

Table 1. The clustering performance comparison between reparameterization and nuclear norm regularization on Θ .

| Metric | ACC \uparrow | NMI \uparrow | ARI \uparrow | PUR \uparrow | FIS \uparrow | Time \downarrow | Rank | ACC \uparrow | NMI \uparrow | ARI \uparrow | PUR \uparrow | FIS \uparrow | Time \downarrow | Rank |
|--------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------|------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|-------------------------|------------|
| NGs | | | | | | | | 3Sources | | | | | | |
| Reparameterization | 0.986 ± 0.00 | 0.953 ± 0.00 | 0.965 ± 0.00 | 0.986 ± 0.00 | 0.972 ± 0.00 | 0.052 | 5 | 0.776 ± 0.00 | 0.693 ± 0.00 | 0.666 ± 0.00 | 0.805 ± 0.00 | 0.736 ± 0.00 | 0.021 | 6 |
| Nuclear Norm | 0.978 ± 0.00 | 0.928 ± 0.00 | 0.945 ± 0.00 | 0.978 ± 0.00 | 0.956 ± 0.00 | 0.816 | 500 | 0.783 ± 0.00 | 0.652 ± 0.00 | 0.614 ± 0.01 | 0.872 ± 0.00 | 0.711 ± 0.01 | 0.385 | 169 |
| WebKB | | | | | | | | NUS-WIDE | | | | | | |
| Reparameterization | 0.977 ± 0.00 | 0.798 ± 0.00 | 0.901 ± 0.00 | 0.977 ± 0.00 | 0.965 ± 0.00 | 0.033 | 2 | 0.378 ± 0.01 | 0.237 ± 0.00 | 0.168 ± 0.00 | 0.428 ± 0.01 | 0.266 ± 0.00 | 0.136 ± 0.05 | 8 |
| Nuclear Norm | ER | ER | ER | ER | ER | ER | ER | 0.129 ± 0.00 | 0.004 ± 0.00 | 0.000 ± 0.00 | 0.996 ± 0.00 | 0.221 ± 0.00 | 1.142 ± 0.04 | 1600 |
| BBCSport | | | | | | | | 100Leaves | | | | | | |
| Reparameterization | 0.985 ± 0.00 | 0.949 ± 0.01 | 0.957 ± 0.01 | 0.985 ± 0.01 | 0.967 ± 0.00 | 0.054 | 5 | 0.918 ± 0.01 | 0.959 ± 0.00 | 0.879 ± 0.01 | 0.941 ± 0.01 | 0.881 ± 0.01 | 0.844 | 100 |
| Nuclear Norm | 0.895 ± 0.00 | 0.821 ± 0.00 | 0.849 ± 0.00 | 0.930 ± 0.00 | 0.886 ± 0.00 | 1.264 | 537 | 0.630 ± 0.04 | 0.840 ± 0.02 | 0.509 ± 0.07 | 0.835 ± 0.01 | 0.515 ± 0.07 | 4.913 | 1600 |
| Youtube | | | | | | | | ALOI | | | | | | |
| Reparameterization | 0.461 ± 0.00 | 0.308 ± 0.00 | 0.244 ± 0.00 | 0.507 ± 0.01 | 0.322 ± 0.01 | 0.244 | 10 | 0.890 ± 0.00 | 0.848 ± 0.00 | 0.773 ± 0.00 | 0.888 ± 0.00 | 0.796 ± 0.00 | 0.089 | 10 |
| Nuclear Norm | 0.275 ± 0.00 | 0.158 ± 0.00 | 0.082 ± 0.00 | 0.389 ± 0.01 | 0.194 ± 0.00 | 103.065 | 1997 | 0.586 ± 0.00 | 0.620 ± 0.02 | 0.488 ± 0.03 | 0.832 ± 0.01 | 0.550 ± 0.03 | 0.254 | 630 |
| Mfeat | | | | | | | | BBCNews | | | | | | |
| Reparameterization | 0.889 ± 0.00 | 0.898 ± 0.00 | 0.851 ± 0.00 | 0.893 ± 0.02 | 0.866 ± 0.01 | 0.202 | 10 | 0.917 ± 0.00 | 0.818 ± 0.00 | 0.822 ± 0.00 | 0.917 ± 0.00 | 0.864 ± 0.00 | 0.059 | 5 |
