CMPT 295 Assignment 2 Solutions (2%)

- 1. [6 marks] Binary Conversions
 - (a) [1 mark]

Method 1: Continual Subtraction

Hex Conversion:

Method 2: Continual Division

... and the binary digits are read in reverse order for each case and subsequently converted to hex using the steps shown in Method 1.

(b) [2 marks] Using the results from part (a), take their 2's complement: flip all the bits and add 1!

(c) [1 mark] Unsigned: $1010\ 1110_2 = 2^7 + 2^5 + 2^3 + 2^2 + 2^1 = 128 + 32 + 8 + 4 + 2 = 174_{10}$.

2's Complement: The 2's complement (or negative) of $1010\ 1110_2$ is $\overline{1010\ 1110}+1=0101\ 0001+1=0101\ 0010_2$. This has a magnitude of $2^{\overline{6}}+2^4+2^1=64+16+2=82$. Therefore, $1010\ 1110_2=-82_{10}$.

(d) [2 marks]

2. [5 marks] leal

(a) [2 marks] Using only one instruction is fairly limiting in that there are only two useful forms:

```
leal (, %edi, s), %edi leal (%edi, %edi, s), %edi
```

where $s \in \{1, 2, 4, 8\}$. Thus the possible values of k are $\{1, 2, 4, 8\}$ in the first case, or $\{2, 3, 5, 9\}$ in the second case. Thus the final list of possible k's is: $\{1, 2, 3, 4, 5, 8, 9\}$.

(b) [3 marks] It's possible to feed the result of the first leal into the input of the second leal.

```
k = 13
leal (%edi, %edi, 8), %eax leal (%eax, %edi, 4), %edi
k = 20
leal (%edi, %edi, 4), %edi leal (, %edi, 4), %edi
k = 37
leal (%edi, %edi, 8), %eax leal (%edi, %eax, 4), %edi
```

3. [9 marks] The Root of the Problem

```
# The subroutine sqrt finds the integer square root of a 32-bit unsigned
  value, using binary search.
# pseudocode: result <- 0</pre>
               for k from 15 downto 0 do:
#
                  change the kth bit of result to 1
#
                   if result * result > x then:
#
                      change the kth bit of result back to 0
               return result
sqrt:
                $0, %eax
                                 # result <- 0</pre>
        movl
        movl
                $0x8000, %ecx
                                 # ecx is used to toggle kth bit
loop:
                                 # for k from 15 downto 0 do:
                %ecx, %eax
                                       change the kth bit of result to 1
        xorl
        movl
                %eax, %esi
                %esi, %esi
        imul
                %esi, %edi
        cmpl
                endif
                                 #
                                       if result * result > x then:
        jae
                %ecx, %eax
        xorl
                                 #
                                          change kth bit back to 0
endif:
                $1, %ecx
                                      next k
        shr
        jnz
                loop
                                 # return result
        ret
```