### **CSE 259 - Logic in Computer Science**

**Recitation-10** 

### **Project 3: Wang and Kobsa's Algorithm**

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### **Project 3**

- The partial implementation wangs\_algorithm.pl is runnable
- Sample input/output:
  - Premises as list ([p ^ q])
  - A formula as conclusion.
  - We can derive the conclusion from the premise

We can derive the conclusion from the premises. **true**.

### **Project 3**

- Write your codes here
- I have implemented some. The rest is your task

## **Project 3**

- Two types of rules
  - Non-branching
  - o Branching

### **Project 3: Non-branching Rules**

#### Rule-1

If one of the formulae separated by commas is the negation of a formula, drop the negation sign and move it to the other side of the arrow.

#### **Example:**

Formula:  $p, \sim (q \land r) \Rightarrow p \land r$ 

**Change to:** p => p ^ r, q ^ r

### **Project 3: Non-branching Rules**

#### Rule-2

If the last connective of a formula on the left is ^ (and), or on the right of the arrow is v (or), replace the connective by a comma.

Example-1:

Formula:  $p, p ^ q => r, s$ 

Change to:  $p, p, q \Rightarrow r, s$ 

**Example-2:** 

Formula:  $p, q \Rightarrow r \vee p$ 

Change to:  $p, q \Rightarrow r, p$ 

### **Project 3: Non-branching Rules**

#### Rule-3

If the last connective of a formula on the right is  $A \rightarrow B$ , remove  $A \rightarrow B$  from the right and then add A to the left and B to the right.

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#### Example-1:

Formula:  $p \vee q \Rightarrow q \rightarrow p$ 

Change to:  $p \vee q, q \Rightarrow p$ 

### **Project 3: Branching Rules**

#### Rule-4

If the last connective of a formula on the left is v (or), or on the right of the arrow is ^ (and), then produce two new lines, each with one of the two sub formulae replacing the formula. Both of these must be proved in order to prove the original theorem.

**Example-1:** 

Formula:  $p v q, r, s \Rightarrow q v p$ 

**Change to:** 

p, r, s => q v p

q, r, s => q v p

**Example-2:** 

Formula:  $p, r, s \Rightarrow q p$ 

Change to:

p, r, s => q

p, r, s => p

### **Project 3: Branching Rules**

#### Rule-5

If the last connective of a formula on the left is  $A \rightarrow B$ , remove  $A \rightarrow B$  from the left and then create two new lines, one with B added to the left, and the other with A added to the right.

#### **Example-1:**

Formula:  $p, p \rightarrow q \Rightarrow p \vee q$ 

#### **Change to:**

$$p, q => p v q$$

$$p => p v q, p$$

### **Project 3: Non-branching Rules – Rule 1**

```
* example rule: negation
 * non-branching rule
 * If one of the formulae separated by commas is the
 * negation of a formula, drop the negation sign and
 * move it to the other side of the arrow.
prove(L => R):-
   member(~X, L),
   del(~X, L, NewL),
   nl, write('=\t'), write(NewL => [X \mid R]),
   write('\t (by negation/left)'),
   prove(NewL => [X | R]).
prove(L => R):-
   member(~X, R),
   del(~X, R, NewR),
   nl, write('=\t'), write([X | L] => NewR),
   write('\t (by negation/right)'),
   prove([X | L] => NewR).
```

#### **Example:**

Formula:  $p, \sim (q \wedge r) \Rightarrow p \wedge r$ 

Change to:  $p \Rightarrow p r, q r$ 

#### **Output:**

### **Project 3: Non-branching Rules – Rule 2**

```
* Rule-2
* example rule: left conjuction
* non-branching rule
* If the last connective of a formula on the left is ^ (and),
st or on the right of the arrow is v (or), replace the connective by a comma.
prove(L => R) :-
 member(A ^ B, L),
 del(A ^ B, L, NewL),
 nl, write('=\t'), write([A, B | NewL] => R),
 write('\t (by and/left)'),
 prove([A, B | NewL] => R).
prove(L => R) :-
 member(A v B, R),
 del(A v B, R, NewR),
 nl, write('=\t'), write(L => [A, B | NewR]),
 write('\t (by or/right)'),
 prove(L \Rightarrow [A, B | NewR]).
```

# Project 3: Non-branching Rules – Rule 2 contd.

#### **Example-1:**

Formula:  $p, p ^ q => r, s$ 

Change to:  $p, p, q \Rightarrow r, s$ 

#### **Example-2:**

Formula:  $p, q \Rightarrow r \vee p$ 

Change to: p, q => r, p

### **Project 3: Branching Rules – Rule 5**

```
* example rule: left implication
* branching rule
* If the last connective of a formula on the left is A \rightarrow B,
* remove A \rightarrow B from the left and then create two new lines,
* one with B added to the left, and the other with A added to the right.
prove(L => R) :-
 member(A \rightarrow B, L),
 del(A \rightarrow B, L, NewL),
 nl,
 write('\tFirst branch: '),
 nl,
 write('=\t'),
 write([B | NewL] => R),
 write('\t (by arrow/left)'),
 prove([B | NewL] => R),
 write('\tSecond branch: '),
 nl.
 write('=\t'),
 write(NewL => [A | R]),
 write('\t (by arrow/left)'),
 prove(NewL => [A | R]).
```

### **Project 3: Your Tasks**

- Rule-3: Non-branching rule
- Rule-4: Branching rule