

# **WebAssembly Specification**

Release 3.0 (Draft 2025-02-13)

## **WebAssembly Community Group**

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## CHAPTER 1

Introduction

## 1.1 Introduction

WebAssembly (abbreviated Wasm<sup>2</sup>) is a *safe*, *portable*, *low-level code format* designed for efficient execution and compact representation. Its main goal is to enable high performance applications on the Web, but it does not make any Web-specific assumptions or provide Web-specific features, so it can be employed in other environments as well.

WebAssembly is an open standard developed by a W3C Community Group<sup>1</sup>.

This document describes version 3.0 (Draft 2025-02-13) of the core WebAssembly standard. It is intended that it will be superseded by new incremental releases with additional features in the future.

#### 1.1.1 Design Goals

The design goals of WebAssembly are the following:

- Fast, safe, and portable semantics:
  - **Fast**: executes with near native code performance, taking advantage of capabilities common to all contemporary hardware.
  - Safe: code is validated and executes in a memory-safe<sup>3</sup>, sandboxed environment preventing data corruption or security breaches.
  - **Well-defined**: fully and precisely defines valid programs and their behavior in a way that is easy to reason about informally and formally.
  - Hardware-independent: can be compiled on all modern architectures, desktop or mobile devices and embedded systems alike.
  - Language-independent: does not privilege any particular language, programming model, or object model.
  - Platform-independent: can be embedded in browsers, run as a stand-alone VM, or integrated in other environments.
  - Open: programs can interoperate with their environment in a simple and universal manner.

<sup>&</sup>lt;sup>2</sup> A contraction of "WebAssembly", not an acronym, hence not using all-caps.

https://www.w3.org/community/webassembly/

<sup>&</sup>lt;sup>3</sup> No program can break WebAssembly's memory model. Of course, it cannot guarantee that an unsafe language compiling to WebAssembly does not corrupt its own memory layout, e.g. inside WebAssembly's linear memory.

- Efficient and portable representation:
  - Compact: has a binary format that is fast to transmit by being smaller than typical text or native code formats.
  - Modular: programs can be split up in smaller parts that can be transmitted, cached, and consumed separately.
  - **Efficient**: can be decoded, validated, and compiled in a fast single pass, equally with either just-in-time (JIT) or ahead-of-time (AOT) compilation.
  - Streamable: allows decoding, validation, and compilation to begin as soon as possible, before all data has been seen.
  - Parallelizable: allows decoding, validation, and compilation to be split into many independent parallel tasks.
  - Portable: makes no architectural assumptions that are not broadly supported across modern hardware.

WebAssembly code is also intended to be easy to inspect and debug, especially in environments like web browsers, but such features are beyond the scope of this specification.

## 1.1.2 Scope

At its core, WebAssembly is a *virtual instruction set architecture* (*virtual ISA*). As such, it has many use cases and can be embedded in many different environments. To encompass their variety and enable maximum reuse, the WebAssembly specification is split and layered into several documents.

This document is concerned with the core ISA layer of WebAssembly. It defines the instruction set, binary encoding, validation, and execution semantics, as well as a textual representation. It does not, however, define how WebAssembly programs can interact with a specific environment they execute in, nor how they are invoked from such an environment.

Instead, this specification is complemented by additional documents defining interfaces to specific embedding environments such as the Web. These will each define a WebAssembly *application programming interface (API)* suitable for a given environment.

## 1.1.3 Security Considerations

WebAssembly provides no ambient access to the computing environment in which code is executed. Any interaction with the environment, such as I/O, access to resources, or operating system calls, can only be performed by invoking functions provided by the embedder and imported into a WebAssembly module. An embedder can establish security policies suitable for a respective environment by controlling or limiting which functional capabilities it makes available for import. Such considerations are an embedder's responsibility and the subject of API definitions for a specific environment.

Because WebAssembly is designed to be translated into machine code running directly on the host's hardware, it is potentially vulnerable to side channel attacks on the hardware level. In environments where this is a concern, an embedder may have to put suitable mitigations into place to isolate WebAssembly computations.

## 1.1.4 Dependencies

WebAssembly depends on two existing standards:

- IEEE 754<sup>4</sup>, for the representation of floating-point data and the semantics of respective numeric operations.
- Unicode<sup>5</sup>, for the representation of import/export names and the text format.

However, to make this specification self-contained, relevant aspects of the aforementioned standards are defined and formalized as part of this specification, such as the binary representation and rounding of floating-point values, and the value range and UTF-8 encoding of Unicode characters.

<sup>4</sup> https://ieeexplore.ieee.org/document/8766229

<sup>&</sup>lt;sup>5</sup> https://www.unicode.org/versions/latest/

#### Note

The aforementioned standards are the authoritative source of all respective definitions. Formalizations given in this specification are intended to match these definitions. Any discrepancy in the syntax or semantics described is to be considered an error.

## 1.2 Overview

## 1.2.1 Concepts

WebAssembly encodes a low-level, assembly-like programming language. This language is structured around the following concepts.

#### Values

WebAssembly provides only four basic *number types*. These are integers and IEEE 754<sup>6</sup> numbers, each in 32 and 64 bit width. 32-bit integers also serve as Booleans and as memory addresses. The usual operations on these types are available, including the full matrix of conversions between them. There is no distinction between signed and unsigned integer types. Instead, integers are interpreted by respective operations as either unsigned or signed in two's complement representation.

In addition to these basic number types, there is a single 128 bit wide vector type representing different types of packed data. The supported representations are four 32-bit, or two 64-bit IEEE 754<sup>7</sup> numbers, or different widths of packed integer values, specifically two 64-bit integers, four 32-bit integers, eight 16-bit integers, or sixteen 8-bit integers.

Finally, values can consist of opaque *references* that represent pointers towards different sorts of entities. Unlike with other types, their size or representation is not observable.

#### **Instructions**

The computational model of WebAssembly is based on a *stack machine*. Code consists of sequences of *instructions* that are executed in order. Instructions manipulate values on an implicit *operand stack*<sup>8</sup> and fall into two main categories. *Simple* instructions perform basic operations on data. They pop arguments from the operand stack and push results back to it. *Control* instructions alter control flow. Control flow is *structured*, meaning it is expressed with well-nested constructs such as blocks, loops, and conditionals. Branches can only target such constructs.

#### Traps

Under some conditions, certain instructions may produce a *trap*, which immediately aborts execution. Traps cannot be handled by WebAssembly code, but are reported to the outside environment, where they typically can be caught.

### **Functions**

Code is organized into separate *functions*. Each function takes a sequence of values as parameters and returns a sequence of values as results. Functions can call each other, including recursively, resulting in an implicit call stack that cannot be accessed directly. Functions may also declare mutable *local variables* that are usable as virtual registers.

#### Tables

A *table* is an array of opaque values of a particular *reference type*. It allows programs to select such values indirectly through a dynamic index operand. Thereby, for example, a program can call functions indirectly through a dynamic index into a table. This allows emulating function pointers by way of table indices.

#### **Linear Memory**

A *linear memory* is a contiguous, mutable array of raw bytes. Such a memory is created with an initial size but can be grown dynamically. A program can load and store values from/to a linear memory at any byte address (including unaligned). Integer loads and stores can specify a *storage size* which is smaller than the

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<sup>&</sup>lt;sup>6</sup> https://ieeexplore.ieee.org/document/8766229

<sup>&</sup>lt;sup>7</sup> https://ieeexplore.ieee.org/document/8766229

<sup>&</sup>lt;sup>8</sup> In practice, implementations need not maintain an actual operand stack. Instead, the stack can be viewed as a set of anonymous registers that are implicitly referenced by instructions. The type system ensures that the stack height, and thus any referenced register, is always known statically.

size of the respective value type. A trap occurs if an access is not within the bounds of the current memory size.

#### Modules

A WebAssembly binary takes the form of a *module* that contains definitions for functions, tables, and linear memories, as well as mutable or immutable *global variables*. Definitions can also be *imported*, specifying a module/name pair and a suitable type. Each definition can optionally be *exported* under one or more names. In addition to definitions, modules can define initialization data for their memories or tables that takes the form of *segments* copied to given offsets. They can also define a *start function* that is automatically executed.

#### Embedder

A WebAssembly implementation will typically be *embedded* into a *host* environment. This environment defines how loading of modules is initiated, how imports are provided (including host-side definitions), and how exports can be accessed. However, the details of any particular embedding are beyond the scope of this specification, and will instead be provided by complementary, environment-specific API definitions.

#### 1.2.2 Semantic Phases

Conceptually, the semantics of WebAssembly is divided into three phases. For each part of the language, the specification specifies each of them.

#### Decoding

WebAssembly modules are distributed in a *binary format*. *Decoding* processes that format and converts it into an internal representation of a module. In this specification, this representation is modelled by *abstract syntax*, but a real implementation could compile directly to machine code instead.

#### Validation

A decoded module has to be *valid*. Validation checks a number of well-formedness conditions to guarantee that the module is meaningful and safe. In particular, it performs *type checking* of functions and the instruction sequences in their bodies, ensuring for example that the operand stack is used consistently.

#### **Execution**

Finally, a valid module can be executed. Execution can be further divided into two phases:

**Instantiation**. A module *instance* is the dynamic representation of a module, complete with its own state and execution stack. Instantiation executes the module body itself, given definitions for all its imports. It initializes globals, memories and tables and invokes the module's start function if defined. It returns the instances of the module's exports.

**Invocation**. Once instantiated, further WebAssembly computations can be initiated by *invoking* an exported function on a module instance. Given the required arguments, that executes the respective function and returns its results.

Instantiation and invocation are operations within the embedding environment.

Structure

## 2.1 Conventions

WebAssembly is a programming language that has multiple concrete representations (its binary format and the text format). Both map to a common structure. For conciseness, this structure is described in the form of an *abstract syntax*. All parts of this specification are defined in terms of this abstract syntax.

#### 2.1.1 Grammar Notation

The following conventions are adopted in defining grammar rules for abstract syntax.

- Terminal symbols (atoms) are written in sans-serif font or in symbolic form: i32, nop,  $\rightarrow$ , [,].
- Nonterminal symbols are written in italic font: valtype, instr.
- $A^n$  is a sequence of  $n \ge 0$  iterations of A.
- $A^*$  is a possibly empty sequence of iterations of A. (This is a shorthand for  $A^n$  used where n is not relevant.)
- $A^+$  is a non-empty sequence of iterations of A. (This is a shorthand for  $A^n$  where  $n \geq 1$ .)
- $A^{?}$  is an optional occurrence of A. (This is a shorthand for  $A^{n}$  where  $n \leq 1$ .)
- Productions are written  $sym := A_1 \mid \ldots \mid A_n$ .
- Large productions may be split into multiple definitions, indicated by ending the first one with explicit ellipses,  $sym ::= A_1 \mid \ldots$ , and starting continuations with ellipses,  $sym ::= \ldots \mid A_2$ .
- Some productions are augmented with side conditions, "if *condition*", that provide a shorthand for a combinatorial expansion of the production into many separate cases.
- If the same meta variable or non-terminal symbol appears multiple times in a production, then all those occurrences must have the same instantiation. (This is a shorthand for a side condition requiring multiple different variables to be equal.)

## 2.1.2 Auxiliary Notation

When dealing with syntactic constructs the following notation is also used:

- $\epsilon$  denotes the empty sequence.
- |s| denotes the length of a sequence s.
- s[i] denotes the *i*-th element of a sequence s, starting from 0.

- s[i:n] denotes the sub-sequence  $s[i] \dots s[i+n-1]$  of a sequence s.
- s[[i] = A] denotes the same sequence as s, except that the i-th element is replaced with A.
- $s[[i:n] = A^n]$  denotes the same sequence as s, except that the sub-sequence s[i:n] is replaced with  $A^n$ .
- $s_1 \oplus s_2$  denotes the sequence  $s_1$  concatenated with  $s_2$ ; this is equivalent to  $s_1$   $s_2$ , but used for clarity.
- $\bigoplus s^*$  denotes the flattened sequence, formed by concatenating all sequences  $s_i$  in  $s^*$ .
- $A \in s$  denotes that A is a member of the sequence s, that is, s is of the form  $s_1$  A  $s_2$  for some sequences  $s_1$ ,  $s_2$ .

Moreover, the following conventions are employed:

- The notation  $x^n$ , where x is a non-terminal symbol, is treated as a meta variable ranging over respective sequences of x (similarly for  $x^*$ ,  $x^+$ ,  $x^2$ ).
- When given a sequence  $x^n$ , then the occurrences of x in an iterated sequence  $(\dots x \dots)^n$  are assumed to denote the individual elements of  $x^n$ , respectively (similarly for  $x^*$ ,  $x^+$ ,  $x^?$ ). This implicitly expresses a form of mapping syntactic constructions over a sequence.
- $e^{i < n}$  denotes the same sequence as  $e^n$ , but implicitly also defines  $i^n$  to be the sequence of values 0 to (n-1).

#### Note

For example, if  $x^n$  is the sequence a b c, then  $(f(x) + 1)^n$  denotes the sequence (f(a) + 1) (f(b) + 1) (f(c) + 1). The form  $e^{i < n}$  additionally gives access to an index variable inside the iteration. For example,  $(f(x) + i)^{i < n}$  denotes the sequence (f(a) + 0) (f(b) + 1) (f(c) + 2).

Productions of the following form are interpreted as records that map a fixed set of fields field i to "values"  $A_i$ , respectively:

$$r ::= \{ \mathsf{field}_1 \ A_1, \mathsf{field}_2 \ A_2, \dots \}$$

The following notation is adopted for manipulating such records:

- Where the type of a record is clear from context, empty fields with value  $\epsilon$  are often omitted.
- r.field denotes the contents of the field component of r.
- r[.field = A] denotes the same record as r, except that the value of the field component is replaced with A.
- $r[.\text{field} = \oplus A^*]$  denotes the same record as r, except that  $A^*$  is appended to the sequence value of the field component, that is, it is short for  $r[.\text{field} = r.\text{field} \oplus A^*]$ .
- $r_1 \oplus r_2$  denotes the composition of two identically shaped records by concatenating each field of sequences point-wise:

$$\{\mathsf{field}_1\,A_1^*,\mathsf{field}_2\,A_2^*,\ldots\}\oplus\{\mathsf{field}_1\,B_1^*,\mathsf{field}_2\,B_2^*,\ldots\}=\{\mathsf{field}_1\,(A_1^*\oplus B_1^*),\mathsf{field}_2\,(A_2^*\oplus B_2^*),\ldots\}$$

•  $\bigoplus r^*$  denotes the composition of a sequence of records, respectively; if the sequence is empty, then all fields of the resulting record are empty.

