

#### Automating Incremental and Asynchronous Evaluation for Recursive Aggregate Data Processing

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For a given algorithm defined by a function, it is a RAP if it satisfies:

- (1) The function consists of a basic rule for an **initiation** and a small set of other rules for **iteratively self-calling** (recursion).
- (2) The recursive part of the function includes **aggregate** operators, such as MIN, MAX, AVG, etc.

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#### **Datalog** perfectly expresses RAPs:

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Aggregate Function
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Aggregate Function Non-aggregate Functions
```

#### Recursive Aggregate Programs are Everywhere

#### Connected Components

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cc(X,X) :- edge (X,_).
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Graph Convolution Neural Network

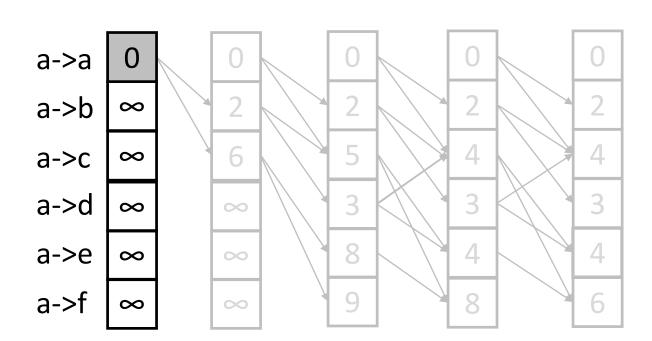
```
GCN (j+1,Y, sum [g1]) :- GCN (j,X,g), A(X,Y,w), Para (p),
p1 = relu(g*p) *w
```

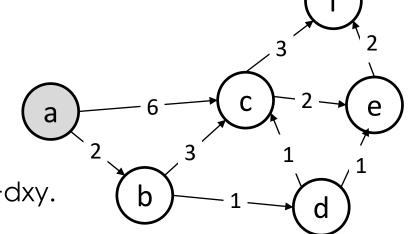
And many others

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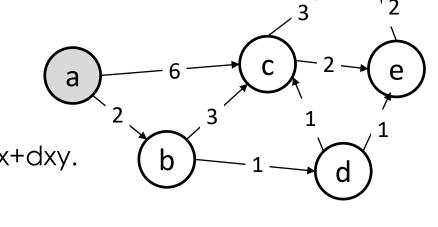




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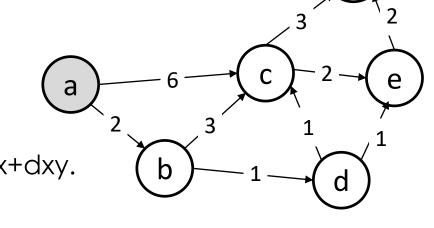
a->a	0	0	0	0	0
a->b	8	2	2	2	2
a->c	8	6	5	4	4
a->d	8	×	3	3	3
a->e	8	$\sim$	8	4	4
a->f	8	~	9	8	6

Iteratively performing aggregate and non aggregate function to derive result until the program reach the convergence.

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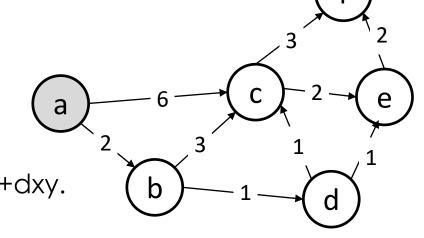
			_			-		_
a->a	0	0		0	0		0	
