

# CS4670: Computer Vision

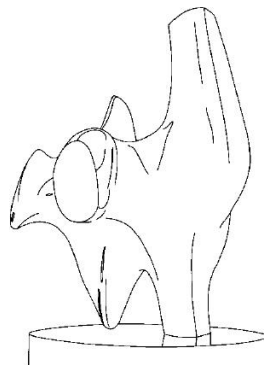
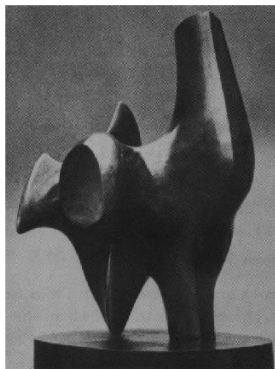
Noah Snavely

## Lecture 2: Edge detection

# SHADOW

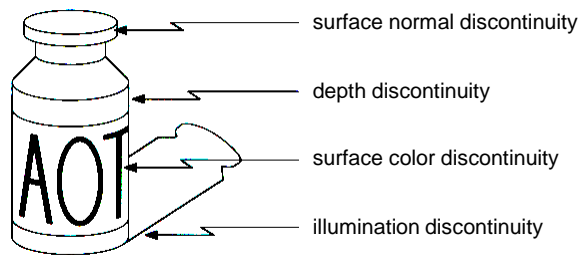
From [Sandlot Science](#)

## Edge detection



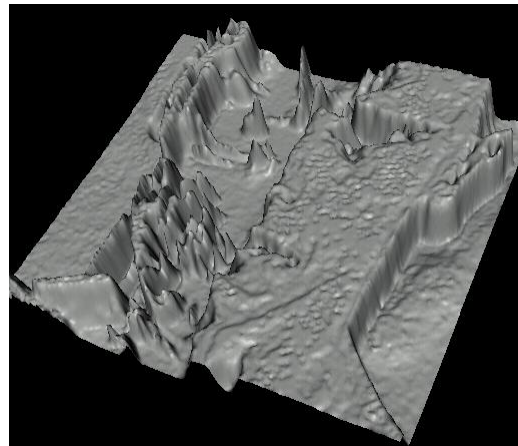
- Convert a 2D image into a set of curves
  - Extracts salient features of the scene
  - More compact than pixels

## Origin of Edges



- Edges are caused by a variety of factors

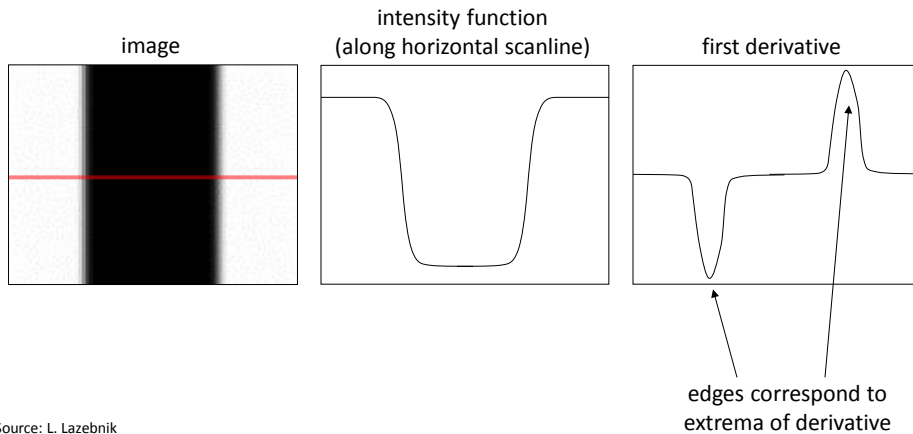
## Images as functions...



