

Pointer analysis

Pointer Analysis

- Outline:
 - What is pointer analysis
 - Intraprocedural pointer analysis
 - Interprocedural pointer analysis
 - Andersen and Steensgaard

Pointer and Alias Analysis

- Aliases: two expressions that denote the same memory location.
- Aliases are introduced by:
 - pointers
 - call-by-reference
 - array indexing
 - C unions

Useful for what?

- Improve the precision of analyses that require knowing what is modified or referenced (eg const prop, CSE ...)
- Eliminate redundant loads/stores and dead stores.

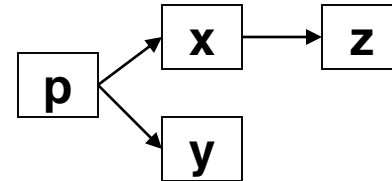
```
x := *p;                                *x := ...;
...                                     // is *x dead?
y := *p; // replace with y := x?
```

- Parallelization of code
 - can recursive calls to quick_sort be run in parallel? Yes, provided that they reference distinct regions of the array.
- Identify objects to be tracked in error detection tools

```
x.lock();
...
y.unlock(); // same object as x?
```

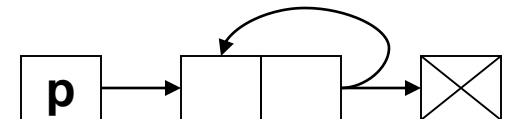
Kinds of alias information

- Points-to information (must or may versions)
 - at program point, compute a set of pairs of the form $p \rightarrow x$, where p points to x .
 - can represent this information in a **points-to graph**



- Alias pairs
 - at each program point, compute the set of all pairs (e_1, e_2) where e_1 and e_2 must/may reference the same memory.

- Storage shape analysis
 - at each program point, compute an abstract description of the pointer structure.



Intraprocedural Points-to Analysis

- Want to compute may-points-to information

- Lattice:

$$\mathbb{D} = 2^{\{x \rightarrow y \mid x \in \text{Var}, y \in \text{Var}\}}$$

$$\sqcup = \cup$$

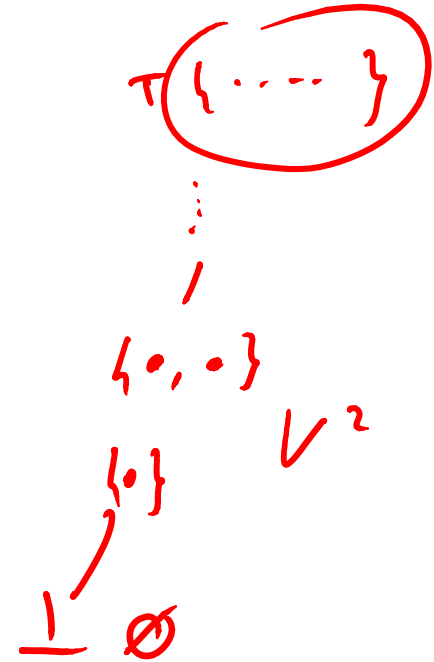
$$\sqsubseteq = \subseteq$$

$$\perp = \emptyset$$

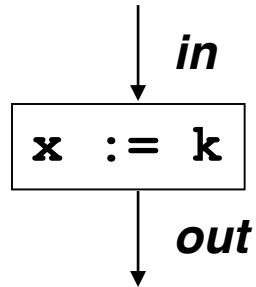
$$\top = \{x \rightarrow y \mid x \in \text{Var}, y \in \text{Var}\}$$

$\begin{pmatrix} a \\ b \\ c \end{pmatrix}$

$a \rightarrow a$
 $a \rightarrow b$
 $a \rightarrow c$



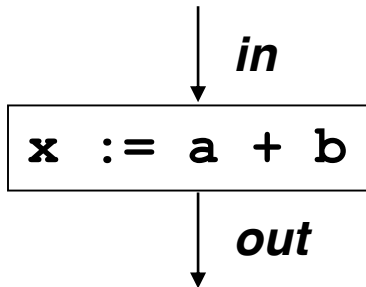
Flow functions



$$F_{x := k}(\text{in}) =$$

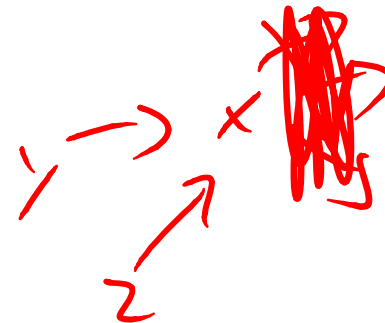
$$\text{in} - \{x \rightarrow * \}$$

$$\begin{array}{l} \wedge \\ x = 87 \\ \cdot x \rightarrow \{y\} \end{array}$$



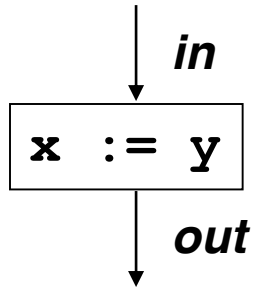
$$F_{x := a+b}(\text{in}) =$$

$$\text{in} - \{x \rightarrow * \}$$



Flow functions

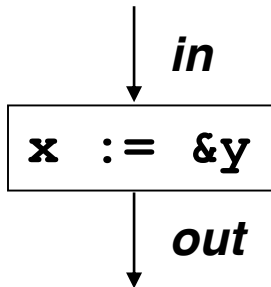
$$\text{kill}(x) = \{x \rightarrow *\}$$



$$F_{x := y}(\text{in}) = \text{in} - \text{kill}(x) \cup \{x \rightarrow z \mid y \rightarrow z \in \text{in}\}$$

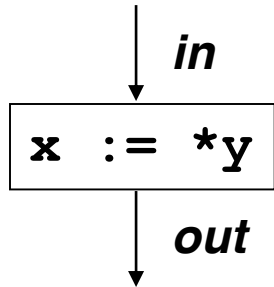
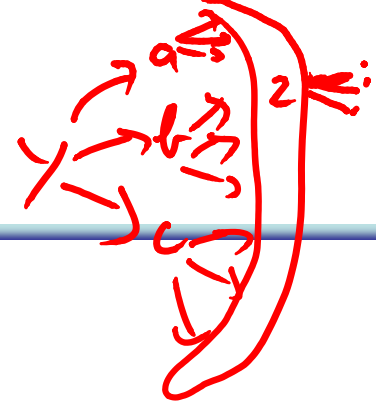
Handwritten annotations for the flow function of `x := y`:

- A checkmark \checkmark is placed next to the $\text{in} - \text{kill}(x)$ term.
- The set notation $\{x \rightarrow z \mid y \rightarrow z \in \text{in}\}$ is written in red.
- Below the set notation, there is a diagram showing a variable y with three arrows pointing to it from above: one labeled a , one labeled b , and one labeled c .



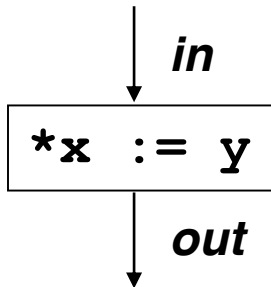
$$F_{x := \&y}(\text{in}) = \text{in} - \text{kill}(x) \cup \{x \rightarrow y\}$$

Flow functions

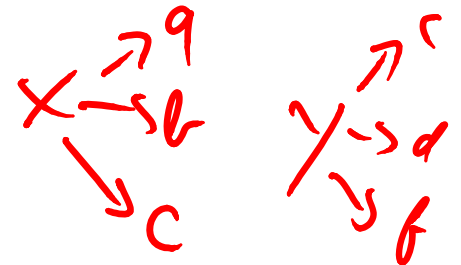


$$F_{x := *y}(in) = in - kill(x)$$

$$V \{ x \rightarrow z \mid \exists t. y \rightarrow t \wedge t \rightarrow z \in in \}$$



$$F_{*x := y}(in) = in \cup \{ z \rightarrow t \mid x \rightarrow z \in in \wedge y \rightarrow t \in in \}$$



Intraprocedural Points-to Analysis

- Flow functions:

$$kill(x) = \bigcup_{v \in Vars} \{(x, v)\}$$

$$F_{x:=k}(S) = S - kill(x)$$

$$F_{x:=a+b}(S) = S - kill(x)$$

$$F_{x:=y}(S) = S - kill(x) \cup \{(x, v) \mid (y, v) \in S\}$$

$$F_{x:=\&y}(S) = S - kill(x) \cup \{(x, y)\}$$

$$F_{x:=*y}(S) = S - kill(x) \cup \{(x, v) \mid \exists t \in Vars. [(y, t) \in S \wedge (t, v) \in S]\}$$

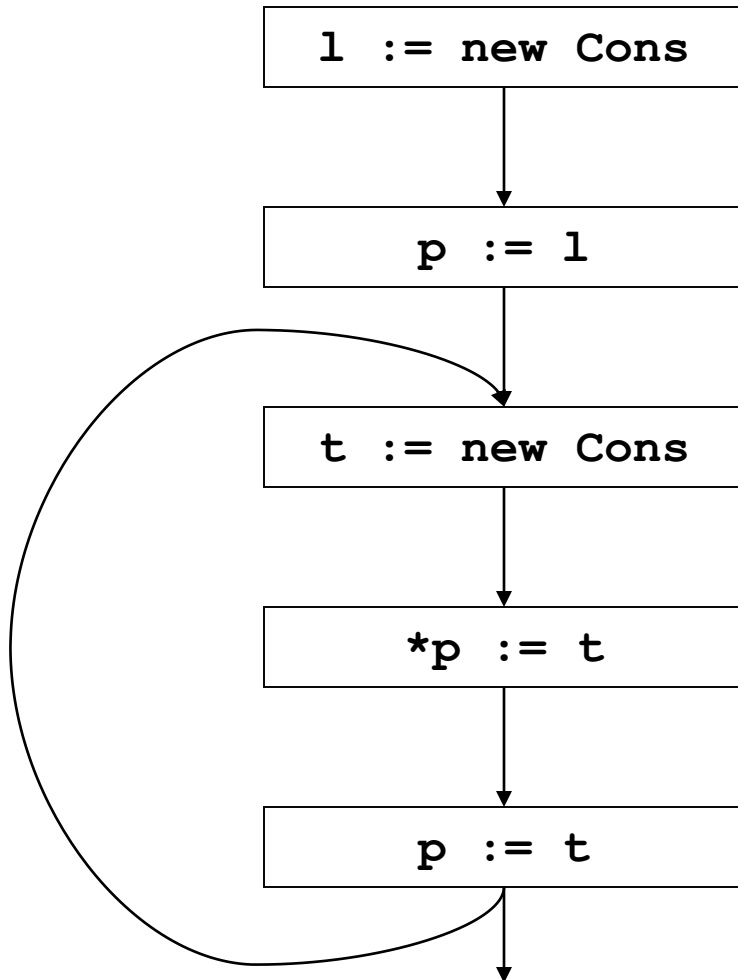
$$\begin{aligned} F_{*x:=y}(S) = & \text{let } V := \{v \mid (x, v) \in S\} \text{ in} \\ & S - (\text{if } V = \{v\} \text{ then } kill(v) \text{ else } \emptyset) \\ & \cup \{(v, t) \mid v \in V \wedge (y, t) \in S\} \end{aligned}$$

