



# *Theories and Observations of Dark Energy*

## Final Presentation

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## 1 Literature introduction

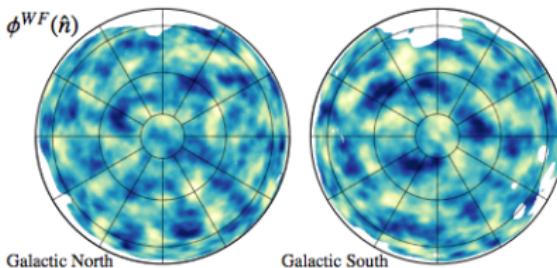
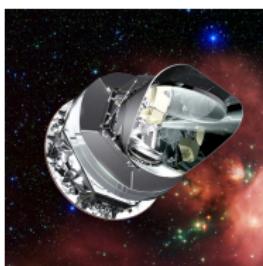
## 2 Background and Details

- CMB Lensing
- Galaxies
- Cross-correlation

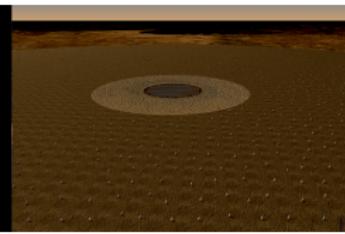
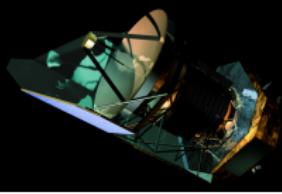
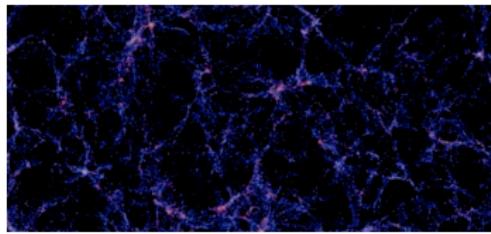
## 3 Conclusion

- Cross-correlation

## 4 "Cross-correlation" with *Dark Energy*



*Cross – correlation* Between The *CMB Lensing Potential*  
Measured By **PLANCK** And High-z Sub-mm *Galaxies*  
Detected By The **HERSCHEL-ATLAS** Survey



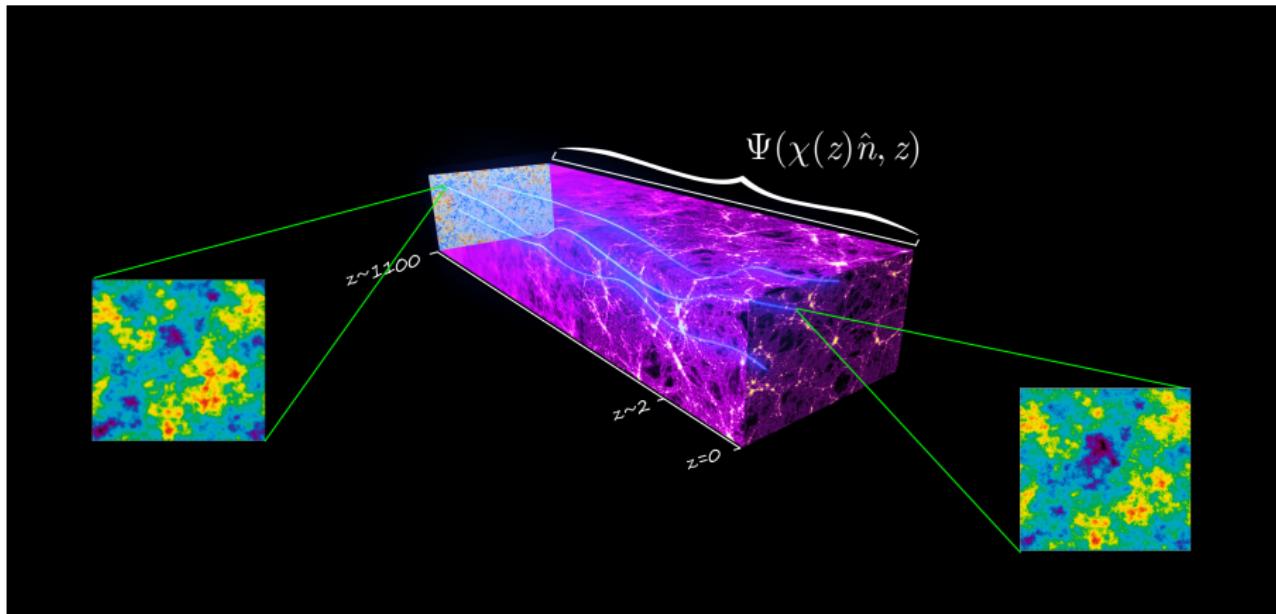
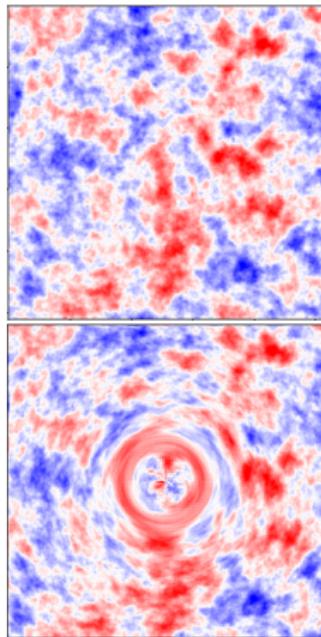


