Lecture 4-1

Tuples

Week 4 Monday

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Adapted from Chapter 12 of Think Python by Allen B Downey

Additional content on Dictionaries adapted from "Whirlwind Tour of Python" by Jake VanderPlas

Tuples are like lists in that they can contain objects of different types. Tuples are ordered and preserve their order.

Tuples are different from lists in that they are **immutable**. You cannot append to a tuple or modify values in a tuple.

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```
In [1]: t = 0, 'apple', 2, 'cat', 'dog', 5, 6 # parentheses are not required to create a tuple
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```
In [1]:    t = 0, 'apple', 2, 'cat', 'dog', 5, 6 # parentheses are not required to create a tuple
In [2]:    t
Out[2]:    (0, 'apple', 2, 'cat', 'dog', 5, 6)
```

Tuples are like lists in that they can contain objects of different types. Tuples are ordered and preserve their order.

Tuples are different from lists in that they are **immutable**. You cannot append to a tuple or modify values in a tuple.

```
In [1]: t = 0, 'apple', 2, 'cat', 'dog', 5, 6 # parentheses are not required to create a tuple
In [2]: t
Out[2]: (0, 'apple', 2, 'cat', 'dog', 5, 6)
In [3]: t = (0, 'apple', 2, 'cat', 'dog', 5, 6) # you can use parentheses
```

Tuples are like lists in that they can contain objects of different types. Tuples are ordered and preserve their order.

Tuples are different from lists in that they are **immutable**. You cannot append to a tuple or modify values in a tuple.

```
In [1]:    t = 0, 'apple', 2, 'cat', 'dog', 5, 6 # parentheses are not required to create a tuple
In [2]:    t
Out[2]:    (0, 'apple', 2, 'cat', 'dog', 5, 6)
In [3]:    t = (0, 'apple', 2, 'cat', 'dog', 5, 6) # you can use parentheses
In [4]:    t
Out[4]:    (0, 'apple', 2, 'cat', 'dog', 5, 6)
```

```
In [5]: t1 = "a",
```

```
In [5]: t1 = "a",
In [6]: t1
Out[6]: ('a',)
```

```
In [5]: t1 = "a",
In [6]: t1
Out[6]: ('a',)
In [7]: type(t1)
Out[7]: tuple
```

```
In [5]:
         t1 = "a",
In [6]:
          ('a',)
Out[6]:
In [7]:
          type(t1)
          tuple
Out[7]:
In [8]:
          len(t1)
Out[8]:
```

```
In [9]: t2 = ("a")
```

```
In [9]: t2 = ("a")
In [10]: type(t2)
Out[10]: str
```

```
In [9]: t2 = ("a")
In [10]: type(t2)
Out[10]: str
In [11]: t2 = ("a",)
```

```
In [9]: t2 = ("a")
In [10]: type(t2)
Out[10]: str
In [11]: t2 = ("a",)
In [12]: type(t2)
Out[12]: tuple
```

You can create an empty tuple with the tuple() function, similar to using the list() or dict() function

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```
In [13]: t3 = tuple()
```

You can create an empty tuple with the tuple() function, similar to using the list() or dict() function

```
In [13]: t3 = tuple()
In [14]: t3
Out[14]: ()
```

```
In [15]: tuple("hello")
Out[15]: ('h', 'e', 'l', 'l', 'o')
```

```
In [15]: tuple("hello")
Out[15]: ('h', 'e', 'l', 'l', 'o')
In [16]: tuple(range(5))
Out[16]: (0, 1, 2, 3, 4)
```

```
In [15]: tuple("hello")
Out[15]: ('h', 'e', 'l', 'l', 'o')
In [16]: tuple(range(5))
Out[16]: (0, 1, 2, 3, 4)
In [17]: tuple([1,4,7])
Out[17]: (1, 4, 7)
```

```
In [18]:
    t = 0, 'apple', 2, 'cat', 'dog', 5, 6
```

```
In [18]: t = 0, 'apple', 2, 'cat', 'dog', 5, 6
In [19]: t[1]
Out[19]: 'apple'
```

```
In [18]:    t = 0, 'apple', 2, 'cat', 'dog', 5, 6
In [19]:    t[1]
Out[19]:    'apple'
In [20]:    t[2:5] # slicing
Out[20]:    (2, 'cat', 'dog')
```