a->b	8	2		2	2		2	
a->c	8	6		5	4		4	
a->d	∞	<b>∞</b>		3	3		3	
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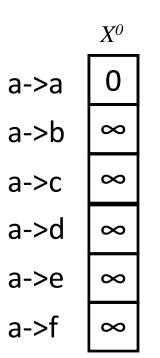
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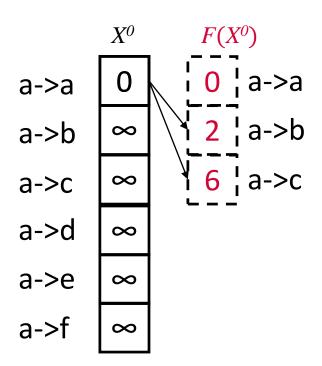
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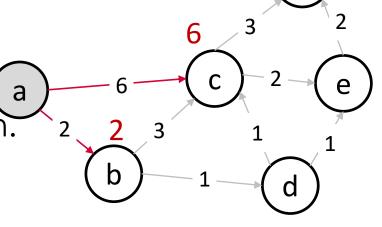
**Naïve Evaluation** 

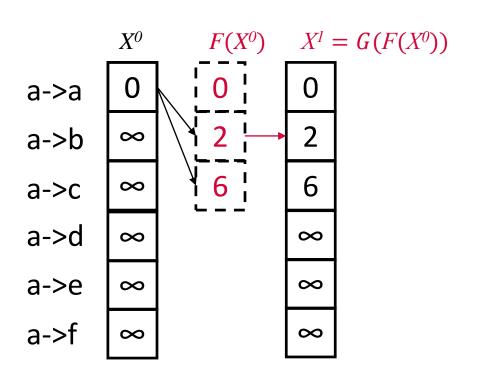
**Semi-naïve Evaluation** 

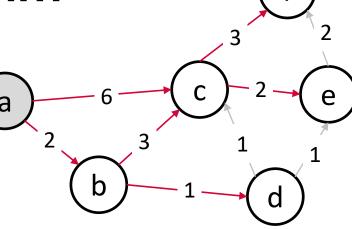
# Naïve Evaluation: A Direct Approach

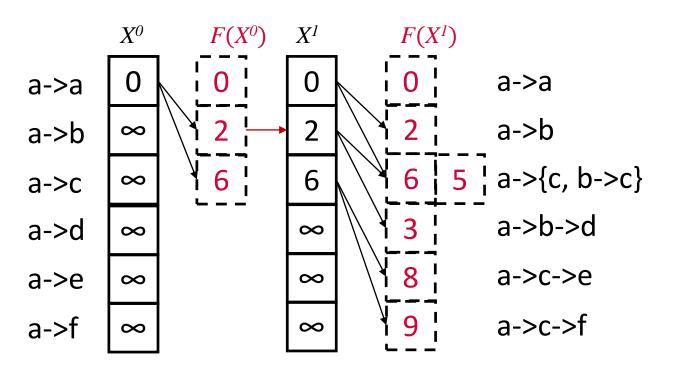


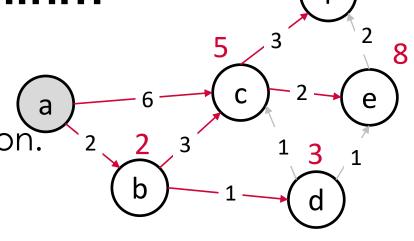


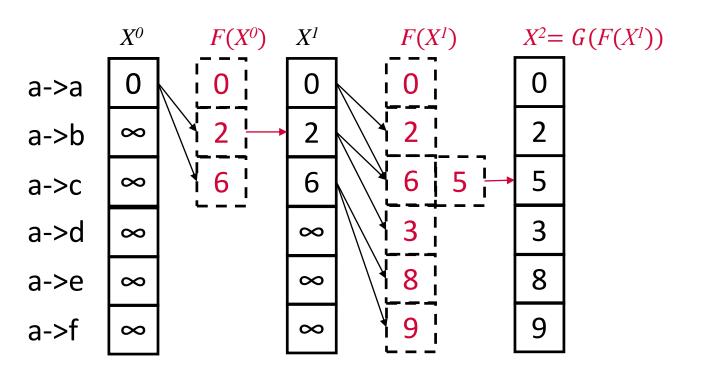


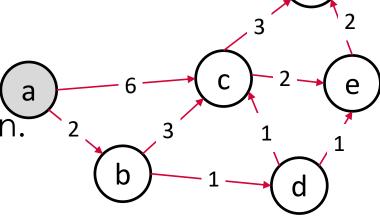


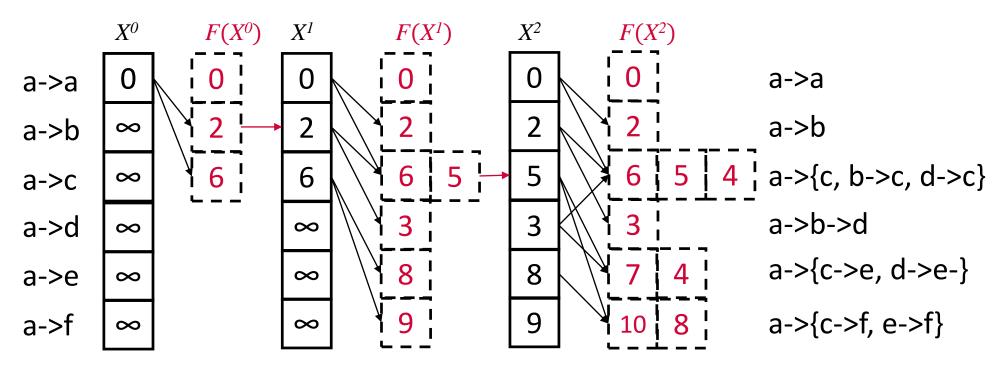


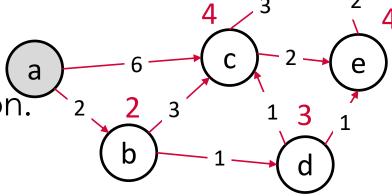


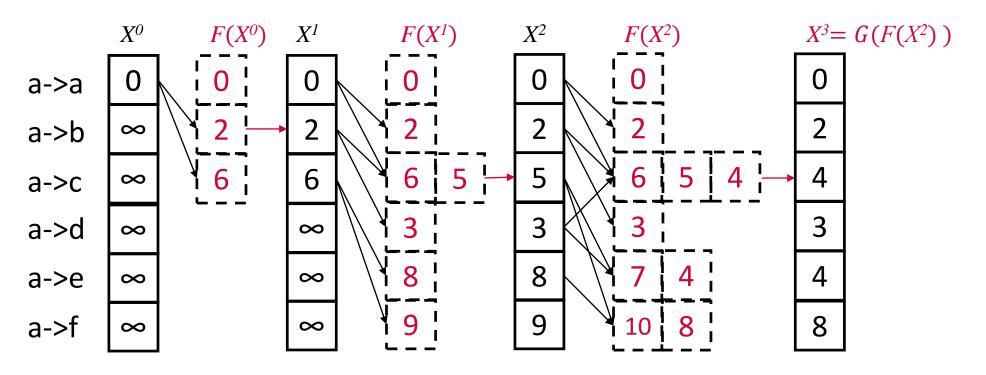


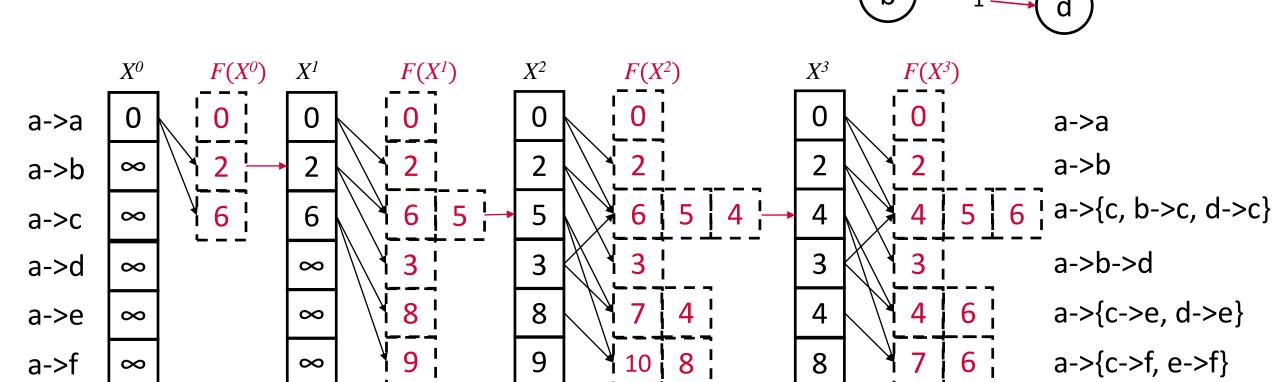




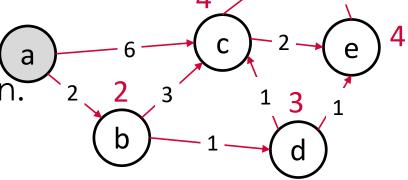




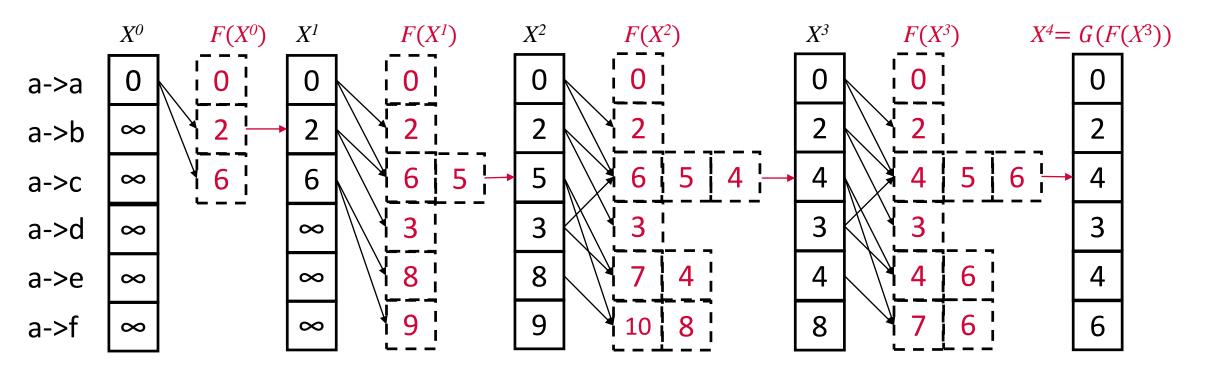




Naïve Evaluation is a direct and intuitive solution.



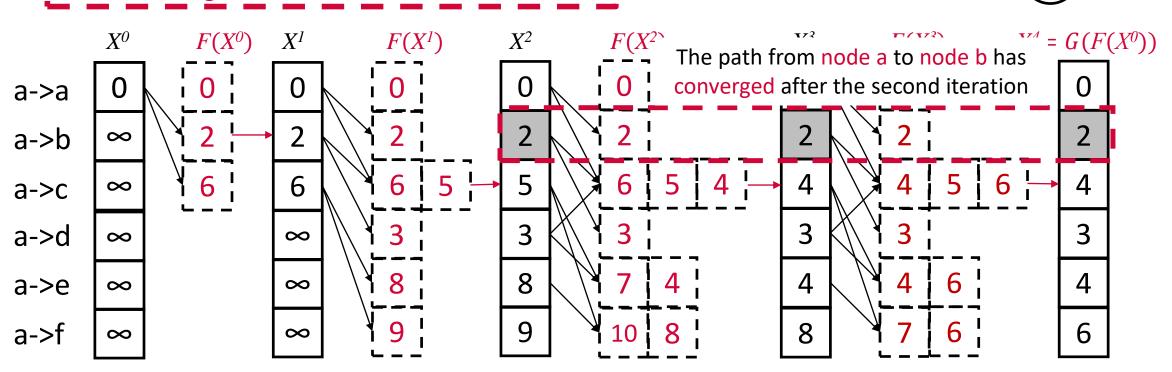
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#### Problems on Naïve Evaluation

Naïve Evaluation is a direct and intuitive solution.

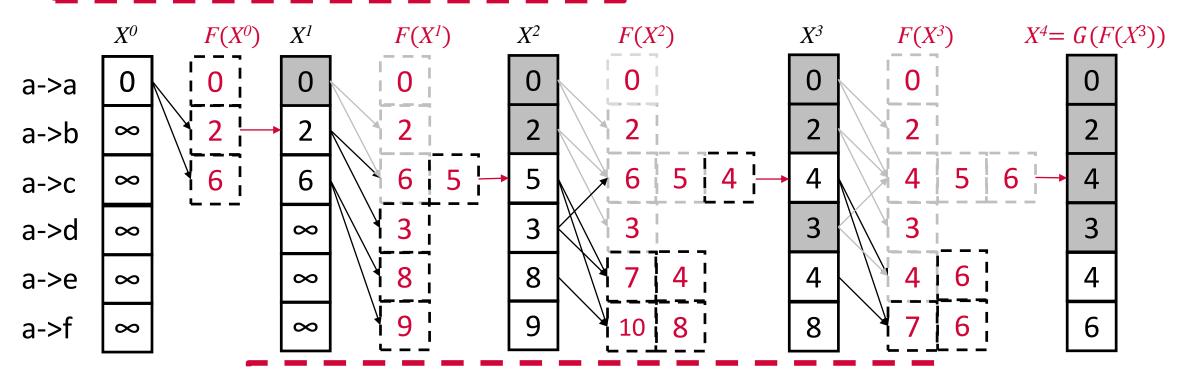
The converged nodes still need to involve.



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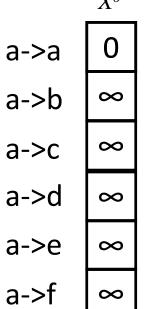
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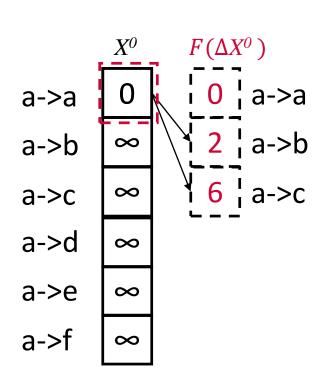
Naïve evaluation brings unnecessary computation.

### Semi-naïve Evaluation: Avoiding Unnecessary computation

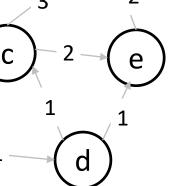




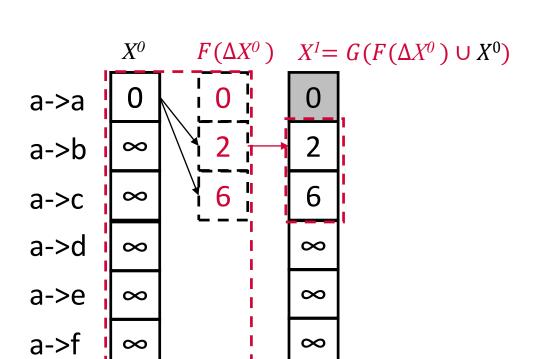
Semi-naïve Evaluation is an incremental approach.



