# 4-bit Arithmetic Logic Unit

Group-3

May 15, 2018

#### 1 Designing an ALU

 ${\bf Truth\ Table:\ Arithmetic\ Operations}$ 

$cs_2$	$cs_1$	$cs_0$	Arithmetic Operation	$x_i$	$y_i$
0	0	0	Transfer A	$A_i$	0
0	0	1	Increment A	$A_i$	0
0	1	0	Subtraction with Borrow	$A_i$	$\overline{B_i}$
0	1	1	Subtraction	$A_i$	$\overline{B_i}$

Subtract with borrow explanation:

$$= A - B - 1$$

$$= (A + \overline{B} + 1) - 1$$

$$=A+\overline{B}$$

So, 
$$Y = CS_1\overline{B_i}$$

### 2 Design of Arithmetic Logic Unit

Truth Table : Logical Operations

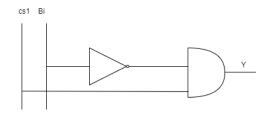


Figure 1:  $Y = CS_1\overline{B_i}$ 

$cs_2$	$cs_1$	$cs_0$	$x_i$	$y_i$	$f_i = X_i \oplus Y_i$	Operation
1	0	0	$A_i$	0	$A_i$	OR
1	0	1	$A_i$	0	$A_i + 1$	OR
1	1	0	$A_i$	$B_i$	$A_i - B_i - 1$	AND
1	1	1	$A_i$	$B_i$	$A_i - B_i$	AND

#### **Explanation:**

we can't modify  $Y_i$  because that would change the arithmetic operations and neither can omit  $A_i$  in any input, So we change  $X_i$ ,

Let, 
$$X_i = A_i + K_i$$

$$F_i = X_i \oplus Y_i$$

$$F_i = X_i \oplus 0$$

$$F_i = X_i$$

$$F_i = A_i + K_i$$

But the desired output is  $A_i + B_i$ . So putting  $K_i = B_i$ 

$$F_i = X_i \oplus Y_i$$

$$F_i = (A_i \oplus K_i) \oplus \overline{B_i}$$

$$F_i = (A_i \oplus K_i)B_i + \overline{(A_i \oplus K_i)}.\overline{B_i}$$

$$F_i = A_i B_i + K_i B_i + \overline{A_i}.\overline{K_i}.\overline{B_i}$$

Here our desired operation is  $A_iB_i$ 

So, 
$$A_iB_i + K_iB_i + \overline{A_i}.\overline{K_i}.\overline{B_i} = A_iB_i$$

if 
$$K_i = \overline{B_i}$$
 Then  $F_i = A_i B_i$ 

So we need  $K_i = B_i$  when we will do OR operation and  $K_i = \overline{B_i}$  for AND operation.

$cs_2$	$cs_1$	$cs_0$	В
1	0	0	$B_i$
1	0	1	$B_i$
1	1	0	$\overline{B_i}$
1	1	1	$\overline{B_i}$

So from the truth table we can derive,

$$X_{i} = A_{i} + CS_{2}(\overline{CS_{1}}.B(CS_{0} + \overline{CS_{0}}) + CS_{1}.\overline{B_{i}}(CS_{0} + \overline{CS_{0}})))$$
  
$$X_{i} = A_{i} + CS_{2}(CS_{1} \oplus B_{i})$$

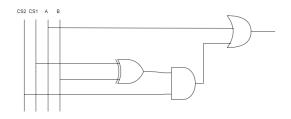


Figure 2:  $X_i = A_i + CS_2(CS_1 \oplus B_i)$ 

## 3 Final Diagram

$$X_{i} = A_{i} + CS_{2}(\overline{CS_{1}}.B(CS_{0} + \overline{CS_{0}}) + CS_{1}.\overline{B_{i}}(CS_{0} + \overline{CS_{0}})))$$

$$X_{i} = A_{i} + CS_{2}(CS_{1} \oplus B_{i})$$

$$Y = CS_{1}\overline{B_{i}}$$

$$C_{out} = \overline{CS_{2}}.C_{i}$$