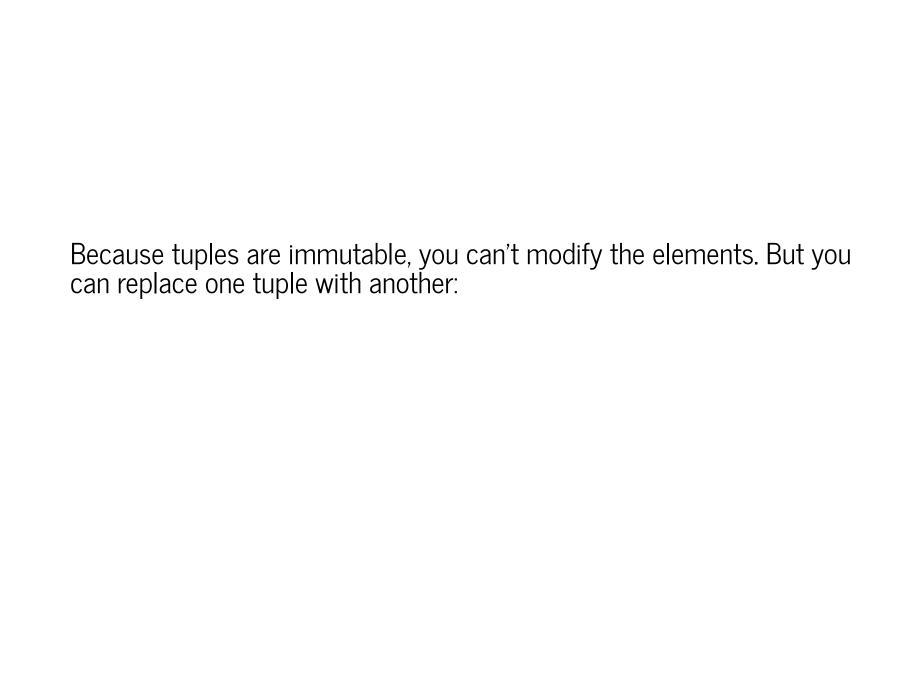
```
In [21]:
    t = (0,'apple',2,'cat','dog',5,6) # tuple
    l = [0,'apple',2,'cat','dog',5,6] # list
```

```
In [21]:
          t = (0, 'apple', 2, 'cat', 'dog', 5, 6) # tuple
           1 = [0,'apple',2,'cat','dog',5,6] # List
In [22]:
           1[0] = 100 # we can change the value of the object at index 0
           print(1)
           [100, 'apple', 2, 'cat', 'dog', 5, 6]
In [23]:
           t[0] = 100 # trying to modify the value in a tuple is not allowed
           TypeError
                                                        Traceback (most recent call last)
           ~\AppData\Local\Temp/ipykernel 19144/3323244693.py in <module>
           ----> 1 t[0] = 100 # trying to modify the value in a tuple is not allowed
           TypeError: 'tuple' object does not support item assignment
```

methods that modify lists in place (e.g. append, insert, pop, etc) do not work for tuples

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Because tuples are immutable, you can't modify the elements. But you can replace one tuple with another:

```
In [26]: t = ("A",) + t[1:]
t
Out[26]: ('A', 'apple', 2, 'cat', 'dog', 5, 6)
```

This creates an entirely new tuple, unrelated to the other one.

```
In [27]: (0, 1, 2) < (0, 3, 4)
Out[27]: True</pre>
```

```
In [27]: (0, 1, 2) < (0, 3, 4)
Out[27]: True
In [28]: (0, 1, 2000000) < (0, 3, 4)
Out[28]: True</pre>
```

```
In [27]:
            (0, 1, 2) < (0, 3, 4)
            True
Out[27]:
In [28]:
            (0, 1, 2000000) < (0, 3, 4)
            True
Out[28]:
In [29]:
            (0, 500, 2) < (0, 3, 4)
            False
Out[29]:
In [30]:
            # abbbb
            # abc
            # abcd
            tuple("abc") <= tuple("abcd")</pre>
            True
Out[30]:
```

Tuple assignment

A common and useful tuple idiom: You can switch value assignments via tuples

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```
In [31]: # old option without tuples
a = 5
b = 1

temp = a
a = b
b = temp
print(a, b)
```

1 5

Tuple assignment

A common and useful tuple idiom: You can switch value assignments via tuples

