

Spectral Clustering in Educational Data Mining

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Spectral Clustering is a graph theoretic technique to represent data in such a way that clustering on this new representation is reduced to a trivial task. It is especially useful in complex datasets where traditional clustering methods would fail to find groupings. In previous work we have shown the utility of using K-means clustering for exploiting structure in the data to affect a significant improvement in prediction accuracy on educational datasets. In this work we show that by using Spectral Clustering we are able to further improve the student performance prediction. We evaluate an educational data mining prediction task: predicting student state test scores from student features derived from a tutor and also explore some other EDM tasks using spectral clustering.

Categories and Subject descriptors: I 2.7 [Artificial Intelligence]

Key Words and Phrases: Educational Data Mining, Intelligent Tutoring Systems, Bootstrap Aggregating, Clustering, Spectral Clustering, Ensemble Learning, Mixture of Experts

1. INTRODUCTION

The highly inter-disciplinary field of Educational Data Mining (EDM) has resulted from a fusion of many different areas, some of which include Machine Learning, Cognitive Science, and Psychology. The main task in EDM is to construct computational models and tools to mine data that originated in an educational setting. With rapidly increasing data repositories from different educational contexts (paper tests, e-learning, Intelligent Tutoring Systems etc.), good practices in EDM can potentially answer important research questions about student learning. This goal of EDM is proving instrumental in combining the knowledge derived from the data to combine with theories from cognitive psychology to formulate the best learning settings and methodologies.

Within data mining, clustering is perhaps one of the most important tools for both exploratory and confirmatory analysis. It is a technique to discern meaningful patterns in unlabeled data. In EDM, clustering has been used in a variety of contexts: Ritter *et al.* In an already influential work essentially used the implicit information compression (albeit lossy) handed by clustering to reduce the Knowledge Tracing parameter space [Ritter 09] without compromising the performance of the system. Dominguez *et al.* used clustering as a tool to generate individualized hints for students [Dominguez 10]. In another

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interesting work, Shih *et al.* employed clustering for unsupervised discovery of student learning tactics [Shih 10]. Clustering has also been used for curriculum planning [Maull 10], for estimating skill set profiles [Nugent 10] amongst numerous other tasks. However, interestingly most of these works employ k-means clustering, expectation maximization based clustering or subspace clustering. This paper aims to introduce to the field of EDM the utility handed by spectral clustering over other clustering algorithms, which is also an easy to implement algorithm with numerous toolboxes available as well [Chen 10].

To understand the weakness of methods such as k-means, a useful way of looking at clustering is the following: Consider a set of K distributions, $\mathcal{D} = \{D_1, D_2 \dots D_K\}$ and that each of these distributions has an associated weight, the collection of which is given by $\{w_1, w_2 \dots w_K\}$ such that $\sum_i w_i = 1$. Consider that a dataset is generated by sampling these K distributions, such that a point might be picked from distribution D_i with probability w_i . The objective of clustering methods is to identify these K distributions given a dataset. Methods such as k-means and Expectation Maximization (EM) are based on estimating explicit models of the data. While k-means finds the clusters by assuming that the set of distributions \mathcal{D} that generated the data was a set of spherical Gaussians, EM algorithms in general learn a mixture of Gaussians with arbitrary shapes. More formally, k-means finds the clusters by minimizing the distortion function:

$$J(c, \mu) = \sum_{i=1}^m \|x^{(i)} - \mu_{c(i)}\|^2 \quad (1)$$

Where μ_c is the cluster centroid to which a point x is assigned. In spite of the great popularity of the k-means algorithm very few theoretical guarantees on its performance are known [Dasgupta 99]. In practice however, k-means performs well on data that at least approximately follows its assumption of being generated by a mixture of well-separated spherical Gaussians [Chaudhuri, Dasgupta 09]. This, coupled with its simplicity makes it a handy tool for a data-miner. However, k-means performs poorly when these assumptions of data generation are not met, which is usually the case. Fig. 1 illustrates this problem by a toy synthetic dataset.

