

Insinöörimatematiikka D Demot 2019

Demo 6 19.2.2018

5.

$$\begin{aligned}y' = y^2 x^3 &\Leftrightarrow \frac{dy}{dx} = y^2 x^3 \\&\Leftrightarrow \frac{1}{y^2} dy = x^3 dx \\&\Leftrightarrow \int \frac{1}{y^2} dy = \int x^3 dx + C \\&\Leftrightarrow -\frac{1}{y} = \frac{1}{4} x^4 + C \\&\Leftrightarrow y = -\frac{4}{x^4} + C, x \neq 0\end{aligned}$$

6.

$$\begin{aligned}y' = x e^{-4} &\Leftrightarrow e^4 dy = x dx \\&\Leftrightarrow \int e^4 dy = \int x dx + C \\&\Leftrightarrow e^4 = \frac{1}{2} x^2 + C \\&\Leftrightarrow y = \ln\left(\frac{1}{2} x^2 + C\right)\end{aligned}$$

7.

$$\begin{aligned}y' = (x+1)(y+1) &\Leftrightarrow \frac{dy}{dx} = (x+1)(y+1) \\&\Leftrightarrow \frac{1}{y+1} dy = (x+1) dx \\&\Leftrightarrow \int \frac{1}{y+1} dy = \int (x+1) dx + C \\&\Leftrightarrow \ln(y+1) = \frac{1}{2} x^2 + x + C \\&\Leftrightarrow y+1 = e^{\frac{1}{2} x^2 + x + C} \\&\Leftrightarrow y = e^{\frac{1}{2} x^2 + x + C} - 1\end{aligned}$$