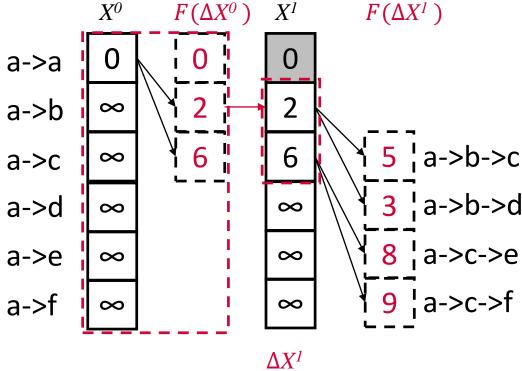
 $\Delta X^0$ 



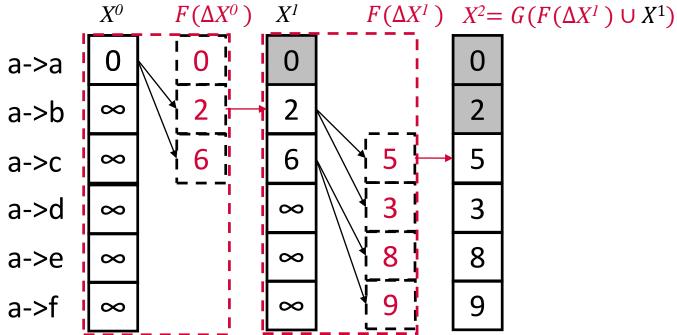
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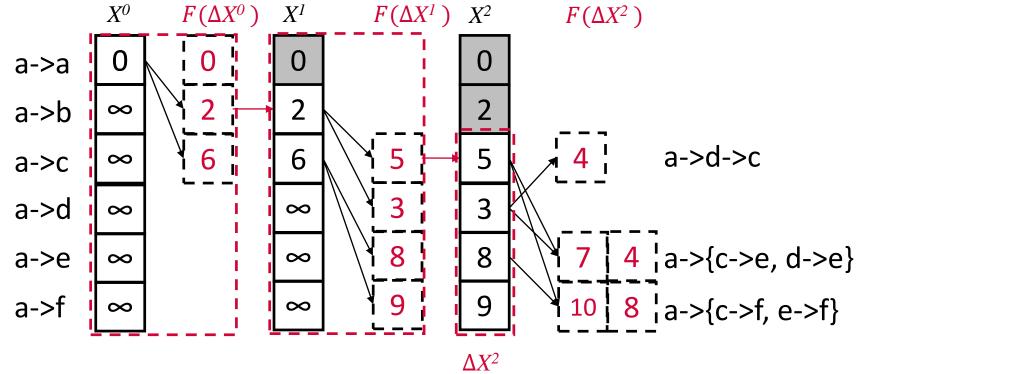


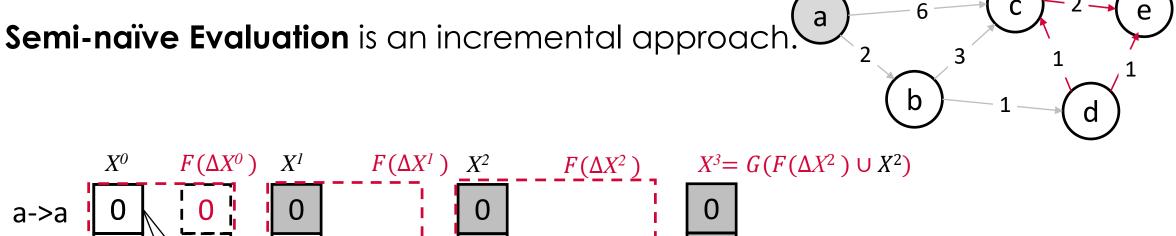


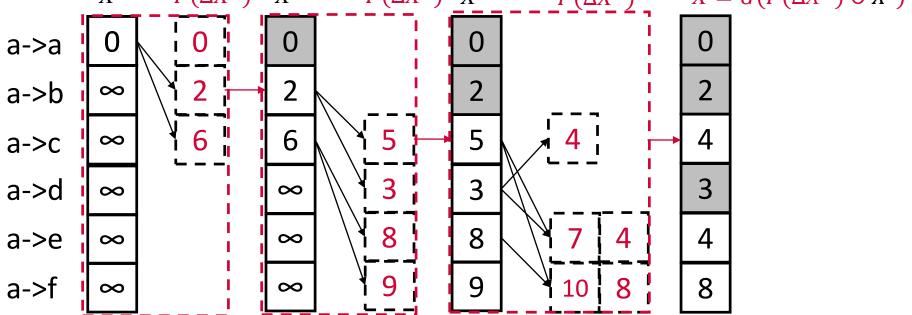


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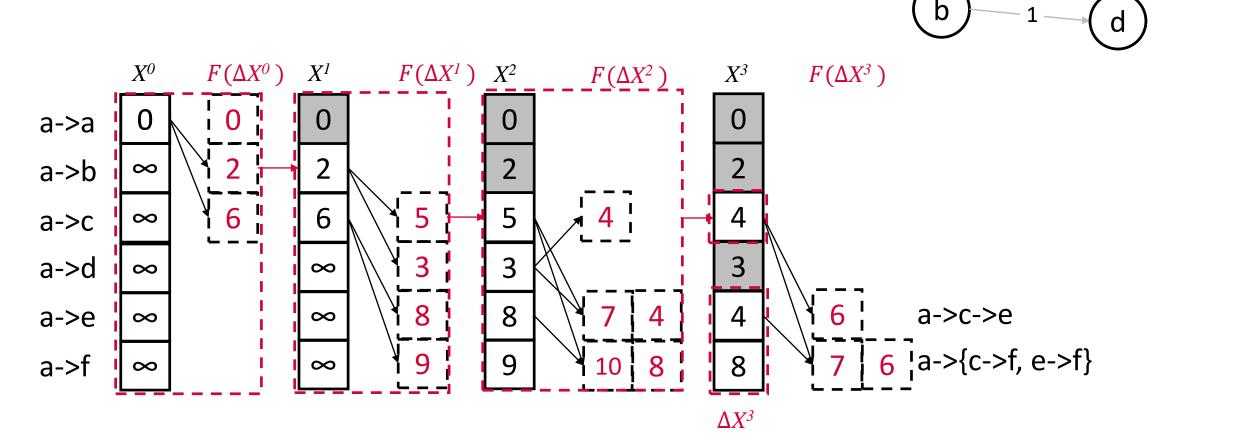






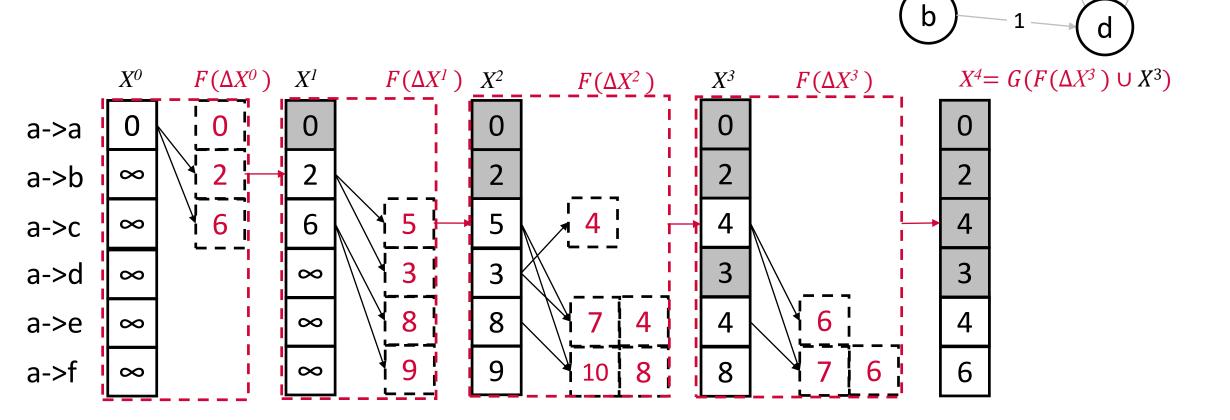


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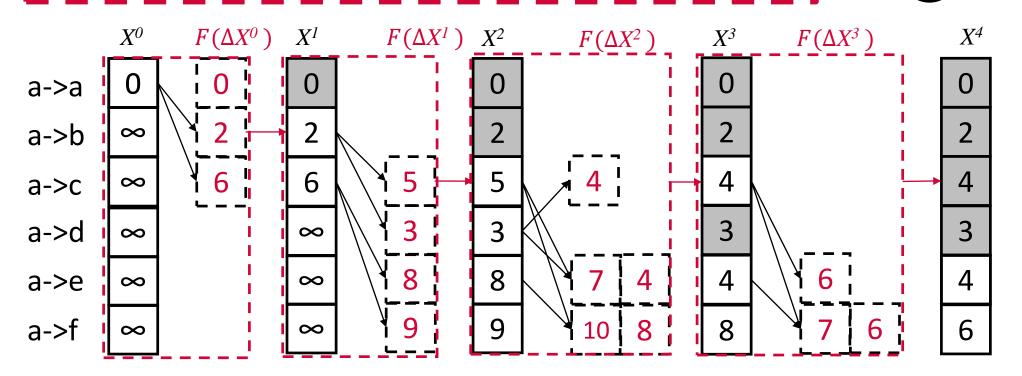
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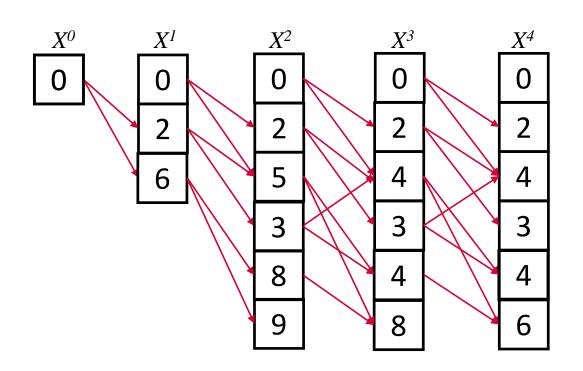
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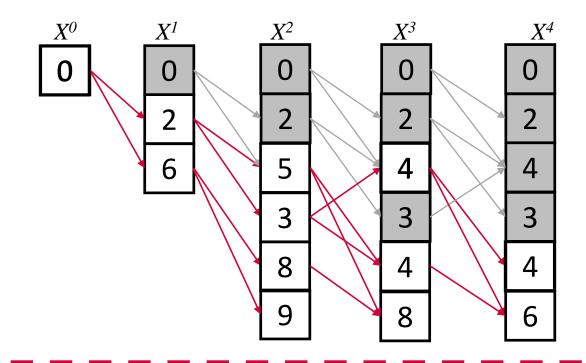
Semi-naïve Evaluation is an incremental approach.

