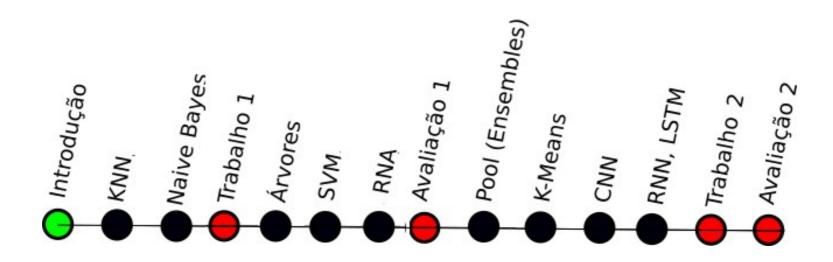
Prof. André Gustavo Hochuli

gustavo.hochuli@pucpr.br
aghochuli@ppgia.pucpr.br
github.com/andrehochuli/teaching

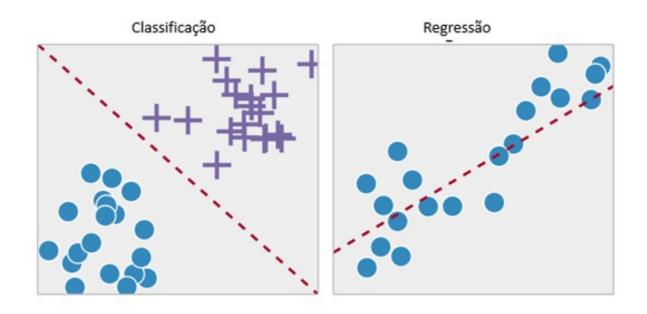
Plano de Aula

- •
- Regressão
- Exercícios



Regressão vs Classificação

- Classificação: Determina uma classe (0,1,2,3)
- Regressão: Determina valores contínuos (preço, clima, vendas, logística, sinais...)

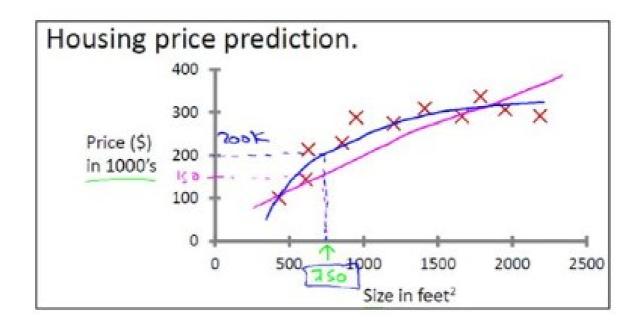


Regressão vs Classificação

Regressão: Compreender a relação entre as características dos dados e a variável dependente (target).

Mapeando X em Y contínuo

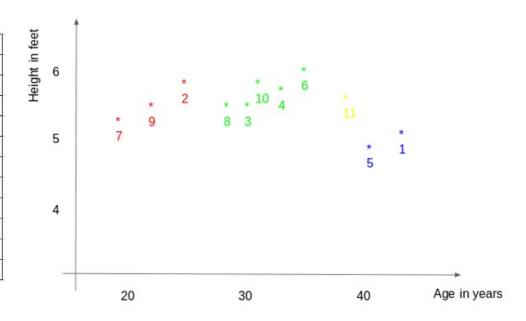
Linear Não Linear



Regressão - KNN

Considere o dataset para determinar o peso de uma pessoa:

ID	Height	Age	Weight	
1	5	45	77	
2	5.11	26	47	
3	5.6	30	55	
4	5.9	34	59	
5	4.8	40	72	
6	5.8	36	60	
7	5.3	19	40	
8	5.8	28	60	
9	5.5	23	45	
10	5.6	32	58	
11	5.5	38	?	