| Nuclear Norm | 0.776 ± 0.01 | 0.715 ± 0.00 | 0.638 ± 0.00 | 0.776 ± 0.01 | 0.674 ± 0.00 | 1.024 | 1994 | 0.872 ± 0.00 | 0.706 ± 0.00 | 0.751 ± 0.00 | 0.885 ± 0.00 | 0.814 ± 0.00 | 2.609 | 682 |
| Cifar10 | | | | | | | | Cifar100 | | | | | | |
| Reparameterization | 0.991 ± 0.00 | 0.974 ± 0.00 | 0.980 ± 0.00 | 0.991 ± 0.00 | 0.982 ± 0.00 | 11.827 | 10 | 0.958 ± 0.01 | 0.989 ± 0.00 | 0.959 ± 0.01 | 0.989 ± 0.00 | 0.959 ± 0.01 | 25.148 | 100 |
| Nuclear Norm | 0.994 ± 0.00 | 0.984 ± 0.00 | 0.986 ± 0.00 | 0.994 ± 0.00 | 0.988 ± 0.00 | 20690.036 | 49994 | 0.906 ± 0.01 | 0.970 ± 0.00 | 0.853 ± 0.02 | 0.972 ± 0.00 | 0.854 ± 0.02 | 22716.224 | 49986 |
| YTF-10 | | | | | | | | YTF-20 | | | | | | |
| Reparameterization | 0.788 ± 0.01 | 0.828 ± 0.01 | 0.741 ± 0.02 | 0.837 ± 0.02 | 0.769 ± 0.02 | 3.638 | 10 | 0.763 ± 0.04 | 0.790 ± 0.02 | 0.637 ± 0.03 | 0.794 ± 0.02 | 0.658 ± 0.03 | 7.252 | 20 |
| Nuclear Norm | 0.751 ± 0.01 | 0.800 ± 0.00 | 0.701 ± 0.01 | 0.820 ± 0.00 | 0.734 ± 0.01 | 495.227 | 36896 | 0.691 ± 0.01 | 0.759 ± 0.00 | 0.565 ± 0.01 | 0.769 ± 0.00 | 0.611 ± 0.01 | 15206.441 | 60051 |
| YTF-50 | | | | | | | | YTF-100 | | | | | | |
| Reparameterization | 0.755 ± 0.02 | 0.849 ± 0.00 | 0.659 ± 0.01 | 0.798 ± 0.01 | 0.667 ± 0.01 | 34.716 | 50 | 0.691 ± 0.01 | 0.837 ± 0.01 | 0.585 ± 0.03 | 0.737 ± 0.01 | 0.590 ± 0.03 | 94.086 | 100 |
| Nuclear Norm | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM |
| YTF-200 | | | | | | | | YTF-400 | | | | | | |
| Reparameterization | 0.635 ± 0.02 | 0.831 ± 0.01 | 0.498 ± 0.04 | 0.686 ± 0.01 | 0.501 ± 0.04 | 367.938 | 200 | 0.558 ± 0.00 | 0.817 ± 0.00 | 0.373 ± 0.02 | 0.622 ± 0.00 | 0.376 ± 0.02 | 921.626 | 400 |
| Nuclear Norm | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM | OOM |

†: Best results are in bold. \uparrow following a metric indicates that a higher value corresponds to better clustering performance whereas \downarrow vice versa.
ER indicates ill-conditioned matrix occurs when performing SVD. OOM indicates the method suffers out-of-memory error.

Table 2. The memory usage (MB) comparison between reparameterization and nuclear norm regularization on Θ .

| Datasets | Cifar10 | Cifar100 | YTF10 | YTF20 | YTF50 | YTF100 | YTF200 | YTF400 |
|--------------------|-----------------|-----------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Reparameterization | 1371.003 | 1405.335 | 790.940 | 1312.318 | 2617.790 | 4135.350 | 6266.856 | 9332.602 |
| Nuclear Norm | 20440.674 | 20440.674 | 12187.311 | 32451.088 | OOM | OOM | OOM | OOM |

†: Best results are in bold. OOM indicates that the method suffers out-of-memory error.