```
In [31]:
            # old option without tuples
            a = 5
            b = 1
            temp = a
            a = b
            b = temp
            print(a, b)
            1 5
In [32]:
            # faster way with tuples
            a = 5
            b = 1
            b, a = a, b
            print(a, b)
```

```
In [33]: addr = "mileschen@stat.ucla.edu"
  addr.split("@") # string.split() normally returns two elements in a list

Out[33]: ['mileschen', 'stat.ucla.edu']
```

```
In [33]: addr = "mileschen@stat.ucla.edu"
    addr.split("@") # string.split() normally returns two elements in a list

Out[33]: ['mileschen', 'stat.ucla.edu']

In [34]: addr = "mileschen@stat.ucla.edu"
    uname, domain = addr.split("@") # we can assign the results of str.split() to a tuple
```

```
In [33]: addr = "mileschen@stat.ucla.edu"
   addr.split("@") # string.split() normally returns two elements in a list

Out[33]: ['mileschen', 'stat.ucla.edu']

In [34]: addr = "mileschen@stat.ucla.edu"
   uname, domain = addr.split("@") # we can assign the results of str.split() to a tuple

In [35]: uname

Out[35]: 'mileschen'
```

```
In [33]:
            addr = "mileschen@stat.ucla.edu"
            addr.split("@") # string.split() normally returns two elements in a list
            ['mileschen', 'stat.ucla.edu']
Out[33]:
In [34]:
            addr = "mileschen@stat.ucla.edu"
            uname, domain = addr.split("@") # we can assign the results of str.split() to a tuple
In [35]:
            uname
            'mileschen'
Out[35]:
In [36]:
            domain
            'stat.ucla.edu'
Out[36]:
```

We saw this when we talked about functions. You can have functions return multiple values in the form of a tuple

```
def my_divide(x, y):
    integer = x // y
    remainder = x % y
    return integer, remainder
```

```
In [37]:
    def my_divide(x, y):
        integer = x // y
        remainder = x % y
        return integer, remainder

In [38]:
    a, b = my_divide(23, 5)
```

```
In [37]: def my_divide(x, y):
    integer = x // y
    remainder = x % y
    return integer, remainder

In [38]: a, b = my_divide(23, 5)

In [39]: a, b

Out[39]: (4, 3)
```

```
In [37]:
            def my_divide(x, y):
                integer = x // y
                remainder = x \% y
                return integer, remainder
In [38]:
            a, b = my_divide(23, 5)
In [39]:
            a, b
            (4, 3)
Out[39]:
In [40]:
            divmod(23, 5) # divmod() is a built-in function that does exactly this.
            (4, 3)
Out[40]:
```

tuples only support two methods: tuple.index() and tuple.count() which return
information about contents of the tuple but do not modify them

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information about contents of the tuple but do not modify them

```
In [41]: t = 0, 'apple', 2, 'cat', 'dog', 5, 6
```

tuples only support two methods: tuple.index() and tuple.count() which return information about contents of the tuple but do not modify them

```
In [41]:    t = 0, 'apple', 2, 'cat', 'dog', 5, 6
In [42]:    t.index('dog')
Out[42]: 4
```

tuples only support two methods: tuple.index() and tuple.count() which return information about contents of the tuple but do not modify them

```
In [41]:    t = 0, 'apple', 2, 'cat', 'dog', 5, 6
In [42]:    t.index('dog')
Out[42]:    4
In [43]:    t.count(5)
Out[43]: 1
```

Functions that support tuples and other iterables as inputs

Even though tuples only have two methods, there are several functions that support tuples (and other iterables like lists, dicts, strings) as inputs

- len()
- sum()
- sorted()
- min()
- max()

None of these functions affect the list or tuple itself.