The update notation for sequences and records generalizes recursively to nested components accessed by "paths"  $pth ::= ([i] \mid .field)^+$ :

- s[[i]pth = A] is short for s[[i] = s[i][pth = A]],
- r[.field pth = A] is short for r[.field = r.field[pth = A]].

#### 2.1.3 Lists

Lists are bounded sequences of the form  $A^n$  (or  $A^*$ ), where the A can either be values or complex constructions. A list can have at most  $2^{32} - 1$  elements.

$$list(X)$$
 ::=  $X^*$  if  $|X^*| < 2^{32}$ 

## 2.2 Values

WebAssembly programs operate on primitive numeric *values*. Moreover, in the definition of programs, immutable sequences of values occur to represent more complex data, such as text strings or other vectors.

## **2.2.1 Bytes**

The simplest form of value are raw uninterpreted *bytes*. In the abstract syntax they are represented as hexadecimal literals.

$$byte ::= 0x00 \mid \dots \mid 0xFF$$

#### **Conventions**

- The meta variable b ranges over bytes.
- Bytes are sometimes interpreted as natural numbers n < 256.

## 2.2.2 Integers

Different classes of *integers* with different value ranges are distinguished by their bit width N and by whether they are unsigned or signed.

$$uN ::= 0 \mid \dots \mid 2^{N} - 1$$
  
 $sN ::= -2^{N-1} \mid \dots \mid -1 \mid 0 \mid +1 \mid \dots \mid +2^{N-1} - 1$   
 $iN ::= uN$ 

The class *i* defines *uninterpreted* integers, whose signedness interpretation can vary depending on context. In the abstract syntax, they are represented as unsigned values. However, some operations convert them to signed based on a two's complement interpretation.

#### Note

The main integer types occurring in this specification are u8, u32, u64, and u128. However, other sizes occur as auxiliary constructions, e.g., in the definition of floating-point numbers.

#### **Conventions**

- The meta variables m, n, i, j range over integers.
- Numbers may be denoted by simple arithmetics, as in the grammar above. In order to distinguish arithmetics like  $2^N$  from sequences like  $(1)^N$ , the latter is distinguished with parentheses.

## 2.2.3 Floating-Point

*Floating-point* data represents 32 or 64 bit values that correspond to the respective binary formats of the IEEE 754<sup>9</sup> standard (Section 3.3).

Every value has a sign and a magnitude. Magnitudes can either be expressed as normal numbers of the form  $m_0 \, . \, m_1 \, m_2 \, ... \, m_m \cdot 2^e$ , where e is the exponent and m is the significand whose most significant bit  $m_0$  is 1, or as a subnormal number where the exponent is fixed to the smallest possible value and  $m_0$  is 0; among the subnormals

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<sup>9</sup> https://ieeexplore.ieee.org/document/8766229

are positive and negative zero values. Since the significands are binary values, normals are represented in the form  $(1 + m \cdot 2^{-M}) \cdot 2^e$  in the abstract syntax, where M is the bit width of m; similarly for subnormals.

Possible magnitudes also include the special values  $\infty$  (infinity) and nan (NaN, not a number). NaN values have a payload that describes the mantissa bits in the underlying binary representation. No distinction is made between signalling and quiet NaNs.

$$\begin{array}{lll} fN & ::= & +fmagN \mid -fmagN \\ fmagN & ::= & (1+m\cdot 2^{-M})\cdot 2^e & \text{if } m < 2^M \wedge 2 - 2^{E-1} \leq e \leq 2^{E-1} - 1 \\ & \mid & (0+m\cdot 2^{-M})\cdot 2^e & \text{if } m < 2^M \wedge 2 - 2^{E-1} = e \\ & \mid & \infty & \\ & \mid & \mathsf{nan}(m) & \text{if } 1 \leq m < 2^M \end{array}$$

where  $M = \operatorname{signif}(N)$  and  $E = \operatorname{expon}(N)$  with

$$signif(32) = 23 
signif(64) = 52 
expon(32) = 8 
expon(64) = 11$$

A *canonical NaN* is a floating-point value  $\pm nan(canon_N)$  where  $canon_N$  is a payload whose most significant bit is 1 while all others are 0:

$$\operatorname{canon}_N = 2^{\operatorname{signif}(N)-1}$$

An arithmetic NaN is a floating-point value  $\pm nan(m)$  with  $m \ge canon_N$ , such that the most significant bit is 1 while all others are arbitrary.

#### Note

In the abstract syntax, subnormals are distinguished by the leading 0 of the significand. The exponent of subnormals has the same value as the smallest possible exponent of a normal number. Only in the binary representation the exponent of a subnormal is encoded differently than the exponent of any normal number.

The notion of canonical NaN defined here is unrelated to the notion of canonical NaN that the IEEE 754<sup>10</sup> standard (Section 3.5.2) defines for decimal interchange formats.

#### **Conventions**

- The meta variable z ranges over floating-point values where clear from context.
- Where clear from context, shorthands like +1 denote floating point values like + $(1+1\cdot 2^{-M})\cdot 2^{0}$ .

### 2.2.4 Vectors

Numeric vectors are 128-bit values that are processed by vector instructions (also known as SIMD instructions, single instruction multiple data). They are represented in the abstract syntax using u128. The interpretation of lane types (integer or floating-point numbers) and lane sizes are determined by the specific instruction operating on them.

#### 2.2.5 Names

Names are sequences of characters, which are scalar values as defined by Unicode<sup>11</sup> (Section 2.4).

name ::= 
$$char^*$$
 if  $|utfs(char^*)| < 2^{32}$   $char$  ::=  $U+00 | ... | U+D7FF | U+E000 | ... | U+10FFFF$ 

Due to the limitations of the binary format, the length of a name is bounded by the length of its UTF-8 encoding.

<sup>10</sup> https://ieeexplore.ieee.org/document/8766229

<sup>11</sup> https://www.unicode.org/versions/latest/

#### Convention

• Characters (Unicode scalar values) are sometimes used interchangeably with natural numbers n < 1114112.

## 2.3 Types

Various entities in WebAssembly are classified by types. Types are checked during validation, instantiation, and possibly execution.

## 2.3.1 Number Types

Number types classify numeric values.

```
numtype ::= i32 | i64 | f32 | f64
```

The types i32 and i64 classify 32 and 64 bit integers, respectively. Integers are not inherently signed or unsigned, their interpretation is determined by individual operations.

The types f<sub>32</sub> and f<sub>64</sub> classify 32 and 64 bit floating-point data, respectively. They correspond to the respective binary floating-point representations, also known as *single* and *double* precision, as defined by the IEEE 754<sup>12</sup> standard (Section 3.3).

Number types are *transparent*, meaning that their bit patterns can be observed. Values of number type can be stored in memories.

#### **Conventions**

• The notation |t| denotes the *bit width* of a number type t. That is, |i32| = |f32| = 32 and |i64| = |f64| = 64.

## 2.3.2 Vector Types

*Vector types* classify vectors of numeric values processed by vector instructions (also known as *SIMD* instructions, single instruction multiple data).

```
vectype ::= v_{128}
```

The type v128 corresponds to a 128 bit vector of packed integer or floating-point data. The packed data can be interpreted as signed or unsigned integers, single or double precision floating-point values, or a single 128 bit type. The interpretation is determined by individual operations.

Vector types, like number types are *transparent*, meaning that their bit patterns can be observed. Values of vector type can be stored in memories.

#### **Conventions**

• The notation |t| for bit width extends to vector types as well, that is,  $|v_{128}| = 128$ .

## 2.3.3 Heap Types

*Heap types* classify objects in the runtime store. There are three disjoint hierarchies of heap types:

- function types classify functions,
- aggregate types classify dynamically allocated managed data, such as structures, arrays, or unboxed scalars,
- external types classify external references possibly owned by the embedder.

The values from the latter two hierarchies are interconvertible by ways of the extern.convert\_any and any.convert\_extern instructions. That is, both type hierarchies are inhabited by an isomorphic set of values, but

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<sup>12</sup> https://ieeexplore.ieee.org/document/8766229

may have different, incompatible representations in practice.

```
\begin{array}{rcl} absheap type & ::= & any \mid eq \mid i31 \mid struct \mid array \mid none \\ & \mid & func \mid nofunc \\ & \mid & exn \mid noexn \\ & \mid & extern \mid noextern \\ & \mid & \dots \\ & heap type & ::= & absheap type \mid type use \\ & type use & ::= & type idx \mid \dots \end{array}
```

A heap type is either *abstract* or *concrete*. A concrete heap type consists of a *type use*, which is a type index. It classifies an object of the respective type defined in a module. Abstract types are denoted by individual keywords.

The type func denotes the common supertype of all function types, regardless of their concrete definition. Dually, the type nofunc denotes the common subtype of all function types, regardless of their concrete definition. This type has no values.

The type exn denotes the common supertype of all exception references. This type has no concrete subtypes. Dually, the type noexn denotes the common subtype of all forms of exception references. This type has no values.

The type extern denotes the common supertype of all external references received through the embedder. This type has no concrete subtypes. Dually, the type noextern denotes the common subtype of all forms of external references. This type has no values.

The type any denotes the common supertype of all aggregate types, as well as possibly abstract values produced by *internalizing* an external reference of type extern. Dually, the type none denotes the common subtype of all forms of aggregate types. This type has no values.

The type eq is a subtype of any that includes all types for which references can be compared, i.e., aggregate values and i31.

The types struct and array denote the common supertypes of all structure and array aggregates, respectively.

The type is denotes *unboxed scalars*, that is, integers injected into references. Their observable value range is limited to 31 bits.

#### Note

Values of type i31 are not actually allocated in the store, but represented in a way that allows them to be mixed with actual references into the store without ambiguity. Engines need to perform some form of *pointer tagging* to achieve this, which is why one bit is reserved. Since this type is to be reliably unboxed on all hardware platforms supported by WebAssembly, it cannot be wider than 32 bits minus the tag bit.

Although the types none, nofunc, noexn, and noextern are not inhabited by any values, they can be used to form the types of all null references in their respective hierarchy. For example, (ref null nofunc) is the generic type of a null reference compatible with all function reference types.

The syntax of abstract heap types and type uses is extended with additional forms for the purpose of specifying validation and execution.

## 2.3.4 Reference Types

Reference types classify values that are first-class references to objects in the runtime store.

```
reftype ::= ref null? heaptype
```

A reference type is characterised by the heap type it points to.

In addition, a reference type of the form ref null ht is nullable, meaning that it can either be a proper reference to ht or null. Other references are non-null.

Reference types are *opaque*, meaning that neither their size nor their bit pattern can be observed. Values of reference type can be stored in tables but not in memories.

#### **Conventions**

- The reference type anyref is an abbreviation for (ref null any).
- The reference type eqref is an abbreviation for (ref null eq).
- The reference type is iref is an abbreviation for (ref null is).
- The reference type structref is an abbreviation for (ref null struct).
- The reference type arrayref is an abbreviation for (ref null array).
- The reference type funcref is an abbreviation for (ref null func).
- The reference type exnref is an abbreviation for (ref null exn).
- The reference type externref is an abbreviation for (ref null extern).
- The reference type nullref is an abbreviation for (ref null none).
- The reference type nullfuncref is an abbreviation for (ref null nofunc).
- The reference type nullexnref is an abbreviation for (ref null noexn).
- The reference type nullexternref is an abbreviation for (ref null noextern).

## 2.3.5 Value Types

*Value types* classify the individual values that WebAssembly code can compute with and the values that a variable accepts. They are either number types, vector types, or reference types.

```
consttype ::= numtype \mid vectype
valtype ::= numtype \mid vectype \mid reftype \mid \dots
```

The syntax of value types is extended with additional forms for the purpose of specifying validation.

#### Conventions

ullet The meta variable t ranges over value types or subclasses thereof where clear from context.

### 2.3.6 Result Types

Result types classify the result of executing instructions or functions, which is a sequence of values, written with brackets.

```
resulttype ::= list(valtype)
```

## 2.3.7 Function Types

*Function types* classify the signature of functions, mapping a list of parameters to a list of results. They are also used to classify the inputs and outputs of instructions.

```
functype ::= resulttype \rightarrow resulttype
```

## 2.3.8 Aggregate Types

Aggregate types describe compound objects consisting of multiple values. These are either *structures* or *arrays*, which both consist of a list of possibly mutable, possibly packed *fields*. Structures are heterogeneous, but require static indexing, while arrays need to be homogeneous, but allow dynamic indexing.

```
structtype ::= list(fieldtype)
arraytype ::= fieldtype
fieldtype ::= mut^? storagetype
storagetype ::= valtype | packtype
packtype ::= is | ii6
```

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#### **Conventions**

- The notation |t| for bit width extends to packed types as well, that is, |is| = 8 and |i16| = 16.
- The auxiliary function unpack maps a storage type to the value type obtained when accessing a field:

```
unpack(valtype) = valtype

unpack(packtype) = i32
```

## 2.3.9 Composite Types

Composite types are all types composed from simpler types, including function types and aggregate types.

```
\begin{array}{cccc} comptype & ::= & \mathsf{struct} \ structtype \\ & | & \mathsf{array} \ arraytype \\ & | & \mathsf{func} \ functype \end{array}
```

## 2.3.10 Recursive Types

*Recursive types* denote a group of mutually recursive composite types, each of which can optionally declare a list of type indices of supertypes that it matches. Each type can also be declared *final*, preventing further subtyping.

```
rectype ::= rec list(subtype)
subtype ::= sub final? typeuse* comptype
typeuse ::= typeidx | ...
```

In a module, each member of a recursive type is assigned a separate type index.

The syntax of *type uses* representing these type indices is later extended with additional forms for the purpose of specifying validation and execution.

## 2.3.11 Address Type

Address types are a subset of number types that classify the values that can be used as offsets into memories and tables.

```
addrtype ::= i32 | i64
```

#### Conventions

The minimum of two address types is defined as the address type whose bit width is the minimum of the two.

```
\min(at_1, at_2) = at_1 \text{ if } |at_1| \le |at_2|

\min(at_1, at_2) = at_2 \text{ otherwise}
```

## 2.3.12 Limits

*Limits* classify the size range of resizeable storage associated with memory types and table types.

```
limits ::= [u_{64} \dots u_{64}]
```

## 2.3.13 Memory Types

Memory types classify linear memories and their size range.

```
memtype ::= addrtype \ limits \ page
```

The limits constrain the minimum and optionally the maximum size of a memory. The limits are given in units of page size.