The converged nodes do not involved in the computation.



#### Naïve Evaluation vs. Semi-naïve Evaluation





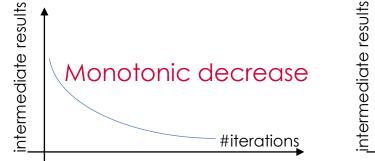
A fully computation is performed.

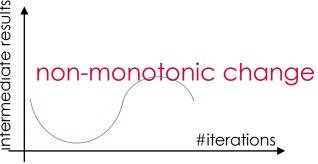
Only the necessary computation is performed.

■ The converged nodes still need to involve. ■ The converged nodes do not need to involve.

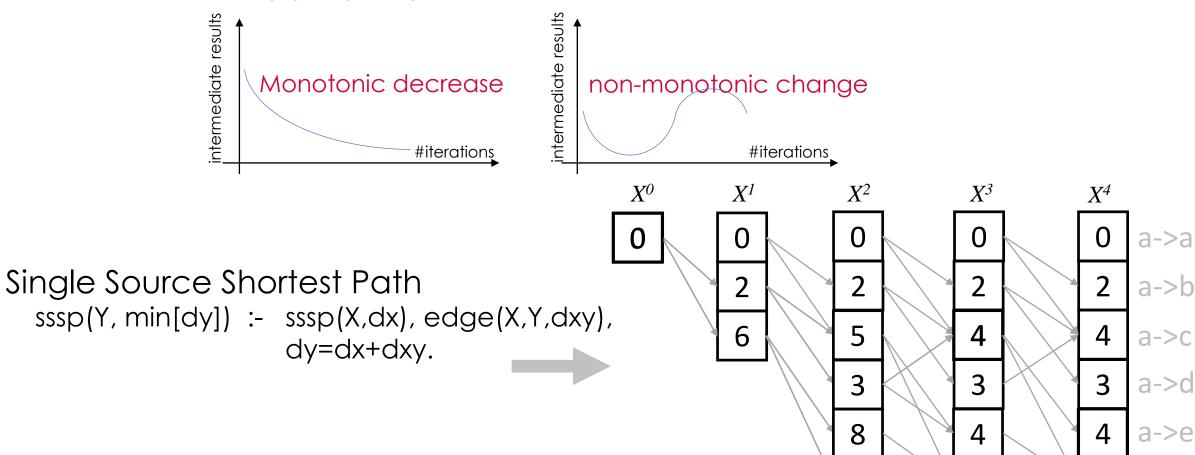
# Monotonicity Requirement for Semi-naïve Evaluation

The monotonicity property





The monotonicity property

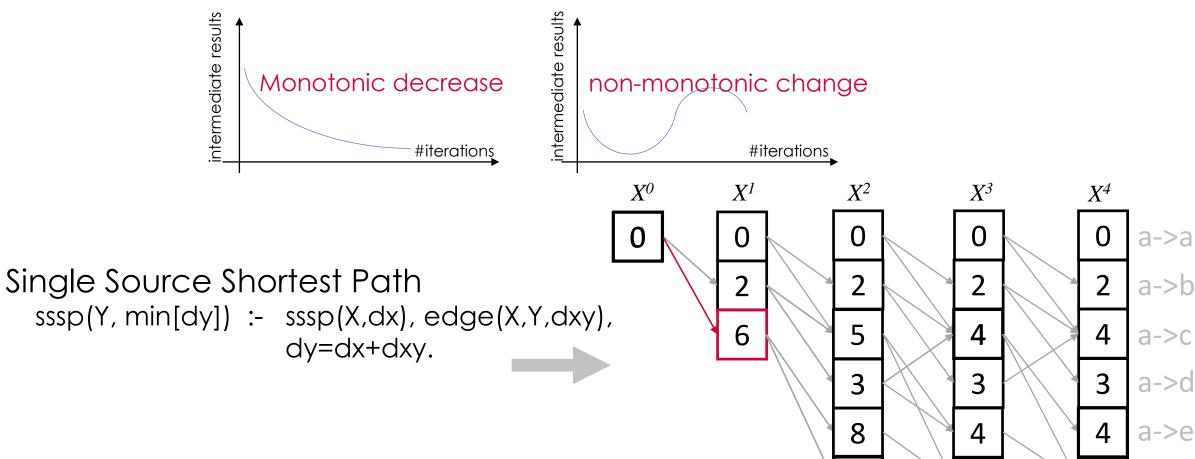


9

8

a->f

The monotonicity property



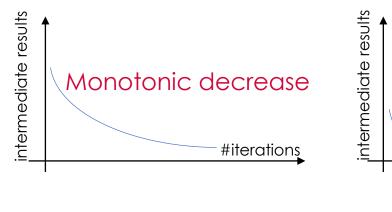
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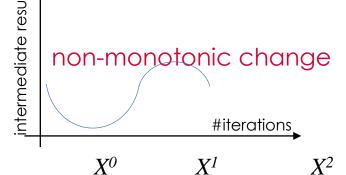
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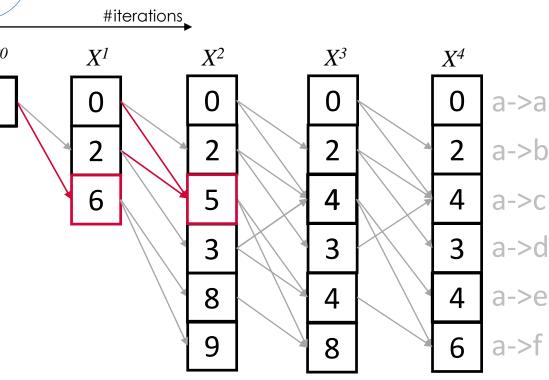
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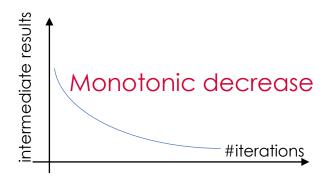


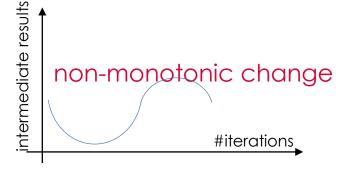


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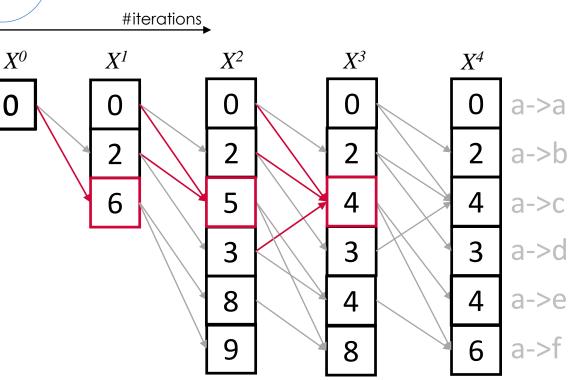


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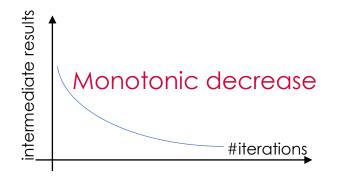


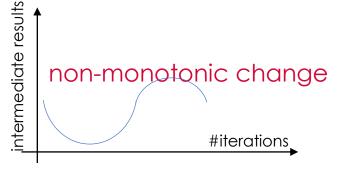


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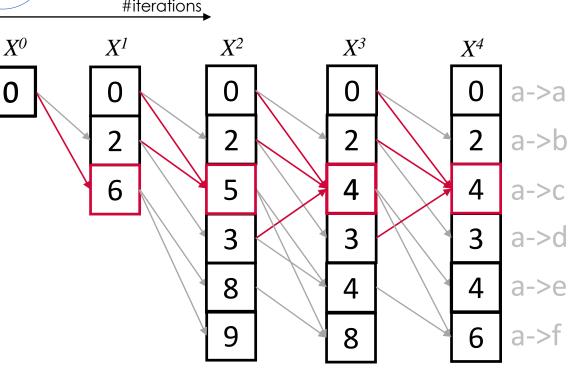


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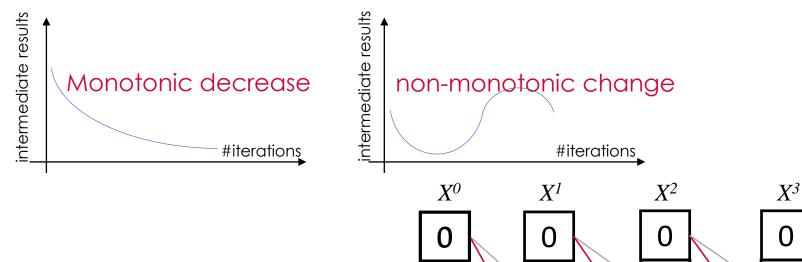




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The monotonicity property



3

8

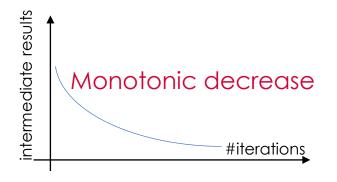
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Single Source Shortest Path
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Distance a->c monotonically decreases iteratively.

