

A New Approach in Preliminary Design of Closed Loop Solar Thermal Systems

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Abstract

In this Paper, a model for closed loop solar systems is presented and an attempt is made to generalize the model to be utilized for primary design of any solar active thermal system. This model may be used for a system where the fluid flow is a gas or a liquid. In this model, two new parameters, namely, the system heat delivery factor and the system heat absorption factor are introduced. These two factors are fully discussed and some equations are developed which determine the values of these factors.

Nomenclature

A_a	overall area of collector
A_c	collector area
A_r	area of receiver
A_s	area of storage tank
$C_{1, 2, s}$	product of mass and specific heat capacity
c_p	specific heat at constant pressure
\dot{c}	mass flow rate- heat capacity product
E	effective factor
E_s	heat exchanger effective factor
F_c	collector heat removal factor
F_p	heat removal factor for design period
F_u	system heat delivers factor
G	dimensionless Parameter
$H_{1, 2, 3}$	heat exchanger
H_p, H_s	integration variables
L	load
$P_{1, 2}$	pump
Q_p	constant heat load
Q_s	Solar heat
Q_u	rate of heat transferred from collector to storage tank
S	solar irradiance
T_a	ambient temperature
T_i	collector entrance temperature
T_o	temperature during design period

$T_{1, 2, 3, 4}$	fluid temperature
t	time
t_d	design time
t_s	storage time
U_l	overall heat loss coefficient
Y_p, Y_∞	integration variables
α'	overall heat absorption factor
α_s	heat absorption factor
$\phi_p, \phi_s, \theta_p, \theta_s$	dimensionless parameters

Introduction

Since 1970, there has been a surge of interest and activity in solar heating systems and many thousands of active systems have been designed, installed and operated [1]. The general method of measuring collector performance employed by the manufactures is basically conducted in three parts; the first is determination of instantaneous efficiency with beam radiation nearly normal to the absorber surface.

The second, is determination of effects of angle of incidence of the solar radiation. The third, is determination of collector time constant, a measure of effective heat capacity. Comparison between various solar collectors can be made by graphs collector efficiency versus performance coefficient.

For most system, the Hottel – Whillier model [2] is used to determine the efficiency of the solar collector where certain parameters such as number of covered plates, absorption covers, number of pipes, etc are considered and related to obtain new parameters, namely, transmittance-absorptance product, overall heat removal factor and overall loss coefficient. This paper, introduces a new method for calculation of collector efficiency, utilizing heat exchanger theory.

Yanadori [3] and Gauthier [4] employed this heat exchanger theory to estimate the performance of solar collectors where NTU^1 was employed for simplification of their results.

The method employed in this paper is different from those mentioned above since the heat transfer surfaces are considered as independent variables.

Analytical Model

The schematic diagram of a solar thermal system is shown in Fig. (1). Pump, P_1 , carries a fluid between a collector and a heat exchanger (H_1). The product of mass flow rate and a specific heat (mc_p) for this circuit is C_1 where the heat exchanger (H_1) transfers heat from fluid into the storage system. Pump (P_2) which receives heat from the storage tank, transfers a fluid from the heat exchanger (H_2) into the heat exchanger (H_3) Where heat is utilized for a specific thermal process.

Mass flow rate – specific heat product for this circuit is C_2 . Each of the three heat exchangers employed in this system is specified by a coefficient, E , and each exchanger can be replaced by considering an appropriate effectiveness new factor.

The model derived in here is based on the following assumptions:

1. The overall area of collector (A_a) and the area of receiver (A_r) are considered to be equal ($A_r=A_a$).
2. The temperature of the storage system is considered to be uniform and homogeneous, even though stratification phenomenon in real storage system occurs.
3. The whole solar heat system receives a constant heat load (Q_p) during process at temperature (T_p) while, the system also receives some amount of time dependent solar heat (Q_s) at an ambient temperature (T_a).
4. Solar irradiant is considered to start at sunrise, $t=0$, and to reach its maximum value at mid – day and goes back to zero at sunset ($t=t_s$).
5. Pump (p_1) is assumed to be operational from sunrise until the sunset and remains unoperational for the rest of design period.
6. Pump (p_2) can be on or off depending on the receivers heat process (Q_p).
7. The model is developed for an active solar system.