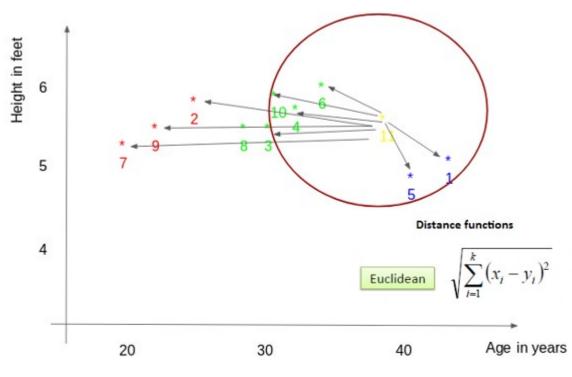
Regressão - KNN

Dado K vizinhos, computa-se a média

$$K=3$$

```
ID11 = (77+72+60)/3
ID11 = 69.66 kg
```

$$K = 50$$



ID	Height	ght Age		Height Age W	
1	5	45	77		
4	5.9	34	59		
5	4.8	40	72		
6	5.8	36	60		
10	5.6	32	58		

Como avaliar o erro?

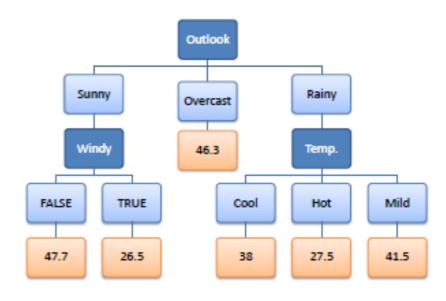
Mean-Square-Error (MSE)

$$ext{MSE} = rac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y_i})^2$$

Height	Age	Weight	Predicted	Diff
5	40	71	69	-2
5.9	23	86	80	-6
4.5	51	65	77	12
5.3	36	89	82	-7
5.1	48	75	67	-8
			MSE	121

Regressão - Árvores

Predictors				Target
Outlook	Temp.	Humidity	Windy	Hours Played
Rainy	Hot	High	Falce	26
Rainy	Hot	High	True	30
Overoast	Hot	High	False	48
Sunny	Mild	High	False	46
Sunny	Cool	Normal	Falce	62
Sunny	Cool	Normal	True	23
Overoast	Cool	Normal	True	43
Rainy	Mild	High	Falce	36
Rainy	Cool	Normal	Falce	38
Sunny	Mild	Normal	False	48
Rainy	Mild	Normal	True	48
Overoast	Mild	High	True	62
Overoast	Hot	Normal	Falce	44
Sunny	Mild	High	True	30



Regressão - Árvores

Determina a homogeneidade pelo do desvio padrão, média e coeficiente de variação

Hours Played
25
30
46
45
52
23
43
35
38
46
48
52
44
30

$$Count = n = 14$$

$$Average = \bar{x} = \frac{\sum x}{n} = 39.8$$



Standard Deviation =
$$S = \sqrt{\frac{\sum (x - \overline{x})^2}{n}} = 9.32$$

Coeffeicient of Variation =
$$CV = \frac{S}{\bar{x}} * 100\% = 23\%$$

Regressão - Árvores

Desvio padrão para dois atributos:

$$S(T, X) = \sum_{c \in X} P(c)S(c)$$

		Hours Played (StDev)	Count
	Overcast	3.49	4
Outlook	Rainy	7.78	5
	Sunny	10.87	5
			14



$$S(Hours, Outlook) = P(Sunny)*S(Sunny) + P(Overcast)*S(Overcast) + P(Rainy)*S(Rainy)$$

