

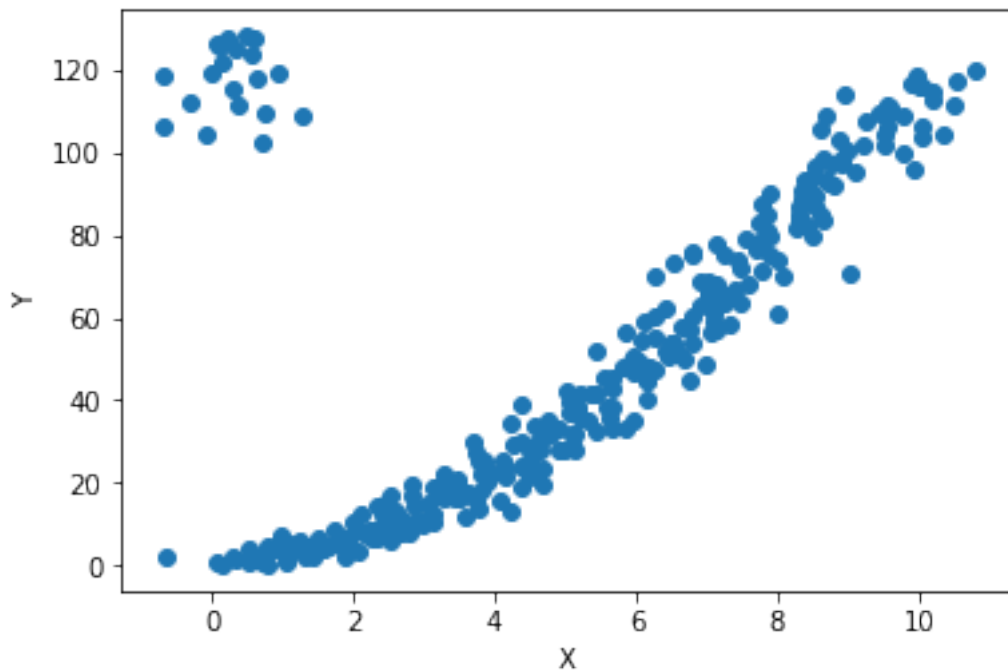
Problem2

May 14, 2018

1 (a)

```
In [88]: import numpy as np
import matplotlib.pyplot as plt
X_and_Y = np.load('./q2-parabola.npy')
X = X_and_Y[:, 0] # Shape: (300,)
Y = X_and_Y[:, 1] # Shape: (300,)
```

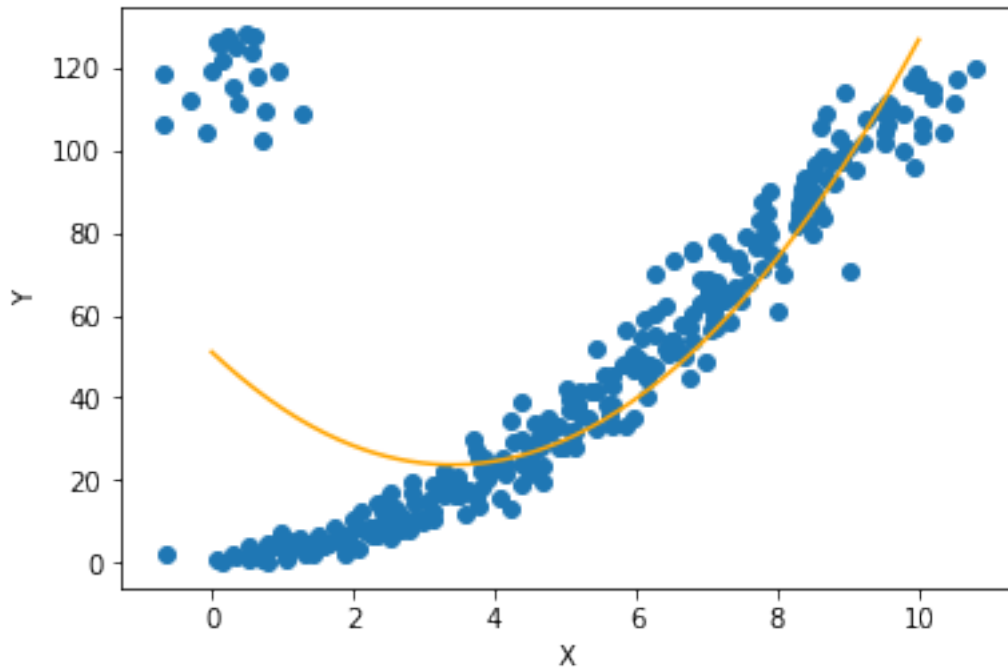
```
In [89]: plt.scatter(X, Y)
plt.xlabel('X')
plt.ylabel('Y')
plt.show()
```



```
In [90]: # Assume  $Y = w_0 + w_1X + w_2X^2 = (w_0, w_1, w_2) \cdot (1, X, X^2) = W \cdot X_2$ 
#  $X_2$  contains 1,  $X$  and  $X^2$ .
X2 = np.matrix(np.hstack((np.ones((len(X),1)),X.reshape(-1,1),np.square(X.reshape(-1,1)))))
W = X2.T.dot(X2).I.dot(X2.T).dot(Y)
w0, w1, w2 = np.array(W).reshape(-1)
print('Y = {:.2f} + {:.2f}*X + {:.2f}*X^2'.format(w0, w1, w2))
```

Y = 51.07 + -16.06*X + 2.36*X²

```
In [91]: X_line = np.linspace(0,10,300)
Y_line = w0 + w1 * X_line + w2 * (X_line**2)
plt.scatter(X, Y)
plt.plot(X_line, Y_line, color='orange')
plt.xlabel('X')
plt.ylabel('Y')
plt.show()
```



2 (b)

```
In [94]: X_L1 = np.matrix(np.hstack((np.ones((len(X),1)),X.reshape(-1,1),np.square(X.reshape(-1,1)))))
W_L1 = np.random.random((1,3))
```

```
In [95]: MAX_ITERATION = 300000
LEARNING_RATE = 0.000001
STOP_CRITERIA = 0.00001
```

```

In [96]: for count in range(MAX_ITERATION):
          error = X_L1.dot(W_L1.T) - Y.reshape(len(X),1)
          if np.sum(np.abs(error))<=STOP_CRITERIA:
              break
          W_L1_grad = np.array(np.sign(error).T.dot(X_L1))
          W_L1_delta = W_L1_grad * LEARNING_RATE
          W_L1 -= W_L1_delta

In [97]: w0_L1, w1_L1, w2_L1 = np.array(W_L1).reshape(-1)
          print('Y = {:.2f} + {:.2f}*X + {:.2f}*X2'.format(w0_L1, w1_L1, w2_L1))

```

Y = 1.69 + 1.12*X + 1.05*X2

```

In [98]: X_line = np.linspace(0,10,300)
          Y_line = w0_L1 + w1_L1 * X_line + w2_L1 * (X_line**2)
          plt.scatter(X, Y)
          plt.plot(X_line, Y_line, color='orange')
          plt.xlabel('X')
          plt.ylabel('Y')
          plt.show()

```