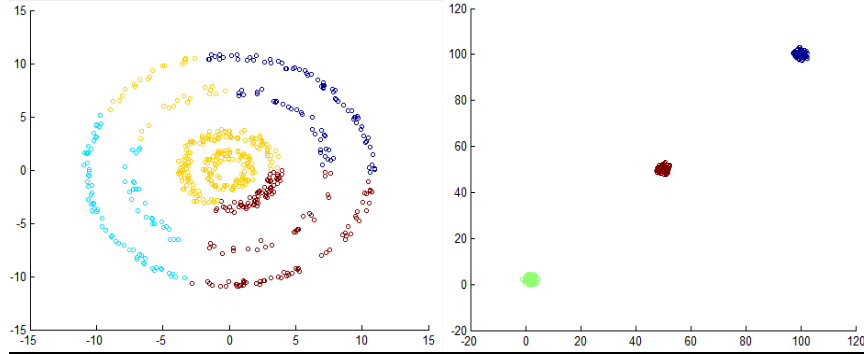


Fig 1: Results of using k-means on synthetic datasets. K-means is unable to identify clusters when the data is distributed in concentric groups (left), while it clearly finds the clusters in well separated and tight spherical Gaussians (right). The clusters identified by the algorithm are indicated by different colors. Both sets have 600 points.

Spectral Clustering makes no such assumptions for data generation and hence usually returns better results.

The rest of the paper is organized as follows: The next section discusses Spectral Clustering. Section 3 uses the spectral clustering method to improve the prediction of

post-test scores employing student features from an Intelligent tutor using a bootstrap aggregating method developed by the authors [Trivedi, Pardos 11] [Trivedi, Pardos 11]. Section 4 is a discussion of results and future work.

2. SPECTRAL CLUSTERING

One of the most important developments in Machine Learning in the past decade has been the use of spectral methods in clustering. They have created a new wave of excitement to understand the problem of clustering and the notion of similarity between points better and formulate it precisely. Therefore it would be good if they are used more widely in EDM.

The broad idea of clustering is essentially to group points that are “similar” in one cluster and points that are “dissimilar” into different clusters. The notion of similarity that is employed in k-means is the Euclidean distance between data points and the cluster centroids to which they are assigned to (which get updated in each iteration). In k-means we work with the data directly, in spectral clustering we work with a representation of the data that encodes the similarities between points better. In a sense, the idea of similarity used in k-means restricts what could be known about the geometry of the data. In spectral clustering the “similarity” is represented in the form of a graph called the similarity graph, represented by $\mathcal{G} = (V, E)$ where V is the set of vertices and E is the set of edges. The idea is that points in the dataset can be represented by a graph with each data point as a vertex of the graph \mathcal{G} and the edges connecting them encoding a notion of similarity $w_{ij} > 0$ between them. Two points are connected in the graph if the similarity or weight between them is either non-zero or above some threshold. The clustering problem can then be re-stated using information from the similarity graph as: We want to find partitions of this graph such that weights between points in the same group are high and those between points in different groups are low. Before talking how we cluster using this representation, we introduce some notation and discuss how the graph \mathcal{G} is used to represent the dataset.

Given the similarity graph \mathcal{G} of n data points $\{s_1, s_2 \dots s_n\}$, there are essentially two things about it that tell us something about the global structure of the data:

1. The degree of a vertex (a data-point in our case): The degree of a vertex tells us the sum of weights of all the edges that originate from a vertex i to all other vertices j . It is given by:

$$d_i = \sum_{j=1}^n w_{ij}$$

The degree matrix of the similarity graph is the diagonal matrix \mathcal{D} with the degrees d_i on the diagonal.

$$D = \begin{pmatrix} d_1 & & & \\ & d_2 & & \\ & & \ddots & \\ & & & d_n \end{pmatrix}$$

Intuitively the degree matrix of a graph tells us how many points each point is connected to (we could connect all points, or choose to connect k-nearest neighbors of each point) and by “how much” (hence the summation of the weights).

