# The kinetics of the oxidation of formic acid by bromine in aqueous media

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#### I. INTRODUCTION

The kinetics of the oxidation of formic acid by bromine in aqueous media has been investigated thoroughly[1, 2]. The total reaction of the oxidation of formic acid by bromine,

$$\operatorname{Br}_2 + \operatorname{HCOOH} \xrightarrow{k} 2\operatorname{Br}^- + 2\operatorname{H}^+ + \operatorname{CO}_2$$

is considered to consist of the following elementary reactions:

$$\begin{split} HCOO^{-} + Br_2 &\xrightarrow{k_1} 2\,Br^{-} + H^{+} + CO_2 \\ HCOOH &\xrightarrow{K_a} HCOO^{-} + H^{+} \\ Br - + Br_2 &\xrightarrow{K_{Br_{\Delta}}} Br_3^{-} \end{split}$$

Then it follows that

$$\begin{cases} [HCOO^{-}] = \frac{K_{a}/c(H^{+})}{1+K_{a}/c(H^{+})}c(HCOOH) \\ [Br_{2}] = \frac{1}{1+K_{Br}/c(Br^{-})}c(Br_{2}) \\ \frac{d}{dt}c(Br_{2}) = -k_{1}[HCOO^{-}][Br_{2}] \end{cases}$$
(1)

if there is abundant supply of HCOOH as well as  $\mathrm{H}^+$  and  $\mathrm{Br}^-$ , the concentration of them can be regarded constant, and the total reaction rate can be written as

$$\frac{dc(Br_2)}{dt} = -\frac{k_1 K_a c(HCOOH) c(Br_2) / c(H^+)}{[1 + K_a / c(H^+)][1 + K_{Br} / c(Br^-)]}$$
(2)

and the total reaction rate constant k is equivalent to

$$k = \frac{k_1 K_{\rm a} c(\text{HCOOH}) / c(\text{H}^+)}{[1 + K_{\rm a} / c(\text{H}^+)][1 + K_{\rm Br} / c(\text{Br}^-)]}$$
(3)

Thus the total reaction can be approximated as a reaction in first order, which enables several methods for the detection of the reaction rate constant under different conditions, including spectrophotometric method and electrochemistry method.

The M06-2X functional is a highnonlocality functional with double the amount of nonlocal exchange (2X), and it is parametrized only for nonmetals, which gains a superiority over widely-used functionals including B3LYP, B98, PBE, among calculations involving main-group thermochemistry, kinetics, noncovalent interactions, and electronic excitation energies to valence and Rydberg states.[3]

### II. METHODS AND PROCEDURES

## III. RESULT AND ANALYSIS

$$\frac{dc_s}{dt} = k(c_l - c_s) \tag{4}$$

where  $c_l$  refers to the concentration of the substance in the liquid phase, while  $c_s$  the concentration in the solid phase. Considering that the diffusion of the substance is comparatively small,  $c_l$  can be regarded as dominated by chemical reaction, namely

$$c_l = c'e^{-k't} \tag{5}$$

where c', k' are constants. (4) can be deduced by assuming the form of  $c_s$  as

$$c_s = \chi(t)e^{-k't} \tag{6}$$

which gives

$$\begin{cases} \chi(t) = C_1 e^{(k'-k)t} + C_2, \\ c_s = \frac{kc'}{k'-k} e^{-k't} (e^{(k'-k)t} - 1) \end{cases}$$
 (7)

