

Aim: To provide hands-on experience with using singly linked list, algorithm design and complexity analysis.

Details: In this programming assignment, you are required to perform *large positive integer arithmetic operations: addition, multiplication and factorial, using a singly linked list.*

For modern computers, the largest integer number they can operate using a **64-bit long** type is:
9,223,372,036,854,775,807 - total 19 digits.

To handle larger numbers of arbitrary digits, we need to use Java's BigInteger class. BigInteger class uses an array as the internal data store. In this assignment, you are **NOT** allowed to use the BigInteger class nor any Java library, but to design your own algorithms and implement programming code to perform large positive integer arithmetic operations. And we will use singly linked list as the data store.

Examples

Addition:

```
314159265358979323846264338327950288419716939937510582097494459230781640628620899862803482534211706798214808651328230664709384460955058223172535940
812848111745028410270193852110555964462294895493038196442881097566593344612847564823378678316527120190914564856692346034861045432664821339360726024
9141273724587006063155881748815209209628292540917153643678925903600113305305488204665213841469519415116094330572703657959195309218611738193261179
3105118548074462379962749567351885752724891227938183011949
```

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```
271828182845904523536028747135266249775724709369995957496696762772407663035354759457138217852516642742746639193200305992181741359662904357290033429
526059563073813232862794349076323382988075319525101901157383418793070215408914993488416750924476146066808226480016847741185374234544243710753907774
499206955170276183860626133138458300075204493382656029760673711320070932870912744374704723069697720931014169283681902551510865746377211125238978442
5056953696770785449969967946864454905987931636889230098793
```

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```
585987448204883847382293085463216538195441649307506539594191222003189303663975659319941700386728349540961447844528536656891125820617962580462569370
338907674818841643132988201186879347450370215018140097600264516359663560021762558311795429241003266257722791336709193776046419667209065050114633799
413334327628976844492184950626610392171487418791827566197462970356072065923967626421356861484392915082175112589408939127470061055595822863432239621
8162072244845247829932717514216340658712822864827413110742
```

Multiplication:

```
314159265358979323846264338327950288419716939937510582097494459230781640628620899862803482534211706798214808651328230664709384460955058223172535940
812848111745028410270193852110555964462294895493038196442881097566593344612847564823378678316527120190914564856692346034861045432664821339360726024
9141273724587006063155881748815209209628292540917153643678925903600113305305488204665213841469519415116094330572703657959195309218611738193261179
3105118548074462379962749567351885752724891227938183011949
```

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```
271828182845904523536028747135266249775724709369995957496696762772407663035354759457138217852516642742746639193200305992181741359662904357290033429
526059563073813232862794349076323382988075319525101901157383418793070215408914993488416750924476146066808226480016847741185374234544243710753907774
499206955170276183860626133138458300075204493382656029760673711320070932870912744374704723069697720931014169283681902551510865746377211125238978442
5056953696770785449969967946864454905987931636889230098793
```

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```
85397342226735670654635508695465744950348885357651149618796011301792286115733080757256386971047394391377494251167746764632118759069602399061836345
379070414542021599488963342852746700046687766093072711290393507480401055727040348627303998656540644166179229285713708216374412976168471172544672318
420340751657873020506707999472076298967964373713900900839870785220633048298035384640173153001978236276770258035741255972055172639898617344959092612
41228968076458278542054316321579541951026175332613932709119381731894732577404563811551518421634572732032669619629681004777405626451358624550657937
465089639230862802486924634707677031305084286996852030412247861263357552487912583970608299629554117426410360526427791080039644155911779602877199
965012892131320785142285937433172266928297800809137677080338681669194915186716867160869157849442386176153054827067151730032517979526491281310779949
5542731427446300956525607946484154600181256827723124910158877299179427239566728952250408905276832679976323569477557
```

Factorial (100! = 100 × 99 × 98 × ... × 3 × 2 × 1):

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```
9332621544394415268169923885626670049071596826438162146859296389521759999322991560894146397615651828625369792082722375825118521091686400000000000000
00000000000
```

Tips: It is a lot more efficient to handle large integer if we store the digits in the singly linked list in a reverse order, see below.

To begin with, we use small numbers as test bed.

Input:

first integer 98765 : [9]<-[8]<-[7]<-[6]<-[5]<-[head]

second integer 123 : [1]<-[2]<-[3]<-[head]

factorial 7

Output:

Addition:

large integer 98888 : [9]<-[8]<-[8]<-[8]<-[8]<-[head]

Multiplication:

large integer 12148095 : [1]<-[2]<-[1]<-[4]<-[8]<-[0]<-[9]<-[5]<-[head]

Factorial:

large integer 5040 : [5]<-[0]<-[4]<-[0]<-[head]

Assignment Details (Total 100 marks):**Part 1) Programming** [70 marks]

You are given the following java files.

LargeIntegerDemo.java	- the driver program for reading data and performing: addition, multiplication and factorial.
LargeIntegerNode.java	- the node of a linked list that stores 1 digit.
LargeIntegerLL.java	- the linked list that provides the functionality of multiplication and printing.

Your task is to modify **LargeIntegerLL.java**, and to fill in the content of the following functions.

