## In-class Activity

ME 570 - Prof. Tron 2023-09-12

For questions tagged with the label scan, answer all the questions in the space provided; to submit, scan your work and submit to Gradescope. To scan your work, you can use the flatbed scanner in the ME department office, or an app on your phone such as Adobe Scan or Dropbox, available for both iOS and Android. Please make sure to upload the pages in the correct order, and that the scans have good contrast. If needed, you can download and print this document from Blackboard.

## **Problem 1: Tangents to parametric curves**

Compute the analytical expression of the tangent to the given curve, draw the curve, and draw the tangents at the given points as arrows.

Question 1.1. Curve:  $x(t) = \begin{bmatrix} t^2 - 3 \\ t \end{bmatrix}$ . Compute the expression for the tangent  $\dot{x}(t)$ .

Draw the curve and tangents.

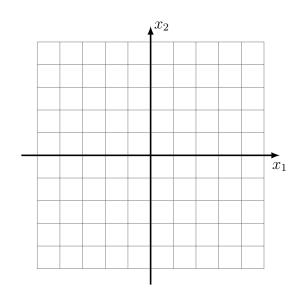
$$t = 2, x(t) =, , \dot{x}(t) =$$

$$t = 1, x(t) =, , \dot{x}(t) =$$

$$t = 0, x(t) =, , \dot{x}(t) =$$

$$t = -1, x(t) =,$$
,  $\dot{x}(t) =$ 

$$t = -2, x(t) =, , \dot{x}(t) =$$



Question 1.2. Curve:  $x(t) = \begin{bmatrix} \cos(t) \\ \sin(t) \end{bmatrix}$ . Compute the expression for the tangent  $\dot{x}(t)$ .

Draw the curve and tangents.

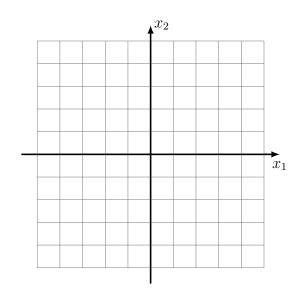
$$t = \frac{3\pi}{4}, x(t) =,$$
,  $\dot{x}(t) =$ 

$$t = \frac{\pi}{2}, x(t) =, \qquad , \dot{x}(t) =$$

$$t = 0, x(t) =, , \dot{x}(t) =$$

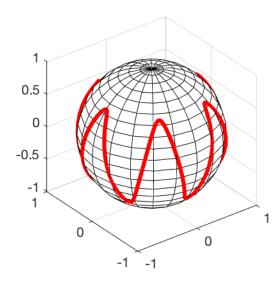
$$t = -\frac{\pi}{2}, x(t) = ,$$
 ,  $\dot{x}(t) =$ 

$$t = -\frac{3\pi}{4}, x(t) = ,$$
 ,  $\dot{x}(t) =$ 



## **Problem 2: Charts for the sphere**

**Question 2.1.** Draw an atlas for the sphere (for best results, use different colors).



Next, consider the path shown in red. Draw the same curve on your charts.

## **Problem 3: Cartesian to polar coordinates**

	$\to \mathbb{R}^2$ defines a transformation from Polar coordin	nates to Cartesian
coordinates:	$\phi(r,\theta) = \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} r\cos\theta \\ r\sin\theta \end{bmatrix}.$	(1)
Question 3.1. Compute to	he Jacobian of $\phi$	
Question 3.2. Compute to	he determinant of the Jacobian.	
Question 3.3. Explain wh	by the transformation (1) is a diffeomorphism, ex	cept at the origin.
	(-) (-)	