In this model, α' is defined as the overall heat absorption factor and U_L is the overall heat loss coefficient. The collector system is specified by an effective factor, E , where $E = \frac{F_R A_c U_L}{C}$ and F_R = Heat removal factor

which is estimated from Hottel – Whillier model. $\dot{c}_1 = \left(\dot{m} c_p \right)_1$ mass flow rate – heat capacity product.

Also, C_s is defined as the product of mass and specific heat capacity of the storage system's sensible heat.

Formulation of the Active System with Forced Circulation

T_i is assumed to be the collector entrance temperature and Q_u the rate of heat transferred from collector to the storage tank. From the energy balance equation for the collector:

$$Q_u = F_R A_c [S - U_L (T_i - T_a)] \quad (1)$$

It is useful to write the energy balance equation in terms of the heat exchanger effectiveness factor (E_c) as below:

$$E_c = F_R A_c \frac{U_L}{\dot{c}_1} \quad (2)$$

From equation (1) and (2):

$$Q_u = \dot{c}_1 E_c \left(\frac{S}{U_L} + T_a - T_i \right) \quad (3)$$

Substituting for α' , as defined before, into equation (3):

$$Q_u = \dot{c}_1 E_c \left(\frac{\alpha' A_a}{A_r U_L} q_s + T_\infty - T_i \right) \quad (4)$$

From the energy balance for heat exchanger (H_1):

$$Q_u = \dot{c}_1 E_1 (T_2 - T_s). \text{ Where:} \quad (5)$$

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$$Q_u = \dot{c}_1 E_1 (T_2 - T_s). \text{ Where:} \quad (5)$$

E_1 = The heat exchanger effective ness factor (up to the entrance of the tap)

T_2 = The fluid temperature leaving the storage tank.

T_s = The ambient temperature of the storage tank.

The heat transferred from the collector to the storage tank can be written as:

$$Q_u = \dot{c}_1 (T_2 - T_1) \quad (6)$$

From equations (5) and (6):

$$Q_u = \dot{c}_1 \left(\frac{E_1}{1 - E_1} \right) (T_1 - T_s) \quad (7)$$

Also, from equations (7) and (4):

$$Q_u = \frac{1}{R_c} (\alpha' A_a R_{Lqs} + T_\infty - T_s) \quad (8)$$

where,

$$R_c = \frac{E_c + E_1 - E_c E_1}{\dot{c}_1 E_c E_1} \quad (9)$$

$$\text{and } R_L = \frac{1}{A_r U_L} \quad (10)$$

for the next step ,it is assumed that all heat loss from the storage tank utilized as a heat process. So, equation (11) can be developed.

$$(mc_p)_s \frac{dT_s}{dt} = Q_u - L - (UA)_s (T_s - T_a) \quad (11)$$

By assuming $\left(\dot{m} c_p \right)_s = C_s$ and $Q_p = L - (UA)_s (T_s - T_a)$, equation (11) can be expressed as:

$$C_s \frac{dT_s}{dt} = Q_u - Q_p \quad (12)$$

Q_u can be obtained from equation (8), during the storage time from $t = 0$ to $t = t_s$. For the rest of the design period (from $t = t_s$ up to $t = t_d$), $Q = 0$. Therefore equation (13) can be developed as:

$$C_s \frac{dT_s}{dt} \begin{cases} \frac{1}{R_c} (\alpha' A_a R_L q_s + T_\infty - T_s) - Q_p, & 0 \leq t \leq t_s \\ -Q_p, & t_s \leq t \leq t_d \end{cases} \quad (13)$$

Let's assume that t_o is the minimum temperature of the storage tank in which allows Q_p leaves the storage tank without receiving heat from any source except those from the sun. From the energy balance for the heat exchanger H_2 :

$$Q_p = \dot{c}_2 E_2 (T_o - T_3), \quad (14)$$

where,

T_3 = The fluid temperature leaving the heat exchangers H_3 and entering the heat exchanger H_2 .