2. The weighted similarity matrix or the affinity matrix of the similarity graph, W on the other hand is a representation of similarity between all the points. Each element in the affinity matrix is given by w_{ij} , which is the weight/edge between two points i and j . A common way of representing the weight is:

$$w_{ij} = \exp\left(\frac{-\|s_i - s_j\|^2}{2\sigma^2}\right) \quad (2)$$

Notice that w_{ij} is simply the exponentiated Euclidean distance between two points scaled by a parameter called the scaling or weighing parameter σ . This parameter is to be tuned and varying it changes the weight between points. A point to note is that if all the points are connected then all w_{ij} such that $i \neq j$ will be non-zero values. If points are connected to only their k-nearest neighbors and not every other point, then most of the matrix W will be populated by zeros.

The matrices W and D tell us something about the global structure of the data, but we don't work with them directly. We instead work with the graph Laplacian matrix given by

$$L = D - W$$

The above is the un-normalized version of the Laplacian. There are two normalized versions that are represented as:

$$L_{sym} = D^{-1/2} W D^{-1/2}$$

$$L_{rw} = D^{-1} W$$

The first is called the symmetric Laplacian while the second is called the random-walk Laplacian. The Laplacian in a way combines both the degree and the affinity matrix and also has some mathematically interesting properties (such as being positive semi-definite) that make it easier to work with [Mohar 91]. Since the Laplacian is a representation of the similarity between the data-points, we can now work with it to find groups in the data.

Given the above background, clusters in a dataset can be found by the following method [Ng 01]:

1. For the dataset having n data points, construct the similarity graph \mathcal{G} . The similarity graph can be constructed in two ways: by connecting each data point to the other $n - 1$ data points or by connecting each data point to its k-nearest neighbors. A rough estimate of a good value of the number of nearest neighbors is $\log(n)$. The similarity between the points is given by equation 1. This will give the matrix W .
2. Given the similarity graph, construct the degree matrix D .
3. Using D and W find L_{sym} .
4. Let K be the number of clusters to be found. Compute the first K eigenvectors of L_{sym} . Sort the eigenvectors according to their eigenvalues.
5. If u_1, u_2, \dots, u_K are the top eigenvectors of L_{sym} , then construct a matrix U such that $U = \{u_1, u_2, \dots, u_K\}$.
6. Normalize the rows of the matrix U to be of unit length.
7. Treat the row normalized matrix U as points in a K dimensional space and use k-means to cluster these.
8. Assign a point in the original dataset s_i to cluster K if and only if the i^{th} row of the normalized U is assigned to cluster K

The important point to note is that we don't cluster L directly. We first transform it to find its top K eigenvectors. These being the most important eigenvectors of L , encode the maximum information about it. At the same time, this reduces the dimensionality which without throwing away much information which makes the task of clustering much

easier. To illustrate the power given by this change of representation, we demonstrate it on a toy dataset.

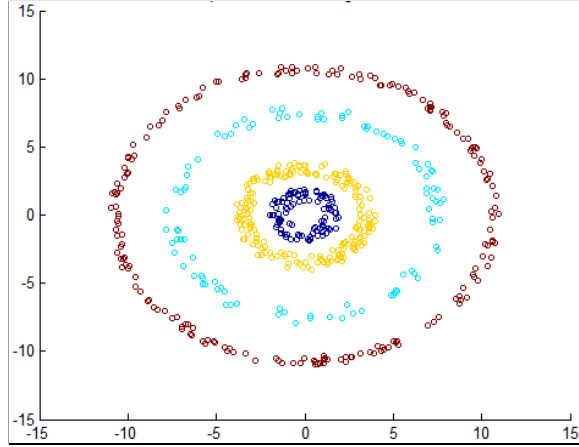


Fig 2: Result of using spectral clustering on a synthetic dataset. This synthetic set has 600 points. The colors indicate the clusters found by spectral clustering. Such groups cannot be found by k-means clustering.

