

Table 1. The clustering performance comparison between reparameterization and nuclear norm regularization on  $\Theta$ .

Metric	ACC $\uparrow$	NMI $\uparrow$	ARI $\uparrow$	PUR $\uparrow$	FIS $\uparrow$	Time $\downarrow$	Rank	ACC $\uparrow$	NMI $\uparrow$	ARI $\uparrow$	PUR $\uparrow$	FIS $\uparrow$	Time $\downarrow$	Rank
NGs								3Sources						
Reparameterization	<b>0.986</b> $\pm 0.00$	<b>0.953</b> $\pm 0.00$	<b>0.965</b> $\pm 0.00$	<b>0.986</b> $\pm 0.00$	<b>0.972</b> $\pm 0.00$	0.052	<b>5</b>	0.776 $\pm 0.00$	<b>0.693</b> $\pm 0.00$	<b>0.666</b> $\pm 0.00$	0.805 $\pm 0.00$	<b>0.736</b> $\pm 0.00$	<b>0.021</b>	<b>6</b>
Nuclear Norm	0.978 $\pm 0.00$	0.928 $\pm 0.00$	0.945 $\pm 0.00$	0.978 $\pm 0.00$	0.956 $\pm 0.00$	0.816	500	<b>0.783</b> $\pm 0.00$	0.652 $\pm 0.00$	0.614 $\pm 0.01$	<b>0.872</b> $\pm 0.00$	0.711 $\pm 0.01$	0.385	169
WebKB								NUS-WIDE						
Reparameterization	<b>0.977</b> $\pm 0.00$	<b>0.798</b> $\pm 0.00$	<b>0.901</b> $\pm 0.00$	<b>0.977</b> $\pm 0.00$	<b>0.965</b> $\pm 0.00$	<b>0.033</b>	<b>2</b>	<b>0.378</b> $\pm 0.01$	<b>0.237</b> $\pm 0.00$	<b>0.168</b> $\pm 0.00$	0.428 $\pm 0.01$	<b>0.266</b> $\pm 0.00$	<b>0.136</b> $\pm 0.05$	<b>8</b>
Nuclear Norm	ER	ER	ER	ER	ER	ER	ER	0.129 $\pm 0.00$	0.004 $\pm 0.00$	0.000 $\pm 0.00$	<b>0.996</b> $\pm 0.00$	0.221 $\pm 0.00$	1.142 $\pm 0.04$	1600
BBCSport								100Leaves						
Reparameterization	<b>0.985</b> $\pm 0.00$	<b>0.949</b> $\pm 0.01$	<b>0.957</b> $\pm 0.01$	<b>0.985</b> $\pm 0.01$	<b>0.967</b> $\pm 0.00$	<b>0.054</b>	<b>5</b>	<b>0.918</b> $\pm 0.01$	<b>0.959</b> $\pm 0.00$	<b>0.879</b> $\pm 0.01$	<b>0.941</b> $\pm 0.01$	<b>0.881</b> $\pm 0.01$	<b>0.844</b>	<b>100</b>
Nuclear Norm	0.895 $\pm 0.00$	0.821 $\pm 0.00$	0.849 $\pm 0.00$	0.930 $\pm 0.00$	0.886 $\pm 0.00$	1.264	537	0.630 $\pm 0.04$	0.840 $\pm 0.02$	0.509 $\pm 0.07$	0.835 $\pm 0.01$	0.515 $\pm 0.07$	4.913	1600
Youtube								ALOI						
Reparameterization	<b>0.461</b> $\pm 0.00$	<b>0.308</b> $\pm 0.00$	<b>0.244</b> $\pm 0.00$	<b>0.507</b> $\pm 0.01$	<b>0.322</b> $\pm 0.01$	<b>0.244</b>	<b>10</b>	<b>0.890</b> $\pm 0.00$	<b>0.848</b> $\pm 0.00$	<b>0.773</b> $\pm 0.00$	<b>0.888</b> $\pm 0.00$	<b>0.796</b> $\pm 0.00$	<b>0.089</b>	<b>10</b>
Nuclear Norm	0.275 $\pm 0.00$	0.158 $\pm 0.00$	0.082 $\pm 0.00$	0.389 $\pm 0.01$	0.194 $\pm 0.00$	103.065	1997	0.586 $\pm 0.00$	0.620 $\pm 0.02$	0.488 $\pm 0.03$	0.832 $\pm 0.01$	0.550 $\pm 0.03$	0.254	630
Mfeat								BBCNews						
Reparameterization	<b>0.889</b> $\pm 0.00$	<b>0.898</b> $\pm 0.00$	<b>0.851</b> $\pm 0.00$	<b>0.893</b> $\pm 0.02$	<b>0.866</b> $\pm 0.01$	<b>0.202</b>	<b>10</b>	<b>0.917</b> $\pm 0.00$	<b>0.818</b> $\pm 0.00$	<b>0.822</b> $\pm 0.00$	<b>0.917</b> $\pm 0.00$	<b>0.864</b> $\pm 0.00$	<b>0.059</b>	<b>5</b>
