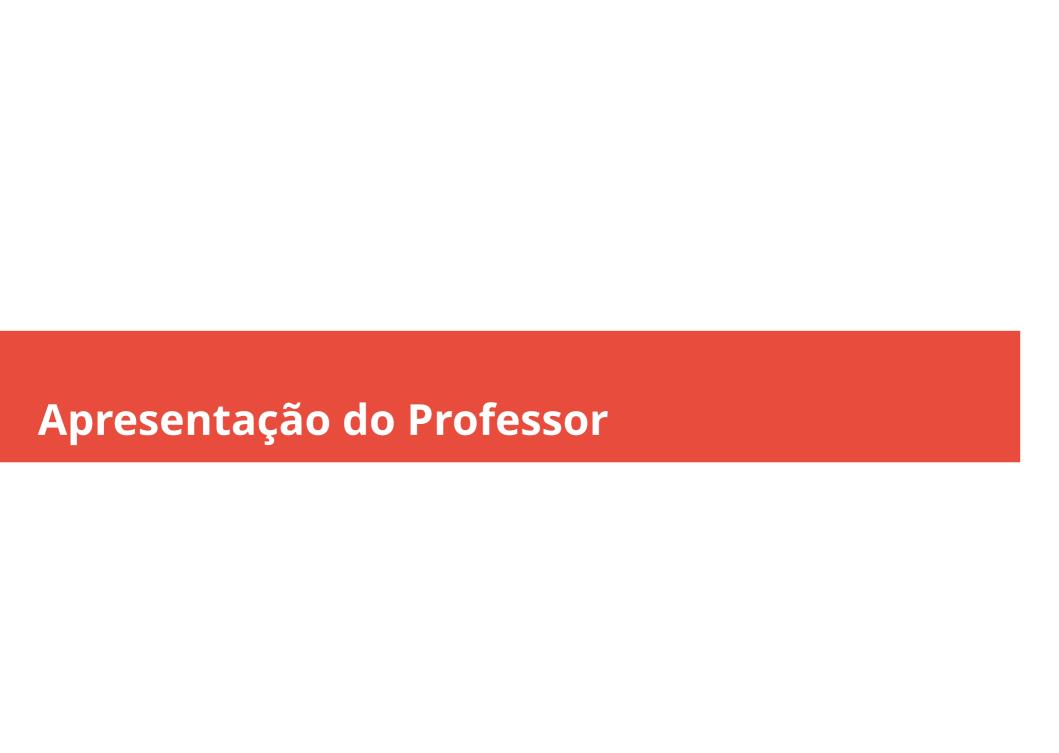
Fundamentos de Algoritmos e Estrutura de Dados

Prof. André Gustavo Hochuli

<u>gustavo.hochuli@pucpr.br</u> <u>aghochuli@ppgia.pucpr.br</u>

Plano de Aula

- Apresentação do Professor
- · Apresentação da Disciplina
 - O que esperar da disciplina?
 - Plano de Ensino
 - Ferramentas
- Tópicos:
 - Complexidade Computacional
 - Introdução a Estrutura de Dados
 - PONTO DE ATENÇÃO: Mesmo para fins pessoais, não é permitido:
 - GRAVAR AÚDIO E VIDEO
 - USAR APLICATIVOS DE ANOTAÇÃO/RESUMO, PRINCIPALMENTE AQUELES BASEADOS EM IA
 - MOTIVO: LGPD



Prof. André Gustavo Hochuli

- · Formação
 - · Ciência da Computação [2004, PUCPR]
 - · Mestre [2007, PPGIA/PUCPR]
 - · Doutor [2018, PPGINF/UFPR]
- · Experiência Profissional
 - P&D em Visão Computacional [2008-2013]
 - · Professor Universitário [2014 Atual]
- · Linhas de Pesquisa
 - Aprendizagem de Máquina
 - Visão Computacional
 - Deep Learning
 - Reconhecimento de Padrões



Hobbies: Aviação Futebol Tecnologia

Handwritten Recognition



Contents lists available at ScienceDirect

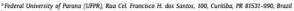
Pattern Recognition

journal homepage: www.elsevier.com/locate/patcog



Handwritten digit segmentation: Is it still necessary?





- b Pontifical Catholic University of Parana (PUCPR), R. Imaculada Conceição, 1155, Curitiba, PR 80215-901, Brazil
- ^cEcole de Technologie Superieure, 1100 rue Notre Dame Ouest, Montreal, Quebec, Canada

ARTICLE INFO

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ABSTRACT

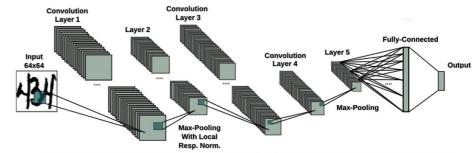
Over the last decades, a great deal of research has been devoted to handwritten digit segmentation. Algorithms based on different features extracted from the background, foreground, and contour of images have been proposed, with those achieving the best results usually relying on a heavy set of heuristics and over-segmentation. Here, the challenge lies in finding a good set of heuristics to reduce the number of segmentation hypotheses. Independently of the heuristic over-segmentation strategy adopted, all algorithms used show their limitations when faced with complex cases such as overlapping digits. In this work, we postulate that handwritten digit segmentation can be successfully replaced by a set of clas-



