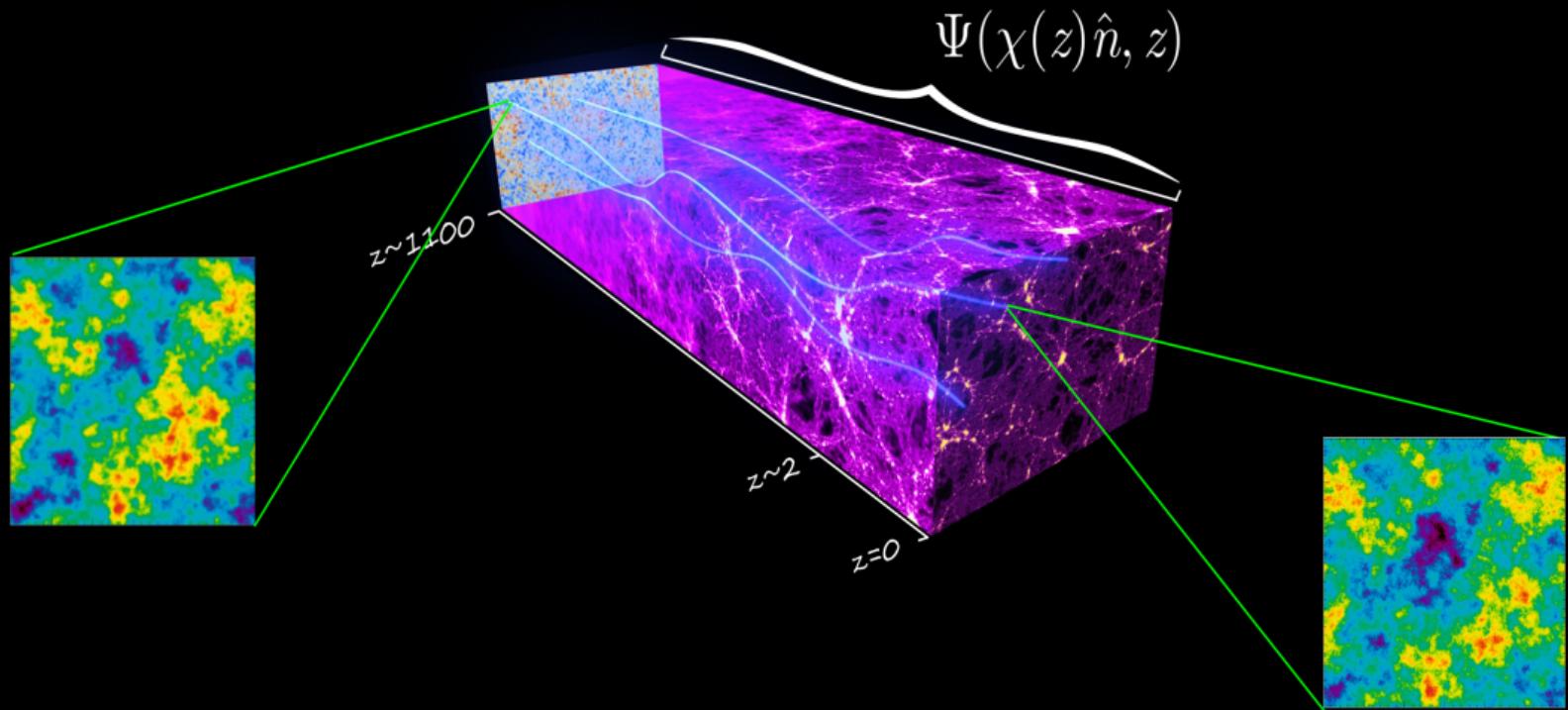


A Forecast of tomographic cross-correlation of CSST cosmic shear and ALiCPT CMB lensing

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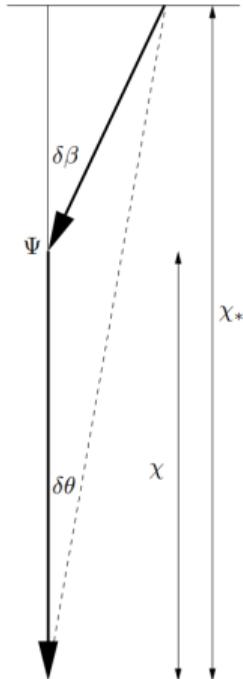
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Gravitational lens

Coforming Newtonian Gauge:



$$ds^2 = a^2(t)[(1 + 2\Psi_N)dt^2 - (1 + 2\Phi_N)d\vec{x}^2]$$

Deflection angle:

$$\alpha = -\frac{2}{c^2} \int_0^{z_*} \frac{cdz}{H(z)} \frac{\chi_* - \chi}{\chi_* \chi} \nabla_{\theta} \Psi(\theta, z)$$