## 2.3.14 Table Types

Table types classify tables over elements of reference type within a size range.

```
table type ::= addrtype \ limits \ reftype
```

Like memories, tables are constrained by limits for their minimum and optionally maximum size. The limits are given in numbers of entries.

## 2.3.15 Global Types

Global types classify global variables, which hold a value and can either be mutable or immutable.

```
globaltype ::= mut? valtype
```

## 2.3.16 Tag Types

Tag types classify the signature of tags with a defined type deftype, which expands to a function type functype.

```
tagtype ::= deftype
```

Tags are used for categorizing exceptions. The parameters of functype define the list of values associated with the exception thrown with this tag. Furthermore, it is an invariant of the semantics that every functype in a valid tag type for an exception has an empty result type.

#### Note

Future versions of WebAssembly may have additional uses for tags, and may allow non-empty result types in the function types of tags.

## 2.3.17 Element Types

Element types classify element segments by the reference type of its elements.

```
elemtype ::= reftype
```

## 2.3.18 Data Types

Data types classify data segments. Since the contents of a data segment requires no further classification, they merely consist of a universal marker ok indicating well-formedness.

```
datatype ::= ok
```

## 2.3.19 External Types

External types classify imports and external addresses with their respective types.

```
externtype ::= func typeuse | global qlobaltype | table tabletype | mem memtype | tag typeuse
```

For functions and tags, the type index has to refer to the definition of a function type. In the case of a tag, the parameters of the function type define the list of values associated with the exception thrown with this tag. The result type is empty for exception tags.

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#### Note

Future versions of WebAssembly may have additional uses for tags, and may allow non-empty result types in the function types of tags.

#### **Conventions**

The following auxiliary notation is defined for sequences of external types. It filters out entries of a specific kind in an order-preserving fashion:

```
funcs(\epsilon)
funcs((func dt) xt^*)
                                   dt \text{ funcs}(xt^*)
funcs(externtype xt^*)
                                  funcs(xt^*)
                                                       otherwise
tables(\epsilon)
                              =
tables((table tt) xt^*)
                              = tt \text{ tables}(xt^*)
tables(externtype xt^*)
                                  tables(xt^*)
                                                       otherwise
mems(\epsilon)
                              =
mems((mem mt) xt^*)
                                  mt \text{ mems}(xt^*)
                             =
mems(externtype xt^*)
                             =
                                  mems(xt^*)
                                                       otherwise
globals(\epsilon)
                              =
                                   \epsilon
globals((global gt) xt^*)
                             =
                                   gt \text{ globals}(xt^*)
globals(externtype xt^*) =
                                  globals(xt^*)
                                                       otherwise
tags(\epsilon)
tags((tag jt) xt^*)
                              = jt \operatorname{tags}(xt^*)
tags(externtype xt^*)
                                                       otherwise
                             = tags(xt^*)
```

## 2.4 Instructions

WebAssembly code consists of sequences of *instructions*. Its computational model is based on a *stack machine* in that instructions manipulate values on an implicit *operand stack*, consuming (popping) argument values and producing or returning (pushing) result values.

In addition to dynamic operands from the stack, some instructions also have static *immediate* arguments, typically indices or type annotations, which are part of the instruction itself.

Some instructions are structured in that they contain nested sequences of instructions.

The following sections group instructions into a number of different categories.

The syntax of instruction is further extended with additional forms for the purpose of specifying execution.

#### 2.4.1 Parametric Instructions

Instructions in this group can operate on operands of any value type.

```
instr ::= nop

| unreachable

| drop

| select (valtype^*)^?
```

The nop instruction does nothing.

The unreachable instruction causes an unconditional trap.

The drop instruction simply throws away a single operand.

The select instruction selects one of its first two operands based on whether its third operand is zero or not. It may include a value type determining the type of these operands. If the type immediate is absent, the operands must be of numeric type.

#### Note

In future versions of WebAssembly, the type annotation on select may allow for more than a single value being selected at the same time.

#### 2.4.2 Numeric Instructions

Numeric instructions provide basic operations over numeric values of specific type. These operations closely match respective operations available in hardware.

```
::= 8 | 16 | 32 | 64
               ::= u | s
      num_{iN} ::= iN
      num_{fN} ::= fN
        instr ::= ...
                   | numtype.const num_{numtype}|
                     numtype.unop_{numtype}
                     numtype.binop_{\,numtype}
                     numtype.testop_{numtype}
                       numtype.relop_{numtype}
                       numtype_1.cvtop_{\,numtype_2,numtype_1}\_numtype_2
     unop_{iN} ::= clz | ctz | popcnt | extend sz_s
                                                                              if sz < N
     unop_{fN} ::= abs \mid neg \mid sqrt \mid ceil \mid floor \mid trunc \mid nearest
     binop_{iN} ::= add | sub | mul | div_sx | rem_sx
                       and or xor shl shr_sx rotl rotr
                       add | sub | mul | div | min | max | copysign
     binop_{fN}
               ::=
    testop_{iN}
                       eqz
     relop_{iN} ::= eq | ne | lt_sx | gt_sx | le_sx | ge_sx
     relop_{fN} ::= eq | ne | It | gt | le | ge
cvtop_{\mathsf{i}N_1,\mathsf{i}N_2} \quad ::= \quad \mathsf{extend}\_sx
                                                                              if N_1 < N_2
                                                                              if N_1 > N_2
                 wrap
                      convert_sx
cvtop_{iN_1,fN_2} ::=
                 reinterpret
                                                                              if N_1 = N_2
cvtop_{\mathsf{f}N_1,\mathsf{i}N_2} \ ::= \ \mathsf{trunc}\_sx
                       trunc_sat_sx
                   reinterpret
                                                                              if N_1 = N_2
cvtop_{\mathsf{f}N_1,\mathsf{f}N_2}\quad ::=\quad \mathsf{promote}
                                                                              if N_1 < N_2
                                                                              if N_1 > N_2
                      demote
```

Numeric instructions are divided by number type. For each type, several subcategories can be distinguished:

- Constants: return a static constant.
- *Unary Operations*: consume one operand and produce one result of the respective type.
- Binary Operations: consume two operands and produce one result of the respective type.
- Tests: consume one operand of the respective type and produce a Boolean integer result.
- Comparisons: consume two operands of the respective type and produce a Boolean integer result.
- *Conversions*: consume a value of one type and produce a result of another (the source type of the conversion is the one after the "\_").

Some integer instructions come in two flavors, where a signedness annotation sx distinguishes whether the operands are to be interpreted as unsigned or signed integers. For the other integer instructions, the use of two's complement for the signed interpretation means that they behave the same regardless of signedness.

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#### 2.4.3 Vector Instructions

Vector instructions (also known as *SIMD* instructions, *single instruction multiple data*) provide basic operations over values of vector type.

```
lanetype ::= numtype \mid packtype
                 dim ::= 1 | 2 | 4 | 8 | 16
                                                                                                                          if |lanetype| \cdot dim = 128
               shape ::= lanetype \times dim
              ishape ::= shape
                                                                                                                          if lanetype(shape) = iN
             bshape
                                                                                                                          if lanetype(shape) = i8
                        ::=
                               shape
                                                                                                                          if 2 \cdot N_1 = N_2
half_{iN_1 \times M_1, iN_2 \times M_2}
                         ::=
                               low | high
                                                                                                                          if 2 \cdot N_1 = N_2 = 64
half_{iN_1 \times M_1, fN_2 \times M_2}
                         ::=
                               low
                                                                                                                          if 2 \cdot N_2 = N_1 = 64
zero_{\mathsf{f}N_1 \times M_1, \mathsf{i}N_2 \times M_2} \quad ::= \quad
                                zero
             laneidx ::=
                instr ::=
                               vectype.const vec_{vectype}
                                vectype.vvunop
                                vectype.vvbinop
                                vectype.vvternop
                                vectype.vvtestop
                                shape.vunop_{\, shape}
                                shape.vbinop_{shape}
                                shape.vternop_{shape}
                                shape.vtestop_{shape}
                                shape.vrelop_{shape}
                                ishape.vshiftop_{ishape}
                                ishape. bitmask
                                bshape.vswizzlop_{bshape} \\ bshape.shuffle \ laneidx^*
                                                                                                                          if |laneidx^*| = \dim(bshape)
                                ishape_1.vextunop_{ishape_2,ishape_1}\_ishape_2
                                ishape_1.vextbinop_{ishape_2,ishape_1}\_ishape_2
                                is hap e_1.vext tern op_{ishap e_2, ishap e_1}\_ishap e_2
                                                                                                                         if |lanetype(ishape_2)| = 2.
                                ishape_1.narrow\_ishape_2\_sx
                                shape_1.vevtop_{shape_2,shape_1}\_zero_{shape_2,shape_1}^?\_shape_2\_half_{shape_2,shape_1}^?
                                shape.splat
                                                                                                                         if sx^? = \epsilon \Leftrightarrow \text{lanetype}(shap)
                                shape.extract lane sx^? laneidx
                                shape.replace lane laneidx
```

Vector instructions have a naming convention involving a *shape* prefix that determines how their operands will be interpreted, written  $t \times N$ , and consisting of a *lane type t*, a possibly *packed* numeric type, and its *dimension* N, which denotes the number of lanes of that type. Operations are performed point-wise on the values of each lane.

Instructions prefixed with  $v_{128}$  do not involve a specific interpretation, and treat the  $v_{128}$  as either an  $i_{128}$  value or a vector of 128 individual bits.

#### Note

For example, the shape  $i32\times4$  interprets the operand as four i32 values, packed into an i128. The bit width of the lane type t times N always is 128.

```
vvunop ::= not
                    vvbinop ::= and | andnot | or | xor
                   vvternop ::= bitselect
                    vvtestop ::= any_true
                                 ::= abs | neg
                vunop_{iN\times M}
                                  popcnt
                                                                                                     if N = 8
                vunop_{\mathsf{f}N\times M}
                                        abs | neg | sqrt | ceil | floor | trunc | nearest
                vbinop_{iN \times M}
                                        add
                                ::=
                                         sub
                                                                                                     if N \leq 16
                                         \mathsf{add\_sat\_}\mathit{sx}
                                        sub_sat_sx
                                                                                                     if N \leq 16
                                                                                                     if N \geq 16
                                     mul
                                                                                                     if N \leq 16
                                     avgr_u
                                                                                                     if N = 16
                                      q15mulr_sat_s
                                                                                                     if N = 16
                                      relaxed_q15mulr_s
                                                                                                     if N \leq 32
                                     \min sx
                                    max_sx
                                                                                                     if N \leq 32
               vbinop_{\mathsf{f}N\times M}
                                ::= add | sub | mul | div | min | max | pmin | pmax
                                  relaxed_min | relaxed_max
                                 ::= relaxed laneselect
              vternop_{iN\times M}
              vternop_{\mathsf{f}N\times M}
                                 ::= relaxed madd | relaxed nmadd
               vtestop_{\mathrm{i}N\times M}
                                 ::= all_true
                vrelop_{\mathrm{i}N\times M}
                                ::= eq | ne
                                                                                                     if N \neq 64 \lor sx = s
                                    lt sx
                                    gt_sx
                                                                                                     if N \neq 64 \vee sx = s
                                                                                                     if N \neq 64 \lor sx = s
                                    le_sx
                                   ge_sx
                                                                                                     if N \neq 64 \lor sx = s
                vrelop_{\mathsf{f}N\times M}
                                ::= eq | ne | It | gt | le | ge
                                 ::= swizzle | relaxed_swizzle
             vswizzlop_{i8\times M}
              vshiftop_{iN \times M}
                                 ::= shl | shr_sx
 vextunop_{iN_1 \times M_1, iN_2 \times M_2}
                                 ::= extadd_pairwise_sx
                                                                                                     if 16 \le 2 \cdot N_1 = N_2 \le 32
                                 ::= \quad \mathsf{extmul}\_\mathit{sx}\_\mathit{half}_{\mathsf{i}N_1 \times M_1, \mathsf{i}N_2 \times M_2}
                                                                                                     if 2 \cdot N_1 = N_2 \ge 16
 vextbinop_{iN_1 \times M_1, iN_2 \times M_2}
                                                                                                     if 2 \cdot N_1 = N_2 = 32
                                  dot s
                                    relaxed dot s
                                                                                                     if 2 \cdot N_1 = N_2 = 16
vextternop_{iN_1 \times M_1, iN_2 \times M_2}
                                ::= relaxed_dot_add_s
                                                                                                     if 4 \cdot N_1 = N_2 = 32
                                                                                                     if N_2 = 2 \cdot N_1
     vcvtop_{iN_1 \times M_1, iN_2 \times M_2}
                                ::= extend_sx
                                                                                                     if N_2 \geq N_1 = 32
    vcvtop_{\mathsf{i}N_1 \times M_1, \mathsf{f}N_2 \times M_2}
                                 ::= convert_sx
                                                                                                     if N_1 \ge N_2 = 32
    vcvtop_{\mathsf{f}N_1 \times M_1, \mathsf{i}N_2 \times M_2}
                                 ::= trunc_sat_sx
                                                                                                     if N_1 \geq N_2 = 32
                                  relaxed_trunc_sx
                                 ::= demote
                                                                                                     if N_1 > N_2
    vcvtop_{fN_1 \times M_1, fN_2 \times M_2}
                                                                                                     if N_1 < N_2
                                         promote
```

Vector instructions can be grouped into several subcategories:

- Constants: return a static constant.
- Unary Operations: consume one v128 operand and produce one v128 result.
- Binary Operations: consume two v128 operands and produce one v128 result.
- Ternary Operations: consume three v128 operands and produce one v128 result.
- Tests: consume one v128 operand and produce a Boolean integer result.
- Shifts: consume a v128 operand and an i32 operand, producing one v128 result.

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- Splats: consume a value of numeric type and produce a v128 result of a specified shape.
- Extract lanes: consume a v128 operand and return the numeric value in a given lane.
- Replace lanes: consume a v128 operand and a numeric value for a given lane, and produce a v128 result.

Some vector instructions have a signedness annotation sx which distinguishes whether the elements in the operands are to be interpreted as unsigned or signed integers. For the other vector instructions, the use of two's complement for the signed interpretation means that they behave the same regardless of signedness.

#### **Conventions**

- The function lanetype(*shape*) extracts the lane type of a shape.
- The function  $\dim(shape)$  extracts the dimension of a shape.