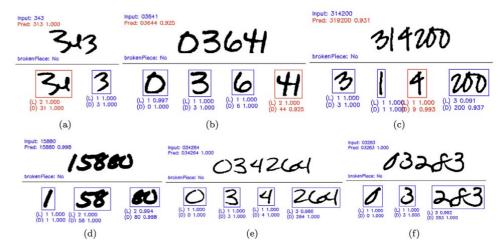
Length	Samples	Britto et al. [2]	Oliveira et al. [19]	Oliveira et al. [18]	Sadri et al. [23]	* Sadri et al. [23]	Gati et a
2	2370	94.8	96.8	97.6	95.5	98.9	99.0
3	2385	91.6	95.3	96.2	91.4	97.2	97.3
4	2345	91.3	93.3	94.2	91.0	96.1	96.5
5	2316	88.3	92.4	94.0	88.0	95.8	95.9
6	2169	89.0	93.1	93.8	88.6	96.1	96.6

314200 03283





Models	Input	Layer 1	Layer 2	Layer 3	Layer 4	Layer 5	Fully Connected	Output
1-Digit	64x64 Binary	Convolution 7x7@3@64	MaxPooling and Local Resp. Norm. 3x3@2@64	Convolution 3x3@1@128	Convolution 3x3@1@32	MaxPooling 3x3@2@32	128	10
2-Digit	64x64 Binary	Convolution 7x7@3@72	MaxPooling and Local Resp. Norm. 3x3@2@72	Convolution 3x3@1@192	Convolution 3x3@1@64	MaxPooling 3x3@2@64	1024	100
3-Digit	64x64 Binary	Convolution 7x7@1@24	MaxPooling and Local Resp. Norm. 2x2@2@24	Convolution 5x5@1@42	Convolution 5x5@1@32	MaxPooling 2x2@2@32	1200	1000



Handwritten Recognition

An End-to-End Approach for Recognition of Modern and Historical Handwritten Numeral Strings

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Universidade Federal do Paraná Curitiba, PR - Brazil lesoliveira@inf.ufpr.br

Luiz E. S. Oliveira

Department of Informatics (DInf)

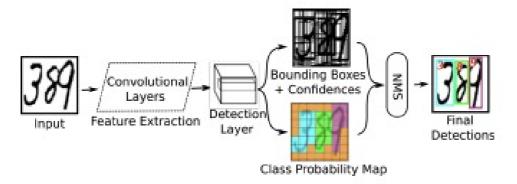
Robert Sabourin

System Engineering Dept. (LIVIA)

École de Technologie Supérieure

Montreal, QC - Canada

robert.sabourin@etsmtl.ca



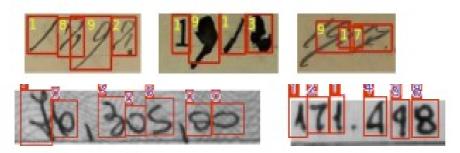


Table V
Comparison of the accuracy (%) on Orand-Car datasets
Reported by [32]

Methods	CAR-A	CAR-B
Tebessa I[31]	37.05	26.62
Tebessa II[31]	39.72	27.72
Hochuli et al.[5]	50.10	40.20
Singapore[31]	52.30	59.30
Pernanbuco[31]	78.30	75.43
Beijing[31]	80.73	70.13
CRNN[33]	88.01	89.79
Saabni[34]*	85	.80
ResNet-RNN[35]	89.75	91.14
ResNet-RNN[32]	91.89	93.79
YoLo	96.20	96.80

* Unified CAR-A and CAR-B datasets

Table VI
BENCHMARK FOR ARDIS DATASET IV (SINGLE DIGITS) OF MODELS ON
DIFFERENT TRAINNING PROTOCOLS (REPORTED BY [1])

	Accuracy (%)			
Method	Case I	Case II	Case III	Case IV
YoLo	87.60	64.10	99.70	99.27
Hochuli et al.[5]	67.20	51.90	83.30	60.55
CNN	58.80	35.44	98.60	99.34
HOG-SVM	56.18	33.18	95.50	98.08
RNN	45.74	28.96	91.12	96.74
kNN	50.15	22.72	89.60	96.63
SVM	43.40	30.62	92.40	96.48
Random Forest	20.12	17.15	87.00	93.12

Parking Lot Monitoring

Evaluation of Different Annotation Strategies for Deployment of Parking Spaces Classification Systems

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(a) UFPR04 (b) UFPR05



Fig. 2. The PKLOT dataset comprises three scenarios named a) UFPR04, b) UFPR05 and c) PUCPR.

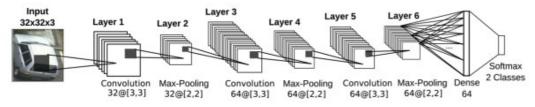


Fig. 1. The 3-convolutional layers architecture used to classify the parking spots.