Pointers to dynamically-allocated memory

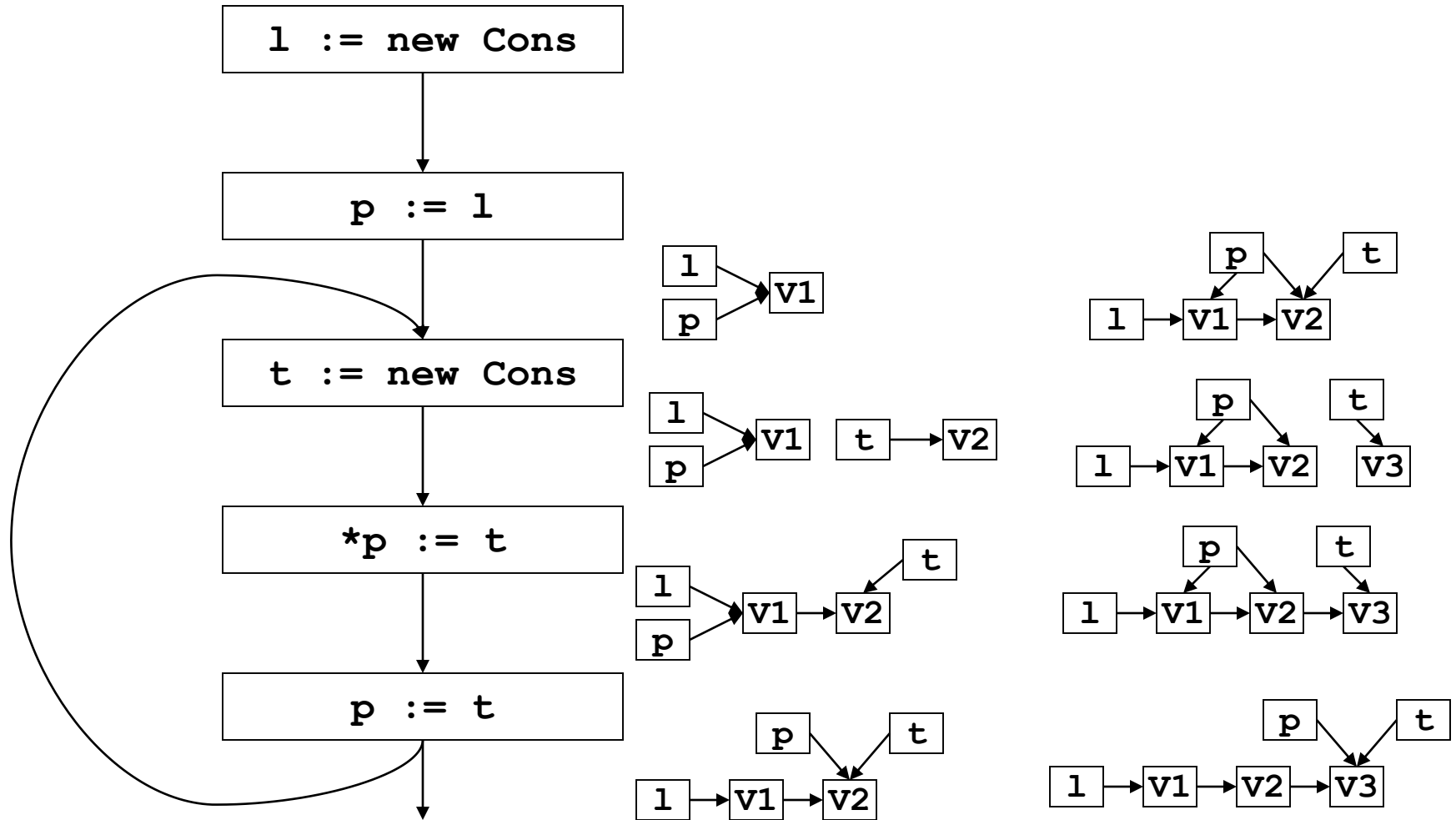
- Handle statements of the form: **$x := \text{new } T$**
- One idea: generate a new variable each time the new statement is analyzed to stand for the new location:

$$F_{x:=\text{new } T}(S) = S - \text{kill}(x) \cup \{(x, \text{newvar}())\}$$

Example



Example solved



What went wrong?

- Lattice infinitely tall!
- We were essentially running the program
- Instead, we need to summarize the infinitely many allocated objects in a finite way
- **New Idea:** introduce summary nodes, which will stand for a whole class of allocated objects.

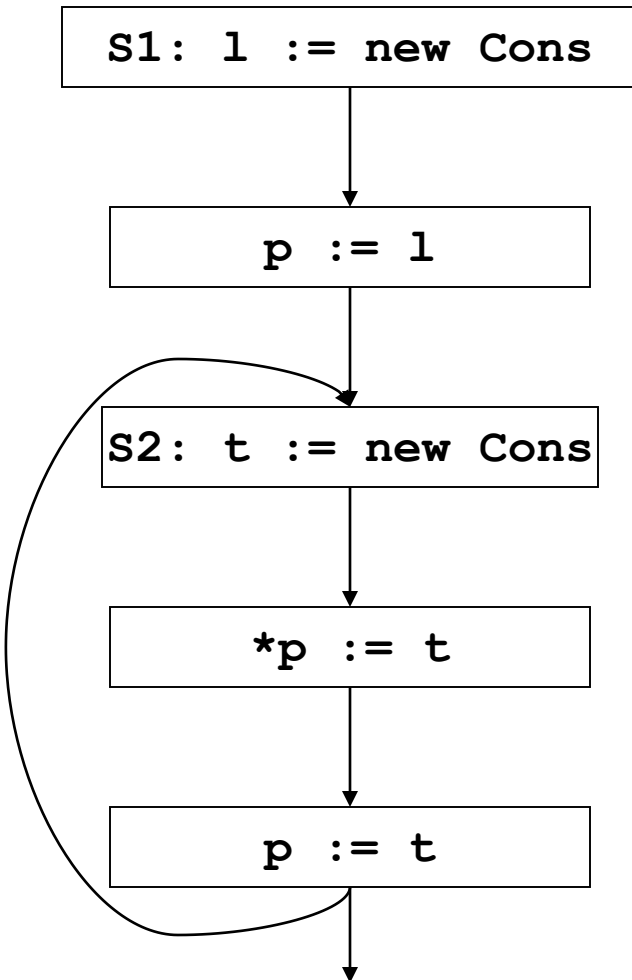
What went wrong?

- Example: For each new statement with label L , introduce a summary node loc_L , which stands for the memory allocated by statement L .

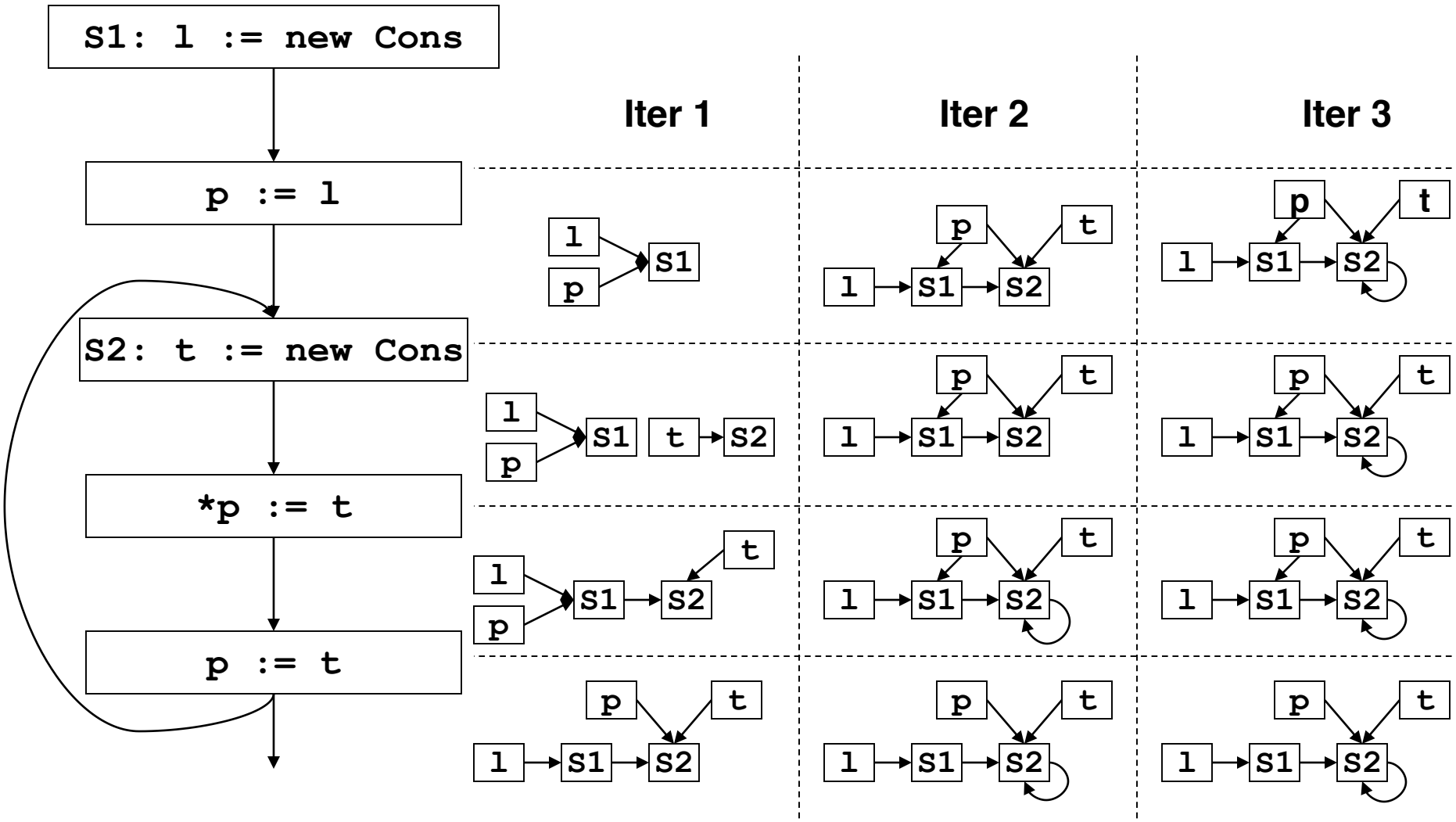
$$F_{L: x := new} T(S) = S - kill(x) \cup \{(x, loc_L)\}$$

- Summary nodes can use other criterion for merging.

Example revisited



Example revisited & solved



Array aliasing, and pointers to arrays

- Array indexing can cause aliasing:
 - `a[i]` aliases `b[j]` if:
 - `a` aliases `b` and $i = j$
 - `a` and `b` overlap, and $i = j + k$, where k is the amount of overlap.
- Can have pointers to elements of an array
 - `p := &a[i]; ...; p++;`
- How can arrays be modeled?
 - Could treat the whole array as one location.
 - Could try to reason about the array index expressions: array dependence analysis.