A detailed tutorial that explains various spectral clustering algorithms and some point of views on why it works is by Luxburg [Luxburg 07]. We now discuss a specific application of spectral clustering in EDM.

3. IMPROVING PREDICTION ON STUDENT PERFORMANCE IN POST TESTS

Feng, Heffernan & Koedinger [Feng 09] reported the result that data from an intelligent tutoring system could better predict state test scores (MCAS or Massachusetts State Test Scores in their experiment) if it considered the extra measures collected (called the dynamic features) while providing the students with feedback and help. These extra measures included metrics such as number of hints that students needed to solve a problem correctly and the time it took them to solve it. The paper had a weakness that time was never held constant. Feng & Heffernan go one step ahead and controlled for time in following work [Feng 10]. In that paper, students did half the number of problems in a dynamic test setting (where help was administered by the tutor) as opposed to the static condition (where students received no help). They reported better predictions on the MCAS state test scores by the dynamic condition, but not a statistically reliable difference. This work effectively showed that dynamic assessment led to better predictions on the post test. This prediction was done by fitting a linear regression model on the dynamic assessment features and making predictions on the MCAS test scores. They concluded that while Dynamic Assessment gave good assessment of students, the MCAS predictions made using those features were only marginally statistically significant as compared to the static condition. Trivedi *et al.* [Trivedi 11] investigated further if the dynamic assessment data could be better utilized to increase prediction accuracy over the static condition (and hence establish the superiority of dynamic assessment). They used a newly introduced method [Trivedi 11] that clusters students using the k-means algorithm and uses multiple cluster models and then ensembles the predictions made by each cluster model to achieve a reliable improvement. Here we show that by using spectral clustering we further improve the prediction on the MCAS post-test based on the dynamic features. The improvement obtained by using spectral clustering is not only significant over the static condition, but also over the results obtained using k-means after $K = 3$.

3.1 Data and Methodology

The data used for this study was the same as used by Feng *et al.* [Feng 10] and Trivedi *et al.* [Trivedi 11]. The data is from the 2004-05 school year and was collected using the ASSISTments tutor in two schools in Massachusetts. ASSISTments [Razzaq 05] is an Intelligent Tutoring System developed at Worcester Polytechnic Institute, MA, USA. The data is for 628 students and the features included the various (six) dynamic features [Feng 10]. The prediction made was for the MCAS test scores that was available for the same students in the following year. A fivefold cross validation is done on the dataset.

The methodology used for making the prediction is a new bootstrap aggregation ensemble method [Trivedi, Pardos 11]. The procedure is the following:

1. Cluster the training data into K clusters.
2. For each cluster train a separate linear regression model using the points from that cluster as the training set.
3. Each such trained predictor (such as Linear Regression) represents a model of the cluster and is hence appropriately called a cluster model.

This collection of cluster models that make a prediction on the entire test set is called a prediction model (PM_K the subscript denotes the number of clusters in each Prediction Model). Making a prediction for a test point would involve: Locating the cluster to which the point belongs, and then using the model trained for that cluster to make the prediction for it. This is represented in figure 3 below:

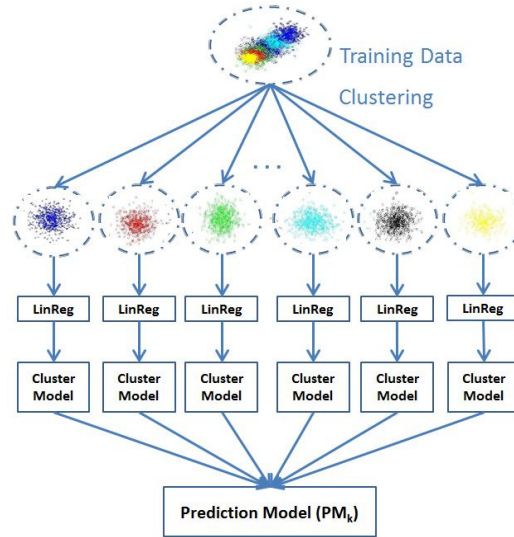


Fig 3: The methodology for using clustering to bootstrap and making a prediction on the training set. The scale of clustering can be varied to generate a number of predictions that can then be aggregated.