Also, from energy balance for the heat exchanger H_3 :

$$Q_p = \dot{c}_2 E_3 (T_4 - T_p), \quad (15)$$

where,

T_4 = The fluid temperature leaving the heat exchangers H_2 and entering the heat exchanger H_3 .

$$\text{Also, } Q_p = \dot{c}_2 (T_4 - T_3) \quad (16)$$

employing equation (16) to eliminate T_4 from equation (15):

$$Q_p = \frac{\dot{c}_2 E_3}{1 - E_3} (T_3 - T_p) \quad (17)$$

Now, using equation (17) to eliminate T_3 from equation (14);

$$Q_p = \frac{1}{R_p} (T_o - T_p) \quad (18)$$

where,

$$R_p = \frac{E_2 + E_3 - E_2 E_3}{\dot{c} E_2 E_3} \quad (19)$$

By utilizing the above equations, a periodic can be designed under steady state conditions in which a constant heat load is undertaken and heat is only supplied from solar energy.

The minimum allowed temperature of the storage tank during design procedure is T_o . So, from equation (18):

$$T_s(0) = T_p + R_p Q_p \quad (20)$$

$$T_s(t_d) = T_p + R_p Q_p \quad (21)$$

Equation (20) can be employed as a primary condition for equation (13) and equation (21) can be used for solving the maximum load heat that the process undergoes (Q_p). Rewriting equation (21):

$$Q_p = \frac{1}{R_p} [T_s(t_d) - T_p] \quad (22)$$

Now, the following integration variables are defined:

$$H_s = A_a \int_0^{t_s} q_s dt \quad (23)$$

$$H_p = \int_0^{t_d} Q_p dt \quad (24)$$

$$Y_p = \int_0^{t_s} T_p dt \quad (25)$$

$$Y_\infty = \int_0^{t_s} T_\infty dt \quad (26)$$

These integration variables can be employed for the following dimensionless parameters:

$$\theta_s = \frac{T_s t_s - Y_\infty}{\alpha' R_L H_s} \quad (27)$$

$$\theta_p = \frac{T_s t_s - Y_\infty}{\alpha' R_L H_s} \quad (28)$$

$$\phi_s = \frac{A_a q_s t_s}{H_s} + \frac{T_\infty t_s - Y_\infty}{\alpha' R_L H_s} \quad (29)$$

$$\phi_p = \frac{H_p}{\alpha' H_s} \quad (30)$$

$$F_c = \frac{R_L}{R_c} \quad (31)$$

$$F_p = \frac{R_L}{R_p} \quad (32)$$

$$G = \frac{R_L C_s}{t_s} \quad (33)$$

$$\tau = \frac{t}{t_s} \quad (34)$$

$$\beta = \frac{t_d}{t_s} \quad (35)$$

By writing equations (13), (20) and (22), in dimensionless form, a complete formulation can be obtained, as follows:

$$G = \frac{d\theta_s}{dr} = \begin{cases} F_c = (\phi_s - \theta_s) - \phi_p \beta & 0 \leq \tau \leq 1 \\ -\phi_p / \beta & 1 \leq \psi \leq \beta \end{cases} \quad (36)$$

$$\theta_s(0) = \frac{\phi_p}{\beta F_p} \quad (37)$$

$$\phi_p = \beta F_p [\theta_s(\beta) - \theta_p] \quad (38)$$

The Solution Method

Integrating equation (36) from $\tau = 0$ to τ for $0 \leq \tau \leq 1$ then :

$$\theta_s(\tau) = \left[\theta_s(0) + \frac{\phi_p}{F_c} - \Psi(0) \right] \exp\left(\frac{-F_c \tau}{G}\right) - \frac{\phi_p}{\beta F_c} + \Psi(\tau) \quad (39)$$

in equation (39), $\Psi(\tau)$ is a specific solution for equation (40) :

$$\frac{G}{F_c} \frac{d\Psi}{d\tau} + \Psi = \phi_s(\tau) \quad (40)$$

By using equation (37) and (4) for $0 \leq \psi \leq 1$:

$$\theta_s(\tau) = \left[\theta_p + \frac{1}{\beta} \left(\frac{1}{F_p} + \frac{1}{F_c} \right) \phi_p - \psi(0) \right] \exp\left(\frac{-F_c \tau}{G}\right) - \frac{\phi_p}{\beta F_c} + \psi(\tau) \quad (41)$$

