

CSCI-UA 472 Artificial Intelligence

Muhammad Wajahat Mirza

mwm356@nyu.edu

Homework 08

December 1, 2020

Problem 1

Solution to A

Consider the following PCFG in Chomsky Normal Form:

$S \rightarrow NP VP$ [0.6]
 $S \rightarrow Noun VP$ [0.3]
 $S \rightarrow NP Verb$ [0.1]
 $NP \rightarrow Adj Noun$ [0.7]
 $NP \rightarrow AdjList Noun$ [0.3]
 $VP \rightarrow Verb Noun$ [0.5]
 $VP \rightarrow Verb NP$ [0.3]
 $VP \rightarrow Verb Adv$ [0.2]
 $AdjList \rightarrow Adj Adj$ [1.0]

Lexicon:

$Noun \rightarrow \text{"fast"}$ [0.1]
 $Noun \rightarrow \text{"fish"}$ [0.6]
 $Noun \rightarrow \text{"swim"}$ [0.2]
 $Verb \rightarrow \text{"fast"}$ [0.1]
 $Verb \rightarrow \text{"fish"}$ [0.8]
 $Verb \rightarrow \text{"long"}$ [0.1]
 $Verb \rightarrow \text{"swim"}$ [0.6]
 $Adj \rightarrow \text{"fast"}$ [0.5]
 $Adj \rightarrow \text{"long"}$ [0.5]
 $Adv \rightarrow \text{"fast"}$ [0.8]
 $Adv \rightarrow \text{"long"}$ [0.2]

A. Trace the workings of the CYK algorithm on the sentence “long fast fish swim” in the style of the example on the course web site.

B. What are the two possible parse trees for this sentence?

Solution to Problem 1

Solution to A:

Iterations of line 4

Create the following leaves:

i=1

A. [Verb | 1 | 1 | long | ---- | --- | 0.1]
B. [Adj | 1 | 1 | long | ---- | --- | 0.5]
C. [Adv | 1 | 1 | long | ---- | --- | 0.2]

i=2

D. [Noun | 2 | 2 | fast | ---- | --- | 0.1]
E. [Verb | 2 | 2 | fast | ---- | --- | 0.1]
F. [Adj | 2 | 2 | fast | ---- | --- | 0.5]
G. [Adv | 2 | 2 | fast | ---- | --- | 0.8]

i=3

H. [Noun | 3 | 3 | fish | ---- | --- | 0.6]
I. [Verb | 3 | 3 | fish | ---- | --- | 0.8]

i=4

J. [Noun | 4 | 4 | swim | ---- | --- | 0.2]
K. [Verb | 4 | 4 | swim | ---- | --- | 0.6]

length=2

i=1

j=2

M=NP

k=1

Create node L. [NP | 1 | 2 | --- | --- | --- | 0]

Rule NP → Adj Noun [0.7]

Combination of B & D and prob of rule has probability $0.5 * 0.1 * 0.7 = 0.035$

Change L to be [NP | 1 | 2 | --- | B | D | 0.035]

M=VP

k=1

Create node M. [VP | 1 | 2 | --- | --- | --- | 0]

Rule VP → Verb Noun [0.5]

Combination of A & D and prob of rule has probability $0.1 * 0.1 * 0.5 = 0.005$
Change M to be [VP | 1 | 2 | --- | A | D | 0.005]

Rule VP → Verb Adv [0.2]

Combination of A & G and prob of rule has probability $0.1 * 0.8 * 0.2 = 0.016$

Change M to be [VP | 1 | 2 | --- | A | G | 0.016]

M=AdjList

k=1

Create node N. [AdjList | 1 | 2 | --- | --- | --- | 0]

Rule AdjList → Adj Adj [1.0]

Combination of B & F and prob of rule has probability $0.5 * 0.5 * 1.0 = 0.25$

Change N to be [AdjList | 1 | 2 | --- | B | F | 0.25]

i=2

j=3

M=NP

k=1

Create node O. [NP | 2 | 3 | --- | --- | --- | 0]

Rule NP → Adj Noun [0.7]

Combination of F & H and prob of rule has probability $0.5 * 0.6 * 0.7 = 0.21$

Change O to be [NP | 2 | 3 | --- | F | H | 0.21]

M=VP

k=1

Create node P. [VP | 2 | 3 | --- | --- | --- | 0]

Rule VP → Verb Noun [0.5]

Combination of E & H and prob of rule has probability $0.1 * 0.6 * 0.5 = 0.03$

Change P to be [VP | 2 | 3 | --- | E | H | 0.03]

i=3

j=4

M=VP

k=1

Create node Q. [VP | 3 | 4 | --- | --- | --- | 0]

Rule VP → Verb Noun [0.5]

Combination of I & J and prob of rule has probability $0.8 * 0.2 * 0.5 = 0.08$

Change Q to be [VP | 1 | 2 | --- | I | J | 0.08]

length=3

i=1

j=3

M=S

k=1

No rules apply.

k=2

Create node R. [S | 1 | 3 | --- | --- | --- | 0]

Rule $S \rightarrow NP \text{ Verb}$ [0.1]
 Combination of L & I and prob of rule has probability $0.035 * 0.8 * 0.1 = 0.0028$
 Change R to be [S | 1 | 3 | --- | L | I | 0.0028]

M=NP

k=1
 No rules apply.

