ECE2277A Lab 3: Multiplexers

Laboratory Report

Name: Waleed Sawan

Student Number: 251085963

Submission Date: 2020-11-17

Boolean Function

Please write your canonical Boolean function here as a sum of minterms (m_p+m_q , etc.) for reference:

$$f(a,b,c,d) = m_0 + m_1 + m_2 + m_4 + m_{10} + m_{12} + m_{13} + m_{14}$$

The truth table for this function is:

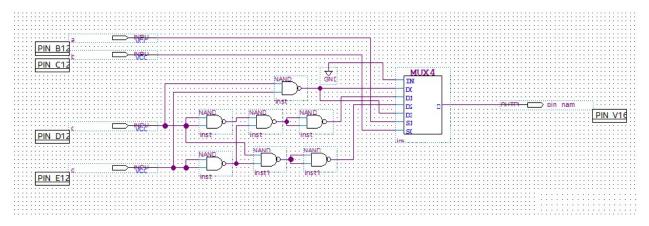
abcd	f(a,b,c,d)
0000	1
0001	1
0010	1
0011	0
0100	1
0101	0
0110	0
0111	0
1000	0
1001	0
1010	1
1011	0
1100	1
1101	1
1110	1
1111	0

Multiplexer Enable

The 4×1 multiplexer in Quartus is enabled by connecting INH to $[v_{CC}/ground]$. This is *active* [high/low] enable.

Multiplexer Circuit

Include an image of the circuit from Quartus. Add extra space if necessary.



The NAND logic function for the multiplexer inputs is:

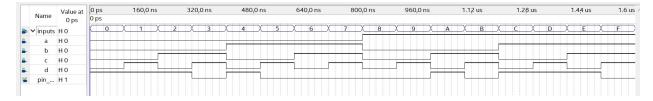
$$D_0(c,d) = \text{NAND(C,D)}$$

$$D_1(c,d) = \text{NAND}(\text{NAND}(\text{NAND}(\text{C,C}), \text{NAND}(\text{D,D})), \text{NAND}(\text{NAND}(\text{C,C}), \text{NAND}(\text{D,D})))$$

$$D_2(c,d) = \text{NAND}(\text{NAND}(C, \text{NAND}(D,D)), \text{NAND}(C, \text{NAND}(D,D)))$$

$$D_3(c,d) = \text{NAND(C,D)}$$

Include an image of the simulated waveforms demonstrating the correct output of the circuit. Add extra space if necessary.



Design Questions

Compare the present multiplexer circuit to your previous AND-OR-NOT circuits for the same Boolean function and answer the questions below. One or two sentences is sufficient. Add extra space if necessary.

1. Which circuit has the lowest cost (check the gate-based implementation of the multiplexer)? Justify your answer.

The circuit cost of the minimized standard product-of-sums was 20, while the cost of the new implementation using multiplexers was 46, which is more. This means that minimized standard product of sums has the lowest circuit cost. It is cheaper because it has a lower cost and simpler expressions.

2. Which circuit has the shortest total propagation time?

The total propagation time of the minimized standard product-of-sums was 3, while the propagation time of the new implementation using multiplexers was 5, which is more. This means that minimized standard product of sums has the lowest propagation time.

3. Finally, we designed the multiplexer circuit using a and b as control variables and c and d as data variables, but really this is an arbitrary choice. Can the cost of your multiplexer circuit be reduced if this is changed (for example, use a, d for control and b, c for data)?

There could be a scenario where a combination of cd would produce simpler circuits, in turn causing a lower circuit cost.

When calculating it for a, d being control and b,c being data – the first input equation (D0) changed to the following:

NAND(B,B) + NAND(B,C)

This shows that the circuit cost can be changed with a change in the control/data variable assignments, so finding the right one will help in optimizing it.