```
In [44]:
some_digits = (4,2,7,9,2,5,3) # a tuple of numbers
some_words = ['dog','apple','cat','hat','hand'] # this is a list
```

```
In [44]: some_digits = (4,2,7,9,2,5,3) # a tuple of numbers
    some_words = ['dog','apple','cat','hat','hand'] # this is a list

In [45]: len(some_digits)

Out[45]: 7
```

```
In [44]:
            some_digits = (4,2,7,9,2,5,3) # a tuple of numbers
            some_words = ['dog','apple','cat','hat','hand'] # this is a list
In [45]:
           len(some_digits)
Out[45]:
In [46]:
            sum(some_digits)
            32
```

Out[46]:

```
In [44]:
           some digits = (4,2,7,9,2,5,3) # a tuple of numbers
           some words = ['dog','apple','cat','hat','hand'] # this is a list
In [45]:
           len(some_digits)
Out[45]:
In [46]:
           sum(some_digits)
           32
Out[46]:
In [47]:
           sum(some words) # won't work on strings
           TypeError
                                                        Traceback (most recent call last)
           ~\AppData\Local\Temp/ipykernel_19144/3741811082.py in <module>
           ---> 1 sum(some words) # won't work on strings
           TypeError: unsupported operand type(s) for +: 'int' and 'str'
```

In [48]: sorted(some_digits) # sorts the tuple, but does not affect the list or tuple itself. # contrast to list.sort() which will sort the list in place # but the object returned is a list

Out[48]: [2, 2, 3, 4, 5, 7, 9]

```
In [48]: sorted(some_digits) # sorts the tuple, but does not affect the list or tuple itself.
# contrast to list.sort() which will sort the list in place
# but the object returned is a list

Out[48]: [2, 2, 3, 4, 5, 7, 9]

In [49]: print(some_digits) # just to show the list is unchanged

(4, 2, 7, 9, 2, 5, 3)
```

```
In [48]:
            sorted(some digits) # sorts the tuple, but does not affect the list or tuple itself.
            # contrast to list.sort() which will sort the list in place
            # but the object returned is a list
           [2, 2, 3, 4, 5, 7, 9]
Out[48]:
In [49]:
            print(some digits) # just to show the list is unchanged
            (4, 2, 7, 9, 2, 5, 3)
In [50]:
            sorted(some_words) # when applied to a list of strings, it will alphabetize them
            ['apple', 'cat', 'dog', 'hand', 'hat']
Out[50]:
In [51]:
            min(some_digits)
            2
Out[51]:
```

```
In [48]:
            sorted(some digits) # sorts the tuple, but does not affect the list or tuple itself.
            # contrast to list.sort() which will sort the list in place
            # but the object returned is a list
           [2, 2, 3, 4, 5, 7, 9]
Out[48]:
In [49]:
            print(some digits) # just to show the list is unchanged
            (4, 2, 7, 9, 2, 5, 3)
In [50]:
            sorted(some words) # when applied to a list of strings, it will alphabetize them
            ['apple', 'cat', 'dog', 'hand', 'hat']
Out[50]:
In [51]:
            min(some digits)
Out[51]:
In [52]:
            max(some words) # max returns the last word if alphabetized,
            # min will return the first in an alphabetized list
            'hat'
Out[52]:
```

```
In [53]:
    dict_num = {1: "a", 2: "b", 3: "c"}
    dict_alpha = {"a":1, "b":2, "c":3}
```

```
In [53]: dict_num = {1: "a", 2: "b", 3: "c"}
dict_alpha = {"a":1, "b":2, "c":3}

In [54]: len(dict_num) # number of items in the dictionary

Out[54]: 3
```

```
In [53]: dict_num = {1: "a", 2: "b", 3: "c"}
dict_alpha = {"a":1, "b":2, "c":3}

In [54]: len(dict_num) # number of items in the dictionary

Out[54]: 3

In [55]: sorted(dict_num) # a list of the keys sorted
```

Out[55]: [1, 2, 3]

```
In [53]:
            dict_num = {1: "a", 2: "b", 3: "c"}
            dict alpha = {"a":1, "b":2, "c":3}
In [54]:
            len(dict num) # number of items in the dictionary
Out[54]:
In [55]:
            sorted(dict_num) # a list of the keys sorted
           [1, 2, 3]
Out[55]:
In [56]:
            sorted(dict_alpha)
Out[56]: ['a', 'b', 'c']
```