k=2
 Create node S. [NP | 1 | 3 | --- | --- | --- | 0]
 Rule $NP \rightarrow \text{AdjList Noun}$ [0.3]
 Combination of N & H and has probability $0.25 * 0.6 * 0.3 = 0.045$
 Change S to be [NP | 1 | 3 | --- | N | H | 0.045]

M=VP

k=1
 Create node T. [VP | 1 | 3 | --- | --- | --- | 0]
 Rule $VP \rightarrow \text{Verb NP}$ [0.3]
 Combination of A & 0 and has probability $0.1 * 0.21 * 0.3 = 0.0063$
 Change T to be [VP | 1 | 3 | --- | A | 0 | 0.0063]

i=2

j=4

M=S

k=1
 Create node U. [S | 2 | 4 | --- | --- | --- | 0]
 Rule $S \rightarrow \text{Noun VP}$ [0.3]
 Combination of D & Q and has probability $0.1 * 0.08 * 0.3 = 0.0024$
 Change U to be [S | 2 | 4 | --- | D | Q | 0.0024]

k=2
 Rule $S \rightarrow NP \text{ Verb}$ [0.1]
 Combination of 0 & K and has probability $0.21 * 0.6 * 0.1 = 0.0126$
 Change U to be [S | 2 | 4 | --- | 0 | K | 0.0126]

length=4

i=1

j=4

M=S

k=1
 No rules apply.

k=2
 Create node V. [S | 1 | 4 | --- | --- | --- | 0]
 Rule $S \rightarrow NP \text{ VP}$ [0.6]
 Combination of L & Q and has probability $0.035 * 0.08 * 0.6 = 0.00168$
 Change V to be [S | 1 | 4 | --- | L | Q | 0.00168]

k=3

Rule $S \rightarrow NP \text{ Verb}$ [0.1]

Combination of T & K and has probability $0.045 * 0.6 * 0.1 = 0.0027$

Change V to be [S | 1 | 4 | --- | T | K | 0.0027]

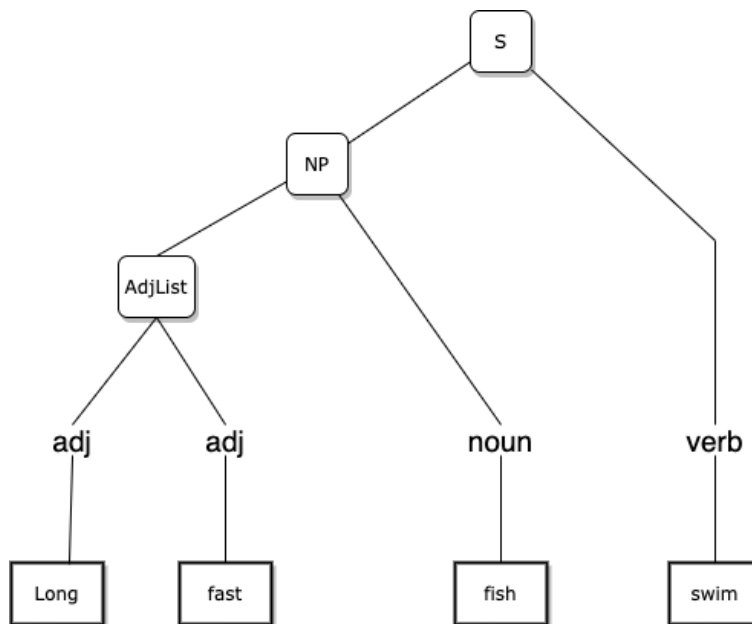
Done. Termination!

Final tree:

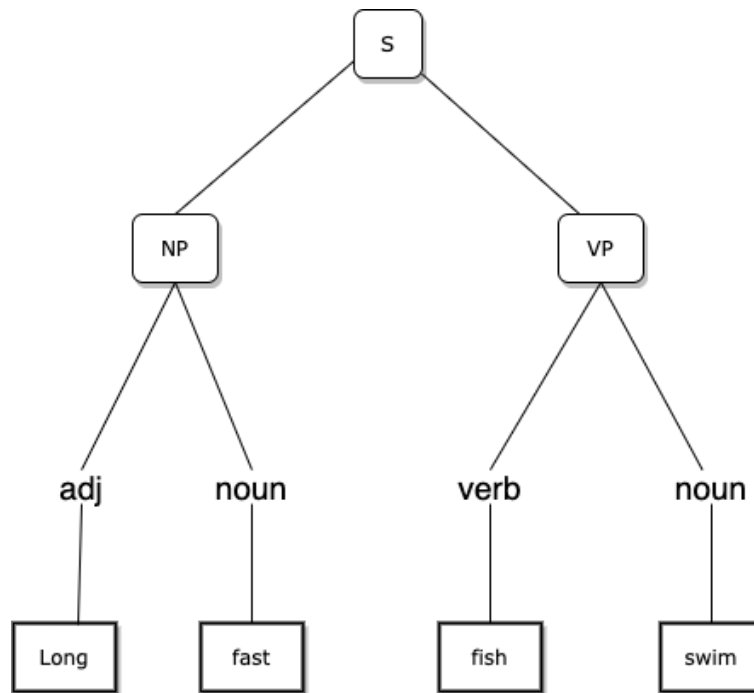
```
S
  NP
    AdjList
      Adj Long
      Adj fast
    Noun fish
  Verb swim
```

Solution to B:

Using the "Final Tree" from part A obtained by the CYK algorithm, the parse tree yielded is as follows:



Based on the last iteration, second possible parse tree could look like this but it is has lower probability.



End of Assignment. Thank you!