                     [,77]
                                                                Γ.781
                0.73000000 0.74000000 0.75000000 0.76000000 0.77000000 0.78000000
## threshold
## sensitivity
                0.26530612 0.24489796 0.20408163 0.16326531 0.16326531 0.16326531
## 1-specificity 0.05882353 0.05882353 0.05882353 0.05882353 0.05882353 0.03921569
##
                     [,80]
                                [,81]
                                           [,82]
                                                     [,83]
                                                                [,84]
                                                                           [,85]
                0.79000000 0.80000000 0.81000000 0.82000000 0.83000000 0.84000000
## threshold
                0.14285714 0.10204082 0.08163265 0.06122449 0.06122449 0.04081633
## sensitivity
## 1-specificity 0.03921569 0.03921569 0.01960784 0.01960784 0.01960784 0.01960784
##
                                                     [,89] [,90] [,91] [,92]
                     [,86]
                                [,87]
                                           [,88]
## threshold
                0.85000000 0.86000000 0.87000000 0.88000000
                                                           0.89
                0.04081633 \ 0.04081633 \ 0.04081633 \ 0.02040816 \ 0.00
## sensitivity
                                                                   0.0 0.00
0.00
                [,93] [,94] [,95] [,96] [,97] [,98] [,99] [,100] [,101]
##
## threshold
                 0.92 0.93 0.94 0.95 0.96 0.97 0.98
                                                           0.99
                 0.00 0.00 0.00 0.00 0.00 0.00 0.00
## sensitivity
                                                           0.00
                                                                     0
## 1-specificity 0.00 0.00 0.00 0.00 0.00 0.00 0.00
                                                           0.00
                                                                     0
plot(tpr ~ fpr,
    coords(new.Roc, "all", ret = c("tpr", "fpr"), transpose = FALSE,),
    type="1")
```



```
auc(new.Roc)
```

Area under the curve: 0.8339

Comments:

As a thumb rule, we have an excellent classifier if AUC is >=0.9 and a good classifier when it's >=0.8.

The AUC of my new model is 0.83, it means there is 83% chance that the model will be able to distinguish between positives class and negative class, and it is a good classifier.

6.Predict the logistic response (susceptibility of landslide) for a specific site

```
fit.model =glm(formula = lslpts ~ slope +
                       cplan + cprof + elev + log10_carea,
                     family = binomial('logit'), data = landslide.train)
newdata = data.frame(slope=50.15,cplan=0.0028,cprof=0.008, elev=2000,log10 carea=3.202)
predict.new = predict(fit.model,newdata, type="response")
fit.model$coefficients
                           slope
                                          cplan
##
      (Intercept)
                                                          cprof
##
     1.4683397017
                    0.1206115459 - 17.3536835501 - 30.1095278647 - 0.0007206025
##
     log10_carea
   -1.8460902506
thr.val <- ifelse(predict.new >= 0.5, print("landslide"), print("no landslide"))
```

Comments:

[1] "no landslide"

• With the threshold of 0.5, the prediction of the landslide at new site would be negative.

7. Quantifying parameter uncertainty with the bootstrap method

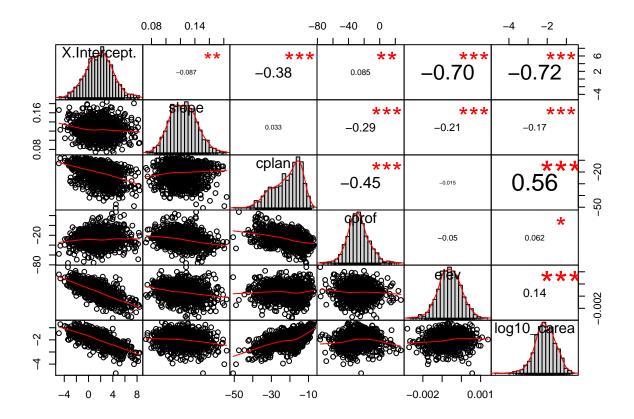
- Parameter uncertainty can be obtained by itteratively fitting a model to a new bootstrap sample numerous times.
- The joint distribution of fitted coefficients generated from the bootstrap samples is a measure of model parameter uncertainty.

Table 1: Descriptive Statistics of Bootstrap

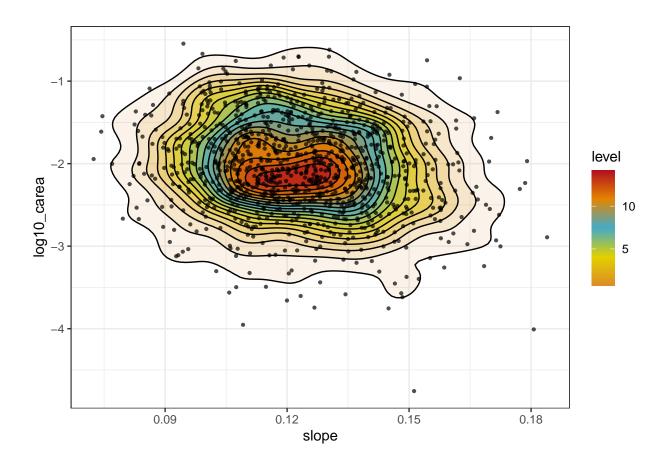
	X.Intercept.	slope	cplan	cprof	elev	log10_carea
mean	1.824189	0.1236007	-21.16199	-28.35183	-0.0006955603	-2.051478
sd	2.135081	0.01923448	8.098713	14.36963	0.0006153951	0.5513765

7.a Quantifying parameter uncertainty