- Edges look like steep cliffs

## Characterizing edges

- An edge is a place of *rapid change* in the image intensity function



## Image derivatives

- How can we differentiate a *digital* image  $F[x,y]$ ?
  - Option 1: reconstruct a continuous image,  $f$ , then compute the derivative
  - Option 2: take discrete derivative (finite difference)

$$\frac{\partial f}{\partial x}[x,y] \approx F[x+1,y] - F[x,y]$$

How would you implement this as a linear filter?

$$\frac{\partial f}{\partial x} : \begin{bmatrix} \square & \square & \square \\ \square & \square & \square \\ \square & \square & \square \end{bmatrix} H_x$$

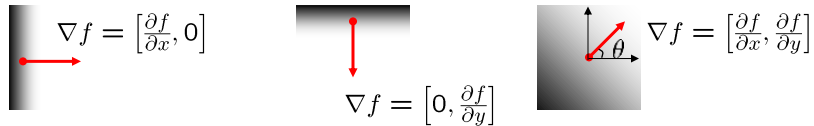
$$\frac{\partial f}{\partial y} : \begin{bmatrix} \square & \square & \square \\ \square & \square & \square \\ \square & \square & \square \end{bmatrix} H_y$$

Source: S. Seitz

## Image gradient

- The *gradient* of an image:  $\nabla f = \left[ \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$

The gradient points in the direction of most rapid increase in intensity



The *edge strength* is given by the gradient magnitude:

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

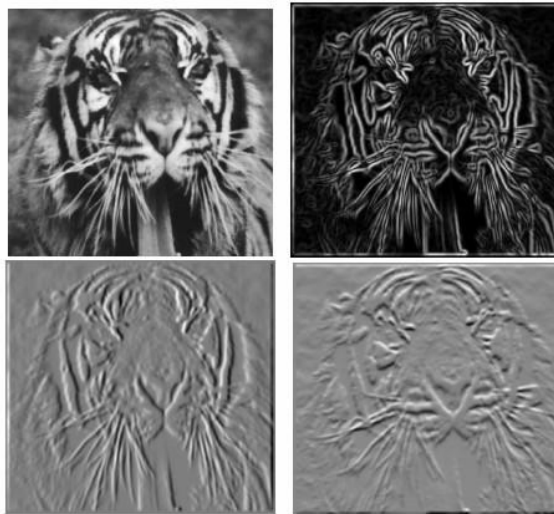
The gradient direction is given by:

$$\theta = \tan^{-1} \left( \frac{\partial f / \partial y}{\partial f / \partial x} \right)$$

- how does this relate to the direction of the edge?

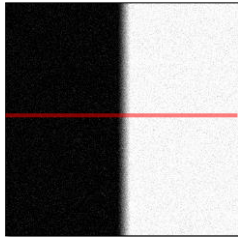
Source: Steve Seitz

## Image gradient

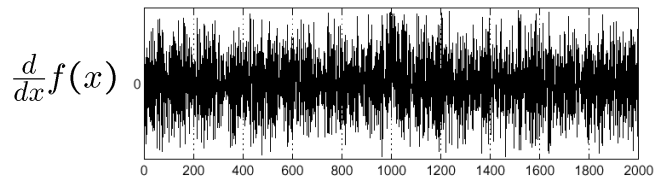
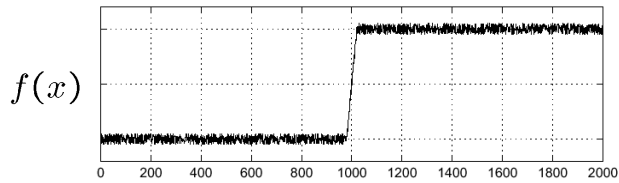