6

The monotonicity property



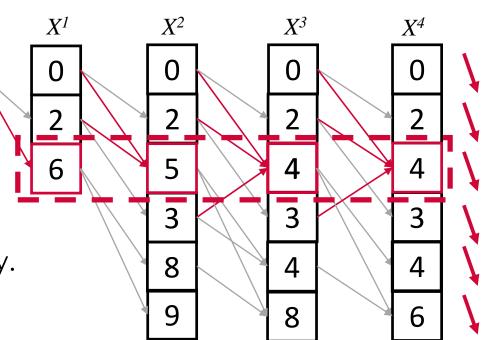
non-monotonic change
#iterations

 $X^0$ 

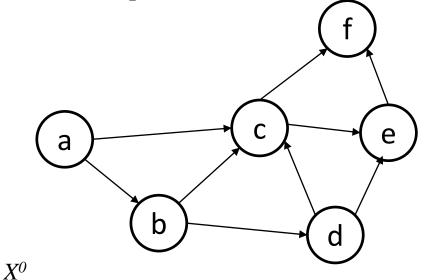
Single Source Shortest Path
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The SSSP algorithm can be semi-naïve evaluated.



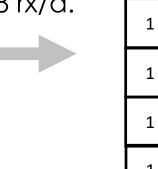
The monotonicity property



#### PageRank

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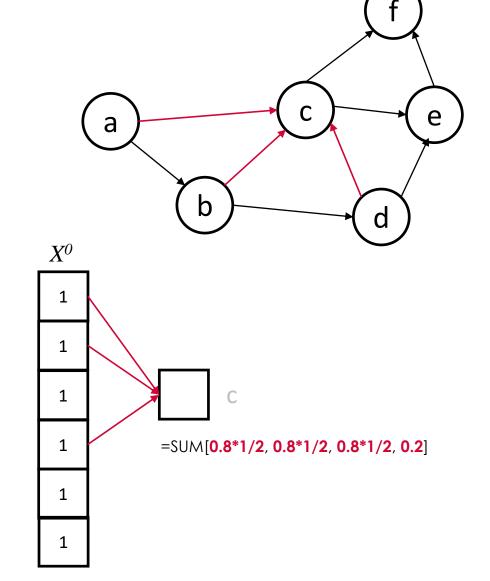


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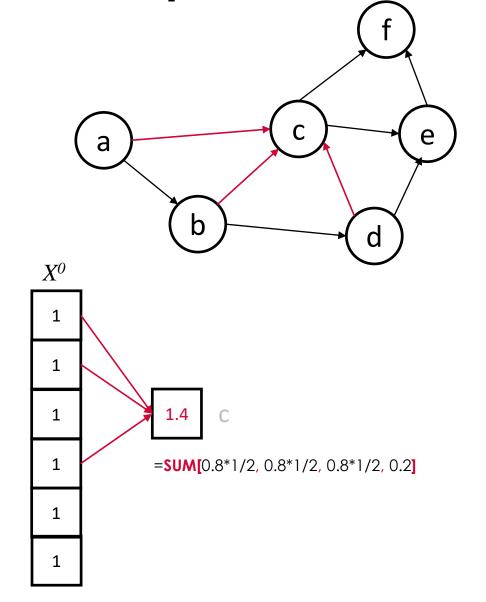


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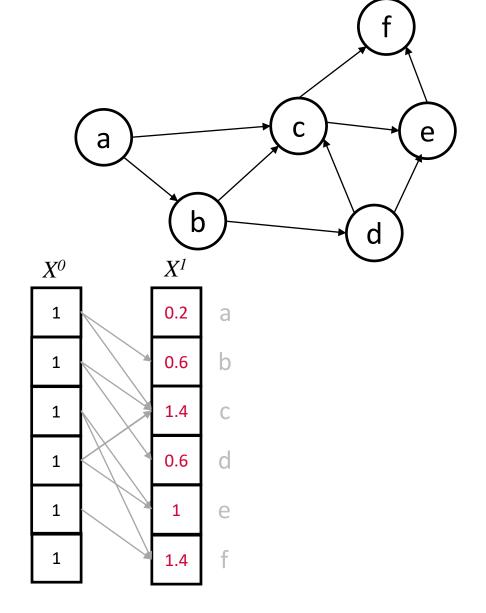


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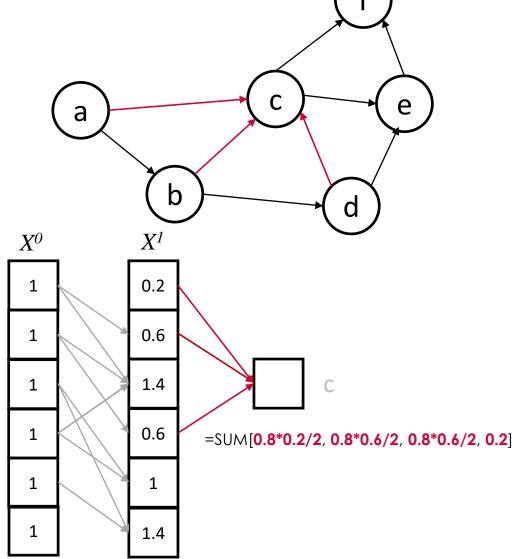


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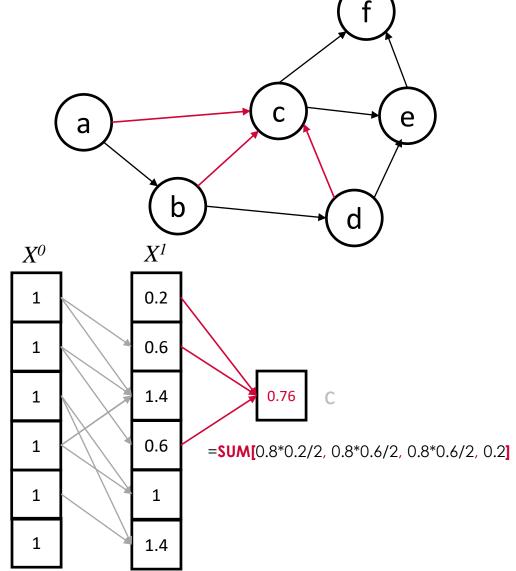


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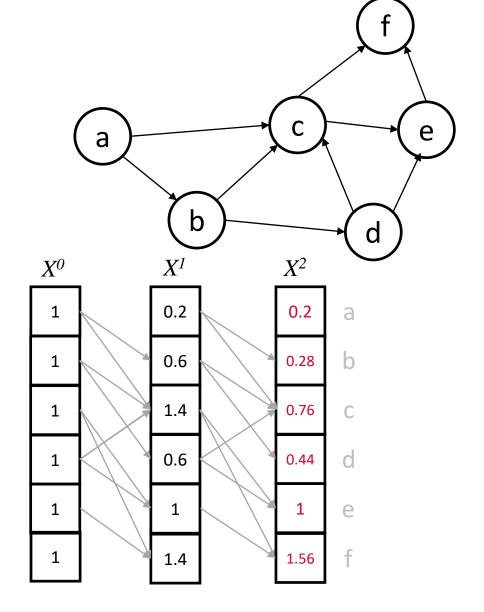


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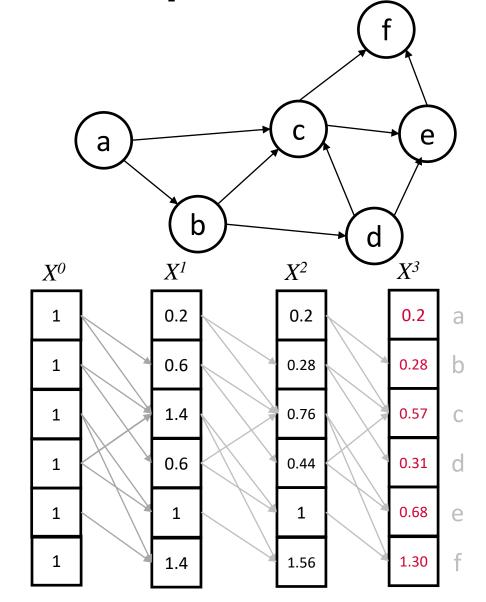


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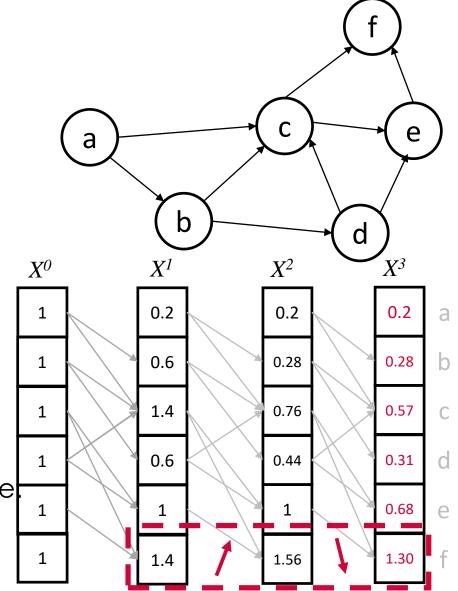
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Rank values are not monotonically increase/decrease



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PageRank

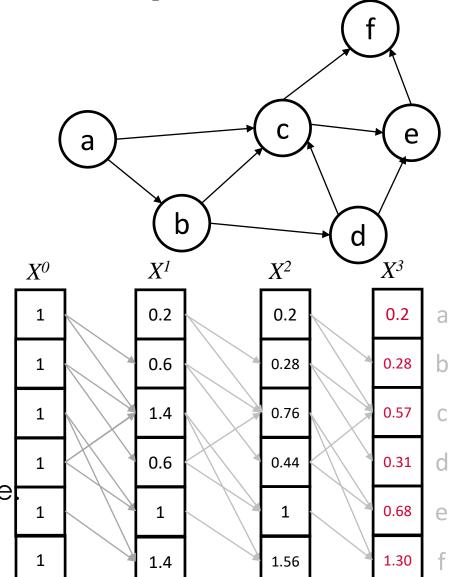
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PageRank is a non-monotonic algorithm.