```
boot.strap = function(landslide.train){
  bootsample = list()
  coef.bootsample = list()
  coef.boot = data.frame()
  for (i in 1:1000) {
    bootsample[[i]] =
    landslide.train[sample(1:nrow(landslide.train),
                           size = nrow(landslide.train),replace = T),]
    coef.bootsample[[i]] = data.frame(t(coefficients(glm(formula = lslpts ~ slope +
                       cplan + cprof + elev + log10_carea,
                     family = binomial('logit'), data = bootsample[[i]]))))
    coef.boot = rbind(coef.boot,coef.bootsample[[i]])
  return(coef.boot)
boot.sum <- sapply(boot.strap(landslide.train),function(x)</pre>
  list(mean=format(mean(x),nsmall = 3), sd=format(sd(x),nsmall = 3)))
boot.strap.data <- boot.strap(landslide.train)</pre>
kable(boot.sum,caption = "Descriptive Statistics of Bootstrap")
```



density.boot

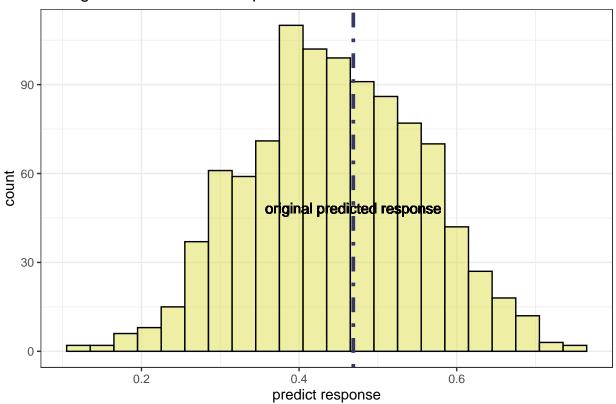


- Compared with the fitted coefficients from previous/orginal model, the mean values of each bootstrap coefficients in this section did change, showing the uncertainty of each of the parameters in this model.
- The level of the geom_density_2d plot is the height at which the 3D "mountains" were sliced while the "height" means the density (the joint distribution in this case), and central region contains the highest density. From the plot we may infer that the region that slope is between 0.10 and 0.15 and log10_carea is between -2.5 and -1.5 contains the highest probability mass, generally meaning that this region contains most of the points (sites).

7.b Prediction uncertainty due to parameter uncertainty