Fields

- Can summarize fields using per field summary
 - for each field F , keep a points-to node called F that summarizes all possible values that can ever be stored in F
- Can also use allocation sites
 - for each field F , and each allocation site S , keep a points-to node called (F, S) that summarizes all possible values that can ever be stored in the field F of objects allocated at site S .

Summary

- We just saw:
 - intraprocedural points-to analysis
 - handling dynamically allocated memory
 - handling pointers to arrays
- But, intraprocedural pointer analysis is not enough.
 - Sharing data structures across multiple procedures is one the big benefits of pointers: instead of passing the whole data structures around, just pass pointers to them (eg C pass by reference).
 - So pointers end up pointing to structures shared across procedures.
 - If you don't do an interproc analysis, you'll have to make conservative assumptions functions entries and function calls.

Conservative approximation on entry

- Say we don't have interprocedural pointer analysis.
- What should the information be at the input of the following procedure:

```
global g;  
void p(x,y) {  
  
    ...  
  
}
```

x

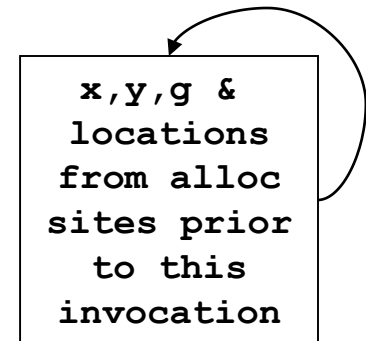
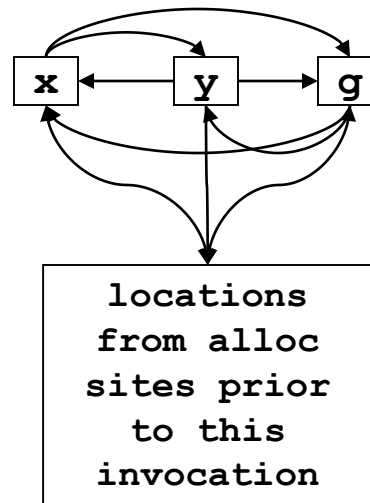
y

g

Conservative approximation on entry

- Here are a few solutions:

```
global g;  
void p(x,y) {  
    ...  
}
```



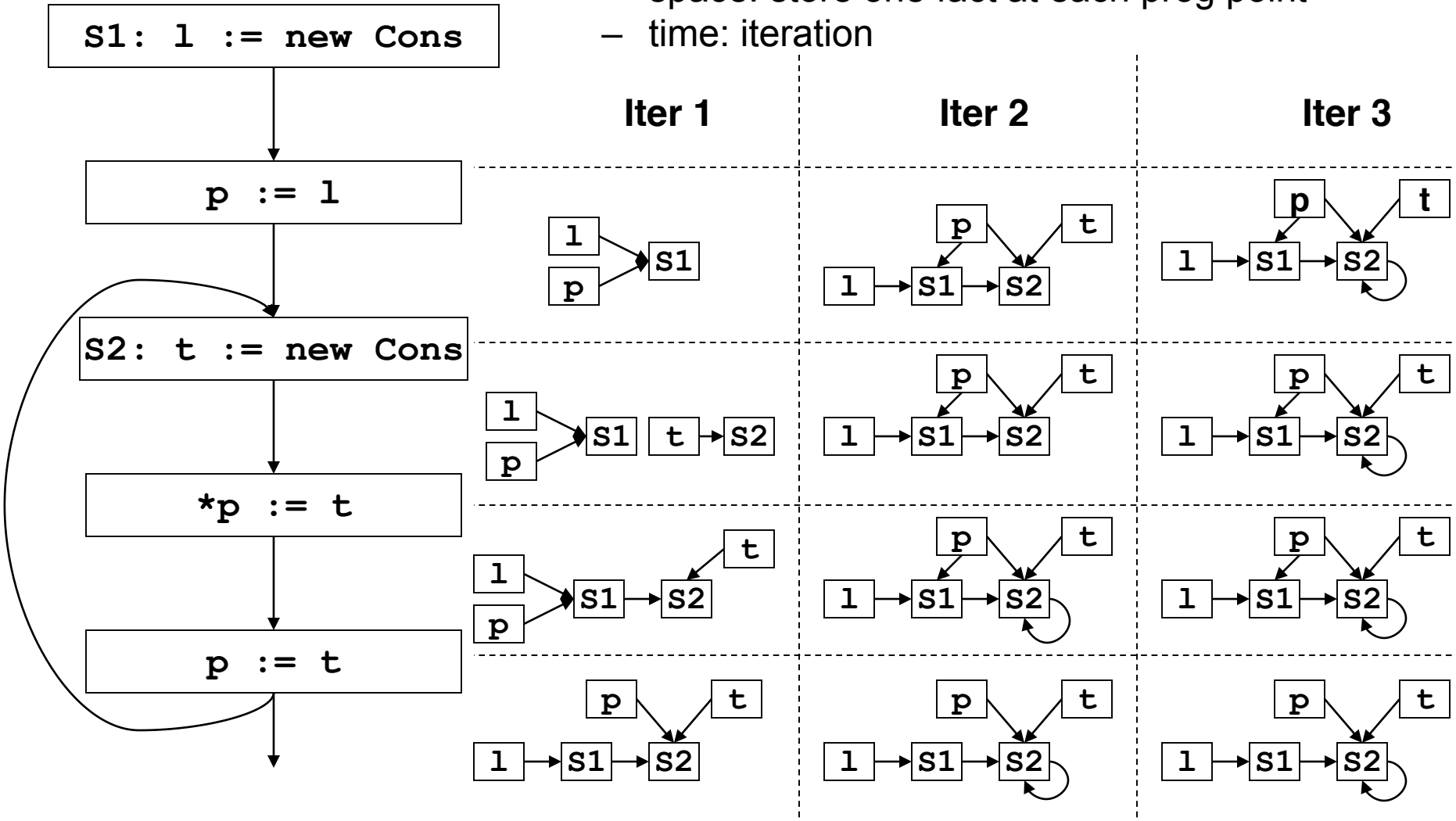
- They are all very conservative!
- We can try to do better.

Interprocedural pointer analysis

- Main difficulty in performing interprocedural pointer analysis is scaling
- One can use a top-down summary based approach (Wilson & Lam 95), but even these are hard to scale

Example revisited

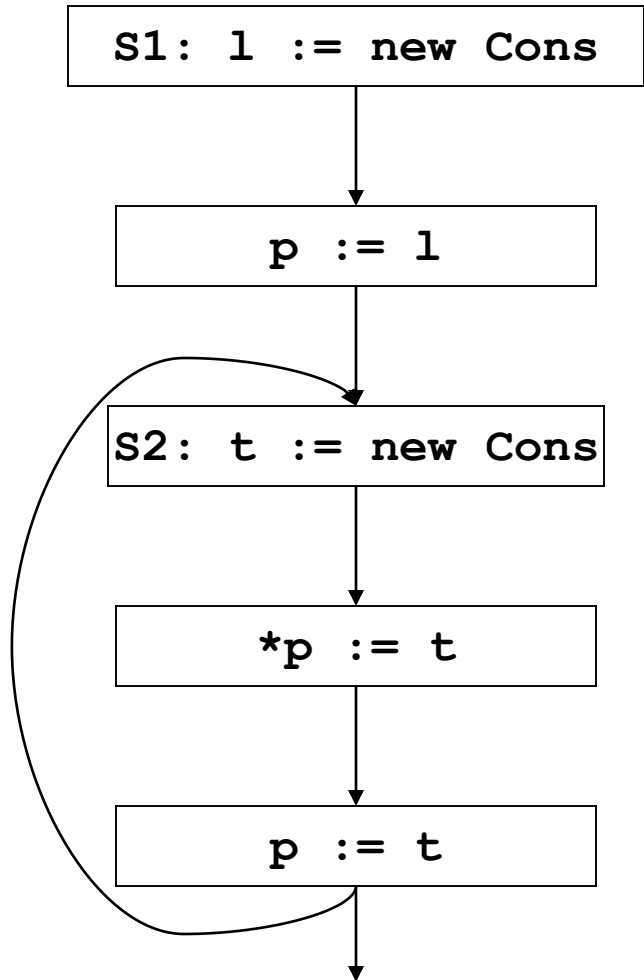
- Cost:
 - space: store one fact at each prog point
 - time: iteration



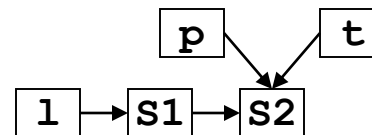
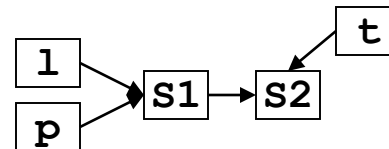
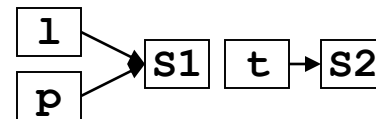
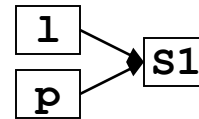
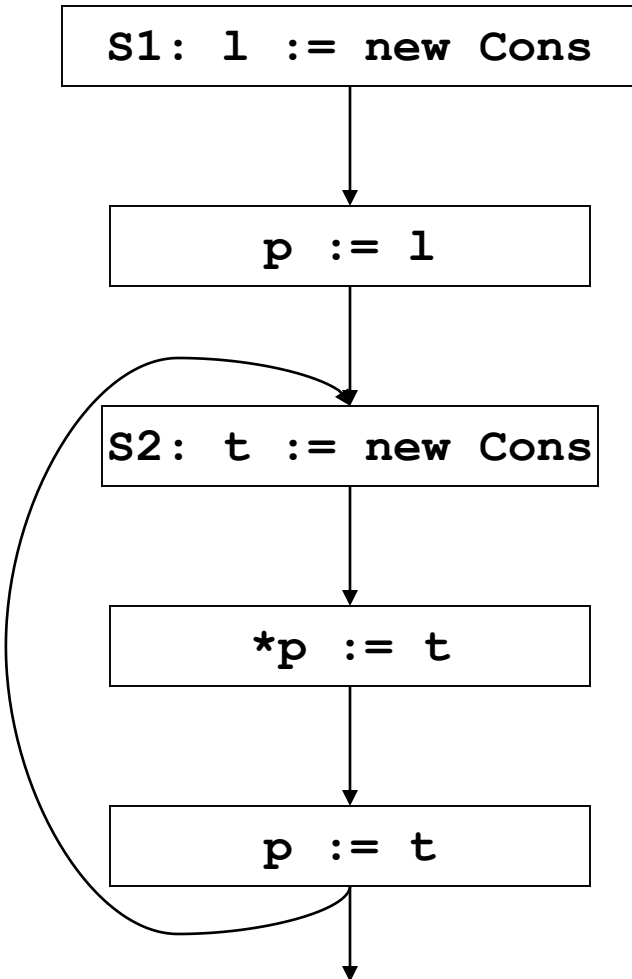
New idea: store one dataflow fact

- Store one dataflow fact for the whole program
- Each statement updates this one dataflow fact
 - use the previous flow functions, but now they take the whole program dataflow fact, and return an updated version of it.
- Process each statement once, ignoring the order of the statements
- This is called a flow-insensitive analysis.

