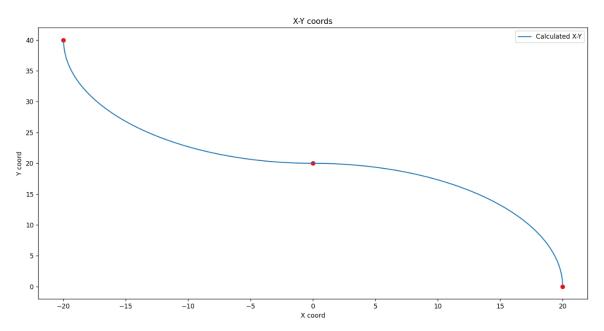


Autonomous Mobile Robotics HW3

Walid Shaker

Path Planning:

The trajectory is defined using two circles as shown below. The code is attached.



Point B (starting point) is selected as (-20, 40)

Point A (final point) is (20,0)

Point C (midpoint) is (0,20)

Since r = 20, so if we set v = 0.5, then $\omega = 0.025$

The simulation time from B to C (t) = $\frac{\pi/2}{\omega}$ = 62.83 sec

So, the total time (t_f) that the vehicle takes from B to A is 125.6 sec

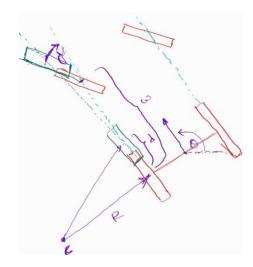
Let the sampling time dt = 0.05, so the number of iterations to reach final point $N = \frac{t_f}{dt} = 2512$

Motion Model: kinematics

I used the same bicycle model explained in the lecture.

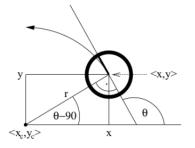
Robot pose $[x, y, \theta]^T$

A robot can be control through linear and angular velocities $u = [v, \omega]^T$



The center of the circle is at

$$egin{bmatrix} x_c \ y_c \end{bmatrix} = egin{bmatrix} x - rac{v}{\omega} \sin(heta) \ y + rac{v}{\omega} \cos(heta) \end{bmatrix}$$



After δt time, ideal robot will be at $\mathbf{x}_{t+1} = [x_{t+1} \quad y_{t+1} \quad heta_{t+1}]$

$$=egin{bmatrix} x_c + rac{v}{\omega} \sin(heta_t + \omega \delta t) \ y_c - rac{v}{\omega} \cos(heta_t + \omega \delta t) \end{bmatrix} = egin{bmatrix} x_t \ y_t \ heta_t \end{bmatrix} + egin{bmatrix} -rac{v}{\omega} \sin(heta_t) + rac{v}{\omega} \sin(heta_t + \omega \delta t) \ rac{v}{\omega} \cos(heta_t) - rac{v}{\omega} \cos(heta_t + \omega \delta t) \ \omega \delta t \end{bmatrix}$$

Real motion model

$$\underbrace{egin{pmatrix} x_{t+1} \ y_{t+1} \ \theta_{t+1} \end{pmatrix}}_{\mathbf{x}_{t+1}} = \underbrace{egin{pmatrix} x_t \ y_t \ \theta_t \end{pmatrix} + egin{pmatrix} -rac{\hat{v}_t}{\hat{\omega}_t}\sin(heta) + rac{\hat{v}_t}{\hat{\omega}_t}\sin(heta + \hat{\omega}_t\delta t) \ rac{\hat{v}_t}{\hat{\omega}_t}\cos(heta) - rac{\hat{t}_t}{\hat{\omega}_t}\cos(heta + \hat{\omega}_t\delta t) \ \hat{\omega}_t\delta t + \hat{\gamma}\delta t \end{bmatrix}}_{f(u_t,\mathbf{x}_t)}$$

, where $\hat{\gamma} \sim arepsilon_{lpha_5 v_t^2 + lpha_6 \omega_t^2}$

• Approximated motion model, i.e., replacing true motion \hat{v}_t and $\hat{\omega}_t$ by executed control (v_t, ω_t)

$$\underbrace{egin{pmatrix} x_{t+1} \ y_{t+1} \ \theta_{t+1} \end{pmatrix}}_{\mathbf{x}_{t+1}} = \underbrace{egin{pmatrix} x_t \ y_t \ \theta_t \end{pmatrix} + egin{pmatrix} -rac{v_t}{\omega_t}\sin(heta) + rac{v_t}{\omega_t}\sin(heta) + rac{v_t}{\omega_t}\cos(heta) - rac{v_t}{\omega_t}\cos(heta + \omega_t\delta t) \ \omega_t\delta t \end{pmatrix}}_{f(u_t,\mathbf{x}_t)} + N(0,Q_t)$$

Sensor Model: correction step

$$\underbrace{egin{bmatrix} r_t^i \ heta_t^i \end{bmatrix}}_{z_t^i} = \underbrace{egin{bmatrix} \sqrt{\left(m_{j,x} - x
ight)^2 + \left(m_{j,y} - y
ight)^2} \ heta h$$

, where $m_{j,x},m_{j,y}$ denotes the coordinates of jth landmark detection at time t, $R=egin{bmatrix}\sigma_r^2&0\\0&\sigma_r^2\end{bmatrix}$, and $\mathbf{x}_{t,x}^-=x,\mathbf{x}_{t,y}^-=y$

EKF:

Extended Kalman filter localization is implemented, and the robot position uncertainty estimation and the traversed trajectory are plotted over the time as shown below.

EKF Robot localization