Jacobian matrix:

$$A_{ij} = \frac{\partial \beta}{\partial \theta} = \delta_{ij} + \frac{\partial \alpha_j}{\partial \theta_i} = \begin{bmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{bmatrix}$$

κ : convergence, isotropic magnification ;

γ : shear, anisotropic stretching

CMB Lensing

Lensing effect:

$$\tilde{\Theta}(\boldsymbol{\theta}) = \Theta(\boldsymbol{\theta} + \boldsymbol{\alpha}(\boldsymbol{\theta})) = \Theta(\boldsymbol{\theta}) + \nabla^i \psi \nabla_i \Theta(\boldsymbol{\theta}) + \mathcal{O}(\psi^2)$$

Where $\boldsymbol{\alpha}(\boldsymbol{\theta}) = \nabla \psi(\boldsymbol{\theta})$, and flat sky with plane wave mode:

$$\Theta(\boldsymbol{\theta}) = \int \frac{d^2 \ell}{(2\pi)^2} \Theta(\boldsymbol{\ell}) e^{i \boldsymbol{\ell} \cdot \boldsymbol{\theta}}, \psi(\boldsymbol{\theta}) = \int \frac{d^2 L}{(2\pi)^2} \psi(\boldsymbol{L}) e^{i \boldsymbol{L} \cdot \boldsymbol{\theta}}$$

$$\tilde{\Theta}(\boldsymbol{\ell}) \approx \Theta(\boldsymbol{\ell}) - \int \frac{d^2 \ell'}{(2\pi)^2} \Theta(\boldsymbol{\ell}) [\boldsymbol{\ell} \cdot (\boldsymbol{\ell} - \boldsymbol{\ell}')] \psi(\boldsymbol{\ell} - \boldsymbol{\ell}')$$

Mode-coupling:

$$\langle \tilde{\Theta}(\boldsymbol{\ell}_1) \tilde{\Theta}^*(\boldsymbol{\ell}_2) \rangle \neq 0, \quad \text{for } \boldsymbol{\ell}_1 \neq \boldsymbol{\ell}_2$$

CMB Lensing noise level

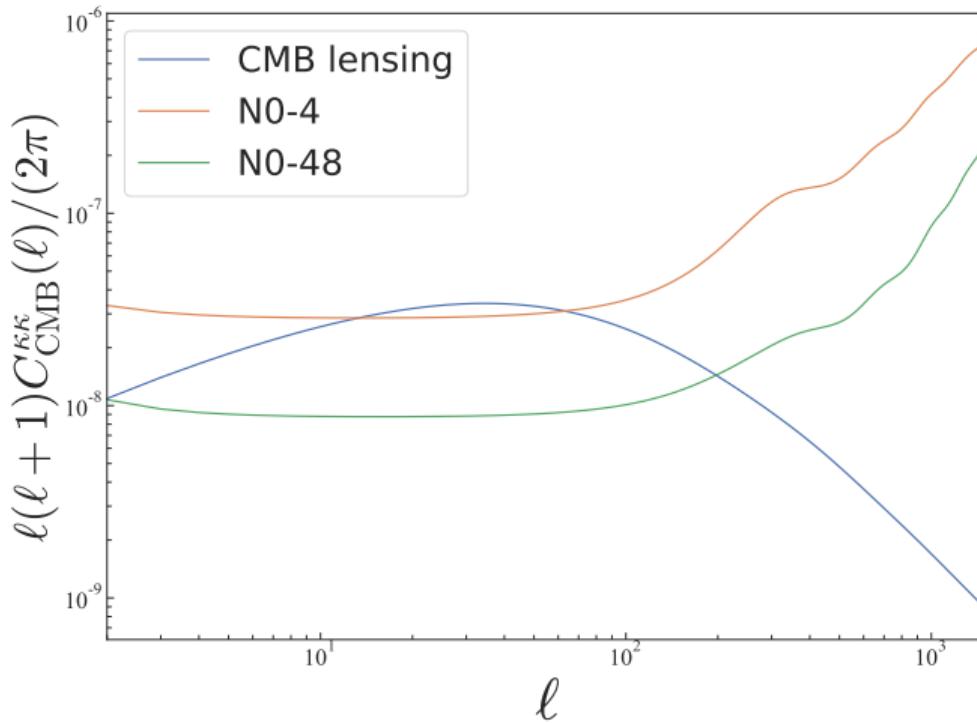
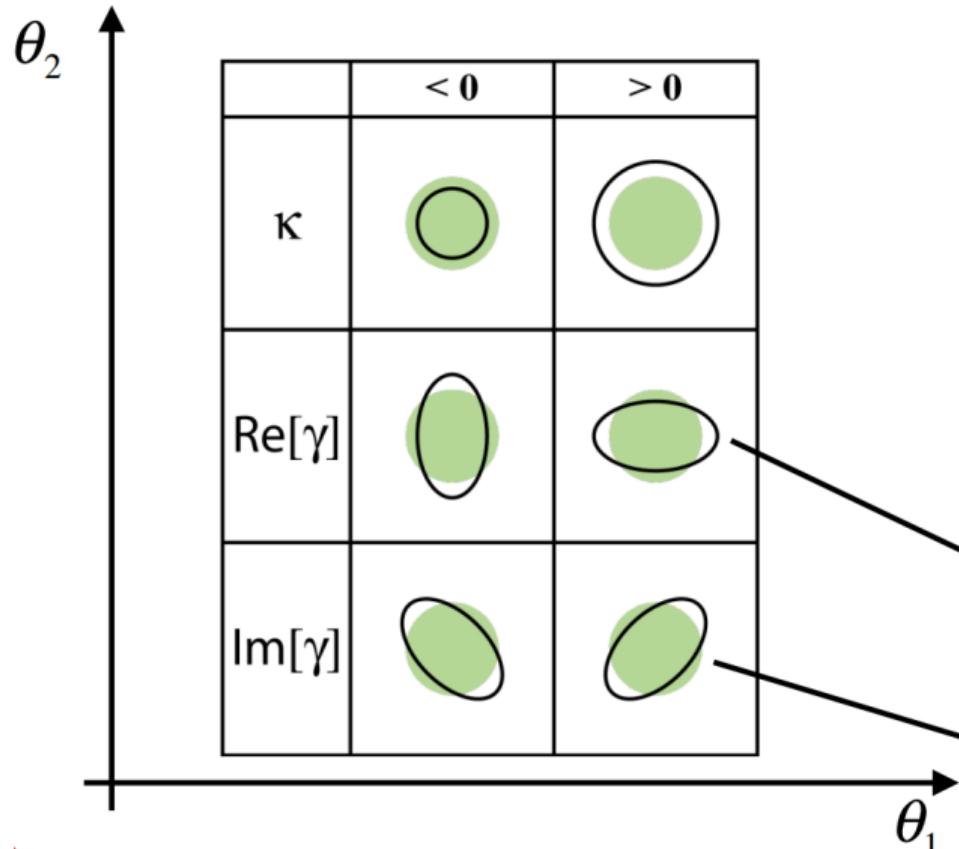