Nuclear Norm	0.776 $\pm 0.01$	0.715 $\pm 0.00$	0.638 $\pm 0.00$	0.776 $\pm 0.01$	0.674 $\pm 0.00$	1.024	1994	0.872 $\pm 0.00$	0.706 $\pm 0.00$	0.751 $\pm 0.00$	0.885 $\pm 0.00$	0.814 $\pm 0.00$	2.609	682
Cifar10								Cifar100						
Reparameterization	0.991 $\pm 0.00$	0.974 $\pm 0.00$	0.980 $\pm 0.00$	0.991 $\pm 0.00$	0.982 $\pm 0.00$	<b>11.827</b>	<b>10</b>	<b>0.958</b> $\pm 0.01$	<b>0.989</b> $\pm 0.00$	<b>0.959</b> $\pm 0.01$	<b>0.989</b> $\pm 0.00$	<b>0.959</b> $\pm 0.01$	<b>25.148</b>	<b>100</b>
Nuclear Norm	<b>0.994</b> $\pm 0.00$	<b>0.984</b> $\pm 0.00$	<b>0.986</b> $\pm 0.00$	<b>0.994</b> $\pm 0.00$	<b>0.988</b> $\pm 0.00$	20690.036	49994	0.906 $\pm 0.01$	0.970 $\pm 0.00$	0.853 $\pm 0.02$	0.972 $\pm 0.00$	0.854 $\pm 0.02$	22716.224	49986
YTF-10								YTF-20						
Reparameterization	<b>0.788</b> $\pm 0.01$	<b>0.828</b> $\pm 0.01$	<b>0.741</b> $\pm 0.02$	<b>0.837</b> $\pm 0.02$	<b>0.769</b> $\pm 0.02$	<b>3.638</b>	<b>10</b>	<b>0.763</b> $\pm 0.04$	<b>0.790</b> $\pm 0.02$	<b>0.637</b> $\pm 0.03$	<b>0.794</b> $\pm 0.02$	<b>0.658</b> $\pm 0.03$	<b>7.252</b>	<b>20</b>
Nuclear Norm	0.751 $\pm 0.01$	0.800 $\pm 0.00$	0.701 $\pm 0.01$	0.820 $\pm 0.00$	0.734 $\pm 0.01$	495.227	36896	0.691 $\pm 0.01$	0.759 $\pm 0.00$	0.565 $\pm 0.01$	0.769 $\pm 0.00$	0.611 $\pm 0.01$	15206.441	60051
YTF-50								YTF-100						
Reparameterization	<b>0.755</b> $\pm 0.02$	<b>0.849</b> $\pm 0.00$	<b>0.659</b> $\pm 0.01$	<b>0.798</b> $\pm 0.01$	<b>0.667</b> $\pm 0.01$	<b>34.716</b>	<b>50</b>	<b>0.691</b> $\pm 0.01$	<b>0.837</b> $\pm 0.01$	<b>0.585</b> $\pm 0.03$	<b>0.737</b> $\pm 0.01$	<b>0.590</b> $\pm 0.03$	<b>94.086</b>	<b>100</b>
Nuclear Norm	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM
YTF-200								YTF-400						
Reparameterization	<b>0.635</b> $\pm 0.02$	<b>0.831</b> $\pm 0.01$	<b>0.498</b> $\pm 0.04$	<b>0.686</b> $\pm 0.01$	<b>0.501</b> $\pm 0.04$	<b>367.938</b>	<b>200</b>	<b>0.558</b> $\pm 0.00$	<b>0.817</b> $\pm 0.00$	<b>0.373</b> $\pm 0.02$	<b>0.622</b> $\pm 0.00$	<b>0.376</b> $\pm 0.02$	<b>921.626</b>	<b>400</b>
Nuclear Norm	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM	OOM

†: Best results are in bold.  $\uparrow$  following a metric indicates that a higher value corresponds to better clustering performance whereas  $\downarrow$  vice versa.

ER indicates ill-conditioned matrix occurs when performing SVD. OOM indicates the method suffers out-of-memory error.

Table 2. The memory usage (MB) comparison between reparameterization and nuclear norm regularization on  $\Theta$ .

Datasets	Cifar10	Cifar100	YTF10	YTF20	YTF50	YTF100	YTF200	YTF400
Reparameterization	<b>1371.003</b>	<b>1405.335</b>	<b>790.940</b>	<b>1312.318</b>	<b>2617.790</b>	<b>4135.350</b>	<b>6266.856</b>	<b>9332.602</b>
Nuclear Norm	20440.674	20440.674	12187.311	32451.088	OOM	OOM	OOM	OOM

†: Best results are in bold. OOM indicates that the method suffers out-of-memory error.