Now, integrating from equation (3), From $\tau = 1$ to τ for $1 \leq \tau \leq \beta$:

$$\theta_s(\tau) = \theta_s(1) - \frac{\phi_p}{\beta G} (\tau - 1) \quad (42)$$

Then using equation (41) for calculating $\theta_s(1)$ when $1 \leq \tau \leq \beta$:

$$\theta_s(\tau) = \left[\theta_p + \frac{1}{\beta} \left(\frac{1}{F_p} + \frac{1}{F_c} \right) \phi_p - \psi(0) \right] \exp\left(\frac{-F_c}{G}\right) + \psi(1) - \frac{\phi_p}{\beta} \left(\frac{1}{F_c} + \frac{\tau - 1}{G} \right) \quad 1 \leq \tau \leq \beta \quad (43)$$

New, equation (43) can be employed to evaluate $\theta_s(\beta)$ and use it in equation (38):

$$\phi_p = \beta F_p \left[\left[\theta_p + \frac{1}{\beta} \left(\frac{1}{F_p} + \frac{1}{F_c} \right) \phi_p - \psi(0) \right] \exp\left(\frac{-F_c}{G}\right) + \psi(1) - \frac{\phi_p}{\beta} \left(\frac{1}{F_c} + \frac{\beta - 1}{G} \right) - \theta_p \right] \quad (44)$$

By solving equation (44) for ϕ_p :

$$\phi_p = F_u (\alpha_s - \theta_p) \quad (45)$$

$$F_u = \beta \left[\frac{1}{F_p} + \frac{1}{F_c} + \frac{\beta - 1}{G[1 - \exp(-F_c/G)]} \right]^{-1} \quad (46)$$

$$\alpha_s = \frac{\psi(1) - \psi(0)}{1 - \exp(-F_c/G)} + \psi(0) \quad (47)$$

In here $\psi(\tau)$ is a specific solution (3), rewriting equation (45) in dimensional form, an expression for the whole-received heat process during period can be obtained:

$$H_p = F_u (\alpha_s \alpha' H_s - A_r U_L (\gamma_p - \gamma_\infty)) \quad (48)$$

Equation (48), gives two variables for the new system, F_u and α_s which are respectively, the system heat deliver factor and heat absorption factor. The delivery heat is defined in equation (46), but the solution for α_s is rather complicated and needs to be explained as follows:

The System Heat Absorption Factor

To obtain a numerical value for α_s , it is necessary to know variation of solar irradiance and ambient temperature with time. By knowing $S(t)$ and $T_a(t)$, from equation (26), the value of $\phi_s(\tau)$ can be calculated.

With these data, equation (3) can be integrated and then by considering some suitable primary conditions, Ψ (1) is obtainable. By substituting for Ψ (1) and Ψ (0) in equation (47), α_s can be found. It should be noted α_s is independent of Ψ (0) and also $\phi_s(\tau)$ is unique. So, α_s is only function of the one dimensional variable $\frac{G}{F_s}$.

The above method can be utilized to calculate α_s numerically, even though it is possible to evaluate α_s analytically, if $\phi_s(\tau)$ is in a suitable form for example, if solar irradiance is in sinusoidal form for $0 \leq t \leq t_s$, then:

$$q_s(\tau) = q_a \sin(\omega t) \quad (49)$$

t_s is the time in which the solar irradiance tends to zero:

$$\omega = \frac{\pi}{t_s} \quad (50)$$

By substituting from equation (49) and (50) into equation (23):

$$H_s = \frac{2A_a q_a t_s}{\pi} \quad (51)$$

Also, from equation (26), when the ambient temperature is constant:

$$\gamma_\infty = T_\infty t_s \quad (52)$$

By substituting from equations (49), (50), (51) and (52) into equation (29):

$$\phi_s(\tau) = \frac{\pi}{2} \sin(\pi \tau) \quad (53)$$

Now, substituting from equation (53) into equation (2):

$$G/F_c \left(\frac{d\Psi}{d\tau} \right) + \Psi = \frac{\pi}{2} \sin(\pi \tau) \quad (54)$$