Figure: Power spectrum of CMB lensing potential and reconstruction noise with N0-4 and N0-48

Weak lensing effect



$$\kappa = \psi_{,11} + \psi_{,22}$$

$$\gamma_1 = \psi_{,11} - \psi_{,22}$$

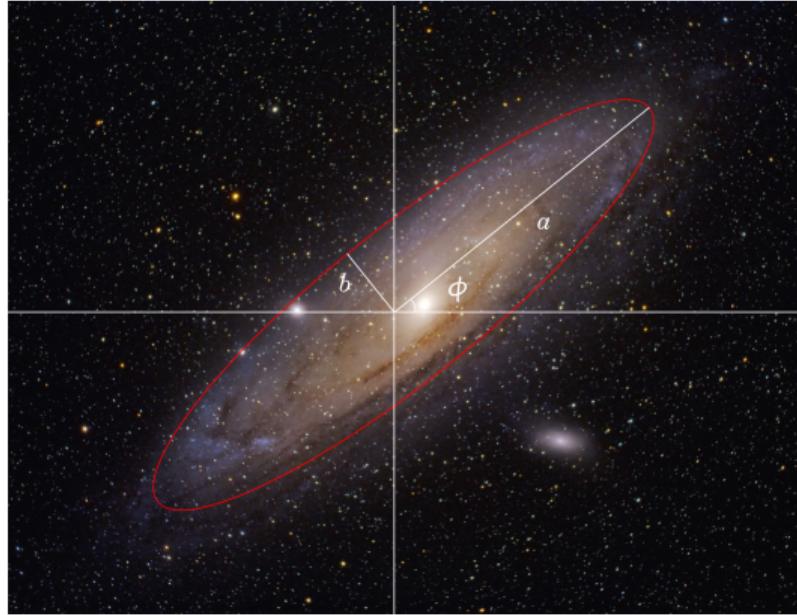
$$\gamma_2 = \psi_{,12}$$

e.g.

$$\psi(\theta_1, \theta_2) = \theta_1^2 + \frac{1}{2}\theta_2^2$$

$$\psi \sim \theta_1 \cdot \theta_2 \Rightarrow \gamma_2$$

Shape of galaxies



Galaxy ellipticity:

$$\varepsilon_s = \frac{a - b}{a + b} \exp(2i\phi) = \varepsilon_{s1} + i\varepsilon_{s2}$$

Shape of galaxies

Centroid:



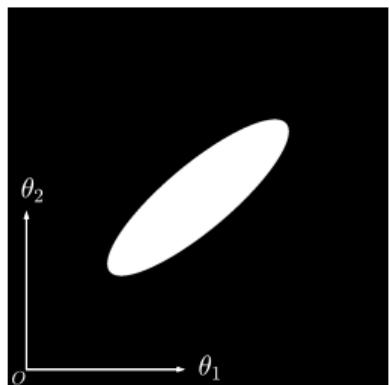
$$\bar{\theta}_i = \int d\theta \theta_i q_I(I(\theta))$$

Surface brightness quadrupole (e.g. Blandford et al. 1991).