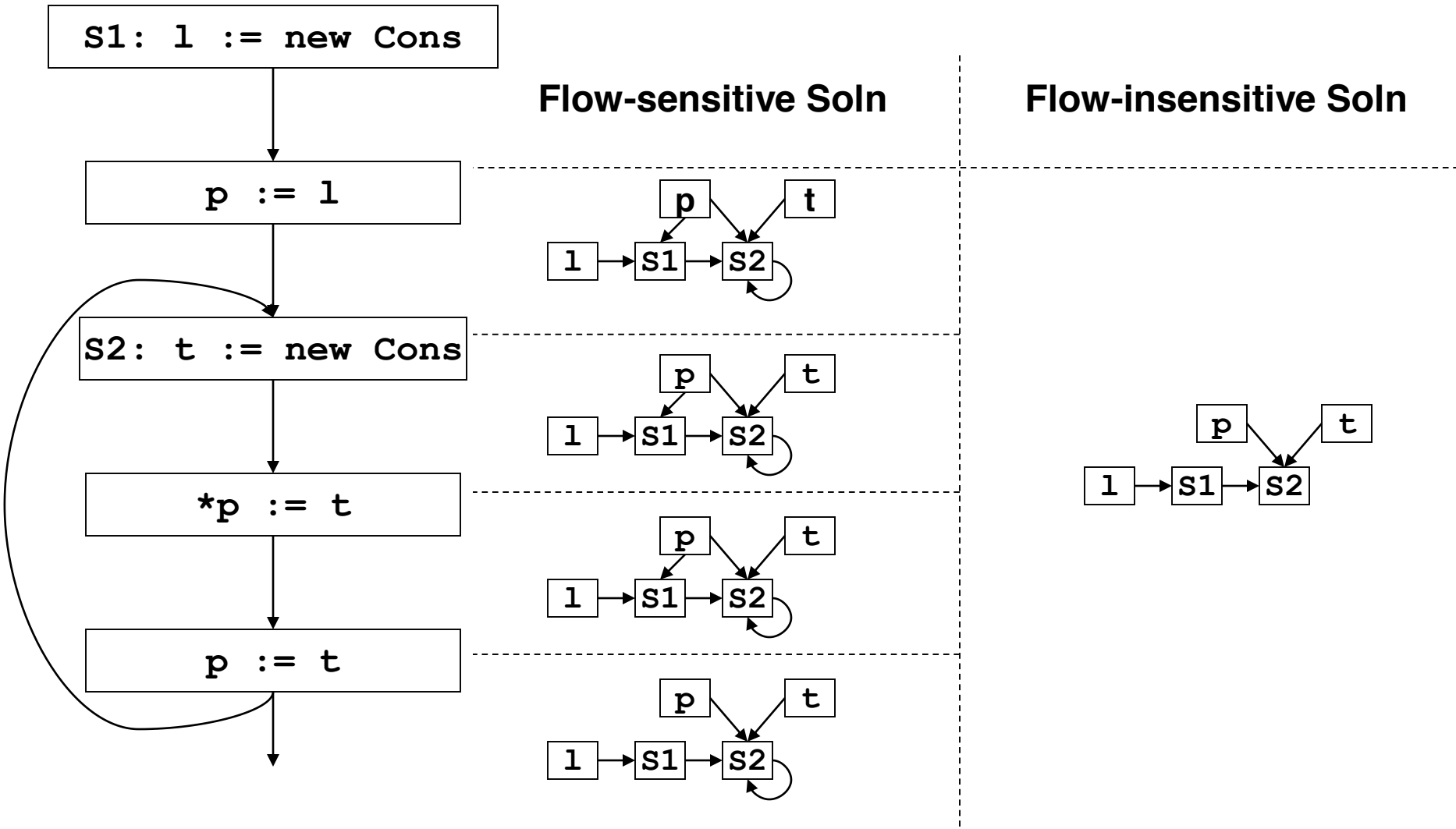
Flow insensitive pointer analysis



Flow insensitive pointer analysis



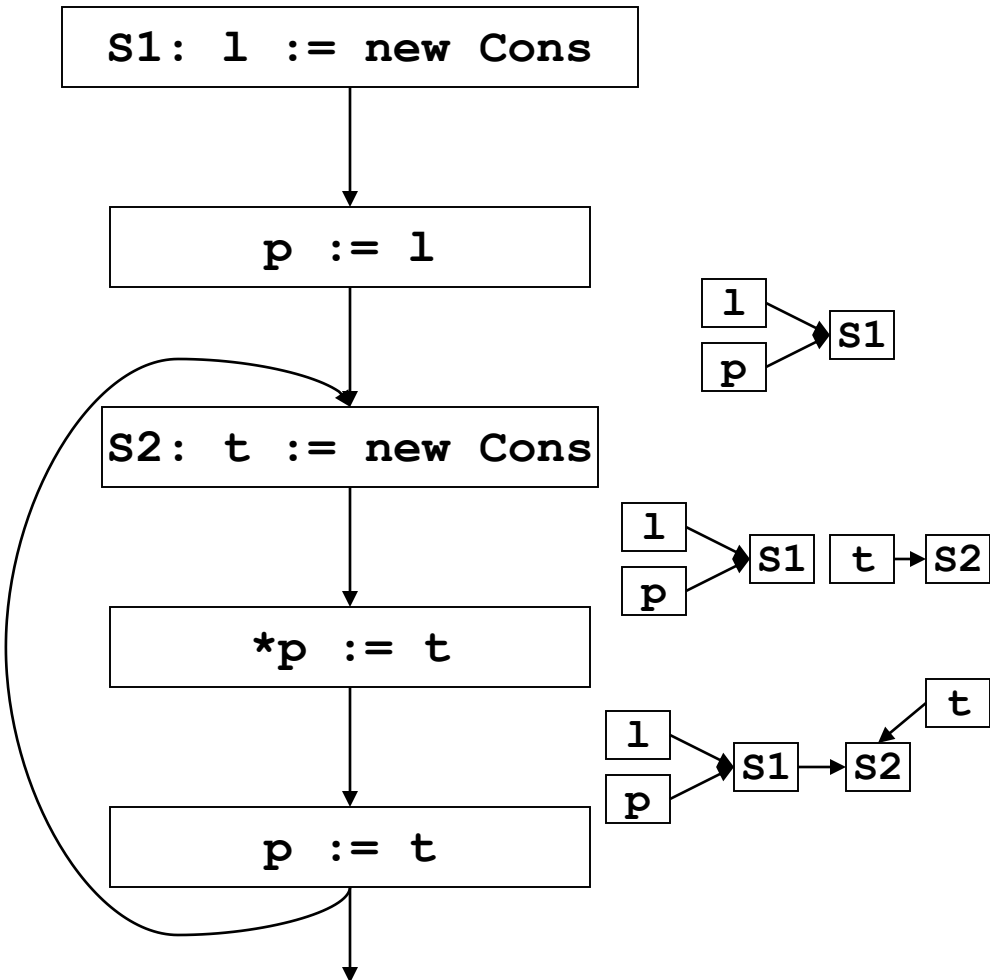
Flow sensitive vs. insensitive



What went wrong?

- What happened to the link between p and S1?
 - Can't do strong updates anymore!
 - Need to remove all the kill sets from the flow functions.
- What happened to the self loop on S2?
 - We still have to iterate!

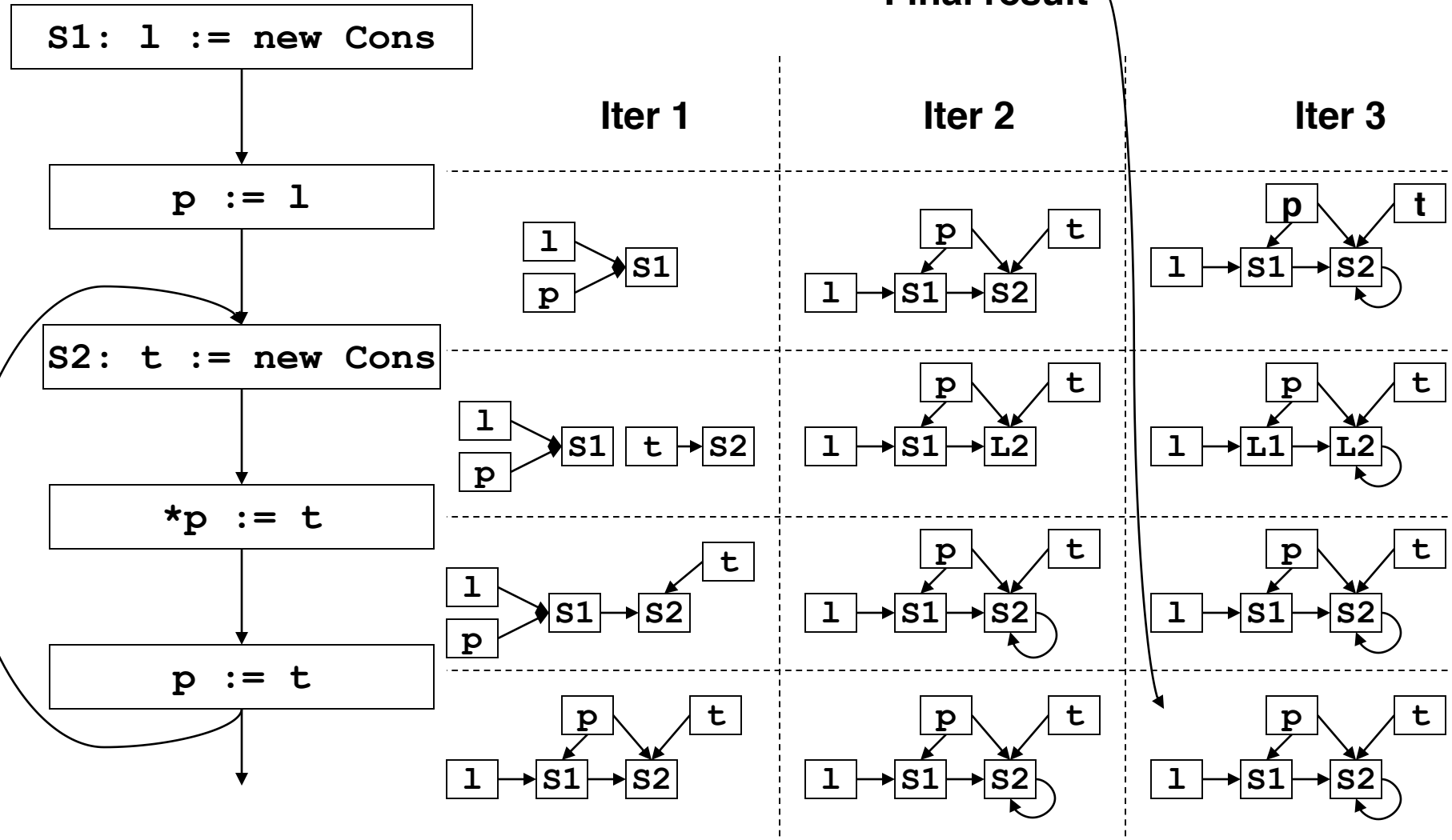
Flow insensitive pointer analysis: fixed