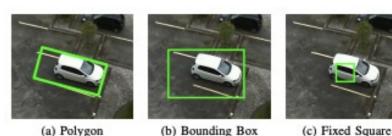


Fig. 3. Types of parking spots location demarcations.

Parking Lot Monitoring

Optimizing Parking Space Classification: Distilling Ensembles into Lightweight Classifiers

Paulo Luza Alves*, André Hochuli[†], Luiz Eduardo de Oliveira*, Paulo Lisboa de Almeida* * Departamento de Informática (DInf), Universidade Federal do Paraná, Curitiba, PR - Brazil {paulomateus,luiz.oliveira,paulorla}@ufpr.br

Abstract-When deploying large-scale machine learning models for smart city applications, such as image-based parking lot monitoring, data often must be sent to a central server to perform classification tasks. This is challenging for the city's infrastructure, where image-based applications require transmitting large volumes of data, necessitating complex network and hardware infrastructures to process the data. To address this issue in image-based parking space classification, we propose creating a robust ensemble of classifiers to serve as Teacher models. These Teacher models are distilled into lightweight and specialized Student models that can be deployed directly on edge devices. The knowledge is distilled to the Student models through pseudo-labeled samples generated by the Teacher model, which are utilized to fine-tune the Student models on the target scenario. Our results show that the Student models, with 26 times fewer parameters than the Teacher models, achieved an average accuracy of 96.6% on the target test datasets, surpassing the Teacher models, which attained an average accuracy of 95.3%.

I. INTRODUCTION

When denloving machine learning models that deal with



Fig. 1. Occupied (red) and empty (blue) parking spaces - PKLot

small-scale deployment with 1,000 cameras. Suppose camera sends a 1280 × 720 pixels JPEG compressed to a central server every 30 seconds. In that case, it will in a transfer of 35 gigabytes of data per hour to the s not accounting for the network's overheads (estimated the PKLot dataset [1]). This data transfer can approxir

Deep Single Models vs. Ensembles: Insights for a Fast Deployment of Parking Monitoring Systems

Andre Gustavo Hochuli* Jean Paul Barddal Graduate Program in Informatics (PPGIa) Pontifícia Universidade Católica do Paraná Pontifícia Universidade Católica do Paraná Curitiba, PR - Brazil {aghochuli, jpbarddal}@ppgia.pucpr.br

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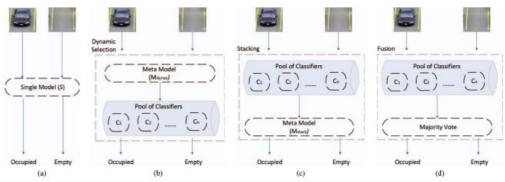


Fig. 1. The proposed strategies assessed for parking lot monitoring systems in cross-dataset scenarios: (a) a single model, and the ensemble-based frameworks named (b) dynamic selection and (c) stacking, and finally (d) the majority vote fusion-based framework.

[†] Programa de Pós-Graduação em Informática (PPGIa), Pontifícia Universidade Católica do Paraná, Curitiba, PR - Brazil aghochuli@ppgia.pucpr.br

Facial Expression Recognition

ORIGINAL ARTICLE



Representation ensemble learning applied to facial expression recognition

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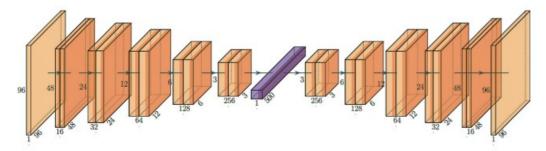
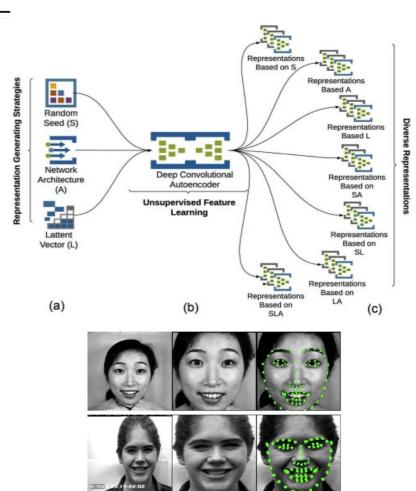


Fig. 3 Default CAE Architecture

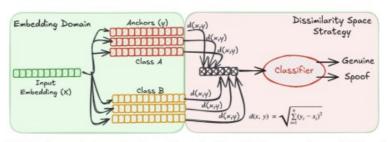


Audio Speaker Verification

A Dissimilarity-Based Countermeasure for Detecting Replay Attacks in Speaker Verification

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similarity Space strategy transforms the embedding (x) by generating a K-dimensional dissimilarity representation, consisting of the Euclidean distances to all anchors $(y_0, ..., y_K)$.