#### 2.4.4 Reference Instructions

Instructions in this group are concerned with accessing references.

The ref.null and ref.func instructions produce a null value or a reference to a given function, respectively.

The instruction ref.is\_null checks for null, while ref.as\_non\_null converts a nullable to a non-null one, and traps if it encounters null.

The ref.eq compares two references.

The instructions ref.test and ref.cast test the dynamic type of a reference operand. The former merely returns the result of the test, while the latter performs a downcast and traps if the operand's type does not match.

#### Note

The br\_on\_null and br\_on\_non\_null instructions provide versions of ref.as\_null that branch depending on the success of failure of a null test instead of trapping. Similarly, the br\_on\_cast and br\_on\_cast\_fail instructions provides versions of ref.cast that branch depending on the success of the downcast instead of trapping.

An additional instruction operating on function references is the control instruction call\_ref.

## 2.4.5 Aggregate Instructions

Instructions in this group are concerned with creating and accessing references to aggregate types.

```
instr ::= ...
            struct.new typeidx
            struct.new_default typeidx
            struct.get_sx? typeidx u32
            struct.set typeidx u32
            array.new typeidx
            array.new_default typeidx
            array.new_fixed typeidx u32
            array.new_data typeidx dataidx
            array.new elem typeidx elemidx
            array.get sx? typeidx
            array.set typeidx
            array.len
            array.fill typeidx
            array.copy typeidx typeidx
            array.init_data typeidx dataidx
            array.init\_elem \ typeidx \ elemidx
            ref.i31
            i31.get\_sx
            extern.convert any
            any.convert_extern
```

The instructions struct.new and struct.new\_default allocate a new structure, initializing them either with operands or with default values. The remaining instructions on structs access individual fields, allowing for different sign extension modes in the case of packed storage types.

Similarly, arrays can be allocated either with an explicit initialization operand or a default value. Furthermore, array.new\_fixed allocates an array with statically fixed size, and array.new\_data and array.new\_elem allocate an array and initialize it from a data or element segment, respectively. The instructions array.get, array.get sx, and array.set access individual slots, again allowing for different sign extension modes in the case of a packed storage type; array.len produces the length of an array; array.fill fills a specified slice of an array with a given value and array.copy, array.init\_data, and array.init\_elem copy elements to a specified slice of an array from a given array, data segment, or element segment, respectively.

The instructions ref.i31 and i31.get sx convert between type i32 and an unboxed scalar.

The instructions any.convert\_extern and extern.convert\_any allow lossless conversion between references represented as type (ref null extern) and as (ref null any).

#### 2.4.6 Variable Instructions

Variable instructions are concerned with access to local or global variables.

These instructions get or set the values of respective variables. The local tee instruction is like local set but also returns its argument.

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#### 2.4.7 Table Instructions

Instructions in this group are concerned with tables table.

The table.get and table.set instructions load or store an element in a table, respectively.

The table.size instruction returns the current size of a table. The table.grow instruction grows table by a given delta and returns the previous size, or -1 if enough space cannot be allocated. It also takes an initialization value for the newly allocated entries.

The table.fill instruction sets all entries in a range to a given value. The table.copy instruction copies elements from a source table region to a possibly overlapping destination region; the first index denotes the destination. The table.init instruction copies elements from a passive element segment into a table.

The elem.drop instruction prevents further use of a passive element segment. This instruction is intended to be used as an optimization hint. After an element segment is dropped its elements can no longer be retrieved, so the memory used by this segment may be freed.

#### Note

An additional instruction that accesses a table is the control instruction call\_indirect.

## 2.4.8 Memory Instructions

Instructions in this group are concerned with linear memory.

```
memarg ::= \{align u32, offset u32\}
                                                                    if sz < N
     loadop_{iN} ::= sz\_sx
                                                                    if sz < N
    storeop_{:N} ::= sz
                                                                    if sz \cdot M = |vectype|/2
vloadop_{vectype} ::= sz \times M_sx
                sz_splat
                                                                    if sz > 32
                sz_zero
        instr ::= ...
                    numtype.\mathsf{load} loadop'_{numtype} \ memidx \ memarg
                    numtype.\mathsf{store}storeop_{numtype}^? memidx\ memarg
                     vectype.loadvloadop? memidx memarg
                     vectype.loadsz_lane memidx memarg laneidx
                    vectype.store memidx memarg
                    vectype.storesz lane memidx memarg laneidx
                    memory.size memidx
                    memory.grow memidx
                     memory.fill memidx
                     memory.copy memidx memidx
                     memory.init memidx dataidx
                     data.drop dataidx
```

Memory is accessed with load and store instructions for the different number types and *vector types <syntax-vectype>*. They all take a memory index and a *memory argument memarg* that contains an address *offset* and the expected *alignment* (expressed as the exponent of a power of 2).

Integer loads and stores can optionally specify a *storage size sz* that is smaller than the bit width of the respective value type. In the case of loads, a sign extension mode *sx* is then required to select appropriate behavior.

Vector loads can specify a shape that is half the bit width of  $v_{128}$ . Each lane is half its usual size, and the sign extension mode sx then specifies how the smaller lane is extended to the larger lane. Alternatively, vector loads can perform a splat, such that only a single lane of the specified storage size is loaded, and the result is duplicated to all lanes.

The static address offset is added to the dynamic address operand, yielding a 33-bit or 65-bit *effective address* that is the zero-based index at which the memory is accessed. All values are read and written in little endian<sup>13</sup> byte order. A trap results if any of the accessed memory bytes lies outside the address range implied by the memory's current size.

The memory.size instruction returns the current size of a memory. The memory.grow instruction grows a memory by a given delta and returns the previous size, or -1 if enough memory cannot be allocated. Both instructions operate in units of page size.

The memory.fill instruction sets all values in a region of a memory to a given byte. The memory.copy instruction copies data from a source memory region to a possibly overlapping destination region in another or the same memory; the first index denotes the destination The memory.init instruction copies data from a passive data segment into a memory.

The data.drop instruction prevents further use of a passive data segment. This instruction is intended to be used as an optimization hint. After a data segment is dropped its data can no longer be retrieved, so the memory used by this segment may be freed.

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<sup>13</sup> https://en.wikipedia.org/wiki/Endianness#Little-endian

#### 2.4.9 Control Instructions

Instructions in this group affect the flow of control.

```
blocktype ::= valtype^?
           funcidx
    instr ::= ...
             | block blocktype instr*
                 loop blocktype instr*
                 if blocktype instr* else instr*
                 br labelidx
                 br if labelidx
                 br_table labelidx^* labelidx
                 br_on_null labelidx
                 br_on_non_null labelidx
                 br_on_cast labelidx reftype reftype
                 br_on_cast_fail labelidx reftype reftype
                 call funcidx
                 call_ref typeuse
                 call_indirect tableidx typeuse
                 return
                 return call funcidx
                 return call ref typeuse
                 return_call_indirect tableidx typeuse
                 throw tagidx
                 throw ref
                 try_table blocktype list(catch) instr*
   catch ::= catch tagidx labelidx
                 catch\_ref tagidx labelidx
                 catch_all labelidx
                 catch\_all\_ref\ labelidx
```

The block, loop, if and try\_table instructions are *structured* instructions. They bracket nested sequences of instructions, called *blocks*, terminated with, or separated by, end or else pseudo-instructions. As the grammar prescribes, they must be well-nested.

A structured instruction can consume *input* and produce *output* on the operand stack according to its annotated *block type*. It is given either as a type index that refers to a suitable function type reinterpreted as an instruction type, or as an optional value type inline, which is a shorthand for the instruction type  $\epsilon \to valtype^2$ .

Each structured control instruction introduces an implicit *label*. Labels are targets for branch instructions that reference them with *label* indices. Unlike with other index spaces, indexing of labels is relative by nesting depth, that is, label 0 refers to the innermost structured control instruction enclosing the referring branch instruction, while increasing indices refer to those farther out. Consequently, labels can only be referenced from *within* the associated structured control instruction. This also implies that branches can only be directed outwards, "breaking" from the block of the control construct they target. The exact effect depends on that control construct. In case of block or if it is a *forward jump*, resuming execution after the matching end. In case of loop it is a *backward jump* to the beginning of the loop.

#### Note

This enforces *structured control flow*. Intuitively, a branch targeting a block or if behaves like a break statement in most C-like languages, while a branch targeting a loop behaves like a continue statement.

Branch instructions come in several flavors: br performs an unconditional branch, br\_if performs a conditional branch, and br\_table performs an indirect branch through an operand indexing into the label list that is an immediate to the instruction, or to a default target if the operand is out of bounds. The br\_on\_null and br\_on\_non\_null instructions check whether a reference operand is null and branch if that is the case or not the case, respectively.

Similarly, br\_on\_cast and br\_on\_cast\_fail attempt a downcast on a reference operand and branch if that succeeds, or fails, respectively.

The return instruction is a shortcut for an unconditional branch to the outermost block, which implicitly is the body of the current function. Taking a branch *unwinds* the operand stack up to the height where the targeted structured control instruction was entered. However, branches may additionally consume operands themselves, which they push back on the operand stack after unwinding. Forward branches require operands according to the output of the targeted block's type, i.e., represent the values produced by the terminated block. Backward branches require operands according to the input of the targeted block's type, i.e., represent the values consumed by the restarted block.

The call instruction invokes another function, consuming the necessary arguments from the stack and returning the result values of the call. The call\_ref instruction invokes a function indirectly through a function reference operand. The call\_indirect instruction calls a function indirectly through an operand indexing into a table that is denoted by a table index and must contain function references. Since it may contain functions of heterogeneous type, the callee is dynamically checked against the function type indexed by the instruction's second immediate, and the call is aborted with a trap if it does not match.

The return\_call, return\_call\_ref, and return\_call\_indirect instructions are *tail-call* variants of the previous ones. That is, they first return from the current function before actually performing the respective call. It is guaranteed that no sequence of nested calls using only these instructions can cause resource exhaustion due to hitting an implementation's limit on the number of active calls.

The instructions throw, throw\_ref, and try\_table are concerned with *exceptions*. The throw and throw\_ref instructions raise and reraise an exception, respectively, and transfers control to the innermost enclosing exception handler that has a matching catch clause. The try\_table instruction installs an exception *handler* that handles exceptions as specified by its catch clauses.

## 2.4.10 Expressions

Function bodies, initialization values for globals, elements and offsets of element segments, and offsets of data segments are given as expressions, which are sequences of instructions.

```
expr ::= instr^*
```

In some places, validation restricts expressions to be *constant*, which limits the set of allowable instructions.

## 2.5 Modules

WebAssembly programs are organized into *modules*, which are the unit of deployment, loading, and compilation. A module collects definitions for types, functions, tables, memories, tags, and globals. In addition, it can declare imports and exports and provide initialization in the form of data and element segments, or a start function.

```
module ::= module type* import* func* global* table* mem* tag* elem* data* start? export*
```

Each of the lists — and thus the entire module — may be empty.

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#### 2.5.1 Indices

Definitions are referenced with zero-based *indices*. Each class of definition has its own *index space*, as distinguished by the following classes.

```
typeidx
             idx
        ::=
funcidx ::=
             idx
globalidx ::= idx
tableidx ::= idx
memidx ::=
             idx
 tagidx ::=
             idx
elemidx ::=
             idx
dataidx ::= idx
labelidx ::= idx
localidx ::= idx
fieldidx ::= idx
```

The index space for functions, tables, memories, globals, and tags includes respective imports declared in the same module. The indices of these imports precede the indices of other definitions in the same index space.

Element indices reference element segments and data indices reference data segments.

The index space for locals is only accessible inside a function and includes the parameters of that function, which precede the local variables.

Label indices reference structured control instructions inside an instruction sequence.

Each aggregate type provides an index space for its fields.

#### **Conventions**

- The meta variable *l* ranges over label indices.
- ullet The meta variables x,y range over indices in any of the other index spaces.
- For every index space abcidx, the notation abcidx(A) denotes the set of indices from that index space occurring free in A. Sometimes this set is reinterpreted as the list of its elements.

#### Note

```
For example, if instr^* is (data.drop 1) (memory.init 2 3), then dataidx_{instrs}(instr^*) = 1 3, or equivalently, the set \{1,3\}.
```

## **2.5.2 Types**

The *type* section of a module defines a list of recursive types, each consisting of a list of sub types referenced by individual type indices. All function or aggregate types used in a module must be defined in this section.

```
type ::= type \ rectype
```

#### 2.5.3 Functions

The *func* section of a module defines a list of *functions* with the following structure:

```
func ::= func typeidx local^* expr local ::= local valtype
```

The type index of a function declares its signature by reference to a function type defined in the module. The parameters of the function are referenced through 0-based local indices in the function's body; they are mutable.

The locals declare a list of mutable local variables and their types. These variables are referenced through local indices in the function's body. The index of the first local is the smallest index not referencing a parameter.

A function's expression is an instruction sequence that represents the body of the function. Upon termination it must produce a stack matching the function type's result type.

Functions are referenced through function indices, starting with the smallest index not referencing a function import.

#### **2.5.4 Tables**

The table section of a module defines a list of tables described by their table type:

```
table ::= table \ table type \ expr
```

A table is an array of opaque values of a particular reference type that is specified by the table type. Each table slot is initialized with a value given by a constant initializer expression. Tables can further be initialized through element segments.

The minimum size in the limits of the table type specifies the initial size of that table, while its maximum restricts the size to which it can grow later.

Tables are referenced through table indices, starting with the smallest index not referencing a table import. Most constructs implicitly reference table index 0.

#### 2.5.5 Memories

The *mem* section of a module defines a list of *linear memories* (or *memories* for short) as described by their memory type:

```
mem ::= memory memtype
```

A memory is a list of raw uninterpreted bytes. The minimum size in the limits of its memory type specifies the initial size of that memory, while its maximum, if present, restricts the size to which it can grow later. Both are in units of page size.

Memories can be initialized through data segments.

Memories are referenced through memory indices, starting with the smallest index not referencing a memory import. Most constructs implicitly reference memory index 0.

#### 2.5.6 Globals

The *global* section of a module defines a list of *global variables* (or *globals* for short):

```
global ::= global global type expr
```

Each global stores a single value of the type specified in the global type. It also specifies whether a global is immutable or mutable. Moreover, each global is initialized with a value given by a constant initializer expression.

Globals are referenced through global indices, starting with the smallest index not referencing a global import.

#### 2.5.7 Tags

The tag section of a module defines a list of tags:

```
tag ::= tag typeidx
```

The type index of a tag must refer to a function type that declares its tag type.

