Quantum Chemistry

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Explain the shape of electron movement.

$$\nabla^2 \Psi = \frac{1}{c^2} \frac{\partial^2 \Psi}{\partial t^2} \tag{1}$$

$$\nabla^2 \phi + \frac{2m}{\hbar^2} (E - V)\phi = 0 \tag{2}$$

$$\hat{H}\Psi = i\hbar \frac{\partial \Psi}{\partial t} \tag{3}$$

$$\frac{\partial^2 \phi_{tr}}{\partial X^2} + \frac{\partial^2 \phi_{tr}}{\partial Y^2} + \frac{\partial^2 \phi_{tr}}{\partial Z^2} + \frac{2M}{\hbar^2} E_{tr} \phi_{tr} = 0 \tag{4}$$

$$\phi_T = \phi_{tr}(X, Y, Z)\phi(x, y, z) \tag{5}$$

$$\nabla^2 \phi + \frac{2\mu}{\hbar^2} (E + \frac{Ze^2}{r}) \phi = 0 \tag{6}$$

$$\phi = \phi(r, \theta, \phi) = R(r)\Theta(\theta)\Phi(\phi) \tag{7}$$

$$\frac{d^2\Phi}{d\phi^2} + m^2\Phi = 0, m = 0, \pm 1, \pm 2\dots$$
 (8)

$$\Phi_m(\phi) = \frac{1}{\sqrt{2\pi}} exp(im\phi) \tag{9}$$

$$\Theta_{lm}(\theta) = (-1)^{\frac{m+|m|}{2}} \sqrt{\frac{(2l+1)(l-|m|)!}{2(l+|m|)!}} P_l^{\dagger} m | (\cos\theta)$$
 (10)

$$R_{nl}(r) = -\sqrt{\frac{2Z^3}{na_0}} \frac{(n-l-1)!}{2n((n+l)!)^3} exp(-\rho/2)\rho^l L_{n+l}^{2l+1}(\rho)$$
 (11)

$$\rho = \frac{2Z}{na_0}r, a_0 = \frac{\hbar^2}{\mu e^2} \tag{12}$$

$$n = 1, 2, 3, 4 \dots$$

 $l = 0, 1, 2, 3, \dots, n - 1$
 $m = 0, \pm 1, \pm 2, \dots, \pm l$ (13)

$$\phi_{1s} = \frac{1}{\sqrt{\phi}} \left(\frac{Z}{a_0}\right)^{\frac{3}{2}} e^{-\frac{Zr}{a_0}}, n = 1, l = 0, m = 0$$
(14)