= $(4/14)*3.49 + (5/14)*7.78 + (5/14)*10.87$
= 7.66

$$SDR(T, X) = S(T) - S(T, X)$$

Redução do Desvio Padrão

$$SDR(Hours, Outlook) = S(Hours) - S(Hours, Outlook)$$

= $9.32 - 7.66 = 1.66$

O maior SDR é escolhido como raiz

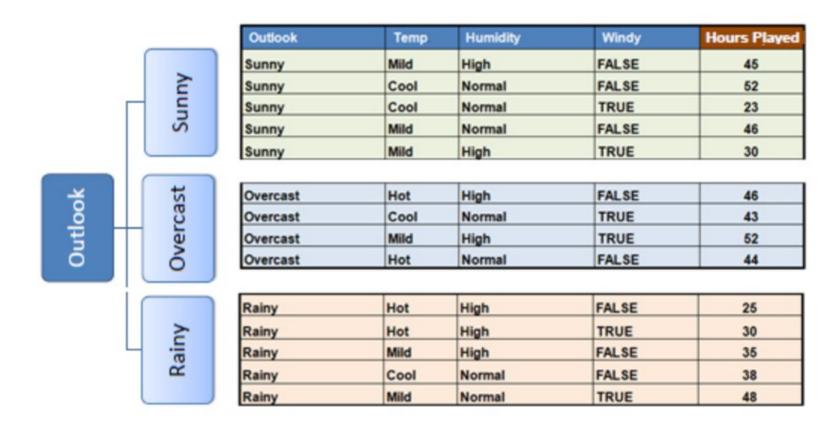
		Hours Played (StDev)	
	Overcast	3.49	
Outlook	Rainy	7.78	
	Sunny	10.87	
SDR=1.66			

		Hours Played (StDev)
n tale	High	9.36
Humidity	Normal	8.37
	SDR=0.28	

		Hours Played (StDev)	
Temp.	Cool	10.51	
	Hot	8.95	
	Mild	7.65	
SDR= 0.48			

		Hours Played (StDev)
Marin de l	False	7.87
Windy	True	10.59
	SDR=0.29)

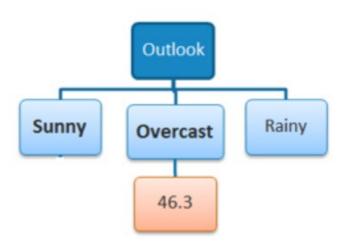
Como escolher o critério de parada?



Considere um limiar de CV < 10% ou count <= 3

Overcast => OK Rainy e Sunny ainda precisam de 'divisões'

		Hours Played (StDev)	Hours Played (AVG)	Hours Played (CV)	Count
Overcast		3.49	46.3	8%	4
Outlook	Rainy	7.78	35.2	22%	5
	Sunny	10.87	39.2	28%	5



Outlook - Sunny

'Windy' é determinante

Major SDR

CV > 8% ou count ≤ 3

Temp	Humidity	Windy	Hours Played
Mild	High	FALSE	45
Cool	Normal	FALSE	52
Cool	Normal	TRUE	23
Mild	Normal	FALSE	46
Mild	High	TRUE	30
			S = 10.87
			AVG = 39.2
			CV = 28%

		Hours Played (StDev)	Count	
T	Cool	14.50	2	
Temp	Mild	7.32	3	

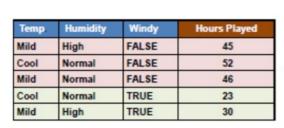
SDR = 10.87-((2/5)*14.5 + (3/5)*7.32) = 0.678

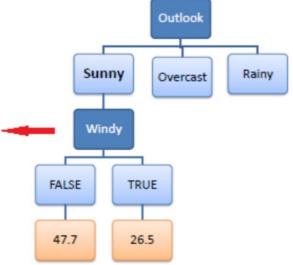
		Hours Played (StDev)	Count
Unmidite	High	7.50	2
Humidity	Normal	12.50	3

SDR = 10.87-((2/5)*7.5 + (3/5)*12.5) = 0.370

		Hours Played (StDev)	Count
Mc-d.	False	3.09	3
Windy	True	3.50	2

SDR = 10.87-((3/5)+3.09 + (2/5)+3.5)=7.62





Outlook - Rainy

Ra	İ	n	y:
			_

'Temp' é determinante

Maior SDR

CV > 8% ou count ≤ 3

Temp	Humidity	Windy	Hours Played
Hot	High	FALSE	25
Hot	High	TRUE	30
Mild	High	FALSE	35
Cool	Normal	FALSE	38
Mild	Normal	TRUE	48
			S = 7.78
			AVG = 35.2
			CV = 22%