Source: L. Lazechnik

## Effects of noise



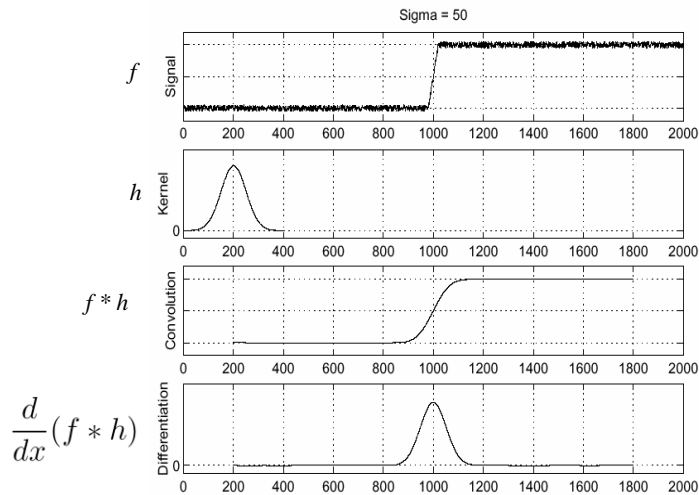
Noisy input image



Where is the edge?

Source: S. Seitz

## Solution: smooth first

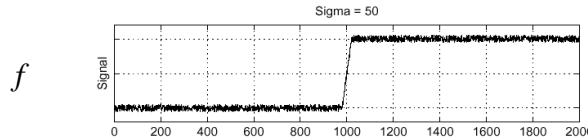


To find edges, look for peaks in  $\frac{d}{dx}(f * h)$

Source: S. Seitz

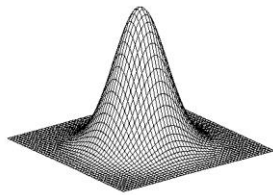
## Associative property of convolution

- Differentiation is convolution, and convolution is associative:  $\frac{d}{dx}(f * h) = f * \frac{d}{dx}h$
- This saves us one operation:



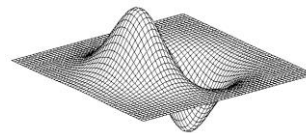
Source: S. Seitz

## 2D edge detection filters



Gaussian

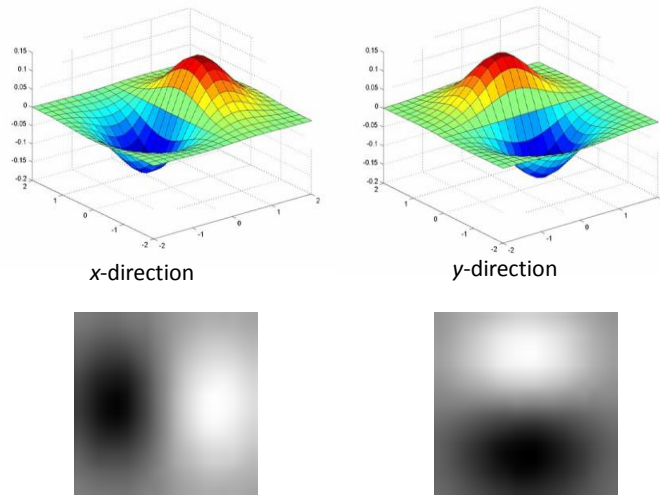
$$h_{\sigma}(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



derivative of Gaussian (x)

$$\frac{\partial}{\partial x} h_{\sigma}(u, v)$$

## Derivative of Gaussian filter



## The Sobel operator

- Common approximation of derivative of Gaussian

$$\frac{1}{8} \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

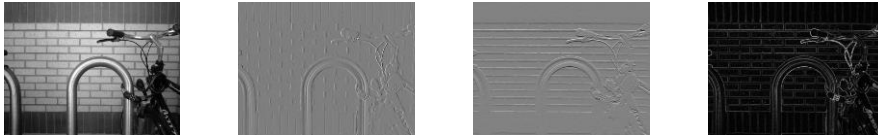
$s_x$

$$\frac{1}{8} \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

$s_y$

- The standard defn. of the Sobel operator omits the  $1/8$  term
  - doesn't make a difference for edge detection
  - the  $1/8$  term **is** needed to get the right gradient magnitude

## Sobel operator: example



Source: Wikipedia

## Example



- original image (Lena)



## Finding edges



gradient magnitude

## Finding edges



where is the edge?

thresholding

Questions?