Tags are referenced through tag indices, starting with the smallest index not referencing a tag import.

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## 2.5.8 Element Segments

The *elem* section of a module defines a list of *element segments*, which can be used to initialize a subrange of a table from a static list of elements.

```
elem ::= elem reftype expr* elemmode
elemmode ::= active tableidx expr | passive | declare
```

Each element segment defines a reference type and a corresponding list of constant element expressions.

Element segments have a mode that identifies them as either *active*, *passive*, or *declarative*. A passive element segment's elements can be copied to a table using the table.init instruction. An active element segment copies its elements into a table during instantiation, as specified by a table index and a constant expression defining an offset into that table. A declarative element segment is not available at runtime but merely serves to forward-declare references that are formed in code with instructions like ref.func. The offset is given by another constant expression.

Element segments are referenced through element indices.

## 2.5.9 Data Segments

The *data* section of a module defines a list of *data segments*, which can be used to initialize a range of memory from a static list of bytes.

Similar to element segments, data segments have a mode that identifies them as either *active* or *passive*. A passive data segment's contents can be copied into a memory using the memory.init instruction. An active data segment copies its contents into a memory during instantiation, as specified by a memory index and a constant expression defining an offset into that memory.

Data segments are referenced through data indices.

#### 2.5.10 Start Function

The *start* section of a module declares the function index of a *start function* that is automatically invoked when the module is instantiated, after tables and memories have been initialized.

```
start ::= start funcidx
```

### Note

The start function is intended for initializing the state of a module. The module and its exports are not accessible externally before this initialization has completed.

## **2.5.11 Exports**

The *export* section of a module defines a set of *exports* that become accessible to the host environment once the module has been instantiated.

```
\begin{array}{lll} export & ::= & \mathsf{export} \ name \ externidx \\ externidx & ::= & \mathsf{func} \ funcidx \ | \ \mathsf{global} \ globalidx \ | \ \mathsf{table} \ tableidx \ | \ \mathsf{memory} \ memidx \ | \ \mathsf{tag} \ tagidx \end{array}
```

Each export is labeled by a unique name. Exportable definitions are functions, tables, memories, globals, and tags, which are referenced through a respective index.

#### **Conventions**

The following auxiliary notation is defined for sequences of exports, filtering out indices of a specific kind in an order-preserving fashion:

```
funcs(\epsilon)
funcs((func x) xx^*)
                                  x \text{ funcs}(xx^*)
funcs(externidx xx^*)
                                  funcs(xx^*)
                                                      otherwise
tables(\epsilon)
tables((table x) xx^*)
                                  x \text{ tables}(xx^*)
tables(externidx xx^*)
                              = tables(xx^*)
                                                      otherwise
mems(\epsilon)
mems((memory x) xx^*)
                                   x \text{ mems}(xx^*)
mems(externidx xx^*)
                              =
                                  mems(xx^*)
                                                      otherwise
globals(\epsilon)
globals((global x) xx^*)
                                   x \text{ globals}(xx^*)
                              =
globals(externidx xx^*)
                              =
                                  globals(xx^*)
                                                      otherwise
tags((tag x) xx^*)
                                  x \operatorname{tags}(xx^*)
tags(externidx xx^*)
                                                      otherwise
                                  tags(xx^*)
```

## **2.5.12 Imports**

The *import* section of a module defines a set of *imports* that are required for instantiation.

```
import ::= import name name externtype
```

Each import is labeled by a two-level name space, consisting of a *module name* and an *item name* for an entity within that module. Importable definitions are functions, tables, memories, globals, and tags. Each import is specified by a respective external type that a definition provided during instantiation is required to match.

Every import defines an index in the respective index space. In each index space, the indices of imports go before the first index of any definition contained in the module itself.

#### Note

Unlike export names, import names are not necessarily unique. It is possible to import the same module/item name pair multiple times; such imports may even have different type descriptions, including different kinds of entities. A module with such imports can still be instantiated depending on the specifics of how an embedder allows resolving and supplying imports. However, embedders are not required to support such overloading, and a WebAssembly module itself cannot implement an overloaded name.

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## CHAPTER 3

Validation

## 3.1 Conventions

Validation checks that a WebAssembly module is well-formed. Only valid modules can be instantiated.

Validity is defined by a *type system* over the abstract syntax of a module and its contents. For each piece of abstract syntax, there is a typing rule that specifies the constraints that apply to it. All rules are given in two *equivalent* forms:

- 1. In *prose*, describing the meaning in intuitive form.
- 2. In formal notation, describing the rule in mathematical form. 14

#### Note

The prose and formal rules are equivalent, so that understanding of the formal notation is *not* required to read this specification. The formalism offers a more concise description in notation that is used widely in programming languages semantics and is readily amenable to mathematical proof.

In both cases, the rules are formulated in a *declarative* manner. That is, they only formulate the constraints, they do not define an algorithm. The skeleton of a sound and complete algorithm for type-checking instruction sequences according to this specification is provided in the appendix.

## **3.1.1 Types**

To define the semantics, the definition of some sorts of types is extended to include additional forms. By virtue of not being representable in either the binary format or the text format, these forms cannot be used in a program; they only occur during validation or execution.

```
\begin{array}{cccc} valtype & ::= & \dots & | \ bot \\ absheaptype & ::= & \dots & | \ bot \\ typeuse & ::= & \dots & | \ deftype \ | \ rec \ n \end{array}
```

The unique value type bot is a *bottom type* that matches all value types. Similarly, bot is also used as a bottom type of all heap types.

<sup>&</sup>lt;sup>14</sup> The semantics is derived from the following article: Andreas Haas, Andreas Rossberg, Derek Schuff, Ben Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman. Bringing the Web up to Speed with WebAssembly<sup>15</sup>. Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017). ACM 2017.

<sup>&</sup>lt;sup>15</sup> https://dl.acm.org/citation.cfm?doid=3062341.3062363

#### Note

No validation rule uses bottom types explicitly, but various rules can pick any value or heap type, including bottom. This ensures the existence of principal types, and thus a validation algorithm without back tracking.

A type use can consist directly of a defined type. This occurs as the result of substituting a type index with its definition.

A type use may also be a *recursive type index*. Such an index refers to the *i*-th component of a surrounding recursive type. It occurs as the result of rolling up the definition of a recursive type.

Both extensions affect occurrences of type uses in concrete heap types, in sub types and in instructions.

A type of any form is *closed* when it does not contain a heap type that is a type index or a recursive type index without a surrounding recursive type, i.e., all type indices have been substituted with their defined type and all free recursive type indices have been unrolled.

#### Note

It is an invariant of the semantics that sub types occur only in one of two forms: either as "syntactic" types as in a source module, where all supertypes are type indices, or as "semantic" types, where all supertypes are resolved to either defined types or recursive type indices.

Recursive type indices are internal to a recursive type. They are distinguished from regular type indices and represented such that two closed types are syntactically equal if and only if they have the same recursive structure.

#### Convention

• The difference  $rt_1 \setminus rt_2$  between two reference types is defined as follows:

```
\begin{array}{lll} (\operatorname{ref\ null}_1^2\,ht_1) \setminus (\operatorname{ref\ null}\,ht_2) & = & (\operatorname{ref\ }ht_1) \\ (\operatorname{ref\ null}_1^2\,ht_1) \setminus (\operatorname{ref\ }ht_2) & = & (\operatorname{ref\ null}_1^2\,ht_1) \end{array}
```

#### Note

This definition computes an approximation of the reference type that is inhabited by all values from  $rt_1$  except those from  $rt_2$ . Since the type system does not have general union types, the definition only affects the presence of null and cannot express the absence of other values.

## 3.1.2 Defined Types

*Defined types* denote the individual types defined in a module. Each such type is represented as a projection from the recursive type group it originates from, indexed by its position in that group.

```
deftype ::= rectype.n
```

Defined types do not occur in the binary or text format, but are formed by rolling up the recursive types defined in a module.

#### Note

It is an invariant of the semantics that all recursive types occurring in defined types are rolled up.

#### Conventions

- $t[x^* := dt^*]$  denotes the parallel *substitution* of type indices  $x^*$  with corresponding defined types  $dt^*$  in type t, provided  $|x^*| = |dt^*|$ .
- $t[(\text{rec }i)^* := dt^*]$  denotes the parallel substitution of recursive type indices  $(\text{rec }i)^*$  with defined types  $dt^*$  in type t, provided  $|(\text{rec }i)^*| = |dt^*|$ .
- $t[:=dt^*]$  is shorthand for the substitution  $t[x^*:=dt^*]$ , where  $x^*=0$  ...  $(|dt^*|-1)$ .

## 3.1.3 Rolling and Unrolling

In order to allow comparing recursive types for equivalence, their representation is changed such that all type indices internal to the same recursive type are replaced by recursive type indices.

#### Note

This representation is independent of the type index space, so that it is meaningful across module boundaries. Moreover, this representation ensures that types with equivalent recursive structure are also syntactically equal, hence allowing a simple equality check on (closed) types. It gives rise to an *iso-recursive* interpretation of types.

The representation change is performed by two auxiliary operations on the syntax of recursive types:

- Rolling up a recursive type substitutes its internal type indices with corresponding recursive type indices.
- Unrolling a recursive type substitutes its recursive type indices with the corresponding defined types.

These operations are extended to defined types and defined as follows:

In addition, the following auxiliary relation denotes the *expansion* of a defined type:

```
deftype \approx comptype if unroll(deftype) = sub final? typeuse^* comptype
```

## 3.1.4 Tag Types

Tag types classify the signature of tags with a defined type that denotes a function type.

```
tagtype ::= deftype
```

## 3.1.5 Instruction Types

*Instruction types* classify the behaviour of instructions or instruction sequences, by describing how they manipulate the operand stack and the initialization status of locals:

```
instrtype ::= resulttype \rightarrow_{localidx^*} resulttype
```

An instruction type  $t_1^* \to_{x^*} t_2^*$  describes the required input stack with argument values of types  $t_1^*$  that an instruction pops off and the provided output stack with result values of types  $t_2^*$  that it pushes back. Moreover, it enumerates the indices  $x^*$  of locals that have been set by the instruction or sequence.

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#### Note

Instruction types are only used for validation, they do not occur in programs.

## 3.1.6 Local Types

Local types classify locals, by describing their value type as well as their initialization status:

```
local type ::= init val type 
init ::= set | unset
```

#### Note

Local types are only used for validation, they do not occur in programs.

#### 3.1.7 Contexts

Validity of an individual definition is specified relative to a *context*, which collects relevant information about the surrounding module and the definitions in scope:

- Types: the list of types defined in the current module.
- Recursive Types: the list of sub types in the current group of recursive types.
- Functions: the list of functions declared in the current module, represented by a defined type that expands to their function type.
- Tables: the list of tables declared in the current module, represented by their table type.
- Memories: the list of memories declared in the current module, represented by their memory type.
- Globals: the list of globals declared in the current module, represented by their global type.
- Tags: the list of tags declared in the current module, represented by their tag type.
- *Element Segments*: the list of element segments declared in the current module, represented by the elements' reference type.
- Data Segments: the list of data segments declared in the current module, each represented by an ok entry.
- *Locals*: the list of locals declared in the current function (including parameters), represented by their local type.
- Labels: the stack of labels accessible from the current position, represented by their result type.
- *Return*: the return type of the current function, represented as an optional result type that is absent when no return is allowed, as in free-standing expressions.
- *References*: the list of function indices that occur in the module outside functions and can hence be used to form references inside them.

In other words, a context contains a sequence of suitable types for each index space, describing each defined entry in that space. Locals, labels and return type are only used for validating instructions in function bodies, and are left empty elsewhere. The label stack is the only part of the context that changes as validation of an instruction sequence proceeds.

More concretely, contexts are defined as records C with abstract syntax:

```
context ::= {types deftype*
    recs subtype*
    funcs deftype*
    globals globaltype*
    tables tabletype*
    mems memtype*
    tags tagtype*
    elems elemtype*
    datas datatype*
    locals localtype*
    labels resulttype*
    return resulttype
    refs funcidx*}
```

#### Convention

A type of any shape can be *closed* to bring it into closed form relative to a context it is valid in, by substituting each type index x occurring in it with its own corresponding defined type C.types[x], after first closing the types in C.types themselves.

```
\begin{array}{lll} \operatorname{clos}_C(t) & = & t[:=dt^*] & \text{if } dt^* = \operatorname{clos}^*(C.\operatorname{types}) \\ \operatorname{clos}^*(\epsilon) & = & \epsilon \\ \operatorname{clos}^*(dt^* \ dt_n) & = & dt'^* \ dt_n[:=dt'^*] & \text{if } dt'^* = \operatorname{clos}^*(dt^*) \end{array}
```

#### 3.1.8 Prose Notation

Validation is specified by stylised rules for each relevant part of the abstract syntax. The rules not only state constraints defining when a phrase is valid, they also classify it with a type. The following conventions are adopted in stating these rules.

• A phrase A is said to be "valid with type T" if and only if all constraints expressed by the respective rules are met. The form of T depends on the syntactic class of A.

#### Note

For example, if A is a function, then T is a function type; for an A that is a global, T is a global type; and so on.

- The rules implicitly assume a given context C.
- In some places, this context is locally extended to a context C' with additional entries. The formulation "Under context C', ... statement ..." is adopted to express that the following statement must apply under the assumptions embodied in the extended context.

## 3.1.9 Formal Notation

## Note

This section gives a brief explanation of the notation for specifying typing rules formally. For the interested reader, a more thorough introduction can be found in respective text books. <sup>16</sup>

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<sup>&</sup>lt;sup>16</sup> For example: Benjamin Pierce. Types and Programming Languages<sup>17</sup>. The MIT Press 2002

 $<sup>^{17}\</sup> https://www.cis.upenn.edu/~bcpierce/tapl/$ 

The proposition that a phrase A has a respective type T is written A:T. In general, however, typing is dependent on a context C. To express this explicitly, the complete form is a *judgement*  $C \vdash A:T$ , which says that A:T holds under the assumptions encoded in C.

The formal typing rules use a standard approach for specifying type systems, rendering them into *deduction rules*. Every rule has the following general form:

$$\frac{premise_1}{conclusion} \quad \frac{premise_2}{conclusion} \quad \dots \quad \frac{premise_n}{conclusion}$$

Such a rule is read as a big implication: if all premises hold, then the conclusion holds. Some rules have no premises; they are *axioms* whose conclusion holds unconditionally. The conclusion always is a judgment  $C \vdash A : T$ , and there usually is one respective rule for each relevant construct A of the abstract syntax.

