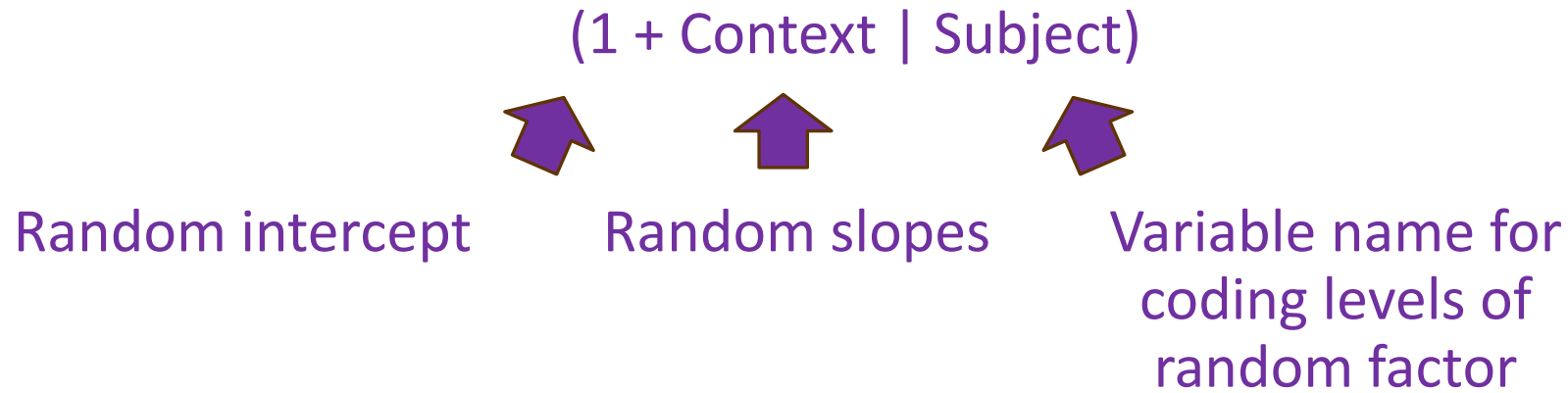


Linear mixed models in R

Day 5

JONAS WALTHER

Random structure: correlations between intercept and slope



\mid - random intercept and random slope are correlated with each other

$\mid \mid$ - no correlations between random effects

$(\text{Context} \mid \mid \text{Subject})$

This expands to:

$(0 + \text{Context} \mid \text{Subject}) + (1 \mid \text{Subject})$

Random structure: correlations between intercept and slope

$y_{iCond} = \beta_0 + (\beta_{Cond} + u_{1i})x_{iCond} + \epsilon_{Cond} + u_{0i}$

```
model_Large8 = lmer(RT ~ Group+Context + (1  
+Context|Subject) + (1| ItemNr), data=PN_Data)
```

Between-subject variability in the intercept:

$$u_0 \sim Normal(0, \sigma_{u0})$$

Between-subject variability in the slope:

$$u_1 \sim Normal(0, \sigma_{u1})$$

Within-subject variability:

$$\epsilon \sim Normal(0, \sigma)$$

```
## Random effects:
```

##	Groups	Name	Variance	Std.Dev.	Corr
##	ItemNr	(Intercept)	23832	154.4	
##	Subject	(Intercept)	19854	140.9	
##		ContextUK	16898	130.0	-0.44
##	Residual		56540	237.8	

Random structure: correlations between intercept and slope

```
(1 +Context|Subject)
```

```
## Random effects:
```

##	Groups	Name	Variance	Std.Dev.	Corr
##	Subject	(Intercept)	19854	140.9	
##		ContextUK	16898	130.0	-0.44
##	Residual		56540	237.8	

```
(1 +Context||Subject)
```

```
## Random effects:
```

##	Groups	Name	Variance	Std.Dev.	Corr
##	Subject	ContextPL	3843	61.99	
##		ContextUK	4623	68.00	-1.00
##	Subject.1	(Intercept)	16011	126.53	
##	Residual		56540	237.78	

Random structure: correlations between intercept and slope

Correlations between intercepts and slopes are frequently assumed in research

- Group with higher intercept will also have a higher slope
- If they are present, they can be used to calculate better estimates
- Even low correlations can contribute to better estimates

But they make the model more complex

Correlations of 1 between slope and intercept can prevent the model from converging

- 1 or very close to one, usually means that the model failed to calculate the correlation
- Usually because there was not enough data
- Removing correlations by using `||` allows model to converge
- But it is recommended to also switch to a simpler model