However, by using the number of clusters as a free parameter we generate a set of K prediction models, such that each has a different number of cluster models. And thus, we can obtain K different predictions on the test set. These predictions are then averaged to obtain a single strong prediction.

This method can be thought of like an adaptive mixture of local experts [Jacobs, Hinton 91] that uses clustering to bootstrap. But unlike in other bagging methods, which select a random subset to bootstrap, this method has a specific expert for each cluster of the data. By varying the granularity of the clustering we are able to obtain a mixture of

experts on the data at different levels each of which gives a prediction on the test set which are then averaged to get one prediction.

3.2 Results Using Spectral Clustering

The results of clustering the data using both kmeans and spectral clustering are represented in figure 5 below. Since the data is high dimensional and the actual partitions cannot be pictured, this visualization is done by doing a multi-dimensional scaling on the dataset to three dimensions with each cluster identified by a different color.

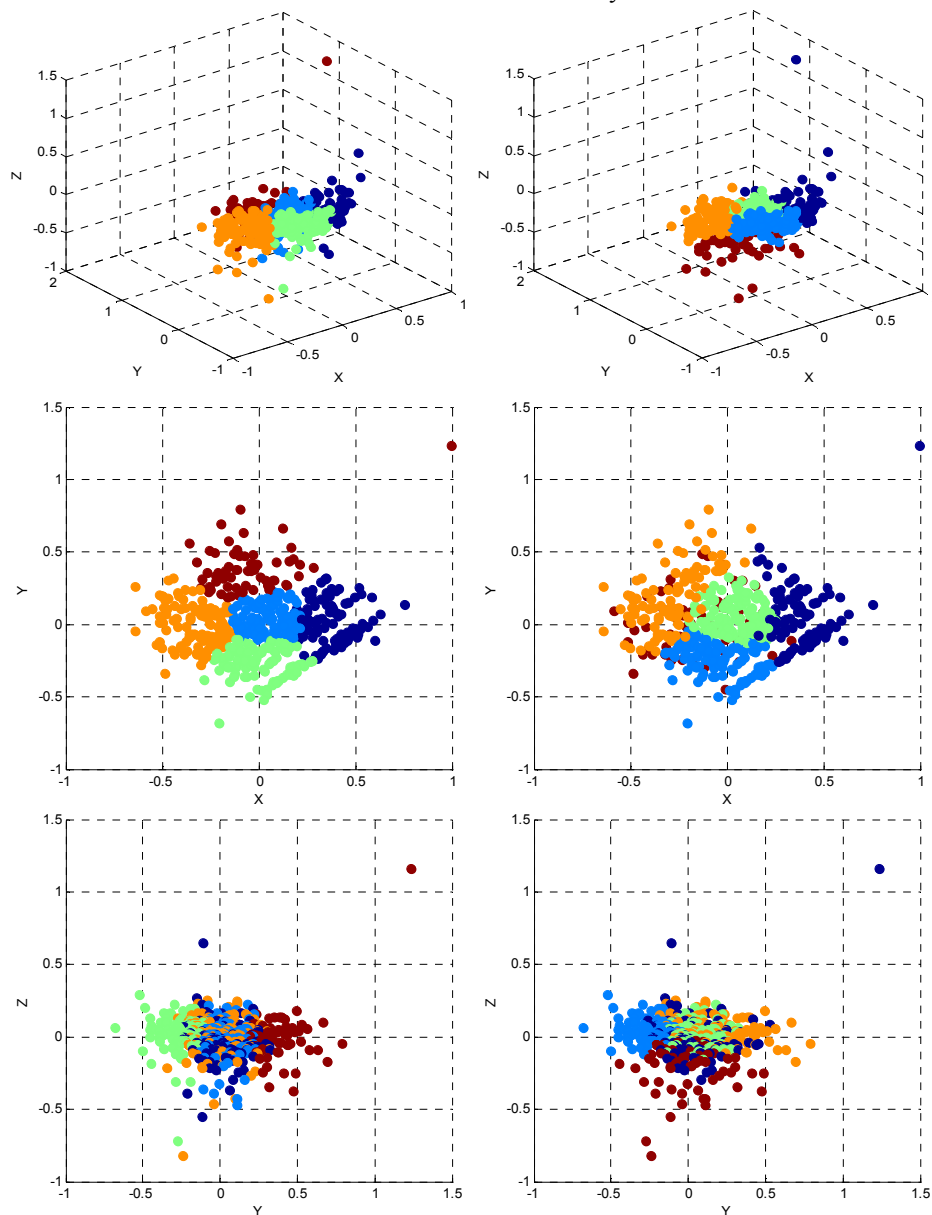


Fig 4: The images on the left column are for k-means clustering and those on the right are the corresponding images for spectral clustering. The top row represents the plot of the ASSISTment data scaled down by multi-dimensional scaling to three dimensions and the clusters identified by both k-means and spectral clustering. The rows below are simply different planar views of the plot in row 1.

The use of spectral clustering gives a significant improvement in prediction accuracy over k-means. The spectral clustering ensemble results are not only significant over the static condition ($K = 1$ in figure 6) but also are significant for the kmeans generated ensemble beyond $K = 3$ with $p < 0.03$ in each case.

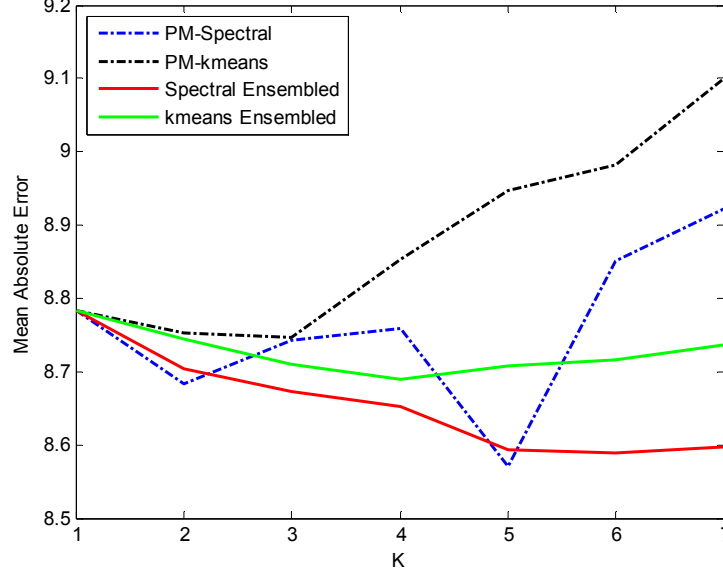


Fig 5: The plots of the 5 fold cross validated errors by the various prediction models (from 1 to $K = 7$) for both kmeans and spectral clustering. The errors of the ensembled predictions for both kmeans and spectral are also shown. The K ensembled prediction is the average of predictions returned by prediction models from 1 to K .