Embedding Domain Anchors (y) d(x,y) d(x,y)

Fig. 3: The Dissimilarity Vectors strategy transforms the embedding (x) into K new representations by calculating the elementwise differences between the input and each of the anchors $(y_0, ..., y_K)$.

A. ASVSpoof 2019 Dataset

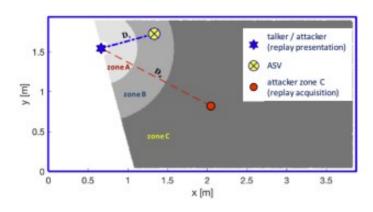




Fig. 4: Proposed Pipeline: a deep architecture performs feature extraction from a MFCC representation, serving as input to the dissimilarity domain.

Plant Species Classification

Combining Muti-Layer Features For Plant Species Classification in a Siamese Network

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TABLE I
CNN AND SNN PERFORMANCE RATES (%) IN FLAVIA AND
MALAYAKEW DATASETS

	Datasets				
Architetures	Fla	via	MalayaKew		
	CNN	SNN	CNN	SNN	
VGG-16	97.9	97.7	90.9	70.8	
MobileNet	99.5	98.8	96.5	84.5	
DenseNet201	98.6	99.4	95.6	82.9	
ResNet50	92.1	74.2	50.2	28.4	
Inception v3	98.2	95.7	87.9	66.8	

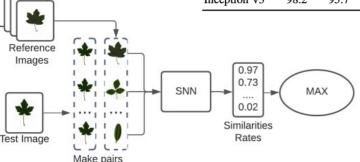


TABLE II PERFORMANCE (%) OF THE SNN WITH MULTI-LAYER FEATURES IN FLAVIA DATASET

VGG-16 Architecture

Intermediate Levens	Entire Vector	Standard (256)		
Intermediate Layers	Concatenate	Concatenate	Add	
FC Layer Only	97.3	-	-	
B5	92.8	95.9	93.3	
B5+B4	96.3	98.4	97.0	
B5+B4+B3	97.0	98.6	98.2	
B5+B4+B3+B2	98.4	98.4	98.2	
B5+B4+B3+B2+B1	97.0	97.2	97.9	

MobileNet Architecture

Intermediate Layers	Entire Vector	Standard (256)		
intermediate Layers	Concatenate	Concatenate	Add	
FC Layer Only	98.7	-	-	
B5	99.3	97.2	99.3	
B5+B4	98.6	98.9	98.4	
B5+B4+B3	98.2	99.4	99.4	
B2+B3+B4+B5	98.0	99.3	99.8	
B1+B2+B3+B4+B5	98.7	98.7	98.2	

DenseNet Architecture

	Entire Vector	Standard (256)		
Intermediate Layers	Concatenate	Concatenate	Add	
FC Layer Only	99.4	-	-	
B5	98.0	99.1	99.5	
B5+B4	98.7	99.4	99.8	
B5+B4+B3	98.9	99.3	100.0	
B2+B3+B4+B5	99.1	99.3	99.4	
B1+B2+B3+B4+B5	99.1	99.8	99.8	

Research Interests

- Medical Image Analysis
- Edge AI
- Federated Learning
- Mixture of Experts
- Domain Adaptation

Rewarding Experiences





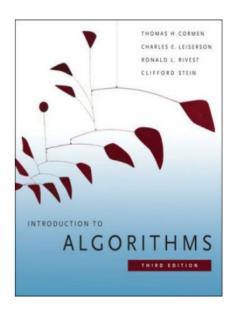


O que esperar da disciplina?

- Abordagem Teórico Prática
- Principais Tópicos em Estrutura de Dados
- Material em Inglês Livros e Artigos
- Resolução de problemas com aplicações no cotidiano computacional
- Espaço para o estudante debater e trazer problemas/dúvidas
- Trabalhos em grupos e avaliações individuais
- Linguagens C e Python

Plano de Ensino

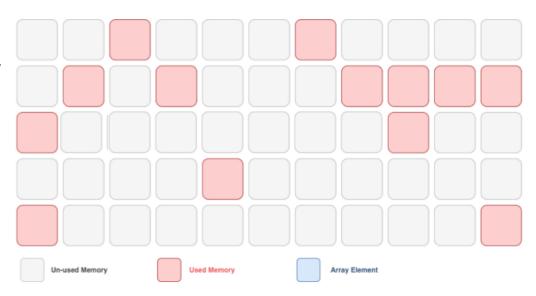
- Introdução e Conceitos Básicos
- Métodos de Ordenação
- Estruturas de Dados Elementares (listas, pilhas, filas)
- Tabela Hash (Hashing)
- Árvores (Binária e AVL) e Métodos de Balanceamento
- Grafos
- Complexidade e Programação Dinâmica
- Avaliação:
 - Trabalhos, Seminários, Avaliações (Provas)
 - Trabalho de Recuperação
- Média: (Trab + Aval) / N
 - N = Qtd Trab + Qtd de Aval





