

# **Linguaggi e compilatori:**

## **Assignment 2**

Davide De Soricellis  
Roberto Wang  
Jun Wu Wang

Maggio 2024

## Contents

<b>1</b>	<b>Very busy expressions</b>	<b>2</b>
1.1	Dataflow analysis framework . . . . .	2
1.2	Iterative table . . . . .	2
<b>2</b>	<b>Dominator analysis</b>	<b>3</b>
2.1	Dataflow analysis framework . . . . .	3
2.2	Iterative table . . . . .	3
<b>3</b>	<b>Constant propagation</b>	<b>4</b>
3.1	Dataflow analysis framework . . . . .	4
3.2	Iterative table . . . . .	4

# 1 Very busy expressions

## 1.1 Dataflow analysis framework

	Very busy expressions
Domain	Sets of expressions
Direction	backward: $in[b] = f_b(out[b])$ $out[b] = \wedge in[succ(b)]$
Transfer function	$f_b(x) = Use_b \cup (x - Def_b)$
Meet operation ( $\wedge$ )	$\cap$
Boundary condition	$in[Exit] = \emptyset$
Initial interior points	$in[b] = U$

Transfer function:

$$in[b] = f_b(out[b]) = Use[b] \cup (out[b] - Def[b])$$

- $Use[b]$ : very busy expressions generate (usi localmente esposti in un BB  $\rightarrow$  usi di espressioni che non sono preceduti nel BB da definizioni dei loro operandi)
- $out[b] - Def[b]$ : very busy expressions propagate
  - $out[b]$ : very busy expressions ereditate
  - $Def[b]$ : very busy expressions che hanno operandi definiti nel BB

## 1.2 Iterative table

	Iterazione 1		Iterazione 2	
	$IN[B]$	$OUT[B]$	$IN[B]$	$OUT[B]$
BB1	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$
BB2	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$
BB3	$\{a - b, b - a\}$	$\{a - b\}$	$\{a - b, b - a\}$	$\{a - b\}$
BB4	$\{a - b\}$	$\emptyset$	$\{a - b\}$	$\emptyset$
BB5	$\{b - a\}$	$\emptyset$	$\{b - a\}$	$\emptyset$
BB6	$\emptyset$	$\{a - b\}$	$\emptyset$	$\{a - b\}$
BB7	$\{a - b\}$	$\emptyset$	$\{a - b\}$	$\emptyset$
BB8	$\emptyset$	undefined	$\emptyset$	undefined

La tabella è generata eseguendo un algoritmo iterativo naive. Con un algoritmo worklist è possibile eseguire in 1 iterazione.

## 2 Dominator analysis

### 2.1 Dataflow analysis framework

	<b>Dominator analysis</b>
Domain	Sets of basic blocks
Direction	forward: $out[b] = f_b(in[b])$ $in[b] = \wedge out[pred(b)]$
Transfer function	$f_b(x) = Gen_b \cup x$
Meet operation ( $\wedge$ )	$\cap$
Boundary condition	$out[Entry] = Entry$
Initial interior points	$out[b] = U$

Transfer function:

$$out[b] = f_b(in[b]) = Gen[b] \cup in[b]$$

- $Gen[b]$ : dominators generati  $\rightarrow$  sè stesso ( $b$ )
- $in[b]$ : dominators ereditati/propagati

### 2.2 Iterative table

	<b>Iterazione 1</b>		<b>Iterazione 2</b>	
	$IN[B]$	$OUT[B]$	$IN[B]$	$OUT[B]$
A	undefined	$\{A\}$	undefined	$\{A\}$
B	$\{A\}$	$\{A, B\}$	$\{A\}$	$\{A, B\}$
C	$\{A\}$	$\{A, C\}$	$\{A\}$	$\{A, C\}$
D	$\{A, C\}$	$\{A, C, D\}$	$\{A, C\}$	$\{A, C, D\}$
E	$\{A, C\}$	$\{A, C, E\}$	$\{A, C\}$	$\{A, C, E\}$
F	$\{A, C\}$	$\{A, C, F\}$	$\{A, C\}$	$\{A, C, F\}$
G	$\{A\}$	$\{A, G\}$	$\{A\}$	$\{A, G\}$

La tabella è generata eseguendo un algoritmo iterativo naive. Con un algoritmo worklist è possibile eseguire in 1 iterazione.

### 3 Constant propagation

#### 3.1 Dataflow analysis framework

	Constant propagation
Domain	Sets of <variable, constant value> pairs
Direction	forward: $out[b] = f_b(in[b])$ $in[b] = \wedge out[pred(b)]$
Transfer function	$f_b(x) = Gen_b \cup (x - Kill_b)$
Meet operation ( $\wedge$ )	$\cap$
Boundary condition	$out[Entry] = \emptyset$
Initial interior points	$out[b] = U$

Transfer function:

$$out[b] = f_b(in[b]) = Gen[b] \cup (in[b] - Kill[b])$$

- $Gen[b]$ : coppie <variable, constant value> generate (definizioni localmente disponibili di variabili con un valore costante  $\rightarrow$  l'ultima definizione di una variabile in  $b$  e con rhs un valore costante)
- $in[b] - Kill[b]$ : coppie <variable, constant value> propagate
  - $in[b]$ : coppie <variable, constant value> ereditate
  - $Kill[b]$ : coppie <variable, constant value> uccise (ridefinizioni di variabili)