The solution of equation (55) is:

$$\Psi(\tau) = \frac{m^2 \pi \sin(\pi \tau) - \pi^2 m \cos(\pi \tau)}{2(m^2 + \pi^2)} + \left[\Psi(0) + \frac{\pi m}{2(m^2 + \pi^2)} \right] \exp(-m\tau) \quad (55)$$

where,

$$m = \frac{F_c}{G}$$

$\Psi(1)$ can be calculated ($\tau = 1$) from equation (55):

$$\Psi(1) = \frac{\pi^2 m}{2(m^2 + \pi^2)} [1 + \exp(-m)] + \Psi(0) \exp(-m) \quad (56)$$

By employing equation (56) in equation (47):

$$a_s(G/F_s) = \frac{\pi^2 (G/F_c) [1 + \exp(-F_c/G)]}{2[\pi^2 + (F_c/G)^2] [1 - \exp(-F_c/G)]} \quad (57)$$

Equation (57) is used whenever the variation of solar irradiance on collector is in sinusoidal form. Phillips [5] showed that the results of numerical solution for most of solar irradiance variations are nearly the same as those obtainable from equation (57). Therefore, if the available data is not enough, then equation (57) can be employee to calculate the system absorption factor, Fig (1).

Presentation of the Results

Utilizing equations developed for the system, with the geometry given in Table 1, the calculation carried out by using a computer programme, CSHS.FOR.

Table 1. Required data for CSHS.FOR Programme

Area of the collector	[m ²]=100.00
Overall loss heat transfer coefficient	[kw/m ² -c]=0.004
Overall solar absorptivity	
Collector efficiency factor	[kw/m ² -c]=0.7500
Mass-specific heat of storage-tank	[----]=0.8500
Mass-specific heat rate of first H.EX	[kj/c]=1050.00
Mass-specific heat rate 2.nd & 3.rd H.EX	[kw/c]=0.4080
Range of variation for storage-tank	[kw/c]=0.2920
First heat-exchanger effectiveness	[kw/c]=8000.000
Second heat-exchanger effectiveness	[----]=1.0000
Third heat -exchanger effectiveness	[----]=0.8000
Time that sun shines on the collector	[----]=0.5000
Time for system operation	[Hour]=8.000
Total receiving radiation on the system	[Hour]=24.0000
Required processing temperature	[kj/m ²]=12500.00
Ambient temperature	[c]=25.0000
	[c]=5.0000

Stop- program terminated

Table 2 The computer results for CSHS.FOR. Programme.

CS (Kj/c)	FR (--)	G/FC (--)	ALFS (--)	FU (--)	HP (Kw/hr)
1300.00	0.5767	0.1580	0.6279	0.1119	11.14
1550.00	0.5767	0.1957	0.7093	0.1325	15.99
1800.00	0.5767	0.2333	0.7699	0.1508	20.59
2050.00	0.5767	0.2709	0.8150	0.1672	24.78
2300.00	0.5767	0.3086	0.8490	0.1817	28.54
2550.00	0.5767	0.3462	0.8749	0.1945	31.84
2800.00	0.5767	0.3838	0.8950	0.2059	34.81