Summary-Output of an LME

- You prepared your final model
- You checked the assumptions
- You understood and interpreted the outcome

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: RT ~ Group + Context + Group:Context + Age + AoA + Trial + (1 +
##   Context | Subject) + (1 + Context | ItemNr)
##   Data: PN_Data
##
## Random effects:
##   Groups   Name                Variance Std.Dev. Corr
##   ItemNr   (Intercept) 24021    154.99
##           ContextUK    3449     58.73  -0.15
##   Subject  (Intercept) 19522    139.72
##           ContextUK    16426    128.16  -0.41
##   Residual                    55688    235.98
## Number of obs: 7227, groups: ItemNr, 210; Subject, 74
##
## Fixed effects:
##                                     Estimate Std. Error t value
## (Intercept)                        1019.6555    79.0877  12.893
## GroupExperimental                   -59.6657    37.2576  -1.601
## ContextUK                          -11.2579    23.2922  -0.483
## Age                                -1.9501     2.4100  -0.809
## AoA                                 3.2835     3.9845   0.824
## Trial                               0.4629     0.2875   1.610
## GroupExperimental:ContextUK        45.7348    32.1411   1.423
##
## Correlation of Fixed Effects:
##              (Intr) GrpExp CntxUK Age    AoA    Trial
## GrpExprmntl  0.196
## ContextUK   -0.127  0.290
## Age         -0.810 -0.309 -0.012
## AoA         -0.269 -0.217  0.001 -0.234
## Trial        -0.110 -0.001 -0.006  0.000  0.001
## GrpExpr:CUK  0.088 -0.404 -0.704  0.010 -0.001  0.000
```

Reporting linear mixed-effects models

“A one-way ANOVA demonstrated that the effect of leadership style was significant for employee engagement, $F(2, 78) = 4.58, p = .013$.”

There are no standardized guidelines for LMEs yet

The complexity, large structure (and a lack of p-values) make reporting LMEs more effortful

- Especially for short-form texts (i.e. abstracts)

Kim, Dedrick, Cao, Ferron (2008) Multilevel Factor Analysis: Reporting Guidelines and a Review of Reporting Practices

Guidelines and checklist for reporting statistical models

- Multilevel factor analysis, not LMEs
- Might still be helpful to remind you about reporting different aspects of your statistical tests

Reporting LME results

As many details as possible

All relevant statistical measures:

- Data structure and size
- Variable transformations and contrast coding
- Maximal model structure
- Final model results for all fixed and random effects
- Post-hoc tests for relevant effects

Reporting as a table

Effect	Estimate	SE	t	by-Picture SD	by-Participant SD
Intercept	−1.14	0.03	−38.00***	0.15	0.18
Group	0.00	0.05	−0.02		
Context	0.02	0.04	0.65	−0.05	−0.11
Word-lexical frequency	0.00	0.01	−0.08	–	
Age	−0.03	0.02	−1.30		–
Age of L2 acquisition	0.03	0.02	1.15		–
log (Trial number)	0.00	0.01	0.78		
Group:Context	0.03	0.07	0.48		–
Group:Word-lexical frequency	0.00	0.00	−0.28	–	–
Control Group:Context:Word-lexical frequency	0.00	0.01	−0.11	–	–
Mig. Group:Context:Word-lexical frequency	0.01	0.01	1.94'	–	–

predict_response()

ggeffects package

Integrated with the ggplots package

Calculates marginal means

Provides them in easily usable format for plots

predict_response()

```
model_Large8 %>%  
  predict_response(c("Group", "Context"))  
  
## # Predicted values of RT  
  
## Context: PL  
  
## Group          | Predicted |          95% CI  
## -----  
## Control        |    994.54 | 945.32, 1043.76  
## Experimental    |    955.29 | 906.37, 1004.20
```

```
## Context: UK  
  
## Group          | Predicted |          95% CI  
## -----  
## Control        |    1006.62 | 957.25, 1055.99  
## Experimental    |     967.37 | 918.04, 1016.69  
  
