$$\operatorname{aff}(X) = \left\{ \sum_{k=1}^{p} \lambda_k x_k : x_1, \ldots, x_k \in X, \sum_{k=1}^{p} \lambda_k = 1 \right\}.$$