UNDERSTANDING PROLOG EVALUATION

$$\begin{array}{c} \text{find (} [X \mid_\] \text{ , } X \text{)} \\ \text{find (} [Y \mid L\] \text{ , } X \text{) :- find (L,X)} \end{array}$$

GOAL
$$\rightarrow$$
 find ([1,X₁,Y₁], 2)

$$\begin{aligned} & \text{find}(\left[X\mid_{-}\right],X)\\ & \text{GOAL} \rightarrow \text{find}\left(\left[1,X_{1},Y_{1}\right],2\right) \\ & X=1\,;_{-}=\left[X_{2},Y_{2}\right];X=2 \quad \text{FALSE} \\ & \quad & \text{find}\left(\left[Y\mid L\right],X\right):\text{-find}\left(L,X\right)\\ & \text{GOAL} \rightarrow \text{find}\left(\left[1,X_{1},Y_{1}\right],2\right) \\ & Y=1\,;L=\left[X_{2},Y_{2}\right];X=2 \; \text{TRUE} \rightarrow \text{Evaluate the body} \\ & \quad & \text{find}\left(L,X\right)\\ & \quad & \text{NEW GOAL} \rightarrow \text{find}\left(\left[X_{2},Y_{2}\right],2\right) \\ & \quad & \quad & \text{find}\left(\left[X\mid_{-}\right],X\right)\\ & \quad & \text{GOAL} \rightarrow \text{find}\left(\left[X_{2},Y_{2}\right],2\right) \\ & X=X_{2}\,;_{-}=Y_{2}\,;X=2 \; \text{TRUE! GOAL SATISFIED WITH } X_{2}=2! \\ & \quad & \text{END } X_{2}=2 \end{aligned}$$