Figure: by PLANCK



$$\tilde{\Theta}(\hat{n}) = \Theta(\hat{n} + \alpha)$$

Deflection Angle:

$$\alpha(\hat{n}) = \nabla\phi(\hat{n})$$

Lensing potential:

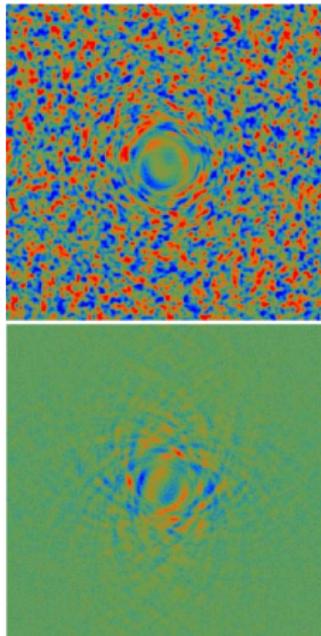
$$\begin{aligned}\phi(\hat{n}) &= -\frac{2}{c^2} \int_0^{z_*} \frac{cdz}{H(z)} \frac{\chi_* - \chi(z)}{\chi_* \chi(z)} \Psi(\chi(z)\hat{n}, z) \\ \chi(z) &= \int_0^z \frac{cdz}{H(z)}, \quad \chi_* = \chi(z_*)\end{aligned}$$

Where  $\Psi$  is Newtonian gravitational potential.

Figure: Unlensed and lensed  
CMB map(Wang Z.Y.,2018)



Polarization:



$$\delta \begin{bmatrix} E(\mathbf{k}) \\ B(\mathbf{k}) \end{bmatrix} = \int \frac{d^2 k'}{(2\pi)^2} W(k', \mathbf{k}') R(2\varphi_{\mathbf{k}'\mathbf{k}}) \begin{bmatrix} \tilde{E}(\mathbf{k}') \\ \tilde{B}(\mathbf{k}') \end{bmatrix}$$

Where:

$$R(2\varphi_{\mathbf{k}'\mathbf{k}}) = \begin{bmatrix} \cos 2\varphi_{\mathbf{k}'\mathbf{k}} & -\sin 2\varphi_{\mathbf{k}'\mathbf{k}} \\ \sin 2\varphi_{\mathbf{k}'\mathbf{k}} & \cos 2\varphi_{\mathbf{k}'\mathbf{k}} \end{bmatrix}$$

$$\varphi_{\mathbf{k}'\mathbf{k}} = \varphi_{\mathbf{k}'} - \varphi_{\mathbf{k}}$$

$$W(\mathbf{k}', \mathbf{k}') = -[\mathbf{k} \cdot (\mathbf{k} - \mathbf{k}')] \phi(\mathbf{k} - \mathbf{k}')$$

**Lens will convert a part of E-mode to B-mode polarization!**

Figure: Lensed E-mode and B-mode(W.Hu,2008)



Lensing convergence, which depends on the projected matter overdensity  
(Bartelmann & Schneider 2001)

$$\kappa(\hat{n}) = -\frac{1}{2} \nabla^2 \phi(\hat{n}) = \int_0^{z_*} dz W^\kappa(z) \delta(\chi(z)\hat{n}, z)$$
$$\delta(\chi(z)\hat{n}, z) = 1 - \frac{\rho_m(\chi(z)\hat{n}, z)}{\bar{\rho}_m}$$

Where the lensing kernel  $W^\kappa$  is:

$$W^\kappa(z) = \frac{3\Omega_{m,0}}{2c} \frac{H_0^2}{H(z)} (1+z) \chi(z) \frac{\chi_* - \chi(z)}{\chi_*}$$





Overdensity:

$$g(\hat{n}) = \int_0^{z_*} dz W^g(z) \delta(\chi(z) \hat{n}, z)$$

Where the kernel is (Xia et al. 2009):

$$W^g(z) = \frac{b(z) \frac{dN}{dz}}{\int dz' \frac{dN}{dz'}} + \frac{3\Omega_m}{2c} \frac{H_0^2}{H(z)} (1+z) \chi(z) \int_z^{z_*} dz' \left(1 - \frac{\chi(z)}{\chi(z')}\right) (\alpha(z') - 1) \frac{dN}{dz'}$$