where  $C_1, C_2$  are constants that are replaced using the boundary condition,

$$c_s\big|_{t=0} = 0 \tag{8}$$

	Group A					Group B					
$c(\mathrm{HCl})$											
c(HCl)/M	0.08000	0.1000	0.1200	0.1600	0.2000	0.08000	0.1000	0.1200	0.2000		
$k \cdot 10^{-3} / s$	4.252	3.491	2.829	2.159	2.059	2.204	1.782	1.593	0.8707		
$R^2$	0.999948	0.999963	0.999774	0.999790	0.999584	0.999868	0.999892	0.999863	0.999490		
$c(\mathrm{KBr})$											
c(KBr)/M	0.05000	0.07500	0.1000	0.1500	0.2000	0.1000	0.1200	0.2000	0.3000	0.4000	
$k \cdot 10^{-3} / s$	4.803	4.035	3.491	2.760	2.626	2.573	2.120	1.940	1.377	1.861	
$R^2$	0.999880	0.999937	0.999963	0.999257	0.999954	0.999913	0.999910	0.999715	0.999885	0.999706	
$c(\mathrm{HCOOH})$											
c(HCOOH)/M	0.05000	0.1000	0.1500	0.2000	0.2500	0.03000	0.05000	0.07000	0.1000	0.1500	
$k \cdot 10^{-3} / s$	1.734	3.491	5.366	6.834	8.257	0.9019	1.248	1.850	2.728	3.560	
$R^2$	0.999924	0.999963	0.999956	0.999953	0.999883	0.999886	0.999846	0.999843	0.999938	0.999907	
$\overline{T}$											
T/°C	25.00	30.00	35.00	40.00	45.00	25.00	30.00	35.00	40.00	45.00	
$k \cdot 10^{-3}/s$	3.491	5.426	8.001	11.47	15.15	1.850	3.104	4.981	8.234	12.49	
$R^2$	0.999963	0.999928	0.999431	0.999916	0.999844	0.999843	0.999913	0.999936	0.999683	0.999425	

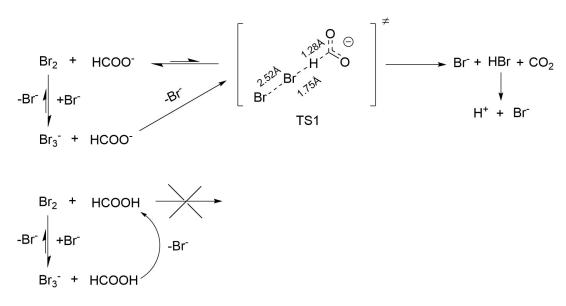


FIG. 1. The proposed mechanism of the oxidation of formic acid by bromine

and infomation from  $c_s$ . It reveals the influence of the diffusion in the measurement, the term  $e^{(k'-k)t}-1$  being the main delimiter. Smaller k with small sets of t will result in larger deficiency in the measurement of k', which might be the case in the electrochemistry method.

The non-constant response function of the measurement system might also contribute to the error. The detection of current is achieved through complicated electromagnetic system, which results in non-constant response function. The output function can be regarded as the convolution of the signal function and the response function, namely

$$P = S * R = \int S(t)R(T-t) dt$$
 (9)

where P stands for the output, while S and R for the signal function and the response function, with T defined as the time interval for a measurement. Given that S is a exponential function, it can be readily proved that P is also a exponential function under the same base. A non-constant response function, however, deviates the output function with considerable error, and it is conspicuous that a larger time interval leads to worse data sets. Compared with spectrophotometric method, electrochemistry method is much more likely to suffer from such a factor, w.r.t. its relatively longer measurement of time.

TABLE I. Calculation result from Gaussian 16 of the energy / Gibbs free energy (without solvent effect) of the HCOO $^-$ Br<sub>2</sub> system in different distance between hydrogen atom in formic acid and bromide atom in bormine, choosing -5337 Hartree as the zero potential energy surface. "N/A" refers to unavailability of the data, due to the fact that the system did not converge during the calculation.

Distance(Å)				2.2		2.6			3.5	5.0
-E(Hartree)	.537892	.533230	.529462	.526210	.520616	.516360	.512932	.508763	.504027	.498300
-G(Hartree)	.555580	.549755	.545271	.541625	.535825	.531732	.528610	.524980	N/A	.525179

TABLE II. Calculation result from Gaussian 16 of the Gibbs free energy of different species in the system, with solvent effect considered.

Species	$\mathrm{Br}_2$	$\mathrm{Br}^-$	Br <sub>3</sub>	HBr	$\mathrm{H}^{+}$	НСООН	HCOO-	$CO_2$
-G(Hartree)	-5148.359998	-2574.362887	-7722.741404	-2574.787315	-0.22518	-189.721106	-189.279246	-188.553856

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