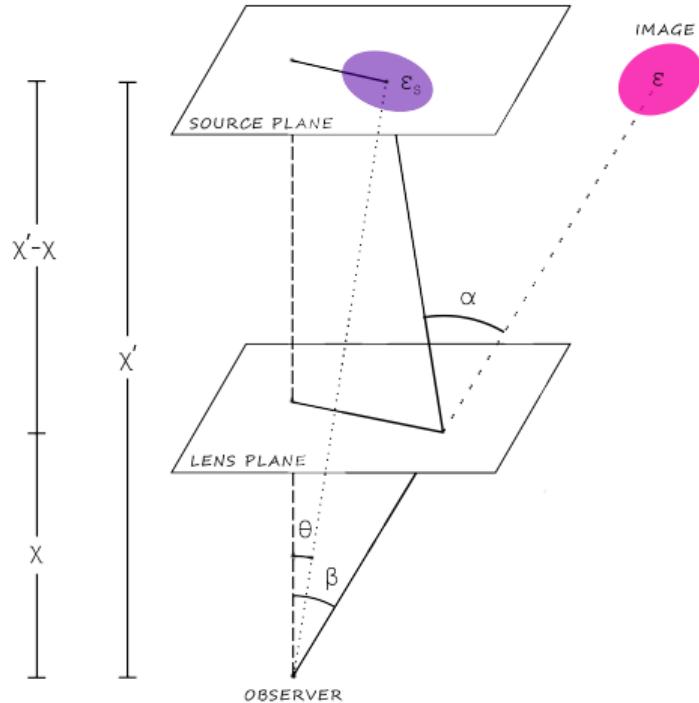
$$Q_{ij} = \int d^2\theta q_I(I(\theta))(\theta_i - \bar{\theta}_i)(\theta_j - \bar{\theta}_j)$$

Ellipticity (Bonnet Mellier 1995) :

$$\varepsilon = \frac{Q_{11} - Q_{22} + 2iQ_{12}}{Q_{11} + Q_{22} + 2\sqrt{\det(Q)}}$$



Weak lensing effect on galaxies

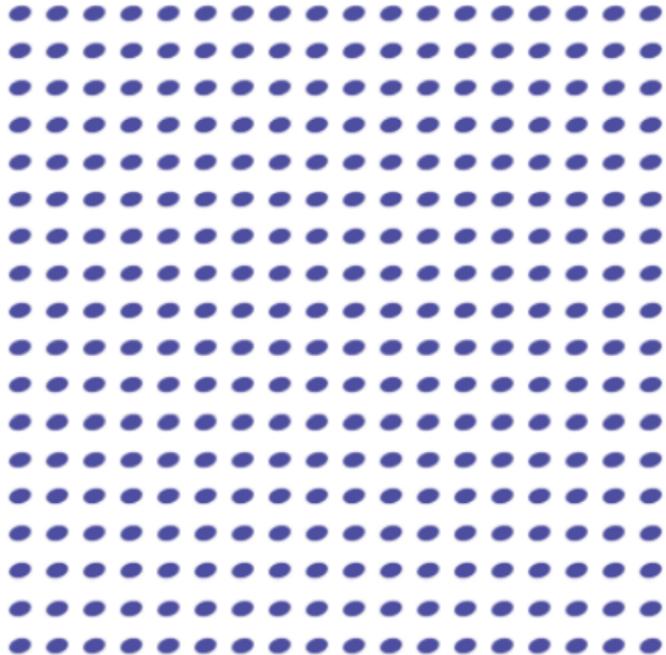


$$\tilde{Q}_{ij} = \frac{\int d^2\beta I_s(\beta)(\beta_i - \bar{\beta}_i)(\beta_j - \bar{\beta}_j)}{\int d^2\beta I_s(\beta)}$$