#### Note

For example, the typing rule for the i32.add instruction can be given as an axiom:

$$C \vdash \mathsf{i32.add} : \mathsf{i32} \mathrel{\mathsf{i32}} \to \mathsf{i32}$$

The instruction is always valid with type  $i32 i32 \rightarrow i32$  (saying that it consumes two i32 values and produces one), independent of any side conditions.

An instruction like global.get can be typed as follows:

$$\frac{C.\mathsf{globals}[x] = \mathsf{mut}^?\ t}{C \vdash \mathsf{global.get}\ x : \epsilon \to t}$$

Here, the premise enforces that the immediate global index x exists in the context. The instruction produces a value of its respective type t (and does not consume any values). If C.globals[x] does not exist then the premise does not hold, and the instruction is ill-typed.

Finally, a structured instruction requires a recursive rule, where the premise is itself a typing judgement:

$$\frac{C \vdash blocktype: t_1^* \rightarrow t_2^* \quad \{ \text{labels } (t_2^*) \} \oplus C \vdash instr^*: t_1^* \rightarrow t_2^*}{C \vdash block \ blocktype \ instr^*: t_1^* \rightarrow t_2^*}$$

A block instruction is only valid when the instruction sequence in its body is. Moreover, the result type must match the block's annotation blocktype. If so, then the block instruction has the same type as the body. Inside the body an additional label of the corresponding result type is available, which is expressed by extending the context C with the additional label information for the premise.

# 3.2 Types

Simple types, such as number types are universally valid. However, restrictions apply to most other types, such as reference types, function types, as well as the limits of table types and memory types, which must be checked during validation.

Moreover, block types are converted to instruction types for ease of processing.

## 3.2.1 Number Types

The number type numtype is always valid.

$$\overline{C \vdash numtype : \mathsf{ok}}$$

## 3.2.2 Vector Types

The vector type vectype is always valid.

 $\overline{C \vdash vectype : \mathsf{ok}}$ 

## 3.2.3 Heap Types

The heap type absheaptype is always valid.

 $\overline{C \vdash absheaptype : \mathsf{ok}}$ 

The heap type *typeidx* is valid if:

- The defined type C.types[typeidx] exists.
- The defined type C.types [typeidx] is of the form dt.

$$\frac{C.\mathsf{types}[typeidx] = dt}{C \vdash typeidx : \mathsf{ok}}$$

# 3.2.4 Reference Types

The reference type (ref null? heaptype) is valid if:

• The heap type *heaptype* is valid.

$$\frac{C \vdash heaptype : \mathsf{ok}}{C \vdash \mathsf{ref null}^? \ heaptype : \mathsf{ok}}$$

## 3.2.5 Value Types

The value type valtype is valid if:

- Either:
  - The value type valtype is of the form numtype.
  - The number type *numtype* is valid.
- Or:
  - The value type valtype is of the form vectype.
  - The vector type *vectype* is valid.
- Or:
  - The value type valtype is of the form reftype.
  - The reference type reftype is valid.
- Or:
  - The value type valtype is of the form bot.

## 3.2.6 Block Types

Block types may be expressed in one of two forms, both of which are converted to instruction types by the following rules.

The block type typeidx is valid as the instruction type  $t_1^* \rightarrow t_2^*$  if:

• The defined type C.types[typeidx] exists.

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• The expansion of the defined type C-types [typeidx] is the composite type (func  $t_1^* \to t_2^*$ ).

$$\frac{C.\mathsf{types}[typeidx] \approx \mathsf{func}\; (t_1^* \to t_2^*)}{C \vdash typeidx: t_1^* \to t_2^*}$$

The block type  $valtype^?$  is valid as the instruction type  $\epsilon \ o \ valtype^?$  if:

- If *valtype* is defined, then:
  - The value type valtype is valid.

$$\frac{(C \vdash valtype : \mathsf{ok})^?}{C \vdash valtype^? : \epsilon \to valtype^?}$$

## 3.2.7 Result Types

The result type  $t^*$  is valid if:

- For all t in  $t^*$ :
  - The value type t is valid.

$$\frac{(C \vdash t : \mathsf{ok})^*}{C \vdash t^* : \mathsf{ok}}$$

# 3.2.8 Instruction Types

The instruction type  $t_1^* \rightarrow_{x^*} t_2^*$  is valid if:

- The result type  $t_1^*$  is valid.
- The result type  $t_2^*$  is valid.
- The length of  $lt^*$  is equal to the length of  $x^*$ .
- For all x in  $x^*$ :
  - The local type C.locals[x] exists.
- For all lt in  $lt^*$ , and corresponding x in  $x^*$ :
  - The local type C.locals[x] is of the form lt.

### Todo

below is the official specification

$$t_1^* \rightarrow_{x^*} t_2^*$$

- The result type  $t_1^*$  must be valid.
- The result type  $t_2^*$  must be valid.
- Each local index  $x_i$  in  $x^*$  must be defined in the context.
- Then the instruction type is valid.

$$\frac{C \vdash t_1^* : \mathsf{ok} \qquad C \vdash t_2^* : \mathsf{ok} \qquad (C.\mathsf{locals}[x] = \mathit{lt})^*}{C \vdash t_1^* \to_{x^*} t_2^* : \mathsf{ok}}$$

# 3.2.9 Function Types

The function type  $t_1^* \rightarrow t_2^*$  is valid if:

- The result type  $t_1^*$  is valid.
- The result type  $t_2^*$  is valid.

$$\frac{C \vdash t_1^* : \mathsf{ok} \qquad C \vdash t_2^* : \mathsf{ok}}{C \vdash t_1^* \to t_2^* : \mathsf{ok}}$$

## 3.2.10 Composite Types

The composite type (func functype) is valid if:

• The function type functype is valid.

$$\frac{C \vdash functype : \mathsf{ok}}{C \vdash \mathsf{func}\ functype : \mathsf{ok}}$$

The composite type (struct  $fieldtype^*$ ) is valid if:

- For all fieldtype in fieldtype\*:
  - The field type field type is valid.

$$\frac{(C \vdash fieldtype : \mathsf{ok})^*}{C \vdash \mathsf{struct}\, fieldtype^* : \mathsf{ok}}$$

The composite type (array fieldtype) is valid if:

• The field type *fieldtype* is valid.

$$\frac{C \vdash fieldtype : \mathsf{ok}}{C \vdash \mathsf{array}\; fieldtype : \mathsf{ok}}$$

# 3.2.11 Field Types

The field type (mut? storagetype) is valid if:

• The storage type storagetype is valid.

$$\frac{C \vdash storagetype : \mathsf{ok}}{C \vdash \mathsf{mut}^? \ storagetype : \mathsf{ok}}$$

The packed type packtype is always valid.

$$\overline{C \vdash packtype : \mathsf{ok}}$$

## 3.2.12 Recursive Types

Recursive types are validated with respect to the first type index defined by the recursive group.

 $rec \ subtype^*$ 

The recursive type (rec  $subtype'^*$ ) is valid for (ok(x)) if:

- Either:
  - The sub type sequence sequence subtype'\* is empty.
- Or:
  - The sub type sequence sequence subtype'\* is of the form subtype<sub>1</sub> subtype\*.
  - The sub type  $subtype_1$  is valid with (ok(x)).

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- The recursive type (rec  $subtype^*$ ) is valid for (ok(x+1)).

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- Either the sequence *subtype*\* is empty.
- Or:
  - The first sub type of the sequence  $subtype^*$  must be valid for the type index x.
  - The remaining sequence  $subtype^*$  must be valid for the type index x + 1.
- Then the recursive type is valid for the type index x.

$$\frac{C \vdash subtype_1 : \mathsf{ok}((x)) \qquad C \vdash \mathsf{rec} \; subtype^* : \mathsf{ok}((x+1))}{C \vdash \mathsf{rec} \; (subtype_1 \; subtype^*) : \mathsf{ok}((x))}$$

sub final?  $y^*$  comptype

The sub type (sub final?  $x^*$  comptype) is valid with  $(ok(x_0))$  if:

- The length of  $x^*$  is less than or equal to 1.
- For all x in  $x^*$ :
  - The index x is less than  $x_0$ .
- The length of  $comptype'^*$  is equal to the length of  $x^*$ .
- The length of  $comptype'^*$  is equal to the length of  $x'^{**}$ .
- For all x in  $x^*$ :
  - The defined type C.types[x] exists.
- For all *comptype'* in *comptype'*\*, and corresponding x in x\*, and corresponding x'\* in x'\*:
  - The sub type  $\operatorname{unroll}(C.\operatorname{types}[x])$  is of the form (sub  $x'^*$  comptype').
- The composite type *comptype* is valid.
- For all *comptype'* in *comptype'*\*:
  - The composite type *comptype* matches the composite type *comptype*'.

## Todo

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- The composite type *comptype* must be valid.
- The sequence  $y^*$  may be no longer than 1.
- For every type index  $y_i$  in  $y^*$ :
  - The type index  $y_i$  must be smaller than x.
  - The type index  $y_i$  must exist in the context C.
  - Let  $subtype_i$  be the unrolling of the defined type C.types $[y_i]$ .
  - The sub type  $subtype_i$  must not contain final.
  - Let  $comptype'_i$  be the composite type in  $subtype_i$ .
  - The composite type comptype must match comptype'<sub>i</sub>.
- ullet Then the sub type is valid for the type index x.

$$\frac{|x^*| \le 1 \quad (x < x_0)^* \quad (\text{unroll}(C.\mathsf{types}[x]) = \mathsf{sub} \ x'^* \ comptype')^*}{C \vdash \mathsf{sub} \ \mathsf{final}^? \ x^* \ comptype : \mathsf{ok}((x_0))}$$

## Note

The side condition on the index ensures that a declared supertype is a previously defined types, preventing cyclic subtype hierarchies.

Future versions of WebAssembly may allow more than one supertype.

## 3.2.13 Defined Types

The defined type (rectype.i) is valid if:

- The recursive type rectype is valid for (ok(x)).
- The recursive type rectype is of the form (rec  $subtype^n$ ).
- i is less than n.

$$\frac{C \vdash rectype : \mathsf{ok}((x)) \qquad rectype = \mathsf{rec} \ subtype^n \qquad i < n}{C \vdash rectype.i : \mathsf{ok}}$$

## 3.2.14 Limits

Limits must have meaningful bounds that are within a given range.

The limits range  $[n \dots m]$  is valid within k if:

- n is less than or equal to m.
- m is less than or equal to k.

$$\frac{n \le m \le k}{C \vdash [n \dots m] : k}$$

## 3.2.15 Table Types

The table type (addrtype limits reftype) is valid if:

- The limits range *limits* is valid within  $2^{32} 1$ .
- The reference type *reftype* is valid.

$$\frac{C \vdash limits: 2^{32} - 1 \qquad C \vdash reftype: \mathsf{ok}}{C \vdash addrtype \ limits \ reftype: \mathsf{ok}}$$

## 3.2.16 Memory Types

The memory type (addrtype limits page) is valid if:

• The limits range limits is valid within  $2^{16}$ .

$$\frac{C \vdash limits: 2^{16}}{C \vdash addrtype\ limits\ \mathsf{page:ok}}$$

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## 3.2.17 Tag Types

The tag type deftype is valid if:

- The defined type deftype is valid.
- The expansion of the defined type deftype is the composite type (func functype).

$$\frac{C \vdash \textit{deftype} : \mathsf{ok} \qquad \textit{deftype} \approx \mathsf{func} \, \textit{functype}}{C \vdash \textit{deftype} : \mathsf{ok}}$$

#### Note

Tag types do not occur in source programs, so this rule is not needed for validation. It is, however, used in the definition of the embedding interface.

## 3.2.18 Global Types

The global type  $(mut^{?} t)$  is valid if:

• The value type t is valid.

$$\frac{C \vdash t : \mathsf{ok}}{C \vdash \mathsf{mut}^? \ t : \mathsf{ok}}$$

## 3.2.19 External Types

The external type (func deftype) is valid if:

- The defined type deftype is valid.
- The expansion of the defined type deftype is the composite type (func functype).

$$\frac{C \vdash \mathit{deftype} : \mathsf{ok} \qquad \mathit{deftype} \approx \mathsf{func}\,\mathit{functype}}{C \vdash \mathsf{func}\,\mathit{deftype} : \mathsf{ok}}$$

The external type (table *tabletype*) is valid if:

• The table type tabletype is valid.

$$\frac{C \vdash tabletype : \mathsf{ok}}{C \vdash \mathsf{table}\ tabletype : \mathsf{ok}}$$

The external type (mem memtype) is valid if:

• The memory type memtype is valid.

$$\frac{C \vdash memtype : \mathsf{ok}}{C \vdash \mathsf{mem}\ memtype : \mathsf{ok}}$$

The external type (tag tagtype) is valid if:

• The tag type tagtype is valid.

$$\frac{C \vdash tagtype : \mathsf{ok}}{C \vdash \mathsf{tag}\; tagtype : \mathsf{ok}}$$

The external type (global *globaltype*) is valid if:

• The global type global type is valid.

$$\frac{C \vdash \mathit{globaltype} : \mathsf{ok}}{C \vdash \mathsf{global} \; \mathit{globaltype} : \mathsf{ok}}$$

# 3.3 Matching

On most types, a notion of *subtyping* is defined that is applicable in validation rules, during module instantiation when checking the types of imports, or during execution, when performing casts.

## 3.3.1 Number Types

The number type *numtype* matches only itself.

 $C \vdash numtype \leq numtype$ 

## 3.3.2 Vector Types

The vector type vectype matches only itself.

 $C \vdash vectype \leq vectype$ 

## 3.3.3 Heap Types

The heap type heaptype" matches the heap type heaptype" if:

- Either:
  - The heap type heap type'' is of the form heap type.
  - The heap type heap type''' is of the form heap type.
- Or:
  - The heap type heap type'' is of the form  $heap type_1$ .
  - The heap type heap type''' is of the form  $heap type_2$ .
  - The heap type heaptype' is valid.
  - The heap type  $heap type_1$  matches the heap type heap type'.
  - The heap type heaptype' matches the heap type heaptype<sub>2</sub>.
- Or:
  - The heap type *heaptype*" is of the form eq.
  - The heap type  $heap type^{\prime\prime\prime}$  is of the form any.
- Or:
  - The heap type heap type'' is of the form i31.
  - The heap type heaptype" is of the form eq.
- Or:
  - The heap type heaptype" is of the form struct.
  - The heap type heap type''' is of the form eq.
- Or:
  - The heap type *heaptype*" is of the form array.
  - The heap type heap type''' is of the form eq.
- Or:
  - The heap type  $heap type^{\prime\prime}$  is of the form def type.