Previous analyses indicate:

Bias(Xia et al. 2012; Cai et al. 2013):

$$b \simeq 3$$

Slope(Béthermin et al. 2012)

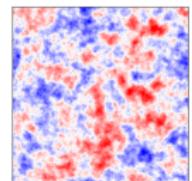
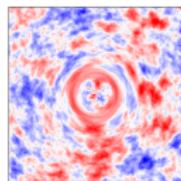
$$\alpha \simeq 2, \text{Noise} \propto S^{-\alpha}$$

# Cross-correlation

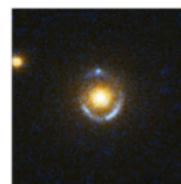


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cross-correlation range





Theoretically(Limber,1953):

Cross-correlation:

$$C_{\ell}^{\kappa g} = \int_0^{z_*} \frac{dz}{c} \frac{H(z)}{\chi^2(z)} W^{\kappa}(z) W^g(z) P(k = \frac{\ell}{\chi(z)}, z)$$

Mean redshift:

$$z = \frac{\int_0^{z_*} z \frac{dz}{c} \frac{H(z)}{\chi^2(z)} \chi^2(z) W^{\kappa}(z) W^g(z) P(k = \frac{\ell}{\chi(z)}, z)}{\int_0^{z_*} \frac{dz}{c} \frac{H(z)}{\chi^2(z)} W^{\kappa}(z) W^g(z) P(k = \frac{\ell}{\chi(z)}, z)} \simeq 2$$

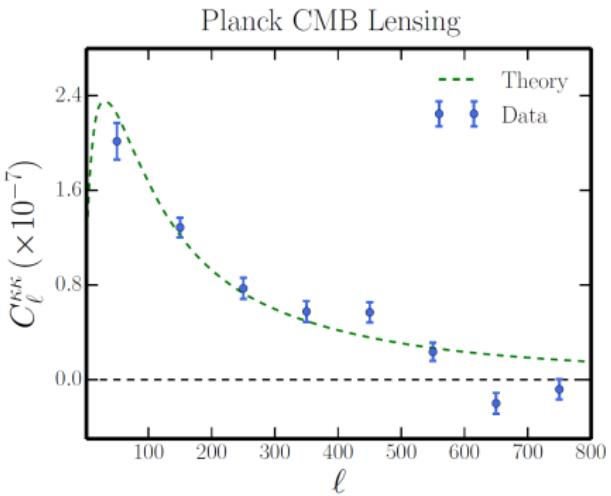


Figure: **CMB convergence autopower spectrum**

$$C_\ell^{\kappa\kappa} = \int_0^{z_*} \frac{dz}{c} \frac{H(z)}{\chi^2(z)} [W^\kappa(z)]^2 P(k = \frac{\ell}{\chi(z)}, z)$$