```
In [53]:
            dict_num = {1: "a", 2: "b", 3: "c"}
            dict_alpha = {"a":1, "b":2, "c":3}
In [54]:
            len(dict_num) # number of items in the dictionary
Out[54]:
In [55]:
            sorted(dict_num) # a list of the keys sorted
           [1, 2, 3]
Out[55]:
In [56]:
            sorted(dict_alpha)
           ['a', 'b', 'c']
Out[56]:
In [57]:
            max(dict_num) # the "maximum" key
Out[57]:
```

multiplication generally duplicates

addition generally appends

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```
In [58]:
L1 = ['a','b','c']
L2 = ['d','e','f']
```

multiplication generally duplicates

addition generally appends

```
In [58]: L1 = ['a','b','c']
L2 = ['d','e','f']

In [59]: L1 * 2 # multiplication extends duplicates

Out[59]: ['a', 'b', 'c', 'a', 'b', 'c']
```

multiplication generally duplicates

addition generally appends

```
In [58]: L1 = ['a','b','c']
L2 = ['d','e','f']

In [59]: L1 * 2 # multiplication extends duplicates

Out[59]: ['a', 'b', 'c', 'a', 'b', 'c']

In [60]: L1 + L2 # addition appends list objects

Out[60]: ['a', 'b', 'c', 'd', 'e', 'f']
```

```
In [61]:

T1 = ('a','b','c')

T2 = ('d','e','f')
```

['a', 'b', 'c', 'd', 'e', 'f']

Out[65]:

Functions can take a variable number of arguments. A parameter name that begins with * gathers arguments into a tuple.

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```
In [66]:
           def printall(args):
              print(args)
In [67]:
           printall(1, 3.0, 5, "hi")
           TypeError
                                                       Traceback (most recent call last)
           ~\AppData\Local\Temp/ipykernel 19144/1583317326.py in <module>
           ----> 1 printall(1, 3.0, 5, "hi")
           TypeError: printall() takes 1 positional argument but 4 were given
In [68]:
           def printall(*args):
              print(args)
```

Functions can take a variable number of arguments. A parameter name that begins with * gathers arguments into a tuple.

```
In [66]:
           def printall(args):
               print(args)
In [67]:
           printall(1, 3.0, 5, "hi")
           TypeError
                                                        Traceback (most recent call last)
           ~\AppData\Local\Temp/ipykernel 19144/1583317326.py in <module>
           ----> 1 printall(1, 3.0, 5, "hi")
           TypeError: printall() takes 1 positional argument but 4 were given
In [68]:
           def printall(*args):
               print(args)
In [69]:
           printall(1, 3.0, 5, "hi")
           (1, 3.0, 5, 'hi')
```

```
In [70]:
    def print_lines(*args):
        for element in args:
            print(element)
```

```
In [70]:    def print_lines(*args):
        for element in args:
            print(element)
In [71]:    print_lines("hi", "goodbye")

hi
goodbye
```

```
In [70]:
            def print_lines(*args):
                for element in args:
                    print(element)
In [71]:
            print_lines("hi", "goodbye")
            hi
            goodbye
In [72]:
            print_lines(1, 5, 7, 9, 10)
            1
            5
7
            9
            10
```

```
In [73]:
    def my_divide(x, y):
        integer = x // y
        remainder = x % y
        return integer, remainder
```

```
In [73]:
    def my_divide(x, y):
        integer = x // y
        remainder = x % y
        return integer, remainder

In [74]:    t = (23, 5)
```

```
In [73]:
           def my_divide(x, y):
               integer = x // y
               remainder = x \% y
               return integer, remainder
In [74]:
          t = (23, 5)
In [75]:
           my divide(t)
           TypeError
                                                        Traceback (most recent call last)
           ~\AppData\Local\Temp/ipykernel 19144/1954193532.py in <module>
           ----> 1 my divide(t)
           TypeError: my divide() missing 1 required positional argument: 'y'
```

```
In [73]:
           def my divide(x, y):
               integer = x // y
               remainder = x \% y
               return integer, remainder
In [74]:
          t = (23, 5)
In [75]:
           my divide(t)
           TypeError
                                                        Traceback (most recent call last)
           ~\AppData\Local\Temp/ipykernel 19144/1954193532.py in <module>
           ----> 1 my divide(t)
           TypeError: my divide() missing 1 required positional argument: 'y'
In [76]:
           my divide(*t)
          (4, 3)
Out[76]:
```

Zipping Lists, Tuples and other iterables

zip() is a built-in function that takes two or more sequences and interleaves them. The name of the function refers to a zipper, which interleaves two rows of teeth.

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zip() is a built-in function that takes two or more sequences and interleaves them. The name of the function refers to a zipper, which interleaves two rows of teeth.