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- The heap type  $heap type^{\prime\prime\prime}$  is of the form struct.
- The expansion of the defined type deftype is the composite type (struct fieldtype\*).

#### • Or:

- The heap type heaptype" is of the form deftype.
- The heap type heap type''' is of the form array.
- The expansion of the defined type deftype is the composite type (array fieldtype).

#### • Or:

- The heap type heap type'' is of the form def type.
- The heap type *heaptype'''* is of the form func.
- The expansion of the defined type deftype is the composite type (func functype).

#### • Or:

- The heap type heap type'' is of the form  $def type_1$ .
- The heap type heap type''' is of the form  $def type_2$ .
- The defined type  $deftype_1$  matches the defined type  $deftype_2$ .

#### • Or:

- The heap type heap type'' is of the form type idx.
- The heap type heap type''' is of the form heap type.
- The defined type C.types [typeidx] exists.
- The defined type C-types [typeidx] matches the heap type heap type.

#### • Or:

- The heap type heaptype" is of the form heaptype.
- The heap type heap type''' is of the form type idx.
- The defined type C.types [typeidx] exists.
- The heap type heap type matches the defined type C.types [type idx].

## • Or:

- The heap type heap type'' is of the form (rec i).
- The heap type heap type''' is of the form  $type use^*[j]$ .
- The length of  $typeuse^*$  is greater than j.
- The sub type C.recs[i] exists.
- The sub type C.recs[i] is of the form (sub final?  $typeuse^* ct$ ).

### • Or:

- The heap type heaptype" is of the form none.
- The heap type heap type''' is of the form heap type.
- The heap type heaptype matches the heap type any.

#### • Or:

- The heap type heap type'' is of the form nofunc.
- The heap type heap type''' is of the form heap type.
- The heap type *heaptype* matches the heap type func.

## • Or:

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- The heap type *heaptype*" is of the form noextern.
- The heap type heap type''' is of the form heap type.
- The heap type *heaptype* matches the heap type extern.
- Or:
  - The heap type heaptype" is of the form bot.
  - The heap type heap type''' is of the form heap type.

#### Todo

below is the official specification

A heap type heaptype<sub>1</sub> matches a heap type heaptype<sub>2</sub> if and only if:

- Either both  $heaptype_1$  and  $heaptype_2$  are the same.
- Or there exists a valid heap type heaptype', such that heaptype<sub>1</sub> matches heaptype' and heaptype' matches heaptype<sub>2</sub>.
- Or  $heaptype_1$  is eq and  $heaptype_2$  is any.
- Or  $heaptype_1$  is one of i31, struct, or array and  $heaptype_2$  is eq.
- Or heaptype<sub>1</sub> is a defined type which expands to a structure type and heaptype<sub>2</sub> is struct.
- Or  $heaptype_1$  is a defined type which expands to an array type and  $heaptype_2$  is array.
- Or heaptype<sub>1</sub> is a defined type which expands to a function type and heaptype<sub>2</sub> is func.
- Or heaptype<sub>1</sub> is a defined type deftype<sub>1</sub> and heaptype<sub>2</sub> is a defined type deftype<sub>2</sub>, and deftype<sub>1</sub> matches deftype<sub>2</sub>.
- Or  $heaptype_1$  is a type index  $x_1$ , and the defined type C.types $[x_1]$  matches  $heaptype_2$ .
- Or  $heaptype_2$  is a type index  $x_2$ , and  $heaptype_1$  matches the defined type C.types[ $x_2$ ].
- Or heaptype<sub>1</sub> is none and heaptype<sub>2</sub> matches any.
- Or heaptype<sub>1</sub> is nofunc and heaptype<sub>2</sub> matches func.
- Or heaptype<sub>1</sub> is noextern and heaptype<sub>2</sub> matches extern.
- Or *heaptype*<sub>1</sub> is bot.

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## 3.3.4 Reference Types

The reference type (ref null?  $ht_1$ ) matches the reference type (ref null?  $ht_2$ ) if:

- The heap type  $ht_1$  matches the heap type  $ht_2$ .
- Either:
  - null? is absent.
  - null?' is absent.
- Or:
  - null? is of the form null?.
  - null?' is of the form null.

## Todo

below is the official specification

A reference type ref  $null_1^2$  heaptype<sub>1</sub> matches a reference type ref  $null_2^2$  heaptype<sub>2</sub> if and only if:

- The heap type  $heap type_1$  matches  $heap type_2$ .
- null<sub>1</sub> is absent or null<sub>2</sub> is present.

$$\frac{C \vdash ht_1 \leq ht_2}{C \vdash \mathsf{ref}\ ht_1 \leq \mathsf{ref}\ ht_2} \qquad \frac{C \vdash ht_1 \leq ht_2}{C \vdash \mathsf{ref}\ \mathsf{null}^?\ ht_1 \leq \mathsf{ref}\ \mathsf{null}\ ht_2}$$

## 3.3.5 Value Types

The value type valtype' matches the value type valtype" if:

- Either:
  - The value type valtype' is of the form  $numtype_1$ .
  - The value type valtype'' is of the form  $numtype_2$ .
  - The number type  $numtype_1$  matches the number type  $numtype_2$ .
- Or:
  - The value type valtype' is of the form  $vectype_1$ .
  - The value type valtype'' is of the form  $vectype_2$ .
  - The vector type  $vectype_1$  matches the vector type  $vectype_2$ .
- Or:
  - The value type valtype' is of the form  $reftype_1$ .
  - The value type valtype'' is of the form  $reftype_2$ .
  - The reference type  $reftype_1$  matches the reference type  $reftype_2$ .
- Or:
  - The value type valtype' is of the form bot.
  - The value type valtype'' is of the form valtype.

$$\overline{C \vdash \mathsf{bot} \leq \mathit{valtype}}$$

## 3.3.6 Result Types

Subtyping is lifted to result types in a pointwise manner.

The result type  $t_1^*$  matches the result type  $t_2^*$  if:

- The length of  $t_1^*$  is equal to the length of  $t_2^*$ .
- For all  $t_1$  in  $t_1^*$ , and corresponding  $t_2$  in  $t_2^*$ :
  - The value type  $t_1$  matches the value type  $t_2$ .

$$\frac{(C \vdash t_1 \le t_2)^*}{C \vdash t_1^* \le t_2^*}$$

## 3.3.7 Instruction Types

Subtyping is further lifted to instruction types.

The instruction type  $t_{11}^* \to_{x_1^*} t_{12}^*$  matches the instruction type  $t_{21}^* \to_{x_2^*} t_{22}^*$  if:

- The result type  $t_{21}^*$  matches the result type  $t_{11}^*$ .
- The result type  $t_{12}^*$  matches the result type  $t_{22}^*$ .
- The local index sequence sequence  $x^*$  is of the form  $x_2^* \setminus x_1^*$ .
- The length of  $t^*$  is equal to the length of  $x^*$ .
- For all x in  $x^*$ :
  - The local type C.locals[x] exists.
- For all t in  $t^*$ , and corresponding x in  $x^*$ :
  - The local type C.locals[x] is of the form (set t).

$$\frac{C \vdash t_{21}^* \leq t_{11}^* \qquad C \vdash t_{12}^* \leq t_{22}^* \qquad x^* = x_2^* \setminus x_1^* \qquad (C.\mathsf{locals}[x] = \mathsf{set}\ t)^*}{C \vdash t_{11}^* \to_{x_1^*} t_{12}^* \leq t_{21}^* \to_{x_2^*} t_{22}^*}$$

#### Note

Instruction types are contravariant in their input and covariant in their output. Moreover, the supertype may ignore variables from the init set  $x_1^*$ . It may also *add* variables to the init set, provided these are already set in the context, i.e., are vacuously initialized.

## 3.3.8 Function Types

The function type  $t_{11}^* o t_{12}^*$  matches the function type  $t_{21}^* o t_{22}^*$  if:

- The result type  $t_{21}^*$  matches the result type  $t_{11}^*$ .
- The result type  $t_{12}^{st}$  matches the result type  $t_{22}^{st}$ .

$$\frac{C \vdash t_{21}^* \leq t_{11}^* \quad C \vdash t_{12}^* \leq t_{22}^*}{C \vdash t_{11}^* \to t_{12}^* \leq t_{21}^* \to t_{22}^*}$$

## 3.3.9 Composite Types

The composite type *comptype* matches the composite type *comptype'* if:

- Either:
  - The composite type comptype is of the form (struct  $yt_1^* yt_1'$ ).
  - The composite type comptype' is of the form (struct  $yt_2^*$ ).

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- The length of  $yt_1^*$  is equal to the length of  $yt_2^*$ .
- For all  $yt_1$  in  $yt_1^*$ , and corresponding  $yt_2$  in  $yt_2^*$ :
  - \* The field type  $yt_1$  matches the field type  $yt_2$ .
- Or:
  - The composite type comptype is of the form (array  $yt_1$ ).
  - The composite type comptype' is of the form (array  $yt_2$ ).
  - The field type  $yt_1$  matches the field type  $yt_2$ .
- Or:
  - The composite type comptype is of the form (func  $ft_1$ ).
  - The composite type comptype' is of the form (func  $ft_2$ ).
  - The function type  $ft_1$  matches the function type  $ft_2$ .

$$\frac{(C \vdash yt_1 \leq yt_2)^*}{C \vdash \mathsf{struct}\; (yt_1^*\; yt_1') \leq \mathsf{struct}\; yt_2^*} \qquad \frac{C \vdash yt_1 \leq yt_2}{C \vdash \mathsf{array}\; yt_1 \leq \mathsf{array}\; yt_2} \qquad \frac{C \vdash ft_1 \leq ft_2}{C \vdash \mathsf{func}\; ft_1 \leq \mathsf{func}\; ft_2}$$

# 3.3.10 Field Types

The field type (mut<sup>?</sup>  $zt_1$ ) matches the field type (mut<sup>?'</sup>  $zt_2$ ) if:

- The storage type  $zt_1$  matches the storage type  $zt_2$ .
- Either:
  - mut? is absent.
  - mut?' is absent.
- Or:
  - mut? is of the form mut.
  - mut?' is of the form mut.
  - The storage type  $zt_2$  matches the storage type  $zt_1$ .

$$\frac{C \vdash zt_1 \leq zt_2}{C \vdash zt_1 \leq zt_2} \qquad \frac{C \vdash zt_1 \leq zt_2}{C \vdash \mathsf{mut} \ zt_1 \leq \mathsf{mut} \ zt_2}$$

The storage type storage type matches the storage type storage type' if:

- Either:
  - The storage type storage type is of the form  $valtype_1$ .
  - The storage type storagetype' is of the form valtype<sub>2</sub>.
  - The value type  $valtype_1$  matches the value type  $valtype_2$ .
- Or:
  - The storage type storage type is of the form  $pack type_1$ .
  - The storage type storagetype' is of the form packtype<sub>2</sub>.
  - The packed type  $packtype_1$  matches the packed type  $packtype_2$ .

The packed type packtype matches only itself.

$$\overline{C \vdash packtype \leq packtype}$$

## 3.3.11 Defined Types

The defined type  $deftype_1$  matches the defined type  $deftype_2$  if:

- Either:
  - The defined type  $\operatorname{clos}_C(\operatorname{deftype}_1)$  is of the form  $\operatorname{clos}_C(\operatorname{deftype}_2)$ .
- Or:
  - The sub type  $unroll(deftype_1)$  is of the form (sub final?  $typeuse^* ct$ ).
  - The length of  $typeuse^*$  is greater than i.
  - The type use  $typeuse^*[i]$  matches the heap type  $deftype_2$ .

$$\frac{\operatorname{clos}_C(\operatorname{deftype}_1) = \operatorname{clos}_C(\operatorname{deftype}_2)}{C \vdash \operatorname{deftype}_1 \leq \operatorname{deftype}_2}$$
 
$$\underline{\operatorname{unroll}(\operatorname{deftype}_1) = \operatorname{sub\ final}^? \operatorname{typeuse}^* \operatorname{ct} \quad C \vdash \operatorname{typeuse}^*[i] \leq \operatorname{deftype}_2}$$
 
$$C \vdash \operatorname{deftype}_1 \leq \operatorname{deftype}_2$$

### Note

Note that there is no explicit definition of type *equivalence*, since it coincides with syntactic equality, as used in the premise of the former rule above.

## 3.3.12 Limits

The limits range  $[n_1 \dots m_1]$  matches the limits range  $[n_2 \dots m_2]$  if:

- $n_1$  is greater than or equal to  $n_2$ .
- $m_1$  is less than or equal to  $m_2$ .

$$\frac{n_1 \geq n_2 \quad m_1 \leq m_2}{C \vdash [n_1 \dots m_1] \leq [n_2 \dots m_2]}$$

## 3.3.13 Table Types

The table type  $(addrtype\ limits_1\ reftype_1)$  matches the table type  $(addrtype\ limits_2\ reftype_2)$  if:

- The limits range  $limits_1$  matches the limits range  $limits_2$ .
- The reference type  $\mathit{reftype}_1$  matches the reference type  $\mathit{reftype}_2$ .
- The reference type reftype, matches the reference type reftype.

$$\frac{C \vdash limits_1 \leq limits_2 \quad C \vdash reftype_1 \leq reftype_2 \quad C \vdash reftype_2 \leq reftype_1}{C \vdash addrtype \ limits_1 \ reftype_1 \leq addrtype \ limits_2 \ reftype_2}$$

## 3.3.14 Memory Types

The memory type ( $addrtype \ limits_1 \ page$ ) matches the memory type ( $addrtype \ limits_2 \ page$ ) if:

• The limits range  $limits_1$  matches the limits range  $limits_2$ .

$$\frac{C \vdash \mathit{limits}_1 \leq \mathit{limits}_2}{C \vdash \mathit{addrtype\ limits}_1\ \mathsf{page} \leq \mathit{addrtype\ limits}_2\ \mathsf{page}}$$

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## 3.3.15 Global Types

The global type (mut? valtype<sub>1</sub>) matches the global type (mut?' valtype<sub>2</sub>) if:

- The value type  $valtype_1$  matches the value type  $valtype_2$ .
- Either:
  - mut? is absent.
  - mut?' is absent.
- Or:
  - mut? is of the form mut.
  - mut?' is of the form mut.
  - The value type  $valtype_2$  matches the value type  $valtype_1$ .

$$\frac{C \vdash valtype_1 \leq valtype_2}{C \vdash valtype_1 \leq valtype_2} \qquad \frac{C \vdash valtype_1 \leq valtype_2}{C \vdash \mathsf{mut} \ valtype_1 \leq \mathsf{mut} \ valtype_2} \leq \frac{C \vdash valtype_2}{C \vdash \mathsf{mut} \ valtype_1} \leq \frac{C \vdash valtype_2}{C \vdash \mathsf{mut} \ valtype_2} \leq \frac{C \vdash valtype_2}{C$$

## 3.3.16 Tag Types

The tag type  $deftype_1$  matches the tag type  $deftype_2$  if:

- The defined type  $deftype_1$  matches the defined type  $deftype_2$ .
- The defined type  $deftype_2$  matches the defined type  $deftype_1$ .

$$\frac{C \vdash \textit{deftype}_1 \leq \textit{deftype}_2}{C \vdash \textit{deftype}_1 \leq \textit{deftype}_1} \leq \textit{deftype}_2$$

### Note

Although the conclusion of this rule looks identical to its premise, they in fact describe different relations: the premise invokes subtyping on defined types, while the conclusion defines it on tag types that happen to be expressed as defined types.