## Adjusted for:  
## * Subject = 0 (population-level)  
## * ItemNr = 0 (population-level)
```

predict_response()

X - the values of the first term, x-values

group - levels of the second term

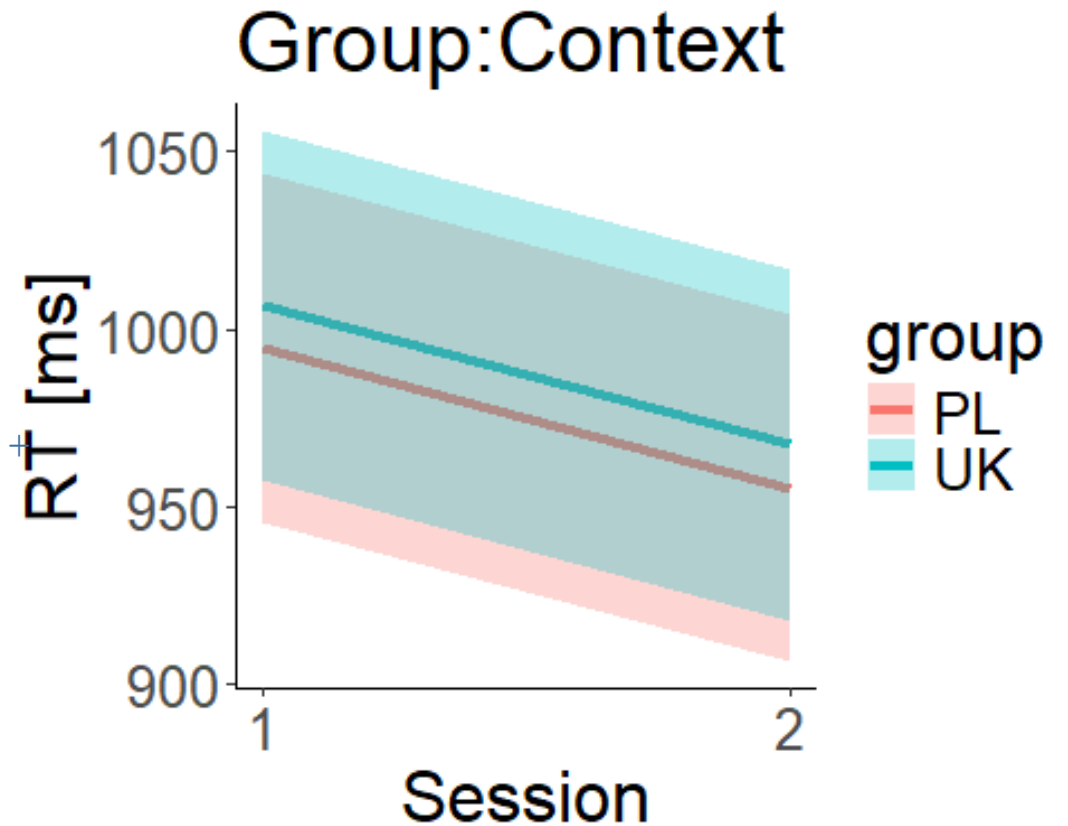
facet – levels of third term

predicted - the predicted y-values

conf.low and conf.high

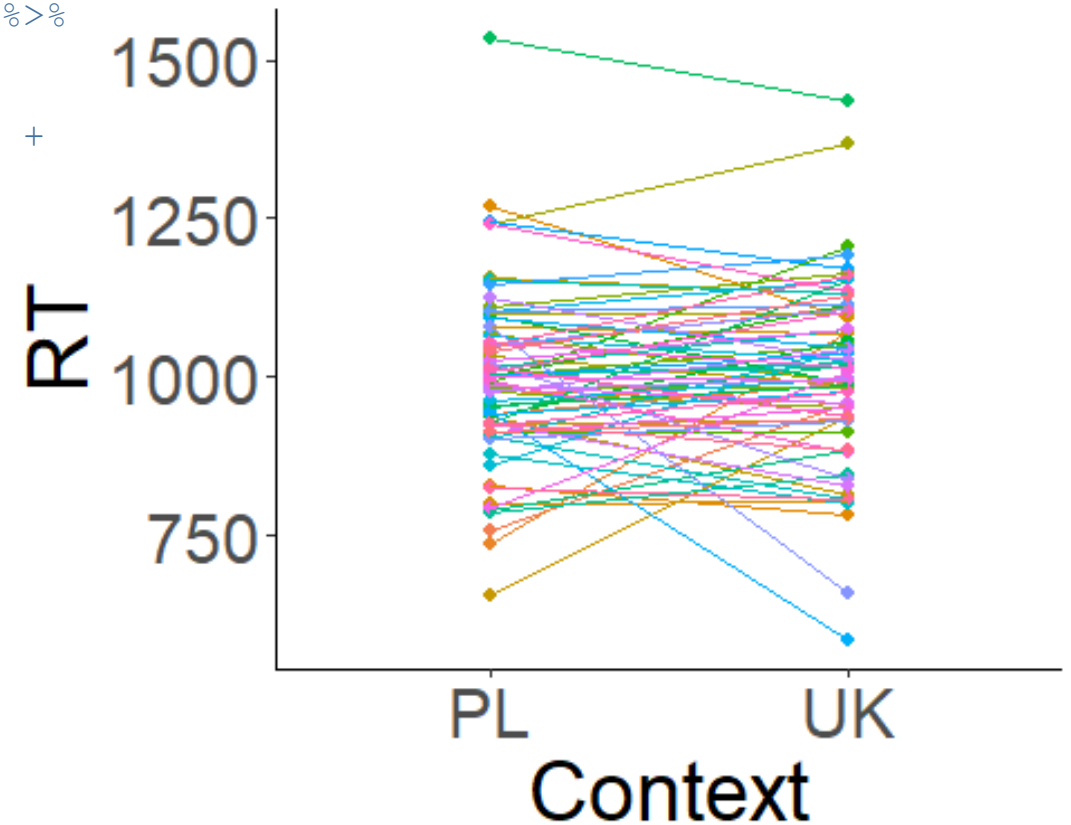
predict_response() for fixed effects