```
In [77]: s = 'abc'
t = 0, 1, 2
zip(s, t)

Out[77]: <zip at 0x1d48eb99708>
```

Zipping Lists, Tuples and other iterables

zip() is a built-in function that takes two or more sequences and interleaves them. The name of the function refers to a zipper, which interleaves two rows of teeth.

A zip object is a kind of iterator, which is any object that iterates through a sequence. Iterators are similar to lists in some ways, but unlike lists, you can't use an index to select an element from an iterator.

It will return a list of tuples

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```
In [79]: list(zip(s,t))
Out[79]: [('a', 0), ('b', 1), ('c', 2)]
```

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```
In [79]: list(zip(s,t))
```

Out[79]: [('a', 0), ('b', 1), ('c', 2)]

If the sequences are not the same length, the result has the length of the shorter one.

It will return a list of tuples

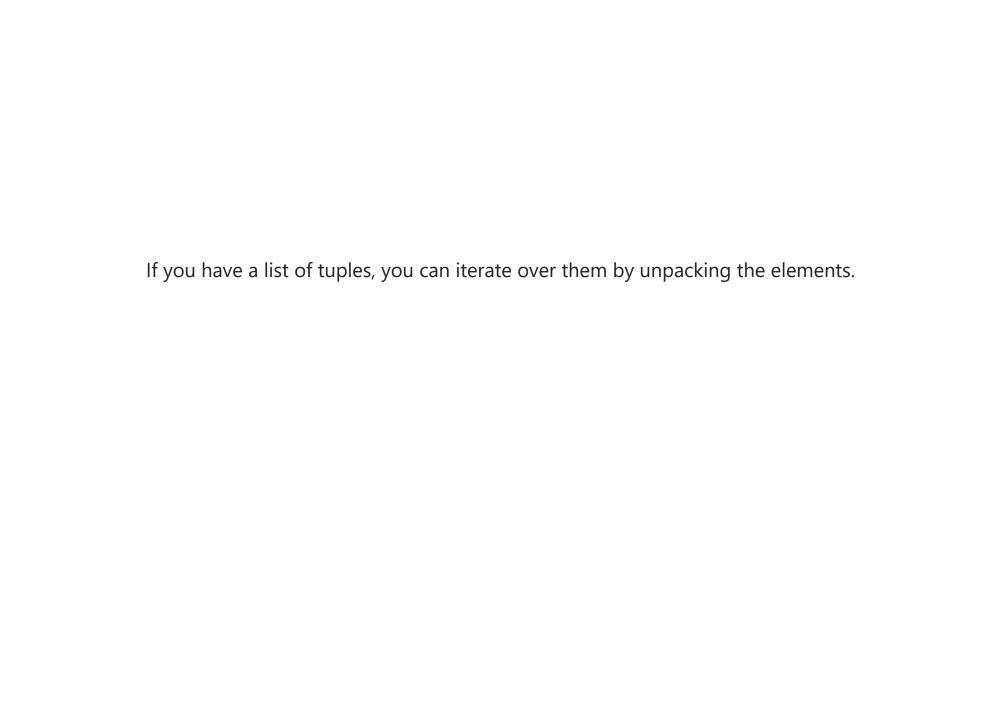
```
In [79]: list(zip(s,t))
```

Out[79]: [('a', 0), ('b', 1), ('c', 2)]

If the sequences are not the same length, the result has the length of the shorter one.

```
In [80]:
list(zip("Anne" , "Elk" ))
```

Out[80]: [('A', 'E'), ('n', 'l'), ('n', 'k')]



If you have a list of tuples, you can iterate over them by unpacking the elements.

```
In [81]:
    t = [('a', 0), ('b', 1), ('c', 2)]
    for letter, number in t:
        print(number, letter)

    0 a
    1 b
    2 c
```

Zipping multiple iterables

You can zip more than two iterables together. Zip will create tuples with all of the items interwoven.