#### **Existing Works on Monotonic Conditions**

Ross and Sagiv [PODS'92], SociaLite [ICDE'13] and Myria [VLDB'15] formalize the conditions for using monotonic aggregate in recursive query.

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As presented in **Myria** [VLDB'15], a recursive aggregate program can be semi-naïve evaluated if

- It require the aggregate function to be bag-monotonic.
- 2. The non-aggregate function is monotonic w.r.t. aggregate function.
- Checking on the monotonicity for arbitrary recursive aggregate programs is still sophisticated.

#### **Existing Works on Monotonic Conditions**

Ross and Sagiv [PODS'92], SociaLite [ICDE'13] and Myria [VLDB'15] formalize the conditions for using monotonic aggregate in recursive query.

```
Existing works Maiter [TPDS'14], GRAPE[SIGMOD'17]
Idemonstrate that some non-monotonic algorithm
I can also be incrementally executed by using a similar approach to semi-naïve evaluation.

1. PageRank
2. SimRank
3. Belief Propagation
```

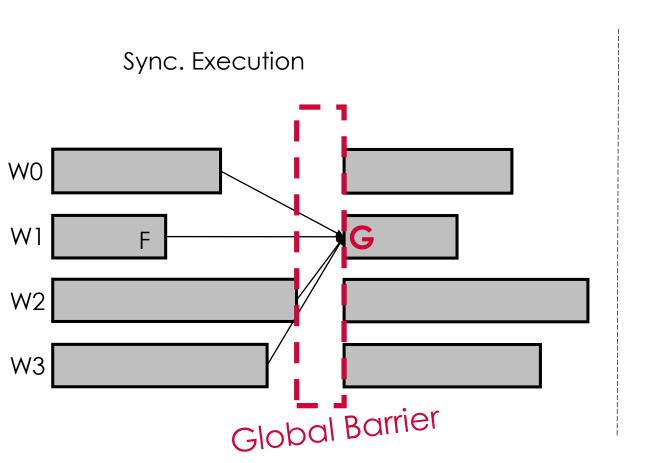
The application scope of existing conditions is narrow.

#### Two Research Questions:

- Under what conditions can a Recursive Aggregate Program be evaluated with semi-naïve evaluation?
- How to automatically verify the conditions for evaluating a recursive aggregate program with semi-naïve evaluation?

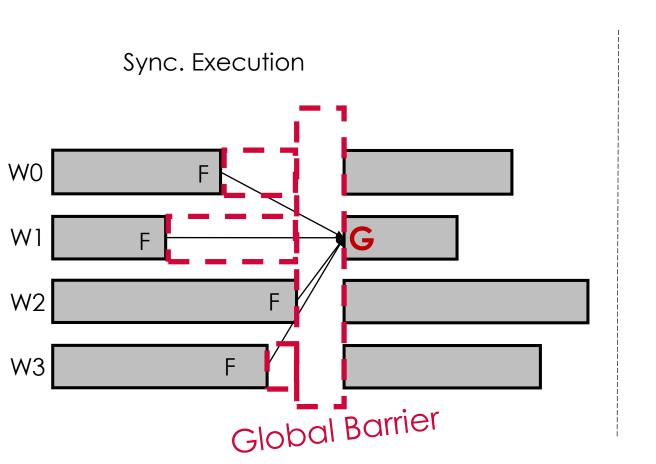
### Async. Execution

The aggregate operations require communications among workers. The global barrier of sync execution can guarantee the correctness.



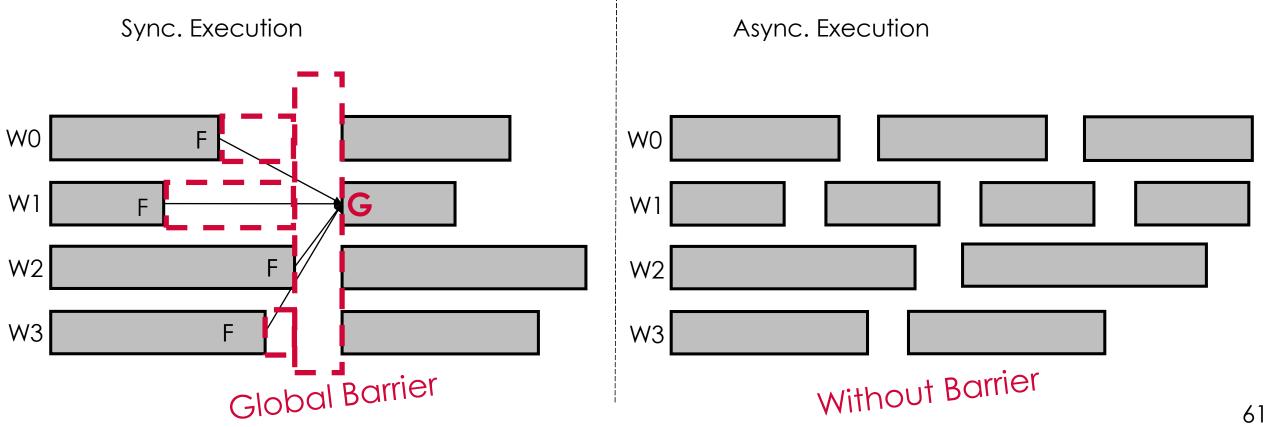
### Async. Execution

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## Async. Execution

Recently, The asynchronous parallel processing in distributed environment have emerged in the past few years, e.g., Maiter[TPDS'14], Giraph++[VLDB'15] and Myria [VLDB'15].



#### Conditions for Async. Execution

- Maiter [TPDS'14] and Grape+ [SIGMOD'18] propose the correctness conditions for graph algorithms with asynchronous execution.
- The conditions are not general enough for recursive aggregate programs.

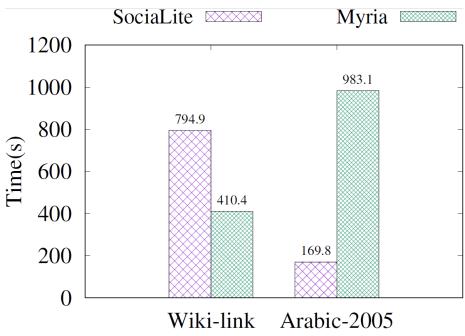
#### Two more Research Questions:

- Under what conditions can a recursive aggregate programs be asynchronously executed?
- How to automatically verify the conditions for executing a recursive aggregate program with async model?