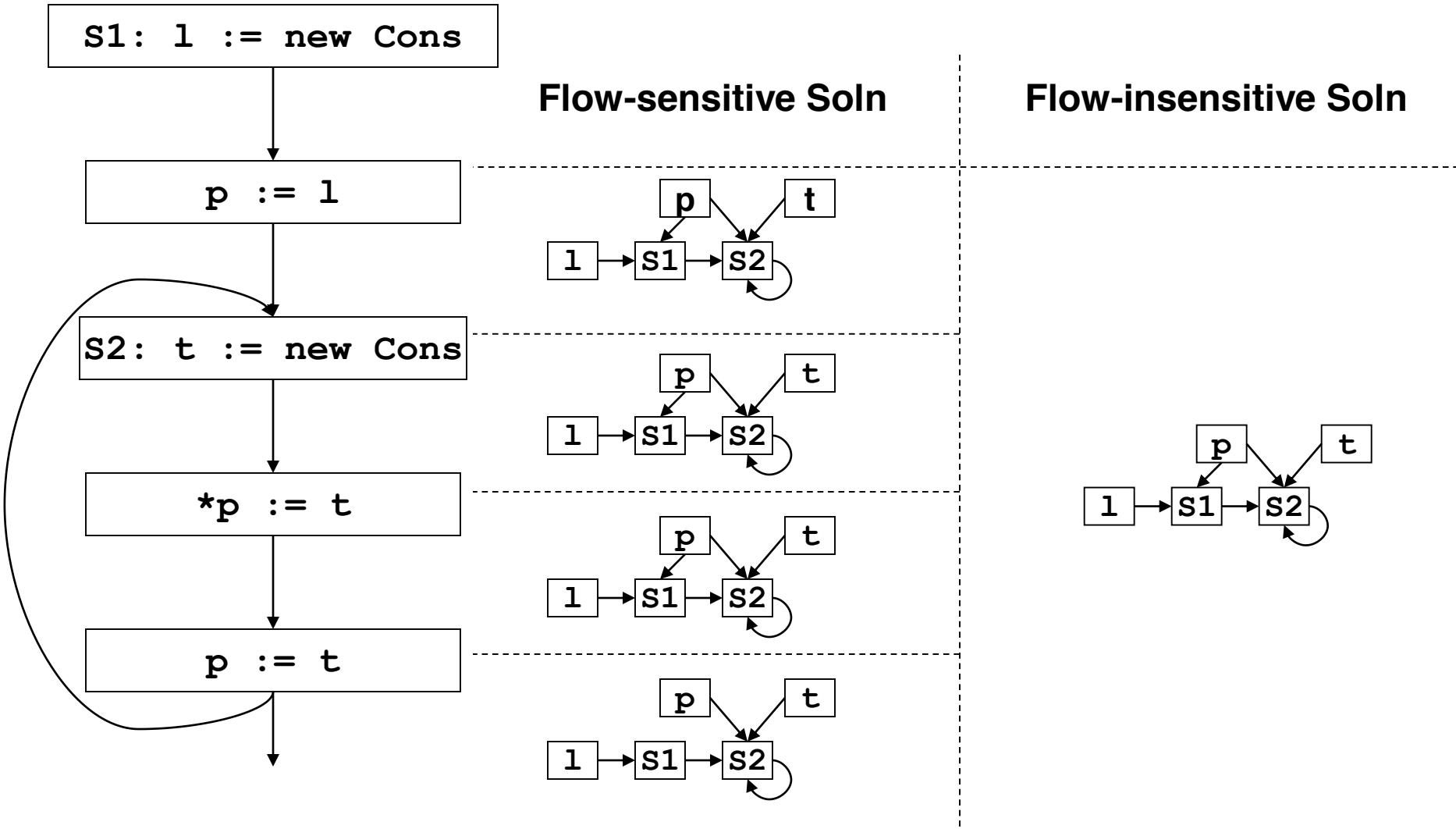
Flow insensitive pointer analysis: fixed

This is Andersen's algorithm '94

Final result



Flow sensitive vs. insensitive, again



Flow insensitive loss of precision

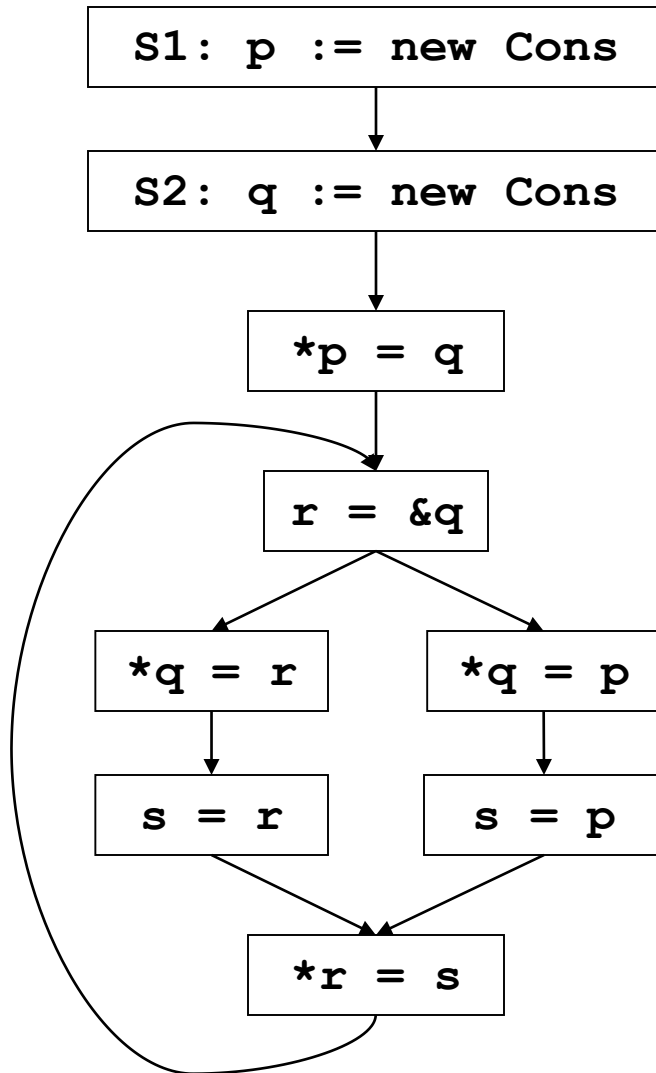
- Flow insensitive analysis leads to loss of precision!

```
main() {  
    x := &y;  
  
    ...  
  
    x := &z;  
}
```

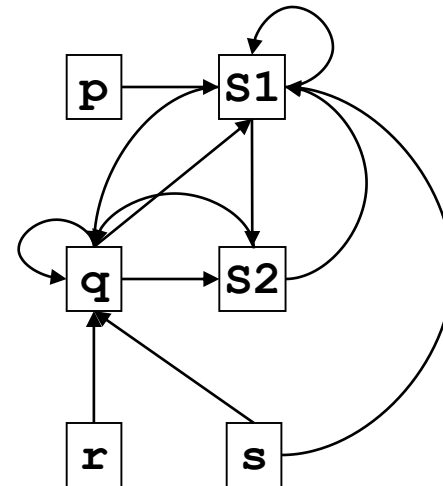
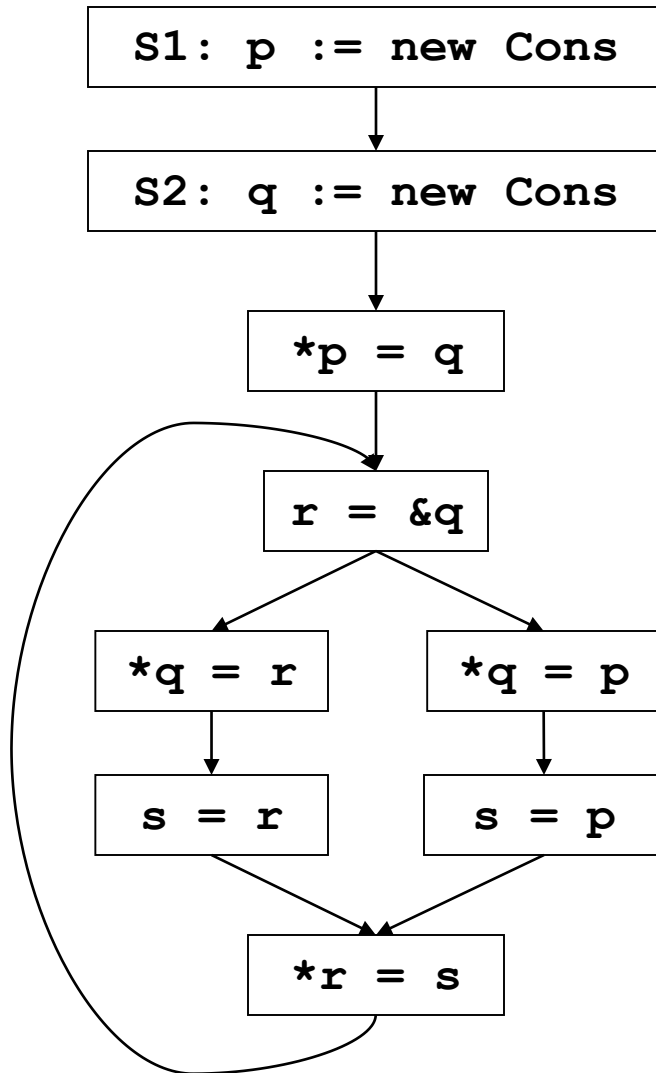
← Flow insensitive analysis tells us that x
may point to z here!

- However:
 - uses less memory (memory can be a big bottleneck to running on large programs)
 - runs faster

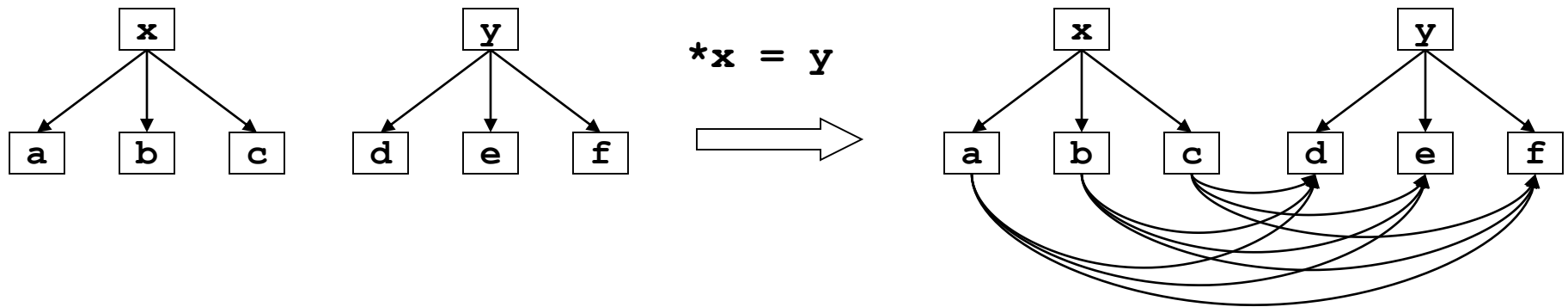
In Class Exercise!