```
family = binomial('logit'), data = bootsample[[i]])
    predict.boot = data.frame(rbind(predict.boot,
                                     predict(fit.boot[[i]],newdata, type="response")))
  }
  return(predict.boot)
predict.data <-data.frame(predict.boot.fun(landslide.train))</pre>
colnames(predict.data) <- c("predict_value")</pre>
his.boot <- ggplot(data=predict.data, aes(x=predict_value))+</pre>
  geom_histogram(binwidth=0.03,color="black",
                 fill = "#E3E36A", alpha = 0.6)+
  theme_bw()+
  ggtitle("Histogram of Predicted Responese")+
  geom_vline(xintercept = predict.new, color = "#353866",
             linetype=4, size=1.3)+
  geom_text(aes(x=predict.new, label="original predicted response", y=50),
            colour="black", angle=0, vjust = 1)+
  xlab("predict response")
his.boot
```

Histogram of Predicted Responese



```
mean(predict.data <0.5)</pre>
```

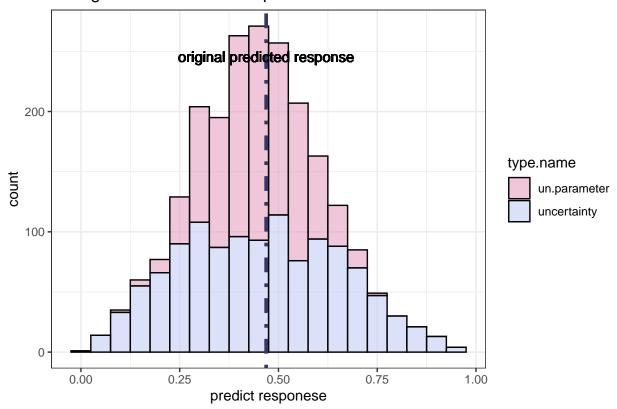
• The threshold of landslide has been set at 0.5 and in this section with the computed susceptibilities of landslide for new site by 1000 bootstramp samples, we have 68% of times predicting it (predict as no-landslide) right.

8.Uncertainty propagation combining input and parameter uncertaintie

- Assume that the measurements at the interested site are uncertain, but the training data have no measurement uncertainty
- Conduct Monte Carlo simulation

```
uncertainty= function(landslide.train){
  bootsample = list()
  fit.boot = list()
  predict.boot = data.frame()
  for (i in 1:1200) {
    newdata[[i]] = data.frame(slope=50.15 + rnorm(1,0,5),
                   cplan=0.0028 + rnorm(1,0,0.01),
                   cprof=0.008 + rnorm(1,0,0.005),
                   elev=2000 + rnorm(1,0,0),
                   log10_carea=3.202 + rnorm(1,0,0.25))
    bootsample[[i]] =
    landslide.train[sample(1:nrow(landslide.train), size = nrow(landslide.train), replace = T),]
    fit.boot[[i]] = glm(formula = lslpts ~ slope +
                       cplan + cprof + elev + log10_carea,
                     family = binomial('logit'), data = bootsample[[i]])
    predict.boot = data.frame(rbind(predict.boot,
                                     predict(fit.boot[[i]],newdata[[i]], type="response")))
  }
  return(predict.boot)
}
predict.uncertainty <-data.frame(uncertainty(landslide.train))</pre>
colnames(predict.uncertainty) <- c("predict_uncertainty")</pre>
colnames(predict.data) <- c("predict_uncertainty")</pre>
type.name<-t(cbind(t(rep("un.parameter",1000)),t(rep("uncertainty",1200))))
colnames(type.name) <- c("type.name")</pre>
predict.all <-rbind(predict.data, predict.uncertainty) %>%
  cbind(type.name)
plot.all<- ggplot(data=predict.all) +</pre>
  geom_histogram(aes(x=predict_uncertainty,fill =type.name),
                 binwidth=0.05, col ="black",alpha = 0.6) +
  scale_fill_manual(values = wes_palette("GrandBudapest2", n = 3))+
```

Histogram of Predicted Responese