```
public LargeIntegerLL add(LargeIntegerLL secondNumber) [30 marks]
```

This function `add` computes the addition of two large integers (`this`, `secondNumber`) and returns the result in a new linked list (`result`).

```
public LargeIntegerLL mul(int digit) [15 marks]
```

Given a digit (`digit`), the function `mul` computes the multiplication of the large integer and the digit, and returns the result in a new linked list (`result`).

```
public LargeIntegerLL mul(LargeIntegerLL secondNumber) [15 marks]
```

This function `mul` computes the multiplication of two large integers (`this`, `secondNumber`) and return the results in a new linked list (`result`).

```
public static LargeIntegerLL factorial(int number) [10 marks]
```

This function `factorial` computes the factorial of a given number (`number`) and returns the result in a new linked list (`result`). You can assume that the given number **K** is ≤ 2000 .

Note:**Tip1:** you are **not** allowed to modify any other files.**Tip2:** You should prepare and test your program to work. Use the provided test case, example:

```
> javac *.java
> java -cp . LargeIntegerDemo < input.txt
First Number: ...
...
```

Use "`< input.txt`" to redirect input from `input.txt`, save you from copy/pasting and making unnecessary errors.

Tip 3: Verify the correctness of your program. For example:

```
> java -cp . LargeIntegerDemo < input.txt > output.txt
> diff output.txt result.txt
>
```

Use "`> output1.txt`" to pipe your result into `output.txt`.

Use "`diff result.txt output.txt`" to check your program's output. `diff` is a program to find "difference" in two files. If there is nothing returned like above, your result is correct. The marker will use `diff` to check your output.

Tip 4: The marker will use different test cases to check your program. You should test your program with more test cases.

Part 2) Complexity Analysis [30 marks]

- A) Discuss the complexity of the `add` function (your algorithm) in Big-O notation, suppose the two input large integers consists of N digits respectively. [15 marks]
- B) Discuss the complexity of the `mul` function in Big-O notation, suppose the two input large integers consists of M and N digits respectively. [10 marks]
- C) Discuss the complexity of the `factorial` function in Big-O notation in terms of the **value** of input number K (Note: not the number of digits in K). [5 marks]

Tip 5: Use these facts for Part 2C)

- The number of digits in K is on the order of $O(\log K)$. For example, if $K = 10$, there are $O(\log_{10}(10) + 1) = 2$ digits in K.
- The number of digits in $K!$ grows on the order of $O(K \log K)$.

Release Date: 23 February, 2016

Due Date: 15 March, 2016, 11:00 (**Zero** marks for **late submission**, in line with College regulation.)

Submission:

You should submit the following to the Blackboard assignment collection page:

1. Part 1: **ONE** working java source file, **clearly commented**: `LargeIntegerLinkedList.java`

The marker will use the **submitted** file and compile against the two **given** files :

`LargeIntegerNode.java` and `LargeIntegerAdditionDemo.java`

If your program does not work and the marker is unable to understand your code, you will score no marks in Part1.

2. A written report (**pdf only**) for Part2.

Compulsory Oral Viva:

A 5-minute oral viva, to be scheduled on 16 March 2016 (Wed afternoon 1pm-3:30pm), time slot TBA, at Instructor's office.

To speed things up, you are advised to bring your own laptop to demonstrate your working java program.

Each student is given a maximum of 5-minute. Strict time limitation is enforced to ensure no delay to subsequent vivas.

Purpose of the oral viva:

- To show your understanding of the program (you actually did the work),
- To show your understanding on complexity analysis, and
- To provide you early feedback.

If you do not attend the viva, there will be a cap of 60% of your CW marks.

Tip 6: Do ensure you have submitted the correct java source file to blackboard. Check your submission after you have uploaded your file.

Tip 7: How do you achieve full marks? Read the assessment matrix.

Feedback

Marks and sample solution will be provided 2 weeks after the submission deadline.