```
model_Large8 %>%  
  predict_response(c("Group", "Context")) %>%  
  ggplot(aes(x=as.numeric(x), y=predicted,  
             color=group, fill=group)) +  
  geom_line(linewidth=1.7) +  
  geom_ribbon(aes(ymin=conf.low, ymax=conf.high),  
             alpha = 0.3, colour = NA) +  
  scale_x_continuous(name =  
"Session", breaks=c(1,2)) +  
  scale_y_continuous(name = "RT [ms]") +  
  ggtitle("Predicted effects for Group:Context") +  
  theme_classic() +  
  theme(text = element_text(size=24),  
        element_line(size = 2))
```



predict_response() for random effects

```
model_Large8 %>%  
  ggpredict(c("Context", "Subject"), type = "re") %>%  
  ggplot(aes(x=x, y=predicted, group=group)) +  
  geom_point(size=1.7, aes(color=group)) +  
  geom_line(aes(color=group)) + theme_classic() +  
  scale_color_discrete(guide="none") +  
  scale_y_continuous(name="RT") +  
  scale_x_discrete(labels = c("PL",  
"UK"), name="Context") +  
  theme(text = element_text(size=28),  
element_line(size = 2))
```



Power analysis

Statistical tool that calculates the minimum sample size for a given study and analysis

It needs four primary components:

- Statistical power: the likelihood that a test will detect an effect of a certain size if there is one, usually set at 80% or higher
- Sample size: the minimum number of observations needed to observe an effect of a certain size with a given power level
- Alpha: usually 0.05
- Expected effect size

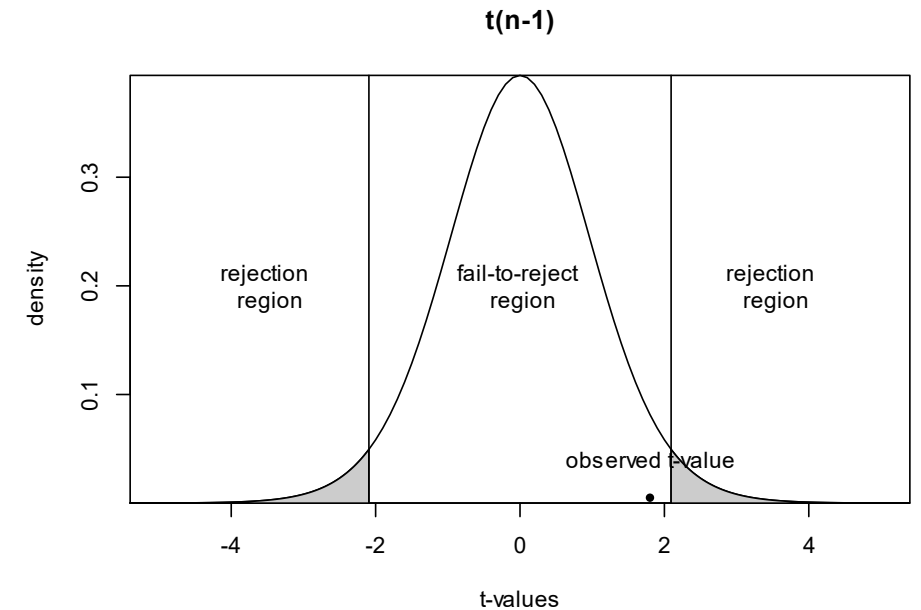
If you have three of those components you can calculate the fourth

- Determine power from existing sample
- Determine necessary sample size to reach a given power

Statistical power

Probability of not rejecting H_1 , if H_1 is true

	<i>If H_0 is True</i>	<i>If H_1 is True</i>
<i>Probability to reject H_0</i>	α	$1 - \alpha$
<i>Probability to not reject H_0</i>	$1 - \beta$ (power)	β



Calculate power of a given sample