```
mean(predict.uncertainty<0.5)</pre>
```

[1] 0.5816667

Comments:

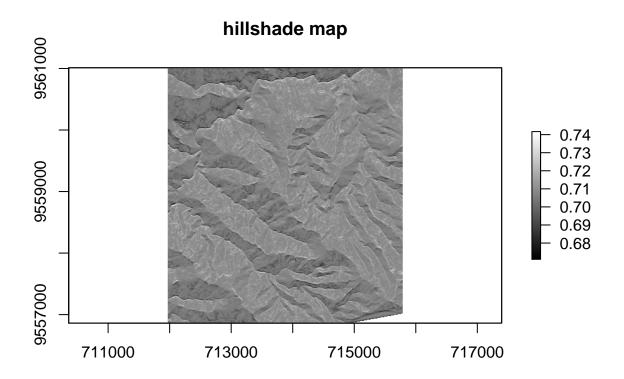
• Compared with the histogram accounting only for uncertainty in model parameters, the histogram accounting for uncertainty in both input variables and model coefficient has higher variance, indicating that its predicted response has higher uncertainty.

However, the mean values of these two are approximately the same and, with the computed susceptibilities of landslide for new site by 1200 bootstramp samples (uncertainty in both input variables and model coefficient), we have 58.92% of times predicting it (predict as no-landslide) right.

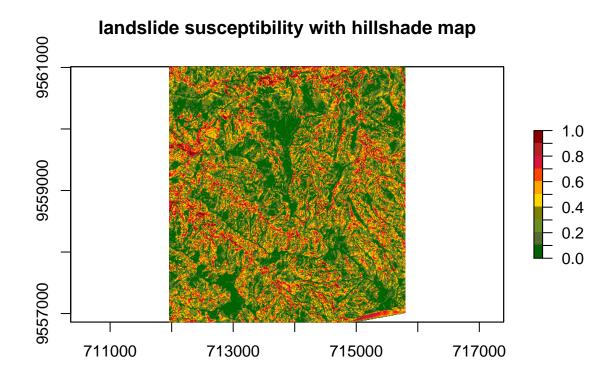
9. Spatial Prediction and Mapping

9.a Computation of terrain variables

```
aspect_ratio = terrain(ta$elev, opt = "aspect")
slope_ratio = terrain((ta$slope)*pi/180, opt = "slope")
hill <- hillShade(slope_ratio, aspect_ratio)
plot(hill, col=grey(0:100/100), legend=TRUE, main='hillshade map')</pre>
```

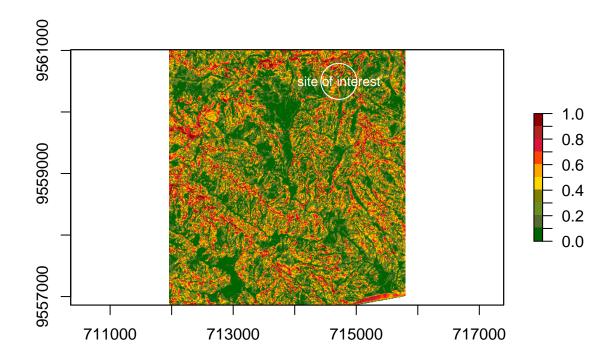


9.b Spatial prediction



9.c Decision making

 \bullet Choose a new site (dev_coordinate) to evaluate its landslide susceptibility and visualize the risk at this site



```
dev_predict

## 1
## 0.1249806

thr.val <- ifelse(dev_predict >= 0.5, print("landslide"), print("no landslide"))

## [1] "no landslide"
```

• The landslide susceptibility of this site is 0.125 and, if we set the threshold as 0.5, then the response indicates that the prediction of landslide is negative. The susceptibility that has been calculated is the probability of landslide occurance, however, the risk of a landslides also depends on its negatively impact on individuals, assets, and/or the environment, which is also uncertain. The uncertain of landslides' negatively impacts in this context may stem from lack of knowledge (e.g.:population density of the interested site) etc., and this can be referred as the epistemic uncertainty.