```
In [84]:
    def has_match(t1, t2):
        for x, y in zip(t1, t2):
            if x == y:
                return True
        return False
```

```
In [84]:
            def has match(t1, t2):
                for x, y in zip(t1, t2):
                    if x == y:
                        return True
                return False
In [85]:
            has_match(('a', 'b', 'c'), ('d', 'e', 'f'))
            False
Out[85]:
In [86]:
            has_match(('a', 'b', 'c'), ('d', 'e', 'c'))
            True
Out[86]:
In [87]:
            has_match(('a', 'b', 'c', 'd'), ('d', 'c', 'b', 'a'))
            False
Out[87]:
```

enumerate()

The built-in function enumerate is useful. It takes an iterable and returns an iterator of the index paired with the elements You can think of enumerate() as zipping a range object of the same length with the iterable.

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```
In [88]: enumerate("morning")
Out[88]: <enumerate at 0x1d48eb67a98>
```

enumerate()

The built-in function enumerate is useful. It takes an iterable and returns an iterator of the index paired with the elements You can think of enumerate() as zipping a range object of the same length with the iterable.

```
In [90]: list(enumerate(['a','b','c','d']))
Out[90]: [(0, 'a'), (1, 'b'), (2, 'c'), (3, 'd')]
```

```
In [90]: list(enumerate(['a','b','c','d']))
Out[90]: [(0, 'a'), (1, 'b'), (2, 'c'), (3, 'd')]
In [91]: list(zip(range(4),['a','b','c','d'])) # zipping a range object with a list
Out[91]: [(0, 'a'), (1, 'b'), (2, 'c'), (3, 'd')]
```

```
In [92]: d = {'a':0, 'b':1, 'c':2}
```

```
In [92]: d = {'a':0, 'b':1, 'c':2}
In [93]: d.items()
Out[93]: dict_items([('a', 0), ('b', 1), ('c', 2)])
```

```
In [95]: d = dict(enumerate("efg"))
```

```
In [95]: d = dict(enumerate("efg"))
In [96]: d
Out[96]: {0: 'e', 1: 'f', 2: 'g'}
```

```
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```

Swap the keys and elements in a dictionary

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In [95]: d = dict(enumerate("efg"))
In [96]: d
Out[96]: {0: 'e', 1: 'f', 2: 'g'}
```

Swap the keys and elements in a dictionary

```
In [97]:
    swapped = {}
    for key, value in d.items():
        swapped[value] = key
```

```
In [95]:
           d = dict(enumerate("efg"))
In [96]:
           {0: 'e', 1: 'f', 2: 'g'}
Out[96]:
         Swap the keys and elements in a dictionary
In [97]:
           swapped = {}
           for key, value in d.items():
               swapped[value] = key
In [98]:
           swapped
           {'e': 0, 'f': 1, 'g': 2}
Out[98]:
In [99]:
           dict(zip("efg", range(3)))
          {'e': 0, 'f': 1, 'g': 2}
Out[99]:
```

We can create dictionaries out of sequences of tuples and with zip objects

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Tuples as dictionary keys

Because tuples are immutable, they can be used as keys in a dictionary

For example, there might be a 2D function that is very expensive to compute for coordinates. You can create a dictionary that will store all of the values that have been calculated for each 2D pair.

Let's say you have a function: $f(x,y) = x^2 + 2y$

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Let's say you have a function: $f(x,y) = x^2 + 2y$

```
In [102]: # this dictionary contains values that are known solutions
known = {(0, 0): 0}
```

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Let's say you have a function: $f(x,y)=x^2+2y$

```
In [102]: # this dictionary contains values that are known solutions
known = {(0, 0): 0}

In [103]: 
    def f(x, y):
        t = (x,y)
        if t in known:
            print("value already exists dictionary")
            return known[t]
            print("value must be calculated")
        res = x ** 2 + 2 * y
        known[t] = res
        return res
```

In [104]: f(0, 0)

value already exists dictionary

Out[104]: 0

```
In [104]: f(0, 0)

value already exists dictionary

Out[104]: 0

In [105]: f(1, 2)

value must be calculated

Out[105]: 5
```

```
In [104]:
            f(0, 0)
            value already exists dictionary
            0
Out[104]:
In [105]:
            f(1, 2)
            value must be calculated
Out[105]:
In [106]:
           f(1, 2)
            value already exists dictionary
Out[106]:
```

```
In [104]:
            f(0, 0)
            value already exists dictionary
Out[104]:
In [105]:
            f(1, 2)
            value must be calculated
Out[105]:
In [106]:
           f(1, 2)
            value already exists dictionary
Out[106]:
In [107]:
            known
           \{(0, 0): 0, (1, 2): 5\}
Out[107]:
```