		Hours Played (StDev)	Count
	Cool	0	1
Temp	Hot	2.5	2
	Mild	6.5	2

SDR = 7.78 - ((1/5)*0+(2/5)*2.5 + (2/5)*6.5) 4.18

10		Hours Played (StDev)	Count
Humidity	High	4.1	3
	Normal	5.0	2

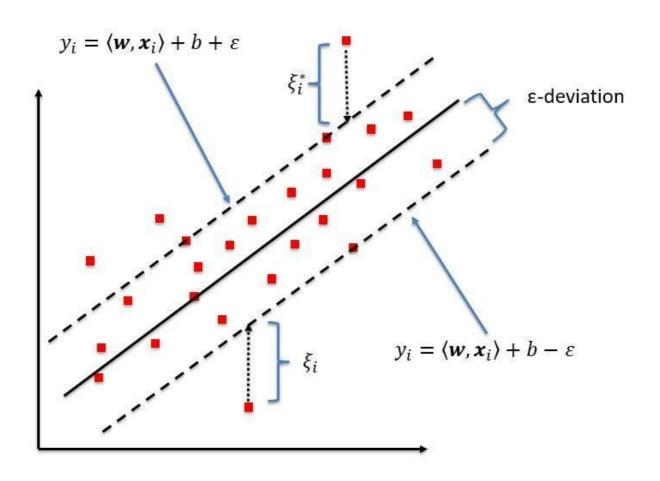
SDR = 7.78 - ((3/5)*4.1 + (2/5)*5.0) = 3.32

÷		Hours Played (StDev)	Count
	False	5.6	3
Windy	True	9.0	2

SDR = 7.78 - ((3/5)*5.6 + (2/5)*9.0) = 0.82

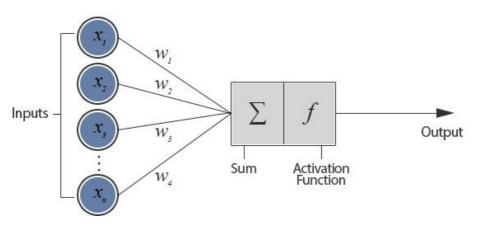
		Outlo	ok	_			
Su	nny	Overcast		Rainy			
		\neg				Temp	Hours Played 38
w	indy	46.3		Temp		Hot	25
	indy	40.3		remp		Hot	30
				三		Mild	35
FALSE	TRUE		Cool	Hot	Mild	Mild	48
47.7	26.5		38	27.5	41.5		

Regressão - SVM

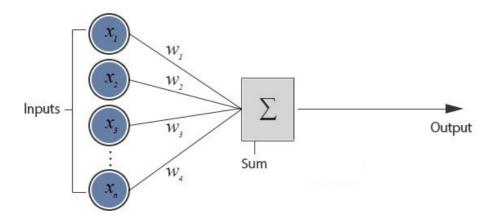


Regressão - MLP

Perceptron - Classificação

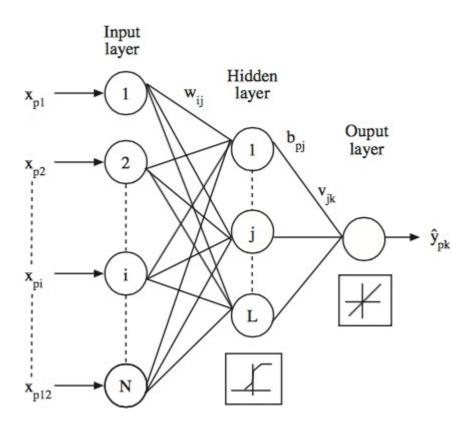


Perceptron - Regressão



Regressão - MLP

MLP - Classificação



Lets Code

Abordaremos a construção dos modelos de regressão utilizando um dataset para prever preços de casas.

Acompanhe e crie sua implementação em conjunto com o professor.

Código base em: <u>Tópico 02 - Regressão.ipynb</u>