In Class Exercise! solved



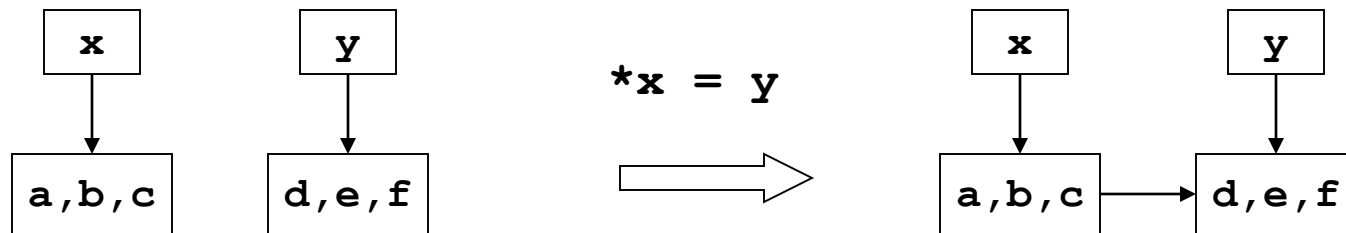
Worst case complexity of Andersen



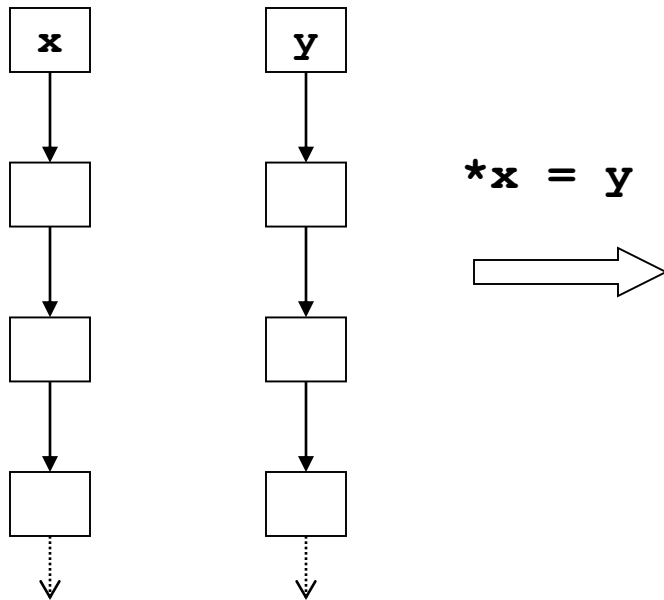
Worst case: N^2 per statement, so at least N^3 for the whole program. Andersen is in fact $O(N^3)$

New idea: one successor per node

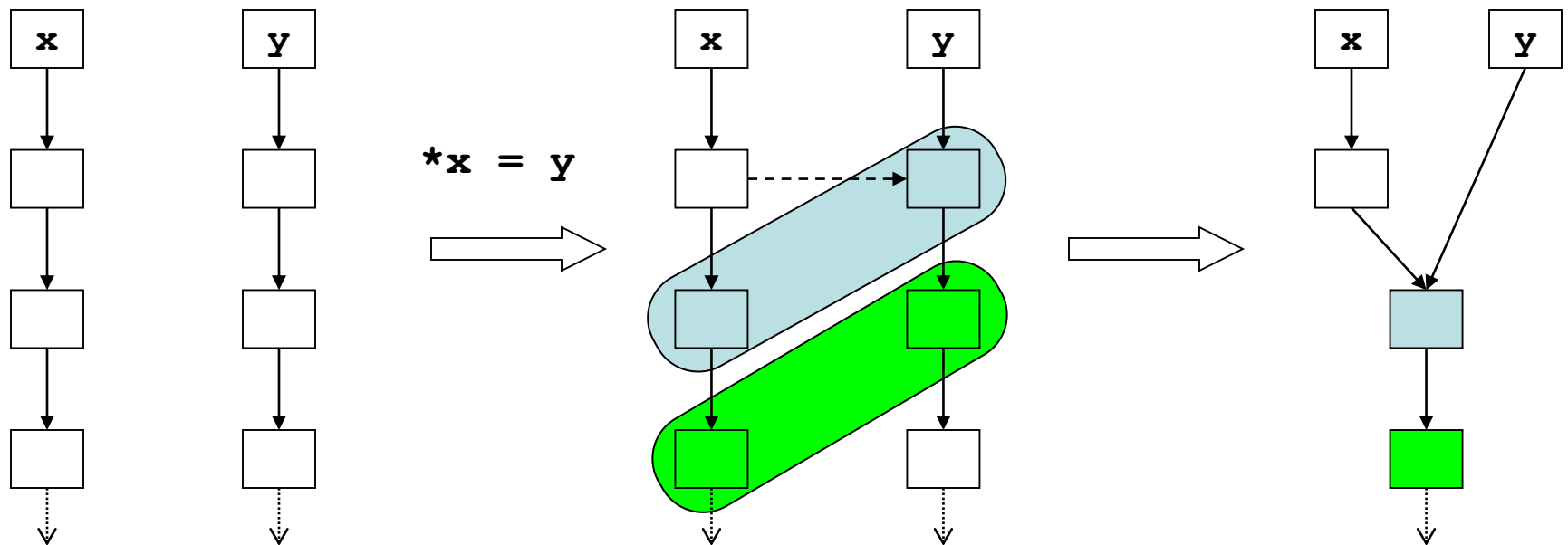
- Make each node have only one successor.
- This is an invariant that we want to maintain.