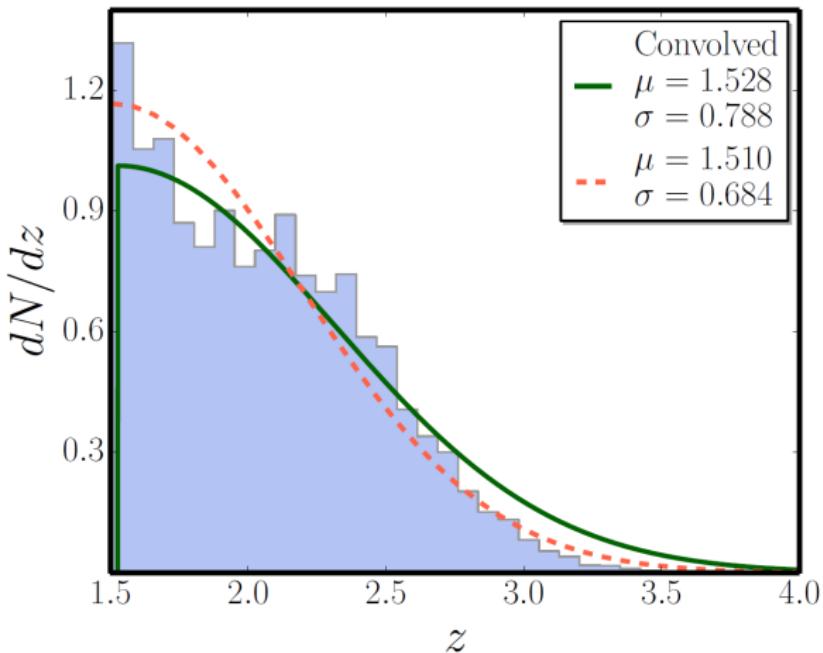


Figure: Redshift distribution of H-ATLAS galaxies

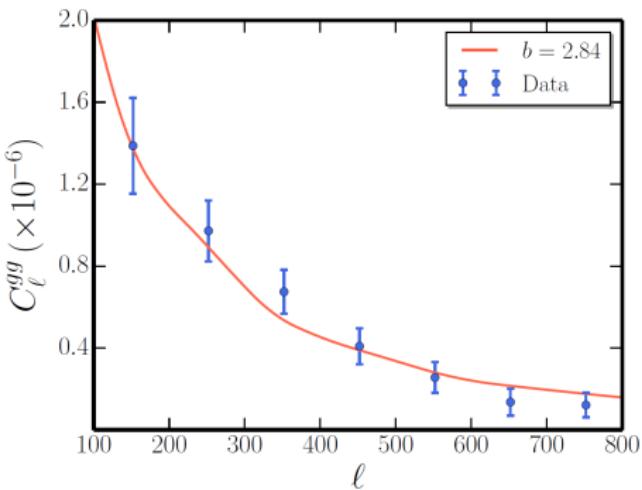


Figure: **Galaxies autopower spectrum**

$$C_\ell^{\text{gg}} = \int_0^{z_*} \frac{dz}{c} \frac{H(z)}{\chi^2(z)} [W^g(z)]^2 P(k = \frac{\ell}{\chi(z)}, z)$$

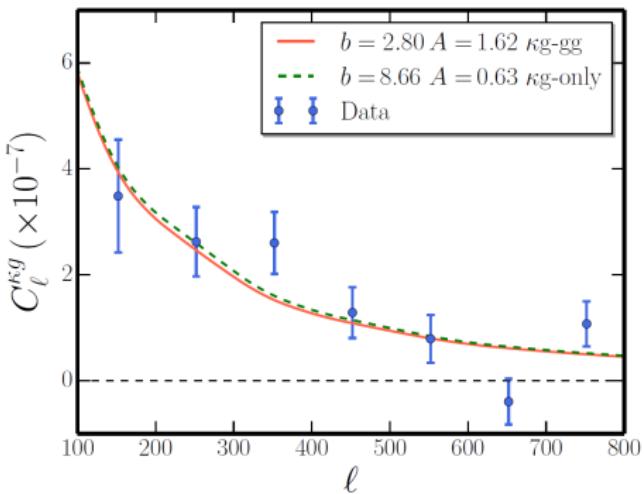


Figure: **Cross-correlation**

$$C_\ell^{\text{kg}} = \int_0^{z_*} \frac{dz}{c} \frac{H(z)}{\chi^2(z)} W^\kappa(z) W^g(z) P(k = \frac{\ell}{\chi(z)}, z)$$

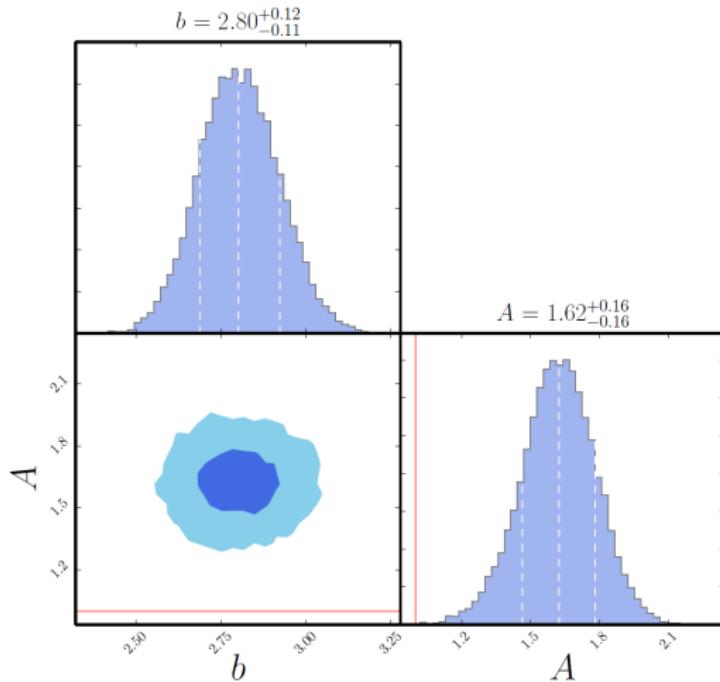


Figure: b-A plane with the 68% and 95% confidence,A is higher than expected from the standard model

# Cross-correlation with *Dark Energy*



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$$b(z) \quad A \text{ of } C_{\ell}^{\kappa g} \quad H_0, H(z) \quad \Omega_m \quad \frac{dN}{dz}$$



$$\Omega_{\Lambda}$$



# Appreciate your Criticism