```
library(simr)

powerSim(model_Large8, nsim=50, test = fcompare(RT~Context), progress = FALSE)

## Power for model comparison, (95% confidence interval):
##      28.00% (16.23, 42.49)
##
## Test: Likelihood ratio
##      Comparison to RT ~ Context + [re]
##
## Based on 50 simulations, (0 warnings, 0 errors)
## alpha = 0.05, nrow = 7227
##
## Time elapsed: 0 h 0 m 51 s
```

Calculate power of a given sample

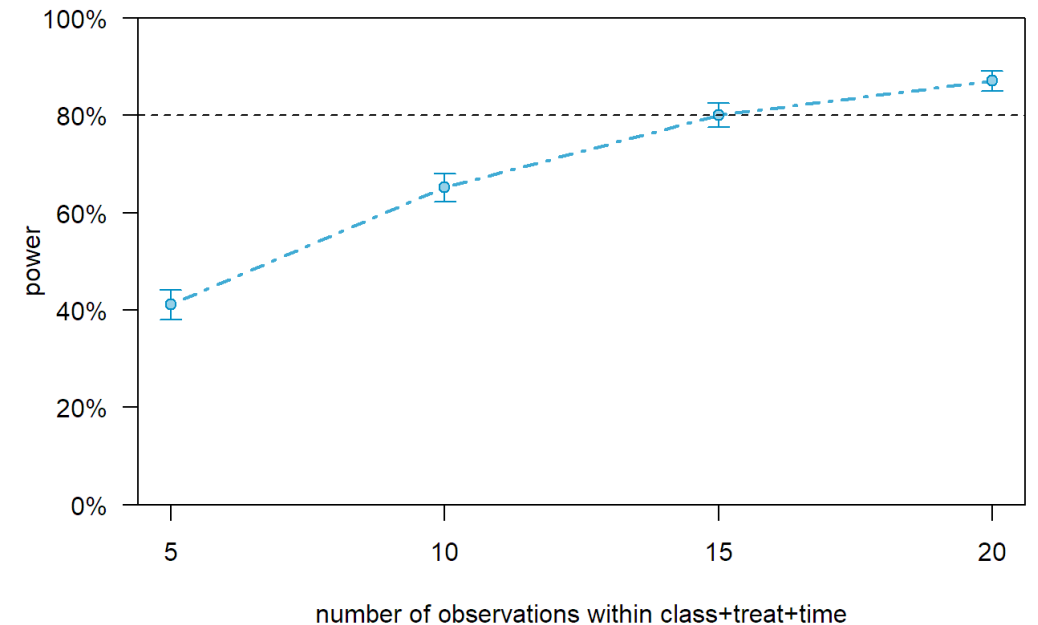
```
Model_11 <- extend(model_Large8, within="Subject+Context", n=10)

powerSim(Model_11, nsim=50, test = fcompare(RT~Context), progress = FALSE)

## Power for model comparison, (95% confidence interval):
##      18.00% ( 8.58, 31.44)
##
## Test: Likelihood ratio
##      Comparison to RT ~ Context + [re]
##
## Based on 50 simulations, (0 warnings, 0 errors)
## alpha = 0.05, nrow = 1467
##
## Time elapsed: 0 h 0 m 11 s
```

Calculate necessary sample size to get a desired result

```
p_curve_treat <-  
powerCurve(model_ext_subj,  
test=fcompare(y~time),within="class+tr  
eat+time", breaks=c(5,10,15,20))  
plot(p_curve_treat)
```



LME to-do list

1 Hypotheses

- Run power analysis

2 Prepare your data

3 Build your model

4 Analyse your model

5 Report your results

- Report the entire maximal model structure
- Report the results of the final model



Thank you
for your
attention!