Introdução - Tipos Primitivos

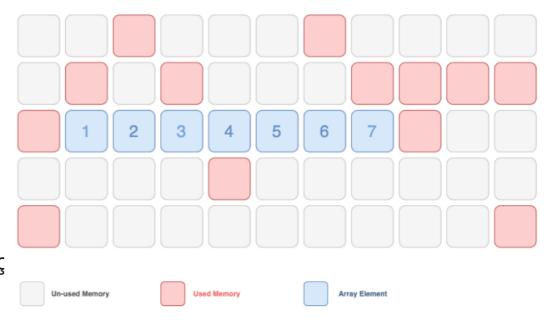
- Tipos de Dados Primitivos
 - Inteiros (int)
 - Ponto Flutuante (float/double),
 - caracteres (char),
 - boleanos (bool).....
- Representação



Dados primitivos (variáveis) vs grandes massas de dados

Introdução - Arrays Estáticos

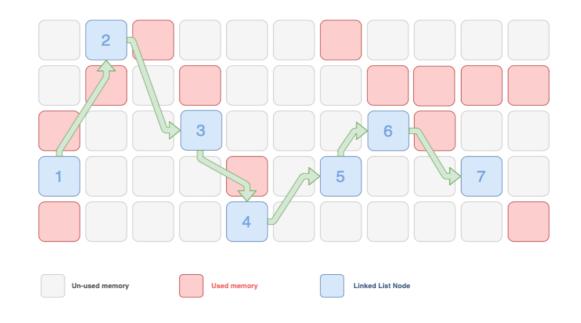
- Arrays Estáticos:
 - Estrutura Indexada
 - Alocação contígua
- Vantagens
 - Acesso é rápido e sequencial
 - Baixo Overhead
 - Requer baixo nível de programaç



- Desvantagem
 - Inviável para grandes massas de dados
 - Fragmentação de mémoria pode impedir a alocação contígua

Introdução - Arrays Dinâmicos

- Arrays Dinâmicos:
 - Não Indexado: Ponteiros garantem o encadeamento sequêncial
 - Alocação não-contígua
- Vantagens
 - Armazenar grandes massas de dados
 - Memória física é o limite
- Desvantagem
 - "Desempenho"
 - Alto Overhead
 - Requer alto nível de programação

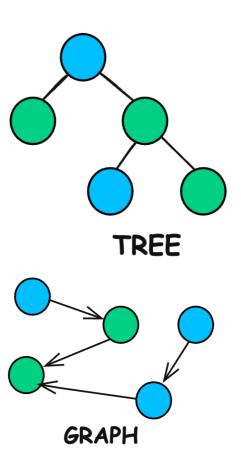


Tradeoff: Time vs Memory Efficiency

Introdução - Topologias

LINEARES Array LINKED LIST QUEUE STACK

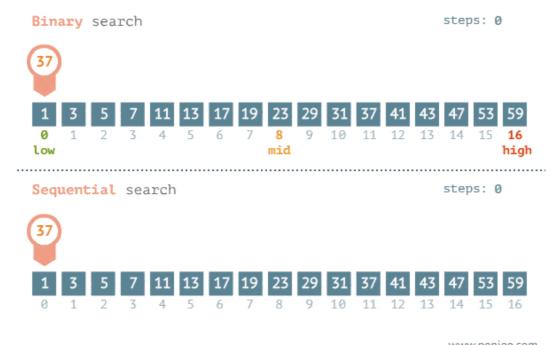
NÃO LINEARES



Tópico 2: Algoritmos de Ordenação e Busca (PARTE 1)

Métodos de Busca

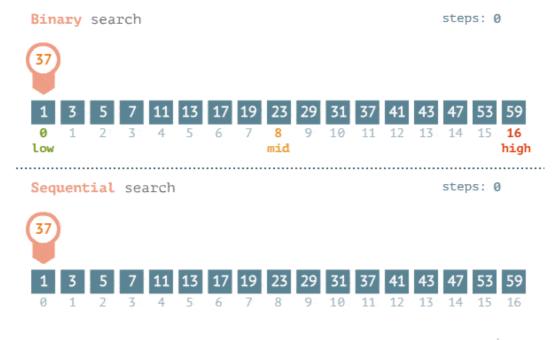
- Encontrar um elemento em um conjunto de dados
- Sequencial ou Linear (arrays ordenados ou não)
- Binária (arrays ordenados)



