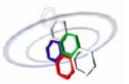




Conception of a complete OFDM communication channel



Main goal of the project



Achieve a wireless communication on a multi-path channel





Narrowband vs Wideband





No memory in a narrowband channel:

$$r(n) = hs(n) + w(n)$$

Memory in a wideband channel:

$$r(n) = h(n) * s(n) + w(n)$$

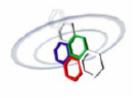
Interferences must be compensated by the equalization

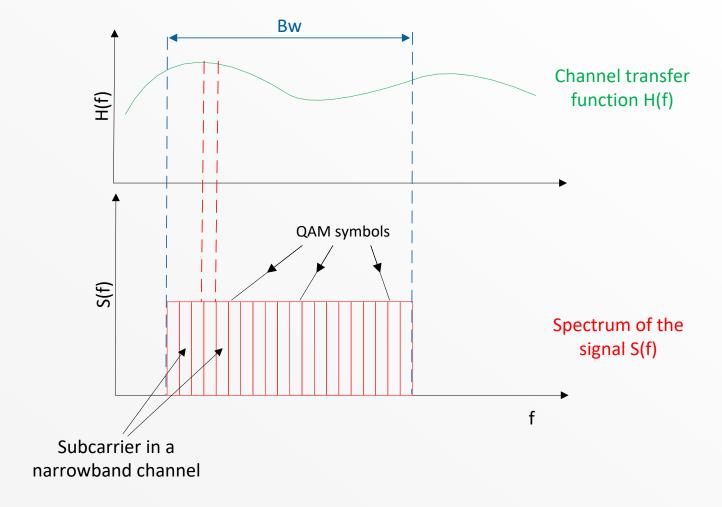
Two solutions of equalization



- Filtering in time domain
 - Creation of a filter g(n) with the following property: $g(n) * h(n) = \delta(n)$
 - The interferences are removed: g(n) * r(n) = g(n) * h(n) * s(n) + g(n) * w(n) = s(n) + g(n) * w(n)
 - Complex and not very efficient for long channel memory
- Frequency domain equalization
 - OFDM: Orthogonal Frequency-Division Multiplexing
 - Most common solution (Wifi, LTE)

Information defined in frequency domain



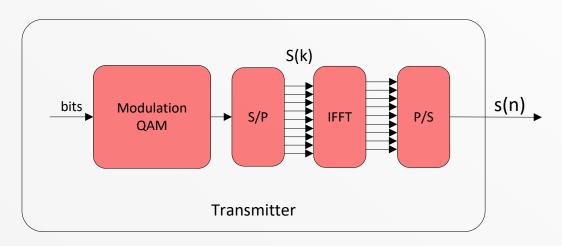




Creation of an OFDM symbol



- Multi-carrier modulation
- Each sub-carrier operates over narrow-band channel
- Transmission
 - 1: Each symbol is placed on a sub-carrier
 - 2: Conversion in time domain (IFFT)



Reception of an OFDM symbol



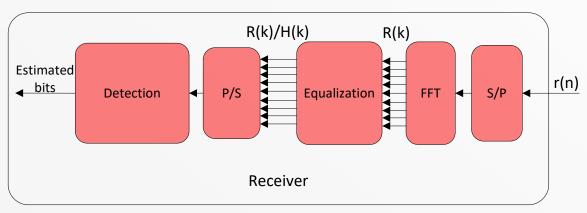
Conversion in frequency domain (FFT)

$$TD: r(n) = h(n) * s(n) + w(n)$$

$$FD: R(k) = H(k)S(k) + W(k)$$

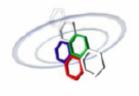
Equalization of each sub-carrier independently

$$\frac{R(k)}{H(k)} = S(k) + \frac{W(k)}{H(k)}$$



ULB

Equalization in Frequency Domain



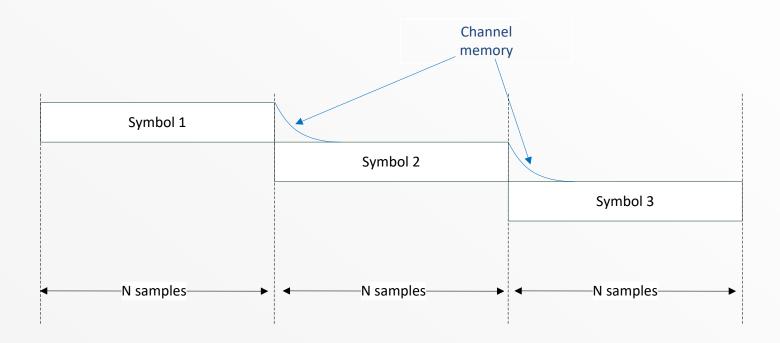
- Complex equalization replaced by a simple division
- Convolution product in time domain is equal to a multiplication in frequency domain...
- ... But a cyclic prefix is also required