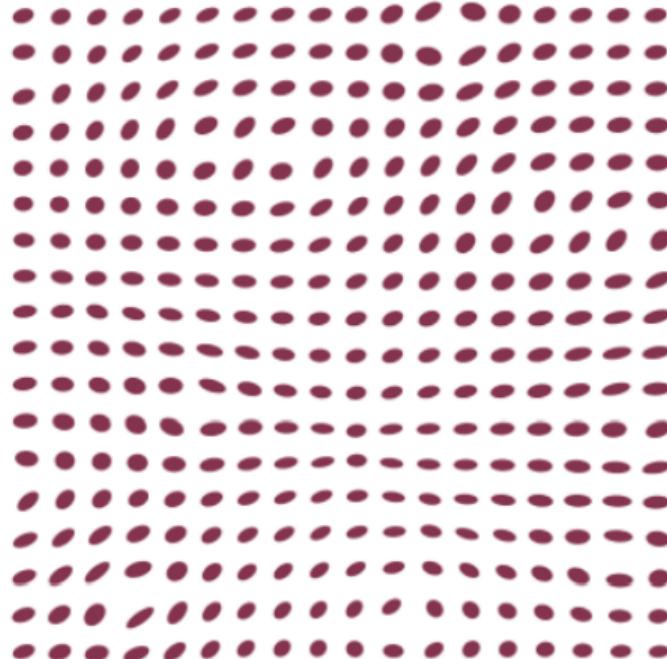
Weak lensing effect:

$$Q = A^{-1} \tilde{Q} A^{-1}$$
$$\Rightarrow \varepsilon = \varepsilon_s + \gamma + \mathcal{O}\left[\left(\frac{\gamma}{1-\kappa}\right)^2\right]$$

Weak lensing effect on galaxies



Unlensed sources



Weak lensing

Ellipticity noise ε_s

$$\varepsilon = \varepsilon_s + \gamma$$

Distribution of intrinsic ellipticity (Bartelmann & Narayan, 1995):

$$p(\varepsilon_s) = \frac{\exp(-|\varepsilon_s|^2/\sigma_\varepsilon^2)}{\pi\sigma_\varepsilon^2[1 - \exp(-1/\sigma_\varepsilon^2)]}$$

$\sigma_\varepsilon \approx 0.2$ (e.g. Miralda-Escudé 1991b; Tyson & Seitzer 1988)

$$\langle \varepsilon \rangle \approx \gamma, \quad e^{4i\varphi} \langle \varepsilon \varepsilon \rangle(\vartheta) = e^{4i\varphi} \langle \gamma \gamma \rangle(\vartheta) = \xi_-(\vartheta), \quad \langle \varepsilon \varepsilon^* \rangle(\vartheta) = \langle \gamma \gamma^* \rangle(\vartheta) = \xi_+(\vartheta)$$

In harmonic space:

$$\langle \gamma(\ell') \gamma^*(\ell) \rangle = (2\pi)^2 \delta_D(\ell' - \ell) (C_\ell^{\gamma\gamma} + N_\ell)$$

Where:

$$N_\ell = \frac{4\pi f_{\text{sky}}}{N_g} \sigma_\varepsilon^2$$

Theoretical C_ℓ

E/B mode of cosmic shear: $\gamma_E(\ell) = \kappa(\ell)$; $\gamma_B(\ell) = 0$
corss-correlation C_ℓ 's:

$$C_i^{\kappa_{\text{CMB}}\gamma_E}(\ell) = \int_0^{z_*} \frac{cdz}{H(z)} \frac{q_{\text{CMB}}(z)q_i(z)}{\chi^2} P_\delta(k = \frac{\ell + 1/2}{\chi}, z)$$

Lensing efficiency:

$$q_i(z) = \frac{3\Omega_{m0}}{2} \frac{H_0^2}{c^2} (1+z)\chi(z) \int_z^{z_*} n_i(z') \frac{\chi(z') - \chi(z)}{\chi(z')} dz'$$

CMB lensing kernel:

$$q_{\text{CMB}}(z) = \frac{3\Omega_{m0}}{2c} \frac{H_0^2}{H(z)} (1+z)\chi(z)$$

Systematic error

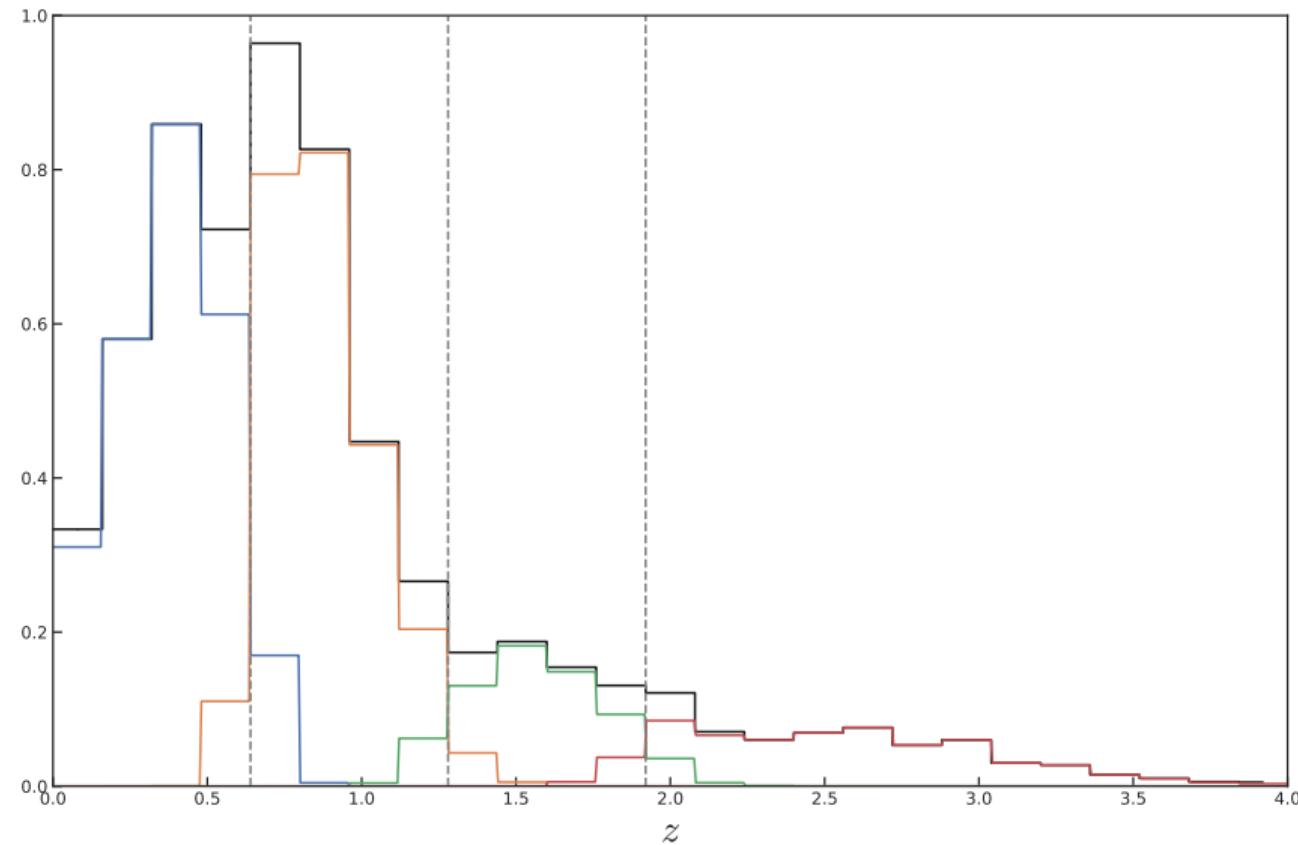
1 Intrinsic Alignment (e.g. Hand et al., 2013):

$$q_{\text{IA},i}(z) = -A_0 \left(\frac{L}{L_0} \right)^\beta \left(\frac{1+z}{1+z_0} \right)^\eta \frac{C_1 \rho_{m,0}}{D(z)} n_i(z)$$