www.penjee.com

Métodos de Busca

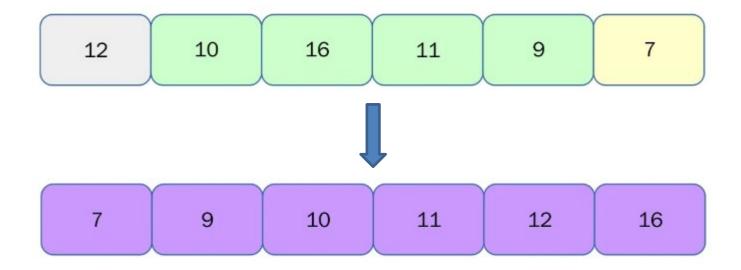
Códificação



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Ordenação

- Organizam os dados
- "Melhoram" a performance de uma busca



Ordenação

BUBBLE SORT

SELECTION SORT

3 2 8 1 5

3 2 8 1 5

INSERTION SORT

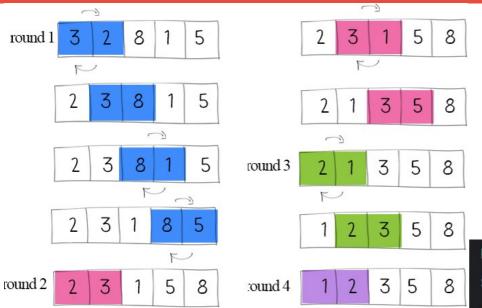
3 2 8 1 5

Ordenação - Bubble Sort

• Pecorre repetidamente trocando elementos adjacentes para ordenar os valores em sequência crescente ou decrescente até que não haja mais trocas.

BUBBLE SORT

Ordenação - Bubble Sort



Lets Code !!! https://shorturl.at/D0JWm

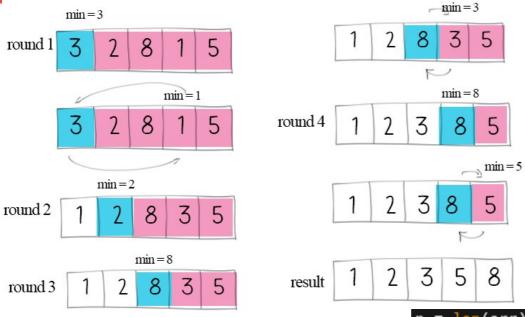
```
n = len(arr)
swap_count = 0
for i in range(n):
    swapped = False
    for j in range(0, n - i - 1):
        if arr[j] > arr[j + 1]:
            arr[j], arr[j + 1] = arr[j + 1], arr[j]
            swapped = True
            swap_count += 1
    if not swapped:
        break
```

Ordenação - Selection Sort

 Percorre o vetor iterativamente, selecionando em cada iteração o menor (ou maior, para ordem decrescente) elemento da sublista não ordenada e trocando-o com o elemento na posição inicial dessa sublista, garantindo a ordenação progressiva do vetor até que todos os elementos estejam posicionados corretamente.

SELECTION SORT

Ordenação - Selection Sort



Lets Code !!!

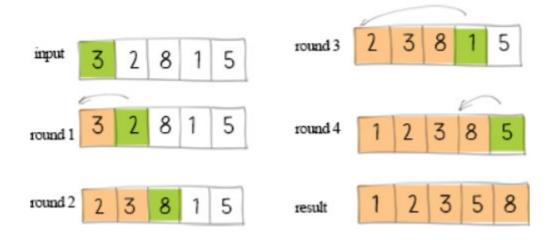
```
n = len(arr)
for i in range(n):
    min_idx = i
    # Encontrar o indice do menor elemento na sublista arr[i:n]
    for j in range(i + 1, n):
        if arr[j] < arr[min_idx]:
            min_idx = j
# Troca o elemento atual com o menor encontrado
    arr[i], arr[min_idx] = arr[min_idx], arr[i]</pre>
```

Ordenação - Insertion Sort

• Percorre iterativamente o vetor a partir do segundo elemento, comparando-o com os elementos anteriores e deslocando-os para a direita até encontrar a posição correta para inserir o elemento atual, garantindo assim a ordenação incremental (crescente ou decrescente) do vetor até que todos os elementos estejam ordenados.

INSERTION SORT

Ordenação - Insertion Sort



Lets Code !!!

```
n = len(arr)
for i in range(1, n):
    key = arr[i]
    j = i - 1
    # Desloca elementos maiores (para ordenação crescente) à direita
    while j >= 0 and arr[j] > key:
        arr[j + 1] = arr[j]
        j -= 1
    arr[j + 1] = key
```

Ordenação

Outros métodos:

- Merge Sort*
- Quick Sort*
- Shell Sort*
- Heap Sort*

• (*) Abordaremos esses algoritmos posteriormente, no contexto de recursão.

Tópico 2: Recursão

Recursão

- Funções que invocam a si mesma (laço)
 - Critério de Parada
 - Incremento ou Decremento

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

    print(i)
    print_rec(i-1) #increment/decrement</pre>
```

Recursão

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

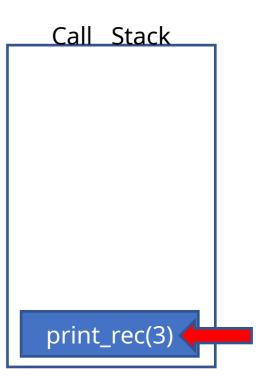
    print(i)
    print_rec(i-1) #increment/decrement

print('main')
print_rec(3) 
print('voltei main')</pre>
```



```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
    print(3)
    print_rec(2) #increment/decrement</pre>
```