Impact of the channel memory on a sequence of symbols

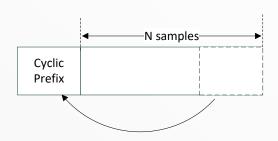


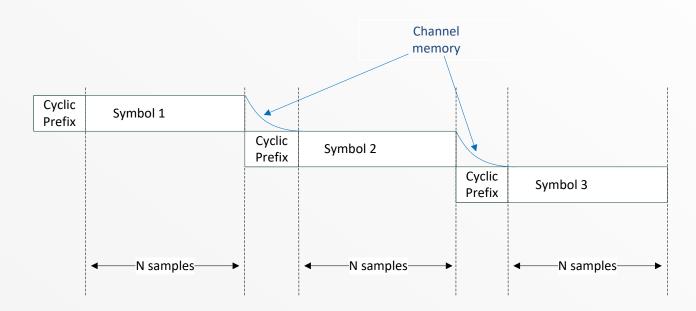
- Interference of symbol 1 on symbol 2
- Equalization impossible



Problem solved with a cyclic prefix





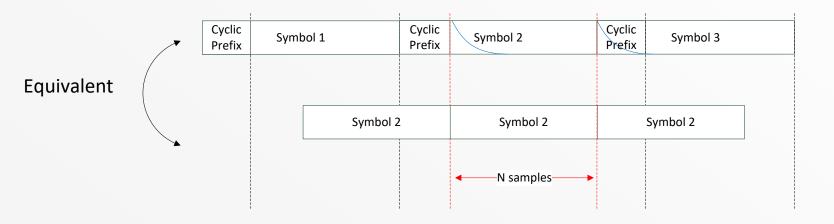




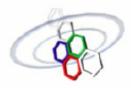
Why does it work?



- This relation : $y(n) = h(n) * s(n) \Rightarrow Y(k) = H(k)S(k)$ works only if s(n) is periodic
- Illusion of periodicity created with the help of a cyclic prefix



Demonstration



- Burst model (see course)
- Use the circular convolution property of the DFT: [1]

$$Y(q) = H(q)X(q) \iff y(n) = h(n) \otimes x(n)$$

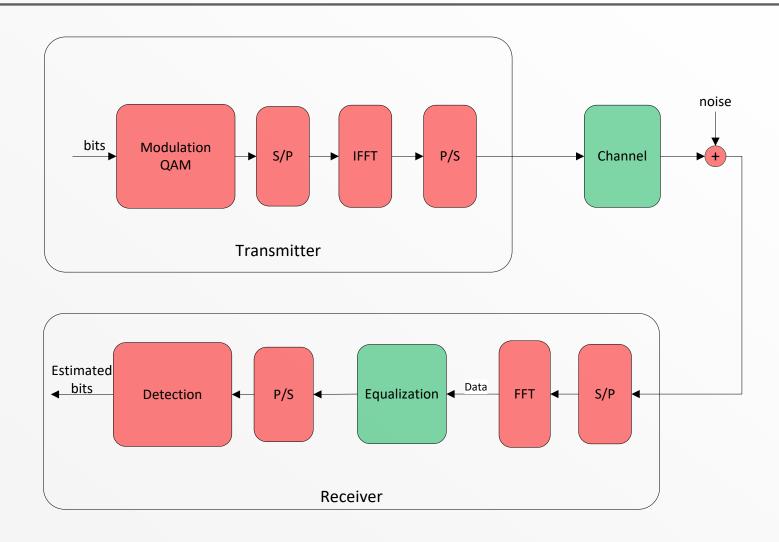
where \otimes denotes a circular convolution

$$h(n) \otimes x(n) = \sum_{l=0}^{Q-1} h(l)x(n-l)modQ$$

[1]: Fundamentals of WiMax, Andrews et. al., pp 117-120

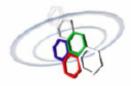
Objective







Objective



- Implement the OFDM transceiver (AWGN channel)
- Assess the BER performance
- Include the statistical channel model (known by the receiver)
- Explain why we need the Cyclic Prefix
- Compare the performances in the LOS and NLOS cases
- Discuss the impact of the channel and modulation parameters
- Confirm that each sub-channel is affected by a narrowband channel