The table below reports the Root Mean Square Error (RMSE) for the same task:

Table 1: The Root Mean Square Errors for the ASSISTment dataset

K	k-means PM_K	Spectral PM_K	k-means ensemble	Spectral ensemble
1 (PM_1)	10.5107	10.5107	10.5107	10.5107
2	10.5431	10.4773	10.4780	10.4391
3	10.5686	10.5171	10.4537	10.4087
4	10.7226	10.5792	10.4225	10.3929
5	10.7739	10.5063	10.4438	10.3434
6	10.8469	10.8057	10.4674	10.3595
7	11.1985	10.9130	10.4966	10.3756

4. CONCLUSION, DISCUSSION AND FUTURE WORK

We employed the methodology described in the paper on some other EDM tasks as well, such as making an in-tutor prediction on the KDD Cup 2010 dataset. The results have been very encouraging. In the same vein, this methodology was also tried on the Performance Factor Analysis (PFA) task [Gong 10], the only difference being that the predictor used to train on each cluster was a logistic regression model. Preliminary work has indicated an improvement in the prediction accuracy. The preliminary results for using this methodology on the PFA task are as follows:

Table 2: Preliminary work on Performance Factor Analysis

AUC	K=1	K=2	K=3	K=4	K=5
Spectral	0.5861	0.6153	0.6252	0.6291	0.6307
Ensemble					

The results indicate an improvement over the base condition as the more prediction models are averaged. But this result is not cross-validated and is a work in progress. Also, given the prohibitive size of the dataset, spectral clustering was not used for all the rows in the training set, but a random subset of them was used. This was done to save time, however this is the reason the detailed results are not reported in this work. Also, more work needs to be done to use spectral clustering methods more efficiently for massive datasets such as the KDD cup dataset.

A very useful way of looking at clustering is essentially as a scheme for lossy data compression. Improvement in prediction accuracy using spectral clustering over k-means indicates that spectral clustering is a better information compression method than k-means and hence tells something deeper about the structure of the data that k-means misses. This would mean an interesting application to reduce the knowledge tracing space like by Ritter *et al* [Ritter 2009] and see how it compares with performance returned by k-means clustering.

The objective of this work was to introduce to the domain of Educational Data Mining the great utility of using spectral clustering methods. We used spectral clustering to enhance the performance of a new ensemble method proposed in an earlier work by the authors. While the objective was to introduce the use of spectral clustering, a very significant result of the work is proving the efficacy of Dynamic Assessment as compared to static assessment. These results show that an Intelligent Tutoring System that can assess as it assists offers a significant advantage to students and teachers. This is because it can not only save time that is wasted on assessment for instruction, but it can also be a better predictor of their performance in post-tests.

The results for the task of predicting the post test scores have been very encouraging; however there are some areas that need further work and could improve prediction accuracy further. One such area of possible improvement is allowing for fuzzy clustering. To make a prediction, the cluster closest to a test point was identified and then the expert for that cluster was used to make a prediction on it. In many real world examples, membership of a data point to a particular cluster is a tricky question to answer. A more realistic view is to allow for fuzzy clustering. That is, given a test point, we determine its probability of occurring in each of the clusters. Then, we can then obtain predictions by the cluster model /expert for each of the clusters and obtain one prediction for one test point that is a weighted average of the predictions returned by each cluster model (earlier a prediction was made on the test point by only one cluster model), with the weights being the probability that the point lies in that cluster. While fuzzy counterparts to the k-means algorithm such as fuzzy c-means are well known, the idea of doing fuzzy spectral clustering is something to be explored. Clearly, spectral clustering uses k-means at a lower dimensional representation of the laplacian and fuzzy c-means can be used at this level. However, the effectiveness of doing the same is not known.

Another possible area of improvement is using methods to merge clusters that are sparsely populated [Cheng 06]. By this method we could improve both the quality of clustering (if the task is purely unsupervised) and prediction accuracy (if the task like in the application discussed is a prediction task).

In this work we combine predictions by averaging them. Clearly this is a sub-optimal choice. Ideally, we would want to pick those predictions (made by prediction models) which are good in prediction and have less correlation with each other (are diverse). Since the method used to make the post-test predictions was an ensemble method, it can be used to combine the predictions themselves. Preliminary work utilizing this idea of using clustering to boot-strap the predictions returned by various prediction models has shown promise.

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