Fund. Algoritmos e Estrutura de Dados - Prof. André Hochuli

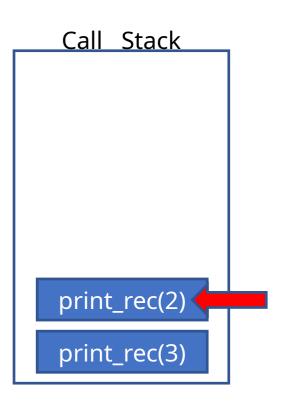
```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return

print(3)
print_rec(2) #increment/decrement

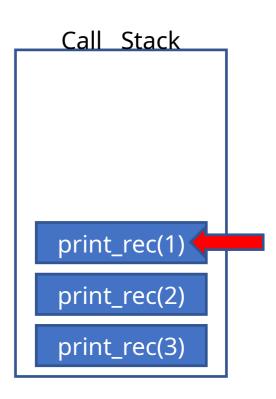
def print_rec(2):
    if (2<=0): #Stop Criteria
        return

print(2)
print_rec(1) #increment/decrement</pre>
```





```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
   print(3)
   print_rec(2) #increment/decrement
               def print_rec(2):
                   if (2<=0): #Stop Criteria
                       return
                  print(2)
                   print_rec(1) #increment/decrement
                                def print_rec(1):
                                    if (1<=0): #Stop Criteria
                                        return
  Main
                                    print(1)
                                    print_rec(0) #increment/decrement
```

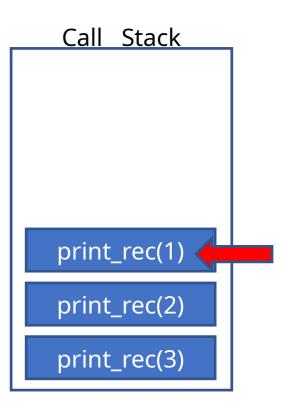


```
def print_rec(3):
   if (3<=0): #Stop Criteria
       return
                                                                                       Call Stack
   print(3)
   print_rec(2) #increment/decrement
              def print_rec(2):
                  if (2<=0): #Stop Criteria
                      return
                                                                                      print_rec(0)
                  print(2)
                  print_rec(1) #increment/decrement
                                                                                      print_rec(1)
                              def print_rec(1):
                                  if (1<=0): #Stop Criteria
                                                                                      print_rec(2)
                                      return
   Main
                                  print(1)
                                                                                      print_rec(3)
                                  print_rec(0) #increment/decrement
                                               def print_rec(0):
                                                   if (0<=0): #Stop Criteria
                                                      return
```

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Aula 01

```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
    print(3)
   print_rec(2) #increment/decrement
               def print_rec(2):
                   if (2<=0): #Stop Criteria
                       return
                   print(2)
                   print_rec(1) #increment/decrement
                                def print_rec(1):
                                    if (1<=0): #Stop Criteria
                                        return
   Main
                                    print(1)
                                    print_rec(0) #increment/decrement
```



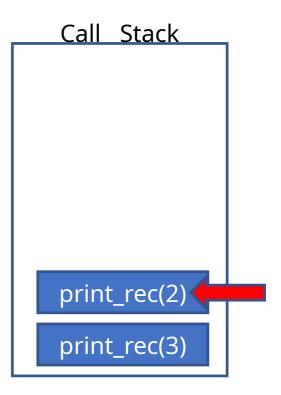
```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return

print(3)
print_rec(2) #increment/decrement

def print_rec(2):
    if (2<=0): #Stop Criteria
        return

print(2)
print_rec(1) #increment/decrement</pre>
```



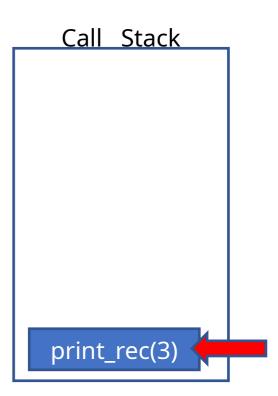


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Aula 01

```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
    print(3)
    print_rec(2) #increment/decrement</pre>
```





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Aula 01

```
def print_rec(i):
    if (i<=0): #Stop Criteria
         return
    print(i)
    print_rec(i-1) #increment/decrement
print('main')
print_rec(3)
print('voltei main')
 Main
 Voltei Main
```

• Qual a diferença entre as duas funções abaixo:

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

    print(i)
    print_rec(i-1) #increment/decrement</pre>
```

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

print_rec(i-1) #increment/decrement
print(i)</pre>
```

• Qual a diferença entre as duas funções abaixo:

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

    print(i)
    print_rec(i-1) #increment/decrement</pre>
```

print(i) executa no empilhamento

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

print_rec(i-1) #increment/decrement
    print(i)</pre>
```

print(i) executa no desempilhamento

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return
    print_rec(i-1) #increment/decrement
    print(i)