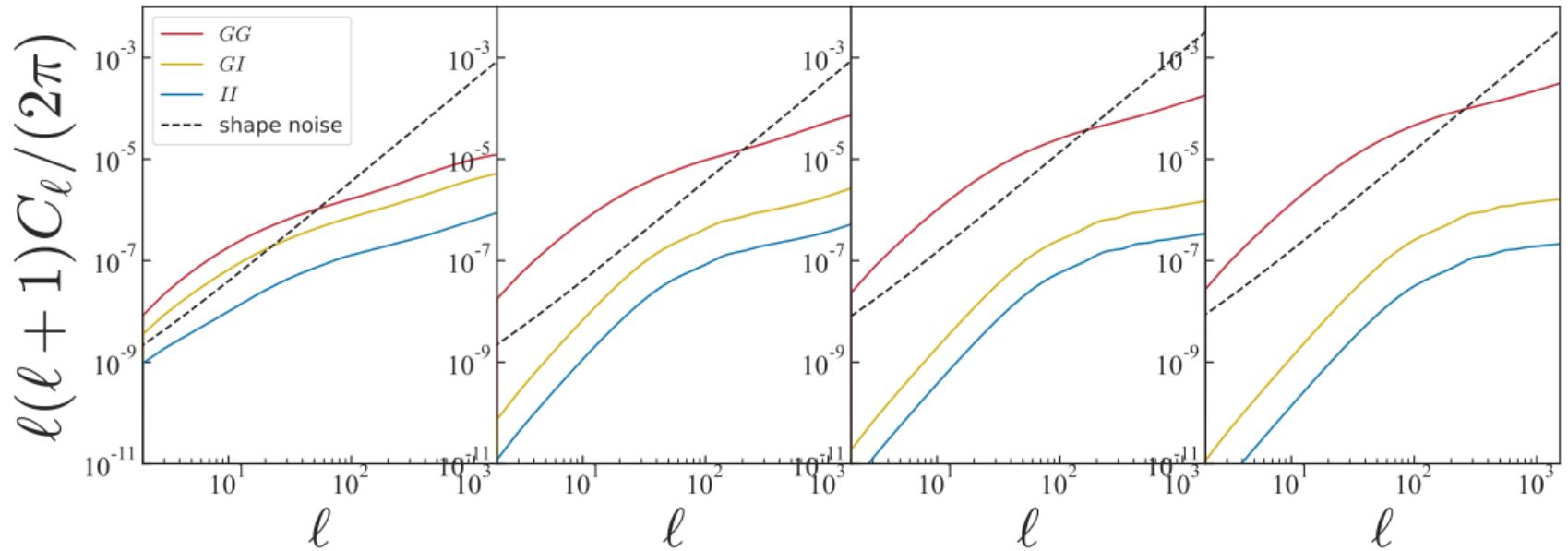
2 Photo-z error

$$p(z^P|z) = \frac{1}{\sqrt{2\pi}\sigma_z(1+z)} \exp\left[-\frac{(z - z^P - \Delta_z^i)^2}{2(\sigma_z(1+z))^2}\right]$$

Photo- z



Noise level



Cross-correlation algorithm

$$\kappa_{\text{CMB}}(\ell) = \zeta_1(\ell)(C_{\text{CMB}}^{\kappa\kappa}(\ell))^{1/2}$$
$$G(\ell) = \zeta_1(\ell) \frac{C_\ell^{G\kappa}}{(C_{\text{CMB}}^{\kappa\kappa}(\ell))^{1/2}} + \zeta_2(\ell) \left[C_\ell^{GG} - \frac{(C_\ell^{G\kappa})^2}{C_{\text{CMB}}^{\kappa\kappa}(\ell)} \right]^{1/2}$$

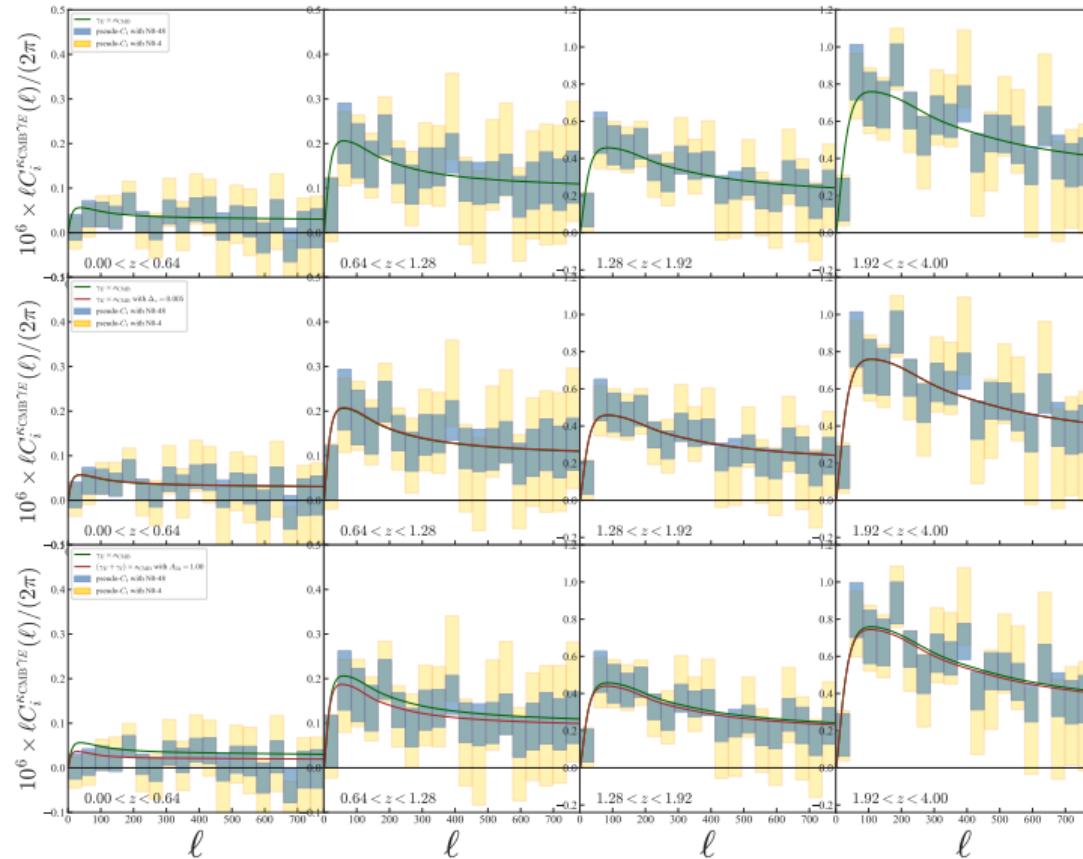
$\zeta_{1,2}$ are two complex numbers drawn from a Gaussian distribution with unit variance (Kamionkowski et al.1997).

