

Figure 1:  $r = 0.500$

# COMPUTATIONAL PHYSICS

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Jona Ackerschott, Julian Mayr

## Problem set 8

### Problem 1

### Problem 2

Using the scipy-builtin RK45 solver, the solution of the Lorenz attractor problem was computed numerically for different values of  $r$ . The initial condition  $y_0$  was chosen to be  $(0.1, 0.1, 0.1)$  + the chosen fixed Point. The solutions were 3d-plotted with matplotlib.

For the stable values of  $r$ , the solutions converge oscillating around the nearest fix point (stable solutions). For the higher values, they move around it chaotically without ever converging (chaotic solutions).

Next, for  $r=27$  and  $y_0$  as chosen in a), a stable solution, the  $z$  cordinate of the local minima in  $z$  of the solution were plotted against the previous  $z$  value. This plot converges against the Point  $(30, 30)$  on the diagonal, so  $z = 30$ . The slope of the funtion is less than 1, so the point seems to be stable, as the  $z$  coordinate also converges.

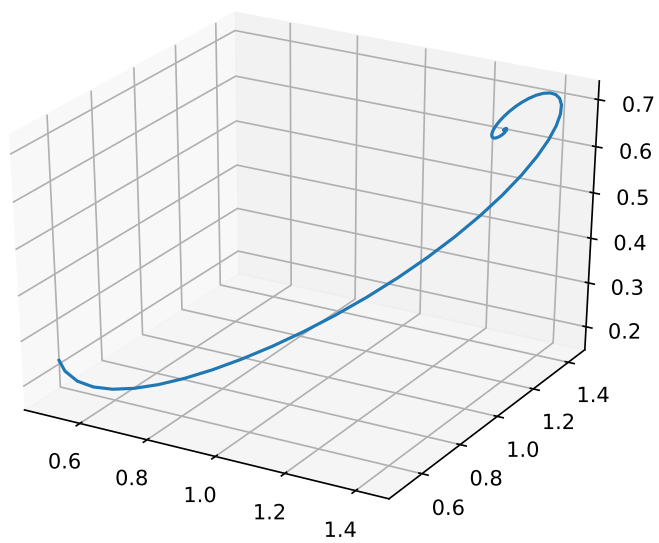


Figure 2:  $r = 1.150$

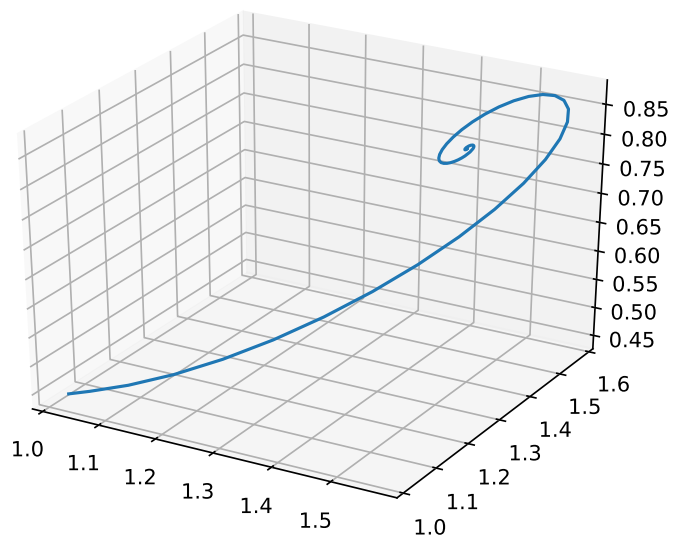


Figure 3:  $r = 1.3456$

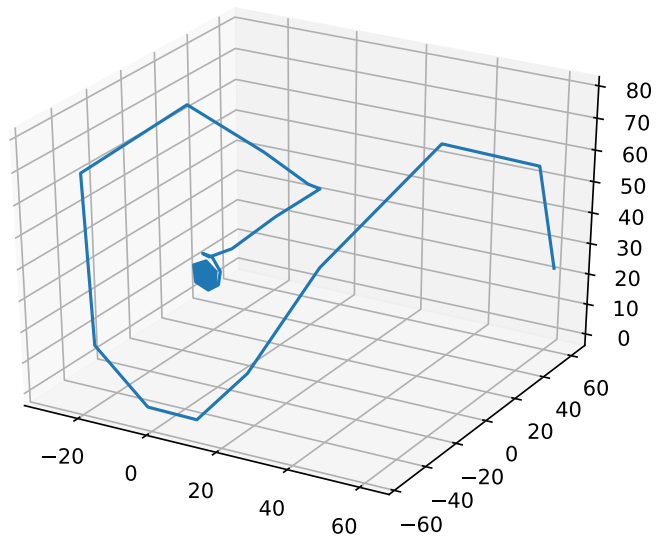
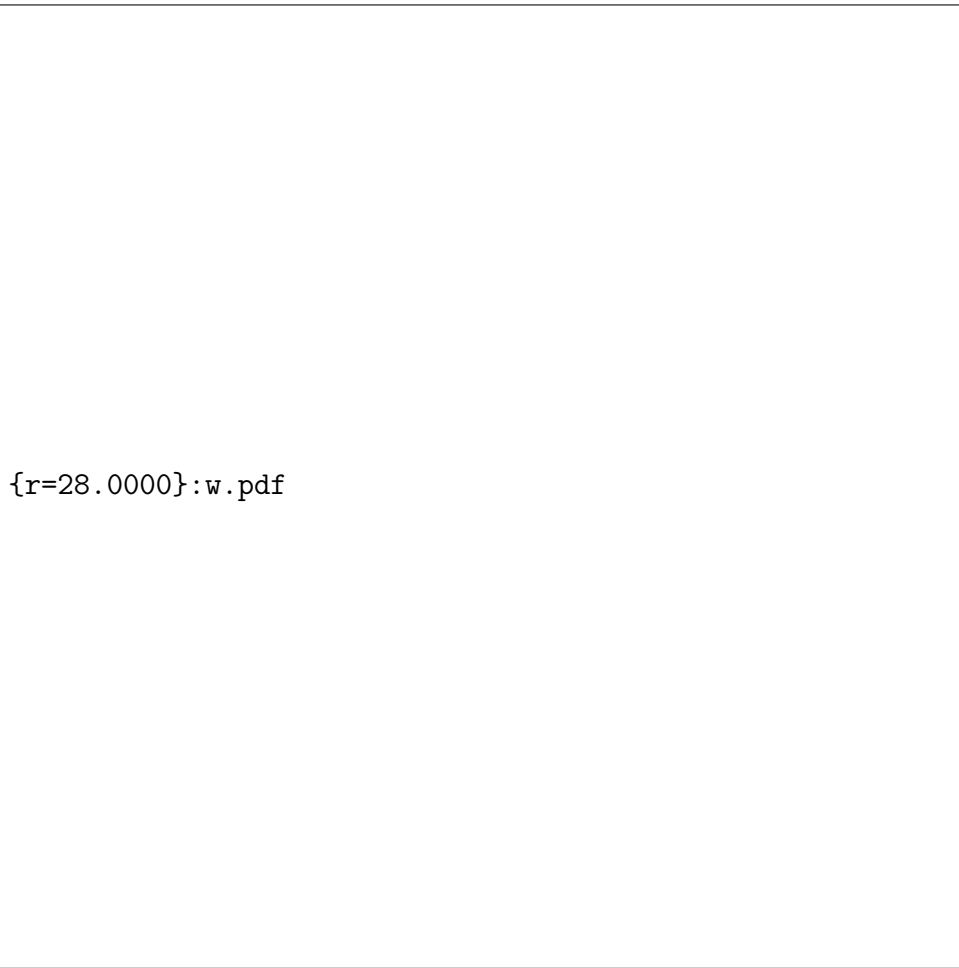


Figure 4:  $r = 24.000$



`{r=28.0000}:w.pdf`

Figure 5:  $r = 28.000$

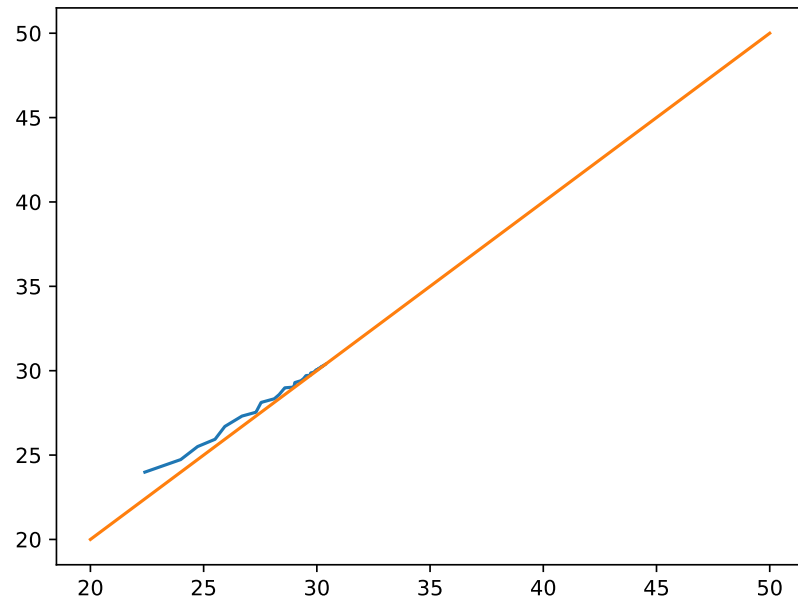


Figure 6:  $z_k(z_{k+1})$  plotted from  $k = 4$  to  $k = 100$

Source code 1: Mathematica input for problem 2