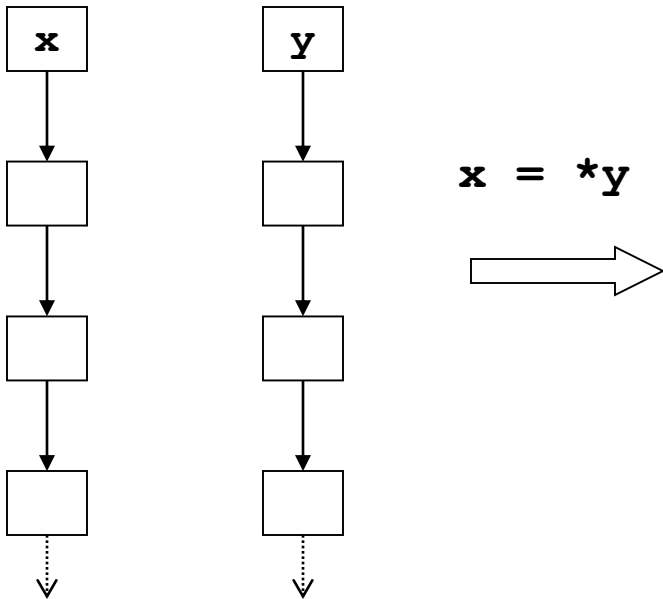
More general case for $*x = y$



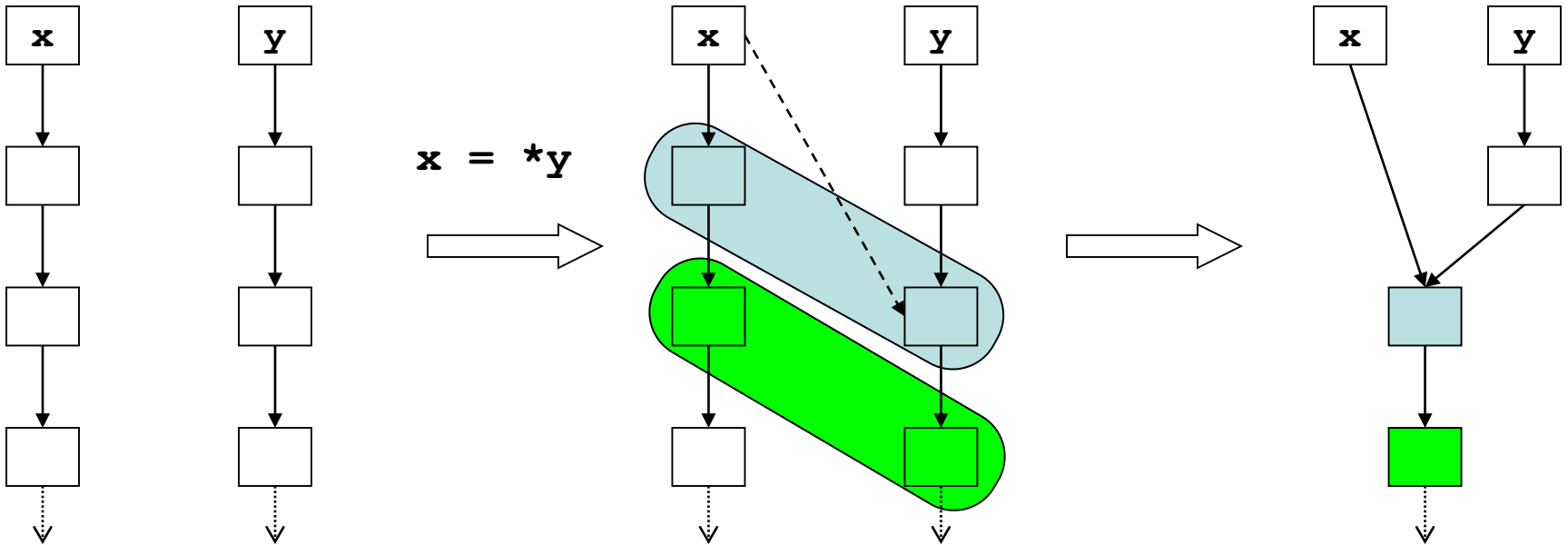
More general case for $*x = y$



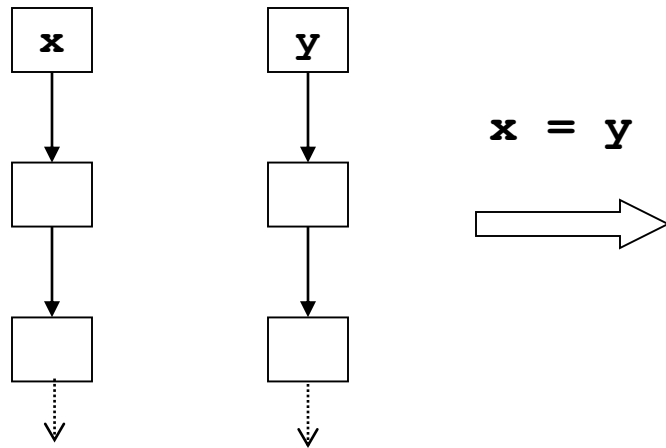
Handling: $x = *y$



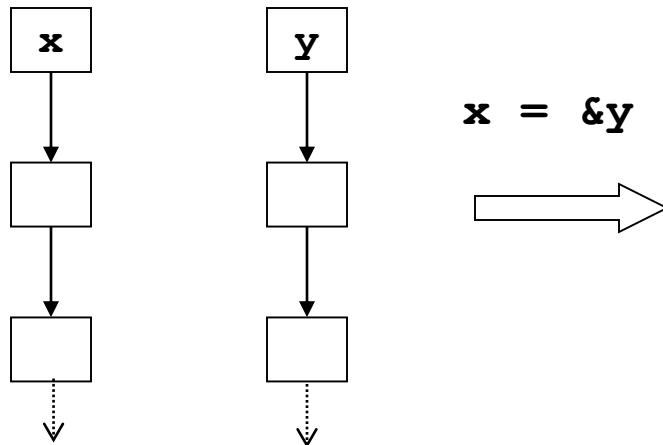
Handling: $x = *y$



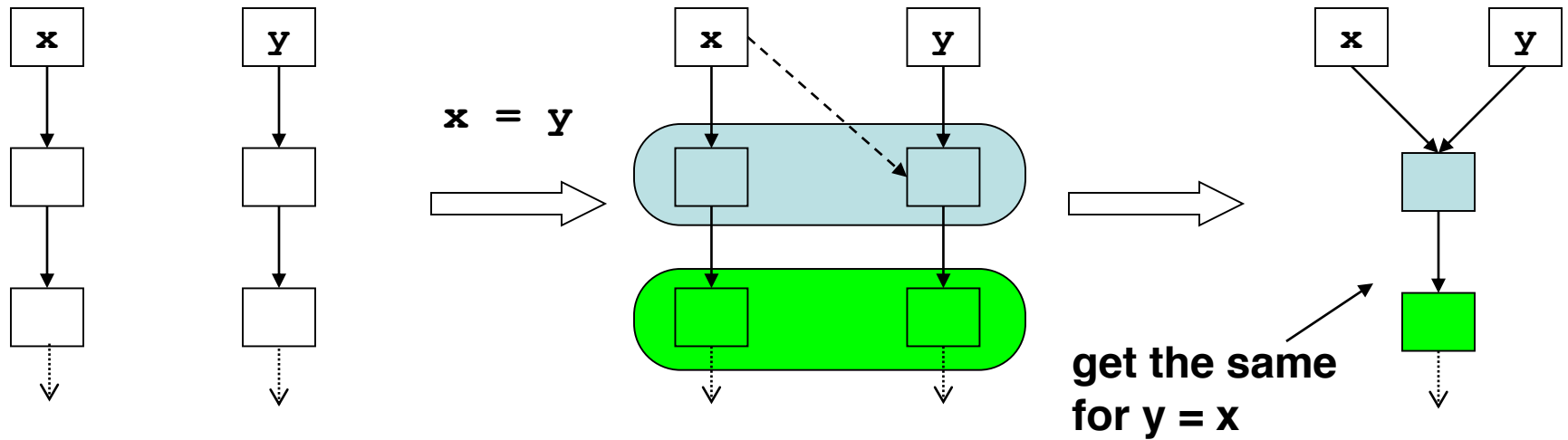
Handling: $x = y$ (what about $y = x$?)



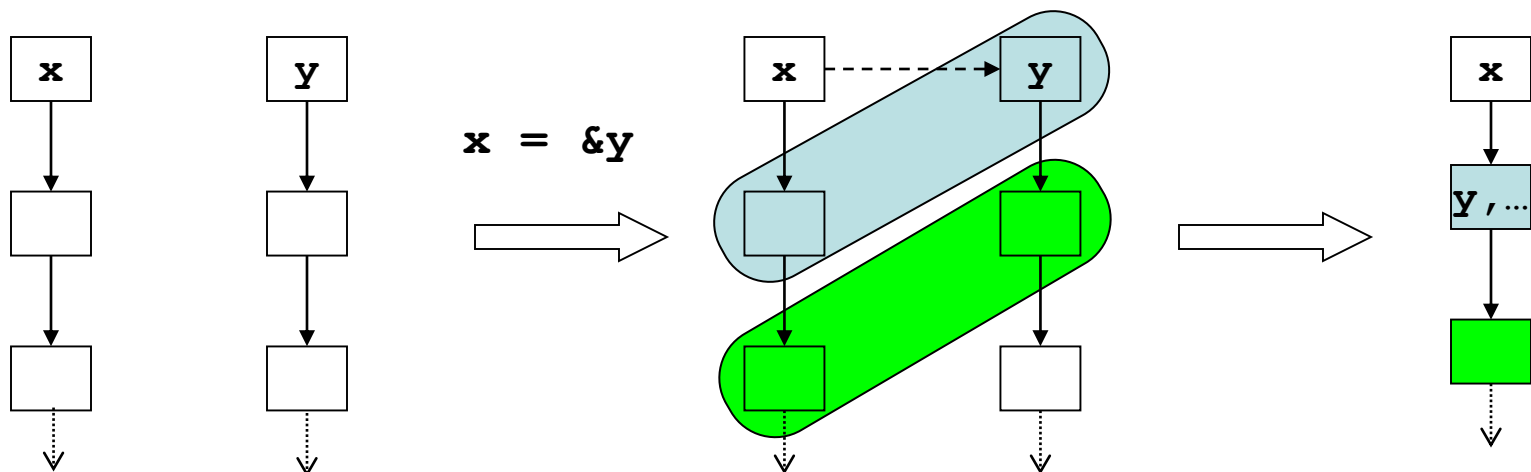
Handling: $x = \&y$



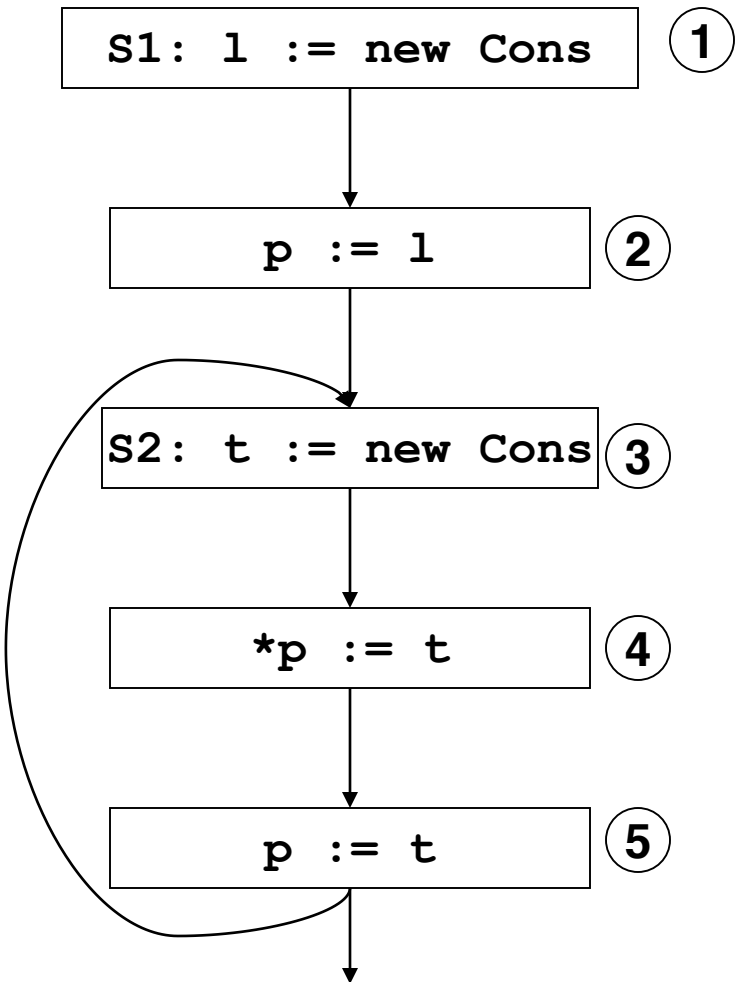
Handling: $x = y$ (what about $y = x$?)



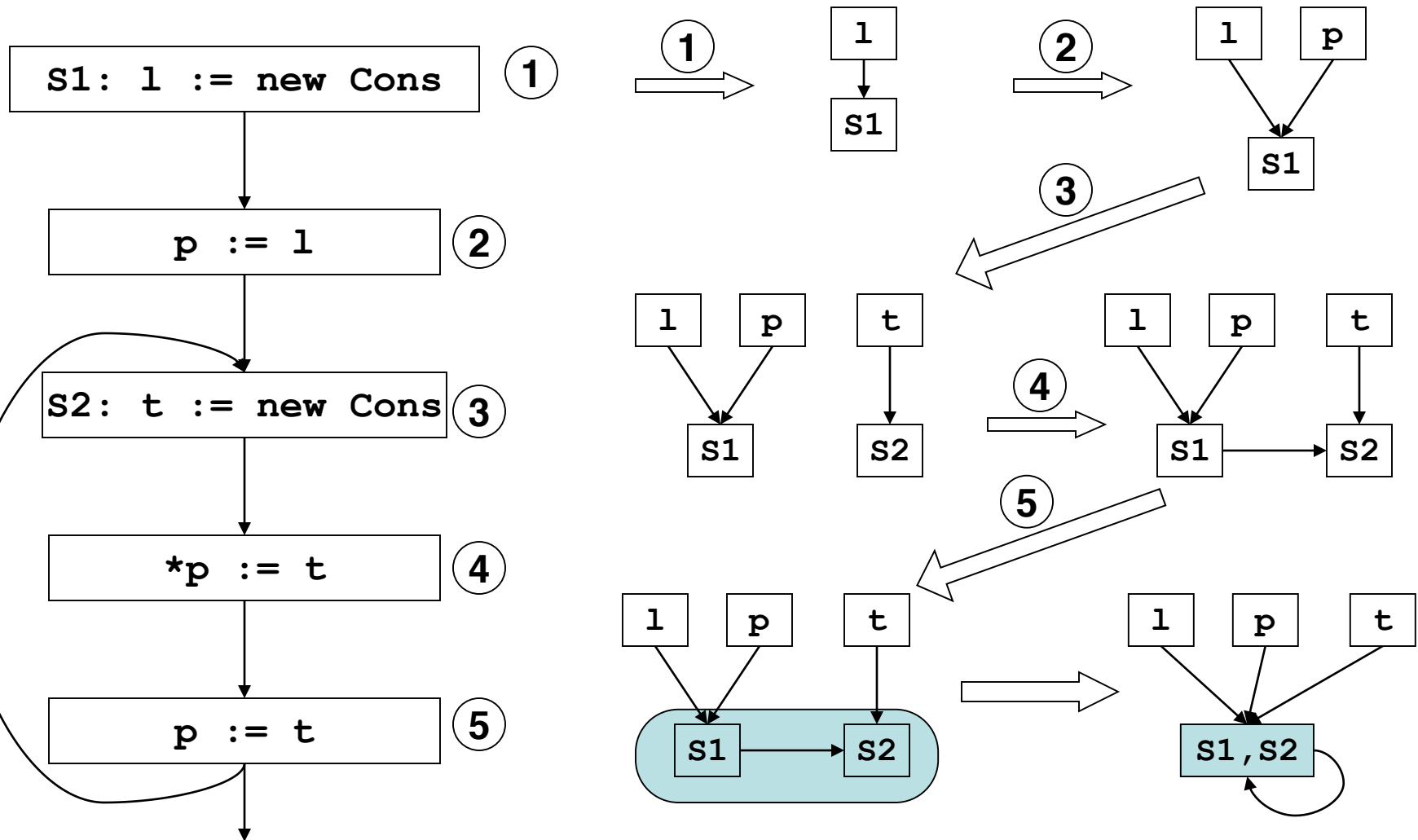
Handling: $x = \&y$



Our favorite example, once more!



Our favorite example, once more!