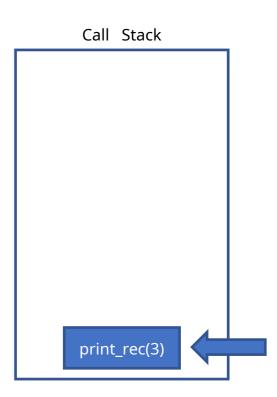
print_rec(3)</pre>
```



```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return

print_rec(2) #increment/decrement
print(3)</pre>
```





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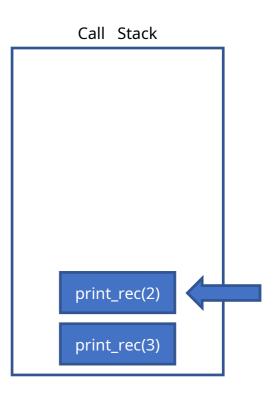
```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return

print_rec(2) #increment/decrement
print(3)

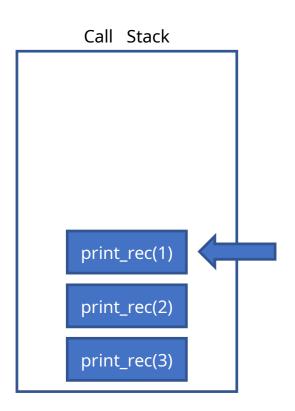
def print_rec(2):
    if (2<=0): #Stop Criteria
        return

print_rec(1) #increment/decrement
print(2)</pre>
```





```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
   print_rec(2) #increment/decrement
    print(3)
              def print_rec(2):
                   if (2<=0): #Stop Criteria
                       return
                   print_rec(1) #increment/decrement
                   print(2)
                                def print_rec(1):
                                    if (1<=0): #Stop Criteria
                                        return
                                    print_rec(0) #increment/decrement
                                    print(1)
```



```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
                                                                                              Call Stack
    print_rec(2) #increment/decrement
    print(3)
               def print_rec(2):
                   if (2<=0): #Stop Criteria
                       return
                                                                                             print_rec(0)
                   print_rec(1) #increment/decrement
                   print(2)
                                def print_rec(1):
                                                                                             print_rec(1)
                                    if (1<=0): #Stop Criteria
                                                                                             print_rec(2)
                                        return
                                    print_rec(0) #increment/decrement.
                                                                                             print_rec(3)
                                    print(1)
                                                 def print_rec(0):
                                                     if (0<=0): #Stop Criteria
                                                          return
```

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```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
    print_rec(2) #increment/decrement
    print(3)</pre>
```

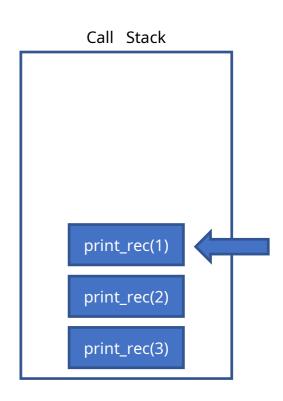
```
def print_rec(2):
    if (2<=0): #Stop Criteria
        return

    print_rec(1) #increment/decrement
    print(2)</pre>
```



```
def print_rec(1):
    if (1<=0): #Stop Criteria
        return

    print_rec(0) #increment/decrement
    print(1)</pre>
```



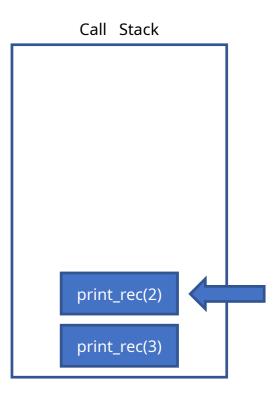
```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return

print_rec(2) #increment/decrement
print(3)

def print_rec(2):
    if (2<=0): #Stop Criteria
        return

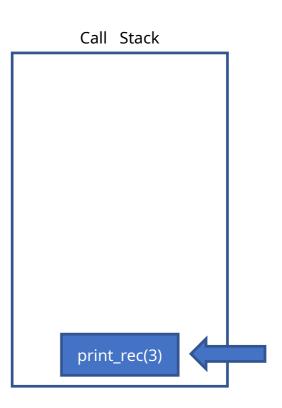
print_rec(1) #increment/decrement
print(2)</pre>
```





```
def print_rec(3):
    if (3<=0): #Stop Criteria
        return
    print_rec(2) #increment/decrement
    print(3)</pre>
```





```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

    print_rec(i-1) #increment/decrement
    print(i)</pre>
```



Recursão - Exercícios

- Implemente uma soma recursiva de 0....N
 - N = 3 | Soma = 3 + 2 + 1 ou 1 + 2 + 3
 - N = 3 | Soma = 5 + 4 + 3 + 2 + 1 ou 1 + 2 + 3 + 4 + 5
- Implemente o Fibonacci Iterativo

Recursão vs Iteração

- Cada situação demanda uma abordagem
- Via de regra, a recursão apresenta *overhead* em relação a iterativa
 - No entanto, veremos que em algumas situações a aplicação de recursão é sugestiva

```
def print_rec(i):
    if (i<=0): #Stop Criteria
        return

print_rec(i-1) #increment/decrement
print(i)</pre>
```

```
def print_iter(i):
    for n in range(i)
        print(n)
```