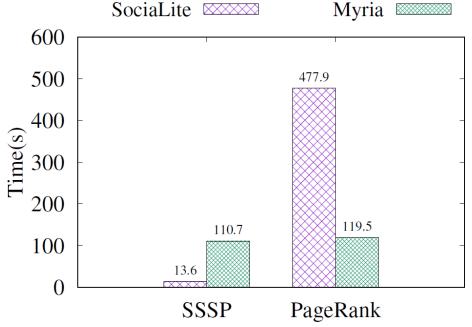
### Neither Sync nor Async Execution is Perfect

Neither Sync nor async execution can outperform each other because

- (1) sync processing may be over-controlled (too much idle time)
- (2) async processing may be under-controlled (stale computation)



The Same algorithm on different Datasets

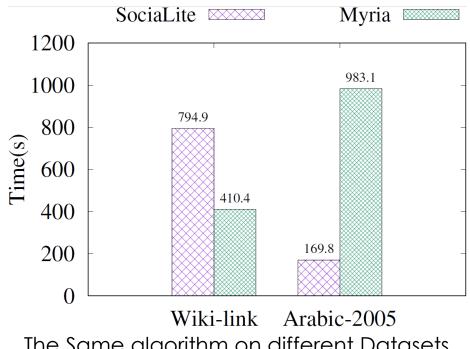


The Same dataset on different Algorithms

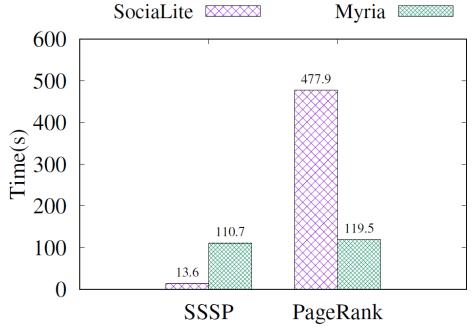
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The Same algorithm on different Datasets



The Same dataset on different Algorithms

We develop a unified sync-async engine to realize properly controlled processing.

#### **Our Work**

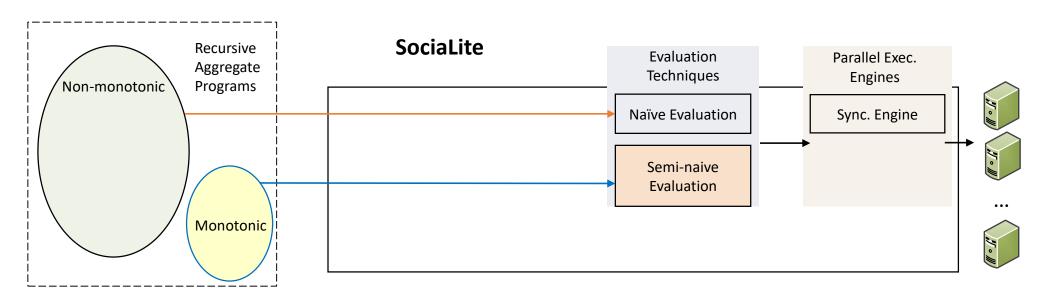
We develop and implement **PowerLog**, a high-performance distributed Datalog system based on **Socialite** [ICDE'13].

#### **Our Work**

We develop and implement **PowerLog**, a high-performance distributed Datalog system based on **SociaLite** [ICDE'13].

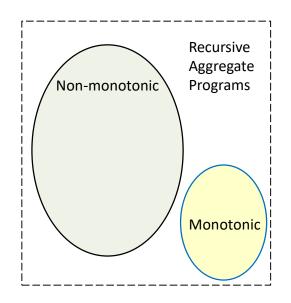
#### SociaLite

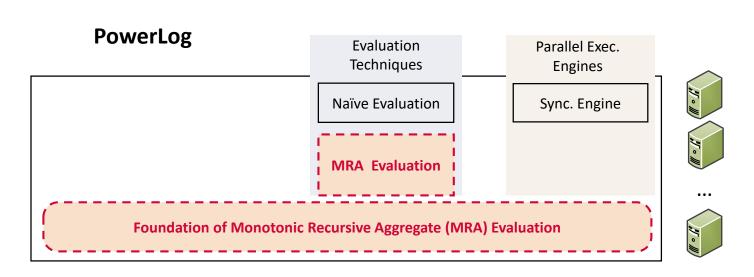
- (1) processes non-monotonic recursive aggregate programs with Naïve Evaluation
- (2) processes monotonic recursive aggregate programs with Semi-naïve Evaluation
- (3) executes both evaluation methods with a synchronous engine



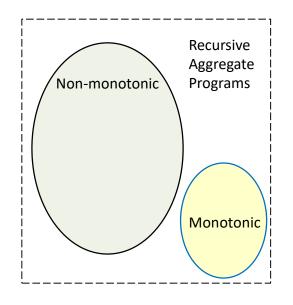
We propose Monotonic Recursive Aggregate evaluation (MRA Evaluation), a variant of Semi-naive Evaluation to answer.

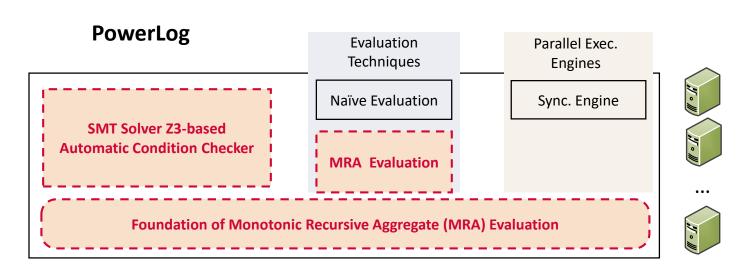
- (1) under what conditions a recursive aggregate program can be executed with Semi-naïve Evaluation (incrementally)
- (2) under what conditions a recursive aggregate program can be executed asynchronously





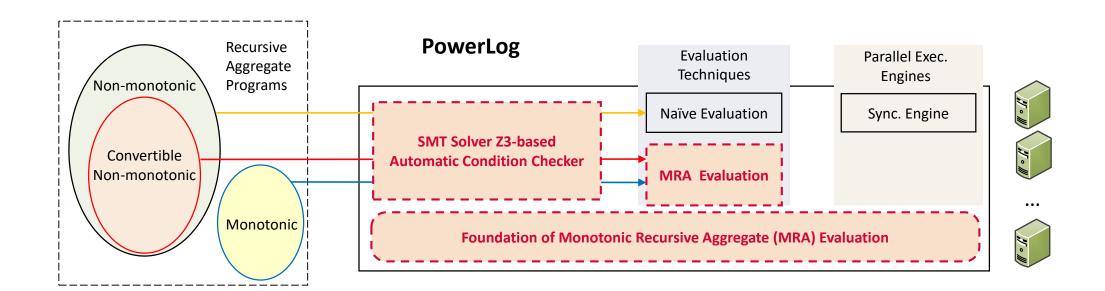
We design and implement a Z3-based condition checker to automatically check if a recursive aggregate program can satisfy the MRA conditions.



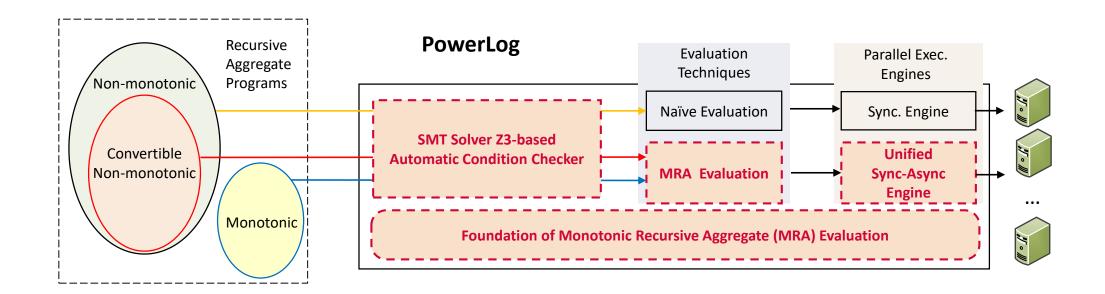


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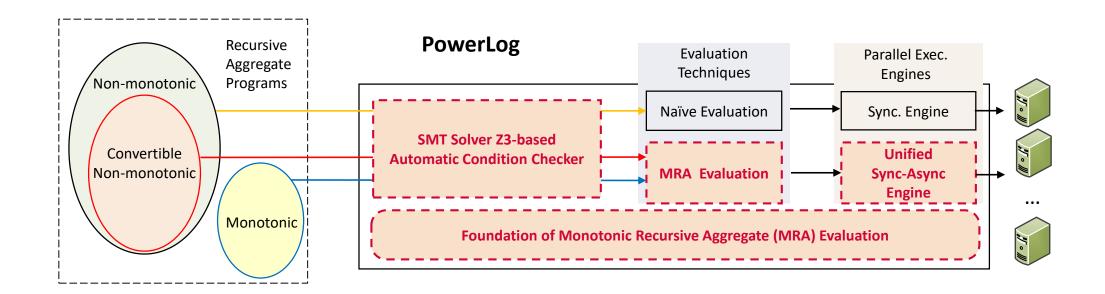
- (1) monotonic programs will be executed with MRA Evaluation
- (2) convertible non-monotonic programs that pass the condition check, e.g., PageRank, will be executed with MRA Evaluation
- (3) others that cannot pass the condition check will be executed with Naïve Evaluation



We design and implement a unified sync-async engine to execute the programs with MRA Evaluation for high performance.



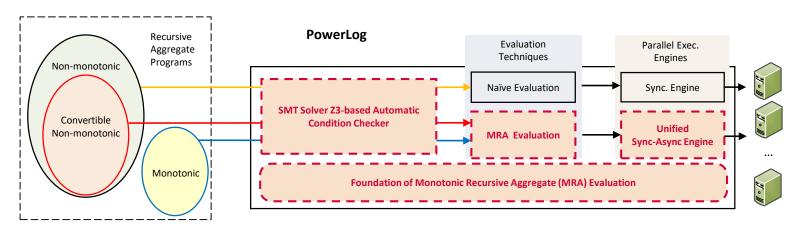
Putting all these together, we develop **PowerLog** (MRA Evaluation + a Z3-based condition checker + a unified sync-async engine).