2800.00	0.5767	0.3838	0.8950	0.2059	34.81
3050.00	0.5767	0.4215	0.9108	0.2160	37.40
3300.00	0.5767	0.4591	0.9234	0.2250	39.70
3550.00	0.5767	0.4967	0.9336	0.2330	41.74
3800.00	0.5767	0.5343	0.9419	0.2403	43.55
4050.00	0.5767	0.5720	0.9488	0.2468	45.18
4300.00	0.5767	0.6096	0.9545	0.2527	46.64
4550.00	0.5767	0.6472	0.9594	0.2580	47.95
4800.00	0.5767	0.6849	0.9635	0.2629	49.14
5050.00	0.5767	0.7225	0.9671	0.2674	50.22
5300.00	0.5767	0.7601	0.9701	0.2715	51.21
5550.00	0.5767	0.7677	0.9728	0.2752	52.11
5800.00	0.5767	0.8354	0.9751	0.2787	52.93
6050.00	0.5767	0.8730	0.9771	0.2819	53.69
6300.00	0.5767	0.9106	0.9789	0.2849	54.40
6550.00	0.5767	0.9483	0.9805	0.2877	55.05
6800.00	0.5767	0.9859	0.9819	0.2903	55.56
7050.00	0.5767	1.0235	0.9832	0.2927	56.21
7300.00	0.5767	1.0612	0.9844	0.2950	56.73
7550.00	0.5767	1.0988	0.9854	0.2971	57.22
7800.00	0.5767	1.1364	0.9863	0.2991	57.68
8050.00	0.5767	1.1740	0.9872	0.3010	58.11
8300.00	0.5767	1.2117	0.9879	0.3027	58.51
8550.00	0.5767	1.2493	0.9887	0.3044	58.89
8800.00	0.5767	1.2869	0.9893	0.3060	59.25
9050.00	0.5767	1.3246	0.9899	0.3075	59.59
9300.00	0.5767	1.3622	0.9904	0.3089	59.91
9550.00	0.5767	1.3998	0.9909	0.3103	60.21
9800.00	0.5767	1.4375	0.9914	0.3116	60.50
10050.00	0.5767	1.4751	0.9918	0.3128	60.77

In this calculation, the design variable is the storage tanks and the other effective parameters in design are considered to be constant. The results are shown in Table 2 and Figs. 2, 3 and 4.