Flow insensitive loss of precision

S1: l := new Cons

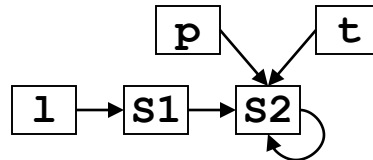
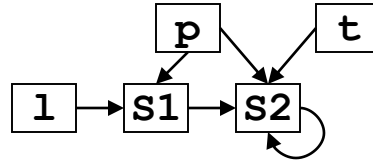
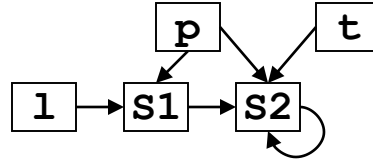
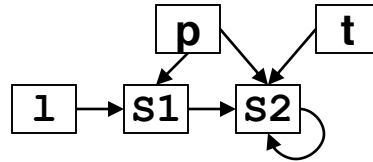
p := l

S2: t := new Cons

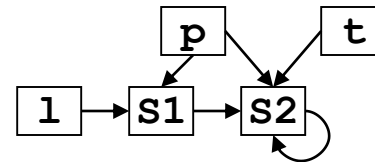
*p := t

p := t

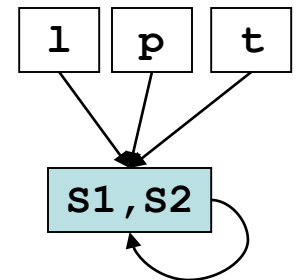
Flow-sensitive
Subset-based



Flow-insensitive
Subset-based



Flow-insensitive
Unification-
based

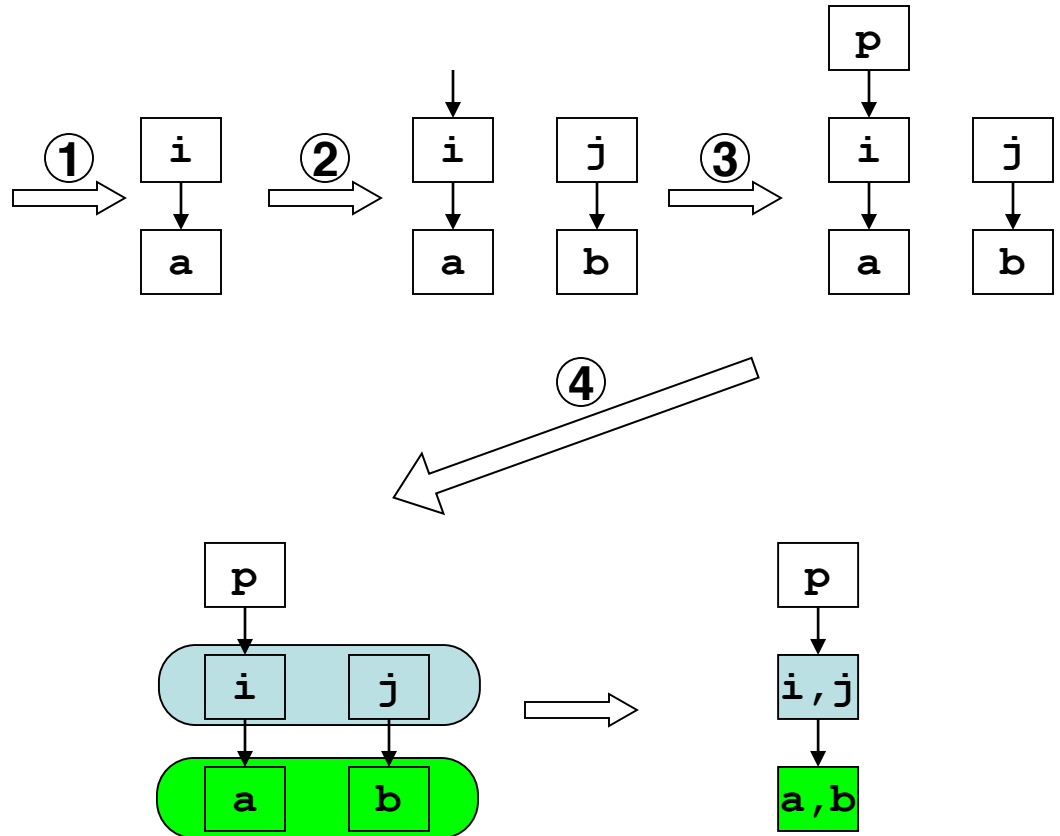


Another example

```
bar() {  
  ① i := &a;  
  ② j := &b;  
  ③ foo(&i);  
  ④ foo(&j);  
    // i pnts to what?  
    *i := ...;  
  
}  
  
void foo(int* p) {  
    printf("%d", *p);  
}
```

Another example

```
bar() {  
  ① i := &a;  
  ② j := &b;  
  ③ foo(&i);  
  ④ foo(&j);  
  // i pnts to what?  
  *i := ...;  
}  
  
void foo(int* p) {  
  printf("%d", *p);  
}
```



Almost linear time

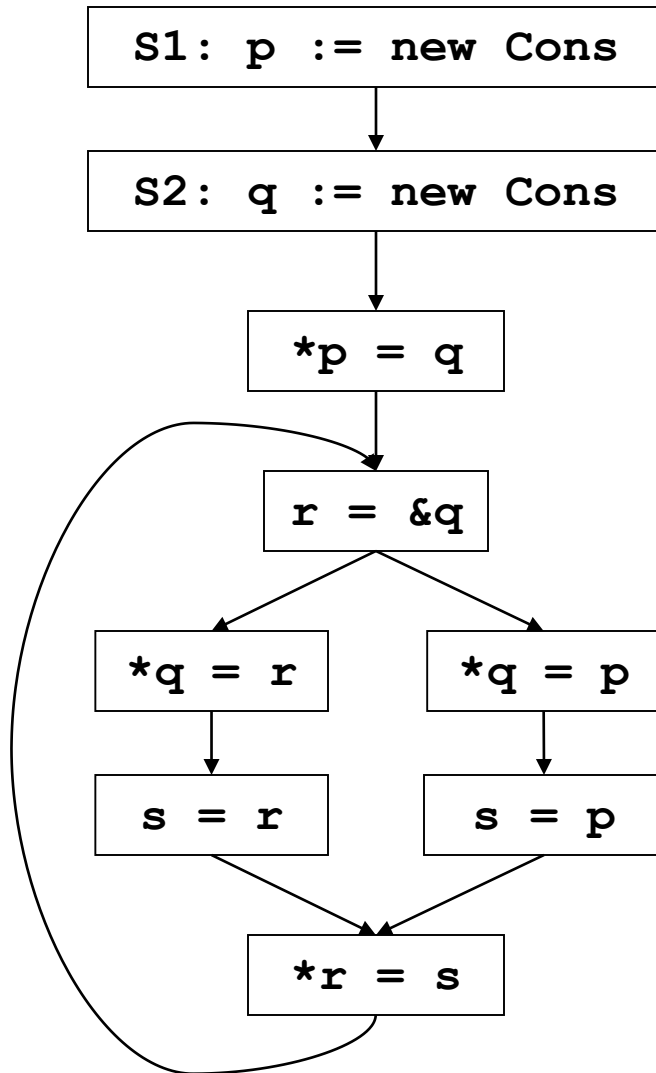
- Time complexity: $O(N\alpha(N, N))$



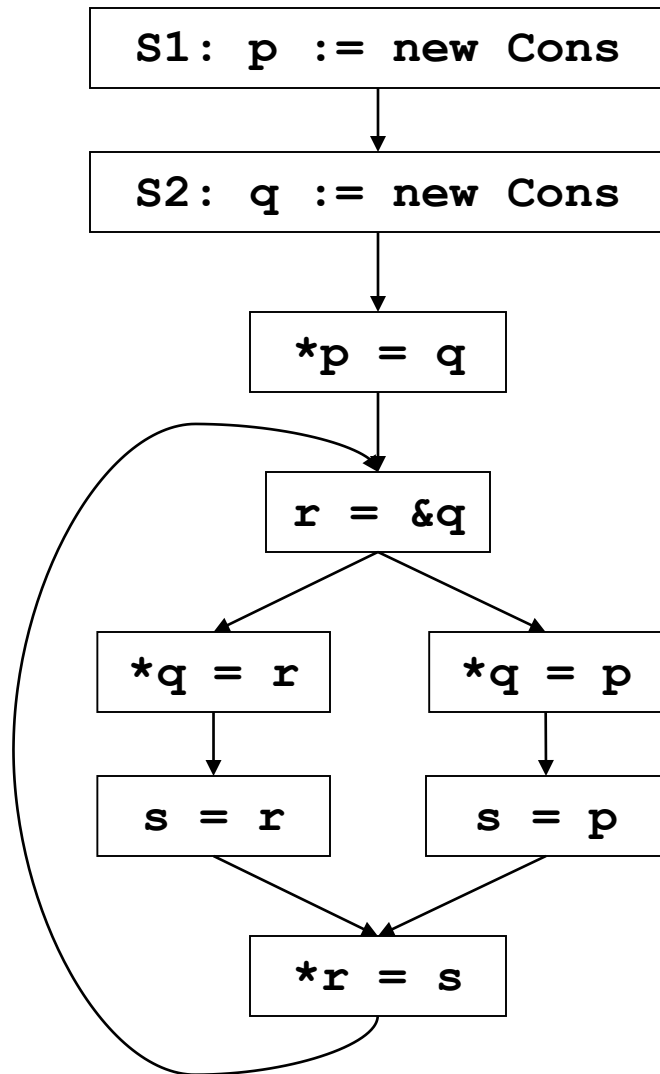
inverse Ackermann
function

- So slow-growing, it is basically linear in practice
- For the curious: node merging implemented using UNION-FIND structure, which allows set union with amortized cost of $O(\alpha(N, N))$ per op. Take CSE 202 to learn more!

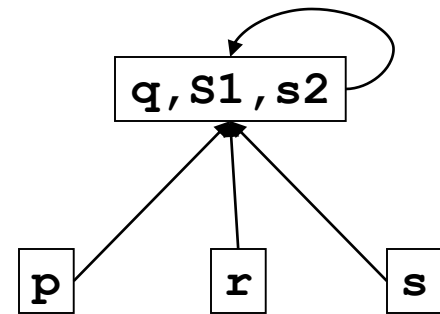
In Class Exercise!



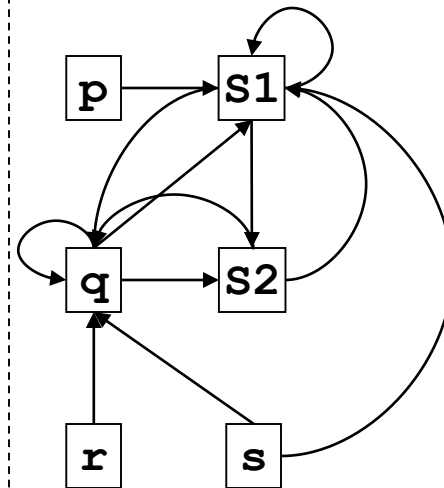
In Class Exercise! solved



Steensgaard



Andersen



Advanced Pointer Analysis

- Combine flow-sensitive/flow-insensitive
- Clever data-structure design
- Context-sensitivity