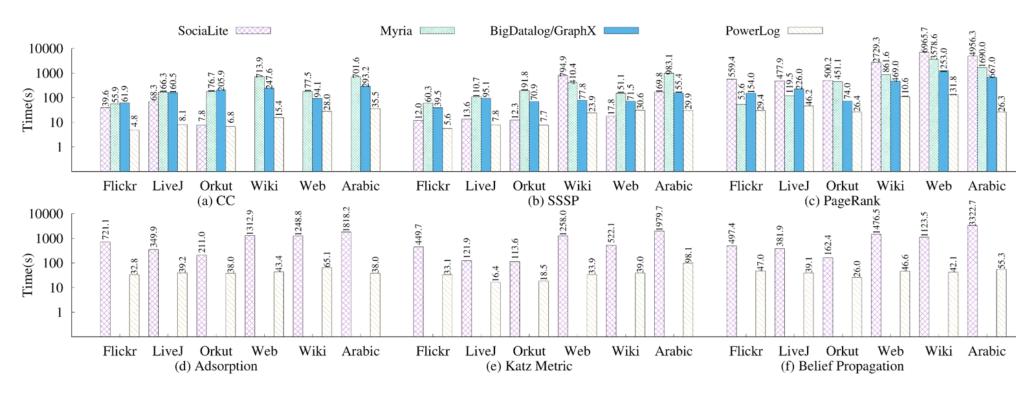
# **Workload Summary**

By using PowerLog, we have checked 14 recursive aggregate programs. 12 of them can be executed incrementally and asynchronously but 2 cannot.

Program	MRA sat.	Aggregator	Program	MRA sat.	Aggregator
SSSP [24]	yes	min	PageRank [39]	yes	sum
CC [24]	yes	min	Adsorption [7]	yes	sum
Katz metric [21]	yes	sum	Belief Propagation [40]	yes	sum
Computing Paths in DAG [50]	yes	count	Cost [50]	yes	sum
Viterbi Algorithm [50]	yes	max	SimRank [20]	yes	sum
Lowest Common Ancestor [44]	yes	min	APSP [50]	yes	min
CommNet [52]	no	sum	GCN-Forward [22]	no	sum



# Performance Summary



Compared with three representative Datalog systems (SociaLite, Myria, BigDatalog), PowerLog can achieve 1.1x – 188.3x speedups on 6 programs and several real datasets.

# Summary

The development of PowerLog involves both theory and system development.

#### Scope enhancement

We lay an analytical foundation to determine the conditions for monotonic and non-monotonic programs for correct execution.

#### Automatic condition verification

We develop a machine tool to eliminate tedious and error-prone efforts.

### A fast execution engine

We implement an highly optimized unified sync-async system.

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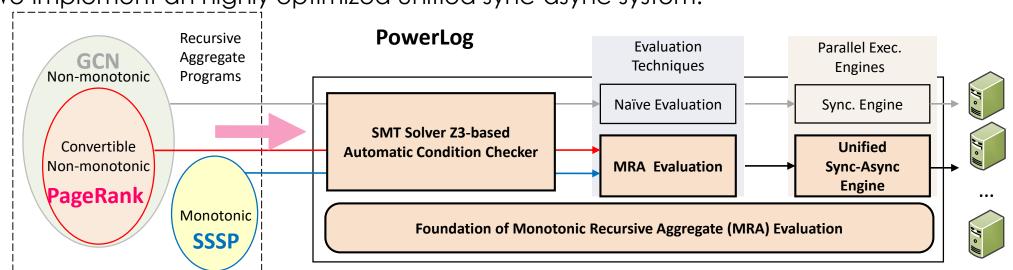
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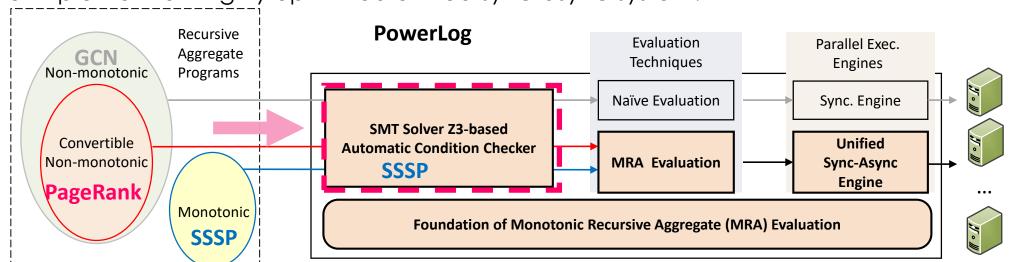
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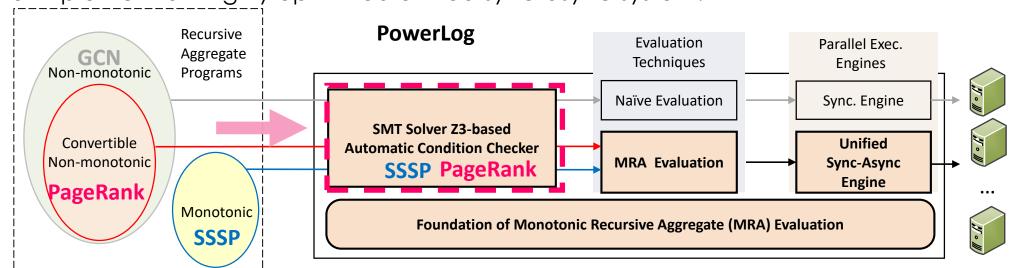
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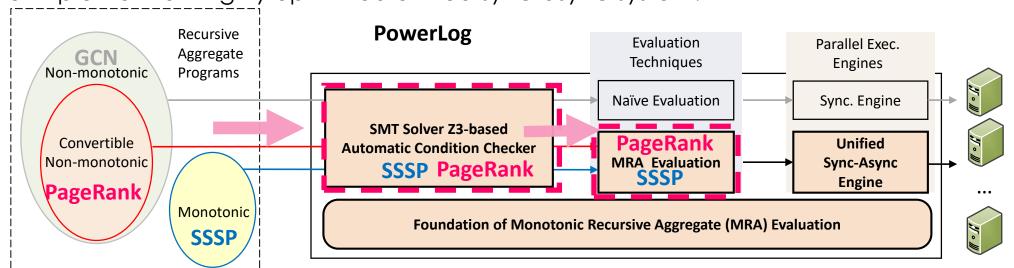
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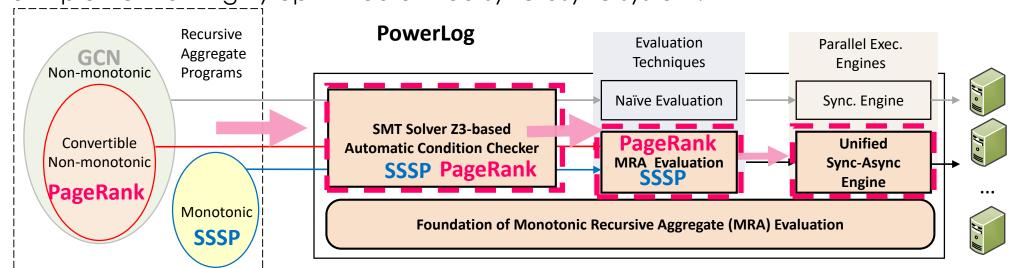
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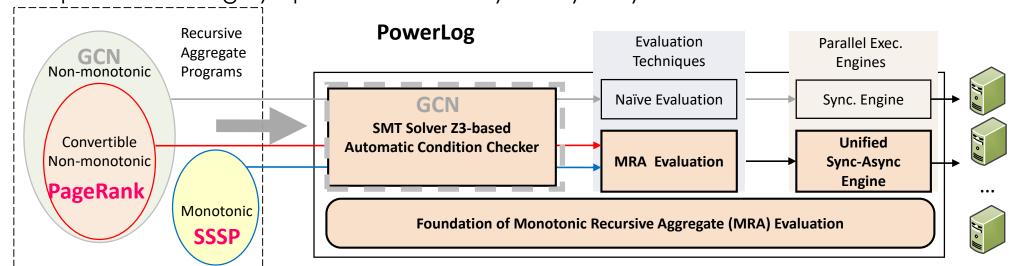
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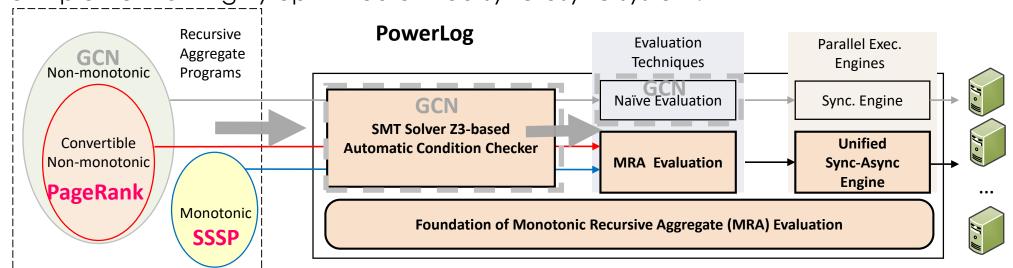
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