#### 3.2 Iterative table

	Iterazione 1	
	$IN[B]$	$OUT[B]$
BB1	undefined	$\emptyset$
BB2	$\emptyset$	$\{<k, 2>\}$
BB3 (if)	$\{<k, 2>\}$	$\{<k, 2>\}$
BB4	$\{<k, 2>\}$	$\{<k, 2>, <a, 4>\}$
BB5	$\{<k, 2>, <a, 4>\}$	$\{<k, 2>, <a, 4>, <x, 5>\}$
BB6	$\{<k, 2>\}$	$\{<k, 2>, <a, 4>\}$
BB7	$\{<k, 2>, <a, 4>\}$	$\{<k, 2>, <a, 4>, <x, 8>\}$
BB8	$\{<k, 2>, <a, 4>\}$	$\{<k, 4>, <a, 4>\}$
BB9 (while)	$\{<k, 4>, <a, 4>\}$	$\{<k, 4>, <a, 4>\}$
BB10	$\{<k, 4>, <a, 4>\}$	$\{<k, 4>, <a, 4>, <b, 2>\}$
BB11	$\{<k, 4>, <a, 4>, <b, 2>\}$	$\{<k, 4>, <a, 4>, <b, 2>, <x, 8>\}$
BB12	$\{<k, 4>, <a, 4>, <b, 2>, <x, 8>\}$	$\{<k, 4>, <a, 4>, <b, 2>, <x, 8>, <y, 8>\}$
BB13	$\{<k, 4>, <a, 4>, <b, 2>, <x, 8>, <y, 8>\}$	$\{<k, 5>, <a, 4>, <b, 2>, <x, 8>, <y, 8>\}$
BB14	$\{<k, 4>, <a, 4>\}$	$\{<k, 4>, <a, 4>\}$
BB15	$\{<k, 4>, <a, 4>\}$	$\{<k, 4>, <a, 4>\}$

	Iterazione 2	
	$IN[B]$	$OUT[B]$
BB1	undefined	$\emptyset$
BB2	$\emptyset$	$\{< k, 2 >\}$
BB3 (if)	$\{< k, 2 >\}$	$\{< k, 2 >\}$
BB4	$\{< k, 2 >\}$	$\{< k, 2 >, < a, 4 >\}$
BB5	$\{< k, 2 >, < a, 4 >\}$	$\{< k, 2 >, < a, 4 >, < x, 5 >\}$
BB6	$\{< k, 2 >\}$	$\{< k, 2 >, < a, 4 >\}$
BB7	$\{< k, 2 >, < a, 4 >\}$	$\{< k, 2 >, < a, 4 >, < x, 8 >\}$
BB8	$\{< k, 2 >, < a, 4 >\}$	$\{< k, 4 >, < a, 4 >\}$
BB9 (while)	$\{< a, 4 >\}$	$\{< a, 4 >\}$
BB10	$\{< a, 4 >\}$	$\{< a, 4 >, < b, 2 >\}$
BB11	$\{< a, 4 >, < b, 2 >\}$	$\{< a, 4 >, < b, 2 >\}$
BB12	$\{< a, 4 >, < b, 2 >\}$	$\{< a, 4 >, < b, 2 >, < y, 8 >\}$
BB13	$\{< a, 4 >, < b, 2 >, < y, 8 >\}$	$\{< a, 4 >, < b, 2 >, < y, 8 >\}$
BB14	$\{< a, 4 >\}$	$\{< a, 4 >\}$
BB15	$\{< a, 4 >\}$	$\{< a, 4 >\}$

	Iterazione 3	
	$IN[B]$	$OUT[B]$
BB1	undefined	$\emptyset$
BB2	$\emptyset$	$\{< k, 2 >\}$
BB3 (if)	$\{< k, 2 >\}$	$\{< k, 2 >\}$
BB4	$\{< k, 2 >\}$	$\{< k, 2 >, < a, 4 >\}$
BB5	$\{< k, 2 >, < a, 4 >\}$	$\{< k, 2 >, < a, 4 >, < x, 5 >\}$
BB6	$\{< k, 2 >\}$	$\{< k, 2 >, < a, 4 >\}$
BB7	$\{< k, 2 >, < a, 4 >\}$	$\{< k, 2 >, < a, 4 >, < x, 8 >\}$
BB8	$\{< k, 2 >, < a, 4 >\}$	$\{< k, 4 >, < a, 4 >\}$
BB9 (while)	$\{< a, 4 >\}$	$\{< a, 4 >\}$
BB10	$\{< a, 4 >\}$	$\{< a, 4 >, < b, 2 >\}$
BB11	$\{< a, 4 >, < b, 2 >\}$	$\{< a, 4 >, < b, 2 >\}$
BB12	$\{< a, 4 >, < b, 2 >\}$	$\{< a, 4 >, < b, 2 >, < y, 8 >\}$
BB13	$\{< a, 4 >, < b, 2 >, < y, 8 >\}$	$\{< a, 4 >, < b, 2 >, < y, 8 >\}$
BB14	$\{< a, 4 >\}$	$\{< a, 4 >\}$
BB15	$\{< a, 4 >\}$	$\{< a, 4 >\}$

La tabella è generata eseguendo un algoritmo iterativo naive.