$$\gamma(\ell) = \left(\frac{\ell_1^2 - \ell_2^2 + 2i\ell_1\ell_2}{|\ell|^2} \right) G(\ell) = G(\ell)e^{2i\beta}$$

pseudo- C_ℓ measurement:

$$\langle \kappa_{\text{CMB}}(\ell) \gamma_{E,i}^*(\ell') \rangle = (2\pi)^2 \delta_D(\ell - \ell') C_i^{\kappa_{\text{CMB}} \gamma_E}(\ell)$$

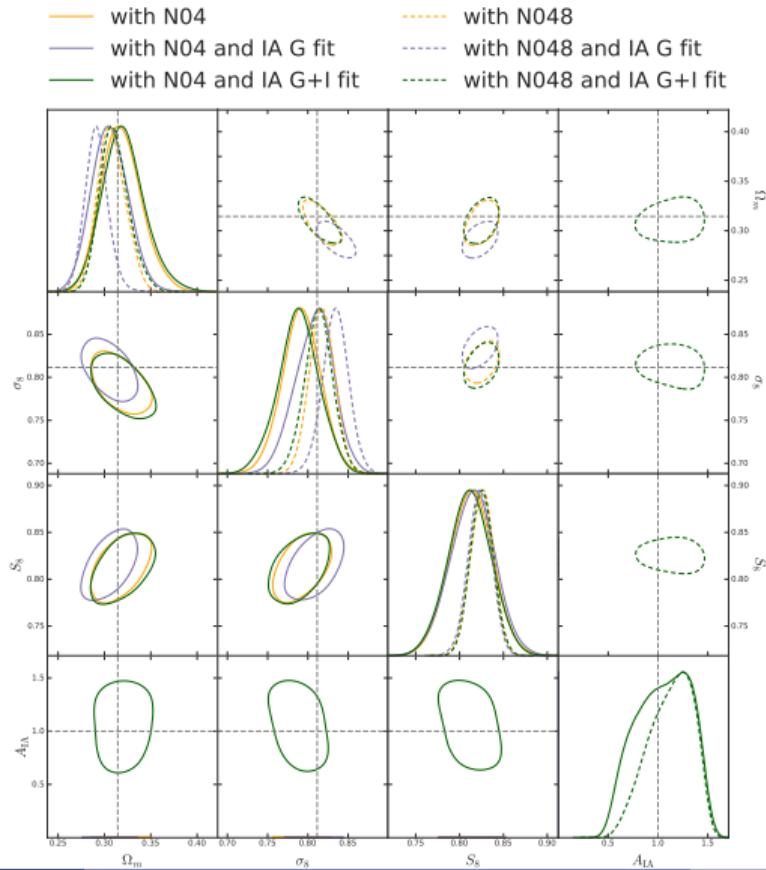
pseudo- C_ℓ



Prior

| Parameters | Fiducial value | Prior |
|-----------------|----------------|----------------|
| Ω_m | 0.314 | $U(0.05, 0.7)$ |
| h | 0.67 | fixed |
| Ω_b | 0.049 | fixed |
| σ_8 | 0.811 | $U(0.3, 1.3)$ |
| n_s | 0.96 | fixed |
| A_{IA} | 1.0 | $U(0.5, 1.5)$ |
| Δ_z^1 | 0.005 | fixed |
| Δ_z^2 | 0.005 | fixed |
| Δ_z^3 | 0.005 | fixed |
| Δ_z^4 | 0.005 | fixed |
| σ_z | 0.05 | fixed |

Cosmological constraint



Cosmological constrain

| Parameter 68% limits | with N04 | N04 IA G fit | N04 IA G+I fit |
|----------------------|---------------------------|---------------------------|---------------------------|
| Ω_m | $0.319^{+0.019}_{-0.023}$ | 0.306 ± 0.020 | $0.321^{+0.020}_{-0.025}$ |
| σ_8 | 0.792 ± 0.024 | $0.808^{+0.026}_{-0.022}$ | 0.788 ± 0.025 |
| S_8 | 0.813 ± 0.024 | 0.815 ± 0.025 | 0.812 ± 0.024 |
| A_{IA} | / | / | $1.05^{+0.34}_{-0.23}$ |
| α | 0.45 | 0.47 | 0.45 |

| Parameter 68% limits | with N048 | N048 IA G fit | N048 IA G+I fit |
|----------------------|---------------------------|---------------------------|---------------------------|
| Ω_m | $0.308^{+0.014}_{-0.016}$ | $0.291^{+0.011}_{-0.013}$ | $0.311^{+0.013}_{-0.017}$ |
| σ_8 | 0.817 ± 0.016 | 0.834 ± 0.016 | 0.813 ± 0.018 |
| S_8 | 0.825 ± 0.013 | 0.823 ± 0.013 | 0.825 ± 0.013 |
| A_{IA} | / | / | $1.13^{+0.27}_{-0.18}$ |
| α | 0.40 | 0.45 | 0.44 |

Appreciate your Criticism