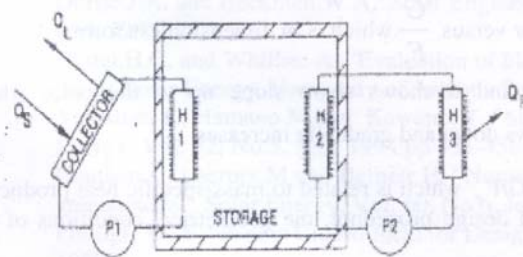


Fig. 1 Schematic diagram of the thermal system

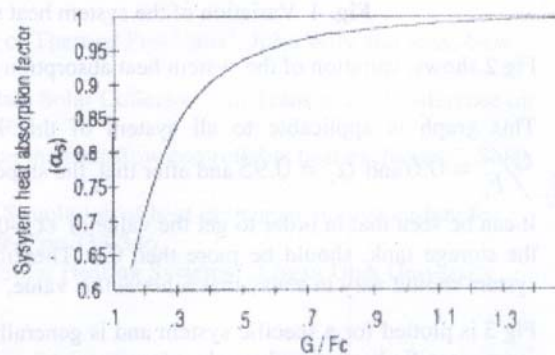


Fig. 2 Variation of the system heat absorption factor versus G/Fc

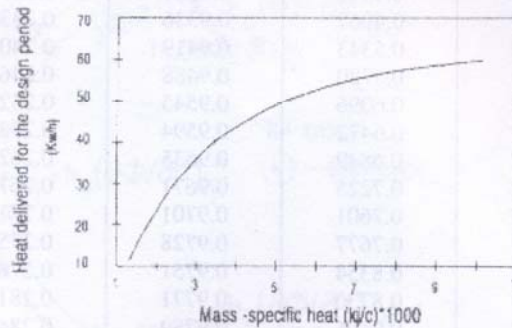


Fig. 3 Heat delivered versus mass-specific heat product

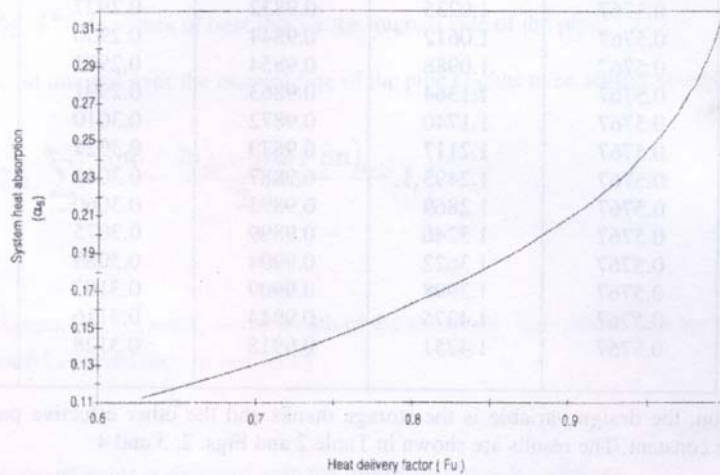


Fig. 4 Variation of the system heat absorption factor versus heat delivery factor

Fig 2 shows, variation of the system heat absorption factor versus $\frac{G}{F_c}$ which is in dimensionless form.

This graph is applicable to all system of this kind, and it shows sharp slope up to the point where $\frac{G}{F_c} = 0.6$ and $\alpha_s = 0.95$ and after that, the slope slows down and gradually increases.

It can be seen that in order to get the value of $\alpha_s > 0.95$, $\frac{G}{F_c}$ which is related to mass-specific heat product in the storage tank, should be more then 0.6. Therefore in design procedure, the geometrical conditions of the system should vary in a way that achieve this value, $\frac{G}{F_c}$.

Fig 3 is plotted for a specific system and is generally applicable to all similar systems. It shows that increasing mass- specific heat of tank product (over a certain amount) does not have any significant effect on the variation of heat load delivery. So, for maximum efficiency point and economical optimization point, the mass-specific

heat product should be kept at a certain value. This is achieved by the use of a computer programme. For the sample design, this value is about 9000 KJ/c.

Fig 4 is an alternative way of showing Fig 2 in non-dimensional condition. This graph shows the variation of system heat absorption factor versus F_u , which is explained in equation (46). It can be seen that by increasing the system heat absorption factor, F_u tends to one and if the value of mass-specific heat product increases more than a certain level, then, F_u variation is not significant. The desired value of mass-specific heat product can be found for this certain value of F_u .

The design producer adopted in here is to achieve the value $G/F_c > 0.6$ and then to obtain F_u from graph (4). By knowing the system heat absorption factor (F_u), and using equation (48), the value of delivered heat can be achieved.

The errors arises from the above design method is due to consideration of stratification phenomena in the tank and the way that the functions of solar variation are defined for obtaining the system absorption factor.

Using this model for designing a closed loop solar system when the rate of delivered heat load is high, leads to time saving where the computer results are accurate enough.

Conclusions

A new method was presented for the preliminary design of a closed loop solar thermal system. A computer programme, CSHS.FOR, was employed to calculate the main parameters affecting the system performance, namely, the system heat absorption factor (α_s), mass-specific heat product, heat delivery factor and G/F_c . The results show that for the maximum efficiency point, the mass-specific heat product should be kept at a certain value [$G/F_c > 0.6$ and $\alpha_s > 0.95$]

The method adopted in this paper shows an economical and quick way for designing an active solar heating system, especially when the delivered heat load is high.

References

- [1] Duffie.J.A, and Beckman.W.A, "Solar Engineering of Thermal Processes", John Wily and sons, New york 1985.
- [2] Hottel.H.C, and Whillier.A, "Evaluation of Flat- Plate Solar Collector" , In Trans of the Conference on use of Solar Energy, University of Arizona Press 1985.
- [3] Yanadori. K, Hamano.M, and Kawano, T. "Study on the heat-flow controllable heat exchanger", Solar Energy, Vol. 52, No.5, May 1994, pp 451-456
- [4] Gauthier.C, Lacroix.M and Bernier.H, "Numerical Simulation of heat exchanger storage system for greenhouses", Solar Energy, Vol. 60, No.6, June 1997, pp 333-346
- [5] Phillips. W. F, "A new Closed form for Designing Solar Heating Systems", Logan Utah University, 1980