## 3.3.17 External Types

The external type (func  $deftype_1$ ) matches the external type (func  $deftype_2$ ) if:

• The defined type  $deftype_1$  matches the defined type  $deftype_2$ .

$$\frac{C \vdash \mathit{deftype}_1 \leq \mathit{deftype}_2}{C \vdash \mathsf{func}\; \mathit{deftype}_1 \leq \mathsf{func}\; \mathit{deftype}_2}$$

The external type (table  $table type_1$ ) matches the external type (table  $table type_2$ ) if:

• The table type  $table type_1$  matches the table type  $table type_2$ .

$$\frac{C \vdash tabletype_1 \leq tabletype_2}{C \vdash \mathsf{table}\ tabletype_1 \leq \mathsf{table}\ tabletype_2}$$

The external type (mem  $memtype_1$ ) matches the external type (mem  $memtype_2$ ) if:

• The memory type  $memtype_1$  matches the memory type  $memtype_2$ .

$$\frac{C \vdash memtype_1 \leq memtype_2}{C \vdash mem \ memtype_1 \leq mem \ memtype_2}$$

The external type (global  $globaltype_1$ ) matches the external type (global  $globaltype_2$ ) if:

• The global type globaltype<sub>1</sub> matches the global type globaltype<sub>2</sub>.

$$\frac{C \vdash globaltype_1 \leq globaltype_2}{C \vdash \mathsf{global} \; globaltype_1 \leq \mathsf{global} \; globaltype_2}$$

The external type (tag  $tagtype_1$ ) matches the external type (tag  $tagtype_2$ ) if:

• The tag type  $tagtype_1$  matches the tag type  $tagtype_2$ .

$$\frac{C \vdash tagtype_1 \leq tagtype_2}{C \vdash \mathsf{tag}\ tagtype_1 \leq \mathsf{tag}\ tagtype_2}$$

## 3.4 Instructions

Instructions are classified by instruction types that describe how they manipulate the operand stack and initialize locals: A type  $t_1^* \to_{x^*} t_2^*$  describes the required input stack with argument values of types  $t_1^*$  that an instruction pops off and the provided output stack with result values of types  $t_2^*$  that it pushes back. Moreover, it enumerates the indices  $x^*$  of locals that have been set by the instruction. In most cases, this is empty.

#### Note

For example, the instruction i32.add has type i32 i32  $\rightarrow$  i32, consuming two i32 values and producing one. The instruction (local.set x) has type  $t \rightarrow_x \epsilon$ , provided t is the type declared for the local x.

Typing extends to instruction sequences  $instr^*$ . Such a sequence has an instruction type  $t_1^* \to_{x^*} t_2^*$  if the accumulative effect of executing the instructions is consuming values of types  $t_1^*$  off the operand stack, pushing new values of types  $t_2^*$ , and setting all locals  $x^*$ .

For some instructions, the typing rules do not fully constrain the type, and therefore allow for multiple types. Such instructions are called *polymorphic*. Two degrees of polymorphism can be distinguished:

- *value-polymorphic*: the value type t of one or several individual operands is unconstrained. That is the case for all parametric instructions like drop and select.
- stack-polymorphic: the entire (or most of the) instruction type  $t_1^* \to t_2^*$  of the instruction is unconstrained. That is the case for all control instructions that perform an unconditional control transfer, such as unreachable, br, or return.

In both cases, the unconstrained types or type sequences can be chosen arbitrarily, as long as they meet the constraints imposed for the surrounding parts of the program.

### Note

For example, the select instruction is valid with type t t is t t, for any possible number type t. Consequently, both instruction sequences

```
(i32.const 1) (i32.const 2) (i32.const 3) (select)
```

and

$$(f_{64}.const + 64) (f_{64}.const + 64) (f_{64}.const + 64) (select)$$

are valid, with t in the typing of select being instantiated to i32 or f64, respectively.

The unreachable instruction is stack-polymorphic, and hence valid with type  $t_1^* \to t_2^*$  for any possible sequences of value types  $t_1^*$  and  $t_2^*$ . Consequently,

```
(unreachable) (i32.add)
```

is valid by assuming type  $\epsilon \to \mathrm{i}$ 32 for the unreachable instruction. In contrast,

```
(unreachable) (i64.const 0) (i32.add)
```

is invalid, because there is no possible type to pick for the unreachable instruction that would make the sequence well-typed.

The Appendix describes a type checking algorithm that efficiently implements validation of instruction sequences as prescribed by the rules given here.

## 3.4.1 Parametric Instructions

nop

The instruction nop is valid with the instruction type  $\epsilon \to \epsilon$ .

$$\overline{C \vdash \mathsf{nop} : \epsilon \to \epsilon}$$

unreachable

The instruction unreachable is valid with the instruction type  $t_1^* \to t_2^*$  if:

• The instruction type  $t_1^* \to t_2^*$  is valid.

$$\frac{C \vdash t_1^* \to t_2^* : \mathsf{ok}}{C \vdash \mathsf{unreachable} : t_1^* \to t_2^*}$$

Note

The unreachable instruction is stack-polymorphic.

drop

The instruction drop is valid with the instruction type  $t \to \epsilon$  if:

• The value type t is valid.

$$\frac{C \vdash t : \mathsf{ok}}{C \vdash \mathsf{drop} : t \to \epsilon}$$

Note

Both drop and select without annotation are value-polymorphic instructions.

select  $(t^*)$ ?

The instruction (select  $valtype^{?}$ ) is valid with the instruction type  $t\ t$  is:

- The value type t is valid.
- Either
  - The value type sequence  $valtype^{?}$  is of the form t.
- Or:
  - The value type sequence *valtype*? is absent.
  - The value type t matches the value type t'.
  - The value type t' is of the form numtype or t' is of the form vectype.

$$\frac{C \vdash t : \mathsf{ok}}{C \vdash \mathsf{select} \ t : t \ \mathsf{t} \ \mathsf{i32} \to t} \qquad \frac{C \vdash t : \mathsf{ok}}{C \vdash \mathsf{select} \ t : t \ \mathsf{t} \ \mathsf{i32} \to t} \qquad \frac{C \vdash t : \mathsf{ok}}{C \vdash \mathsf{select} \ : t \ \mathsf{t} \ \mathsf{i32} \to t}$$

Note

In future versions of WebAssembly, select may allow more than one value per choice.

## 3.4.2 Numeric Instructions

#### $t.\mathsf{const}\ c$

The instruction (nt.const  $c_{nt}$ ) is valid with the instruction type  $\epsilon \rightarrow nt$ .

$$C \vdash nt.\mathsf{const}\ c_{nt} : \epsilon \to nt$$

#### t.unop

The instruction  $(nt.unop_{nt})$  is valid with the instruction type  $nt \rightarrow nt$ .

$$\overline{C \vdash nt.unop_{nt} : nt \rightarrow nt}$$

#### t.binop

The instruction  $(nt.binop_{nt})$  is valid with the instruction type  $nt \ nt \rightarrow nt$ .

$$\overline{C \vdash nt.binop_{nt} : nt \ nt \rightarrow nt}$$

#### t.testop

The instruction  $(nt.testop_{nt})$  is valid with the instruction type  $nt \rightarrow$  i32.

$$\overline{C \vdash nt.testop_{nt} : nt \rightarrow i32}$$

## t.relop

The instruction  $(nt.relop_{nt})$  is valid with the instruction type  $nt \ nt \ o \$ i32.

$$C \vdash nt.relop_{nt} : nt \ nt \rightarrow i32$$

## $t_1.cvtop\_t_2\_sx$ ?

The instruction  $(nt_1.cvtop\_nt_2)$  is valid with the instruction type  $nt_2 \rightarrow nt_1$ .

$$\overline{C \vdash nt_1.cvtop\_nt_2 : nt_2 \to nt_1}$$

## 3.4.3 Reference Instructions

### $ref.null \ ht$

The instruction (ref.null ht) is valid with the instruction type  $\epsilon \to (\text{ref null } ht)$  if:

• The heap type ht is valid.

$$\frac{C \vdash ht : \mathsf{ok}}{C \vdash \mathsf{ref.null} \ ht : \epsilon \to (\mathsf{ref} \ \mathsf{null} \ ht)}$$

### $\mathsf{ref}.\mathsf{func}\; x$

The instruction (ref.func x) is valid with the instruction type  $\epsilon \to (\text{ref } dt)$  if:

- The defined type C.funcs[x] exists.
- The defined type C.funcs[x] is of the form dt.
- x is contained in C.refs.

$$\frac{C.\mathsf{funcs}[x] = dt}{C \vdash \mathsf{ref}.\mathsf{func}\; x : \epsilon \to (\mathsf{ref}\; dt)}$$

#### ref.is null

The instruction ref.is\_null is valid with the instruction type (ref null ht)  $\rightarrow$  i32 if:

• The heap type ht is valid.

$$\frac{C \vdash ht : \mathsf{ok}}{C \vdash \mathsf{ref.is\_null} : (\mathsf{ref} \ \mathsf{null} \ ht) \to \mathsf{i32}}$$

#### ref.as non null

The instruction ref.as\_non\_null is valid with the instruction type (ref null ht)  $\rightarrow$  (ref ht) if:

• The heap type ht is valid.

$$\frac{C \vdash ht : \mathsf{ok}}{C \vdash \mathsf{ref.as\_non\_null} : (\mathsf{ref} \; \mathsf{null} \; ht) \to (\mathsf{ref} \; ht)}$$

#### ref.eq

The instruction ref.eq is valid with the instruction type (ref null eq) (ref null eq)  $\rightarrow$  i32.

$$C \vdash \text{ref.eq} : (\text{ref null eq}) (\text{ref null eq}) \rightarrow i_{32}$$

#### ref.test rt

The instruction (ref.test rt) is valid with the instruction type  $rt' \rightarrow$  i32 if:

- The reference type rt is valid.
- The reference type rt' is valid.
- The reference type rt matches the reference type rt'.

$$\frac{C \vdash rt : \mathsf{ok} \qquad C \vdash rt' : \mathsf{ok} \qquad C \vdash rt \leq rt'}{C \vdash \mathsf{ref.test} \ rt : rt' \to \mathsf{i32}}$$

#### Note

The liberty to pick a supertype rt' allows typing the instruction with the least precise super type of rt as input, that is, the top type in the corresponding heap subtyping hierarchy.

## $ref.cast \ rt$

The instruction (ref.cast rt) is valid with the instruction type  $rt' \rightarrow rt$  if:

- The reference type rt is valid.
- The reference type rt' is valid.
- The reference type rt matches the reference type rt'.

$$\frac{C \vdash rt : \mathsf{ok} \qquad C \vdash rt' : \mathsf{ok} \qquad C \vdash rt \leq rt'}{C \vdash \mathsf{ref.cast} \ rt : rt' \to rt}$$

## Note

The liberty to pick a supertype rt' allows typing the instruction with the least precise super type of rt as input, that is, the top type in the corresponding heap subtyping hierarchy.

## 3.4.4 Aggregate Reference Instructions

#### struct.new x

The instruction (struct.new x) is valid with the instruction type  $t^* \to (\text{ref } x)$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (struct (mut<sup>?</sup> zt)\*).
- Let  $t^*$  be the value type sequence sequence unpack $(zt)^*$ .

$$\frac{C.\mathsf{types}[x] \approx \mathsf{struct} \; (\mathsf{mut}^? \; zt)^*}{C \vdash \mathsf{struct.new} \; x : \mathsf{unpack}(zt)^* \to (\mathsf{ref} \; x)}$$

## $\mathsf{struct}.\mathsf{new\_default}\ x$

The instruction (struct.new\_default x) is valid with the instruction type  $\epsilon \to (\text{ref } x)$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (struct (mut<sup>?</sup> zt)\*).
- For all zt in  $zt^*$ :
  - A default value for the value type unpack(zt) is defined.

$$\frac{C.\mathsf{types}[x] \approx \mathsf{struct} \; (\mathsf{mut}^? \; zt)^* \qquad (\mathsf{default}_{\mathsf{unpack}(zt)} \neq \epsilon)^*}{C \vdash \mathsf{struct}.\mathsf{new\_default} \; x : \epsilon \to (\mathsf{ref} \; x)}$$

$$struct.get\_sx$$
?  $x$   $y$ 

The instruction (struct.get\_ $sx^? x i$ ) is valid with the instruction type (ref null x)  $\rightarrow t$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (struct  $yt^*$ ).
- The length of  $yt^*$  is greater than i.
- The field type  $yt^*[i]$  is of the form (mut<sup>?</sup> zt).
- The signedness  $sx^{?}$  is absent if and only if the storage type zt is of the form unpack (zt).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{struct}\ yt^* \qquad yt^*[i] = \mathsf{mut}^?\ zt \qquad sx^? = \epsilon \Leftrightarrow zt = \mathsf{unpack}(zt)}{C \vdash \mathsf{struct.get}\_sx^?\ x\ i : (\mathsf{ref}\ \mathsf{null}\ x) \to \mathsf{unpack}(zt)}$$

## $\mathsf{struct}.\mathsf{set}\; x\; y$

The instruction (struct.set x i) is valid with the instruction type (ref null x)  $t \to \epsilon$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (struct  $yt^*$ ).
- The length of  $yt^*$  is greater than i.
- The field type  $yt^*[i]$  is of the form (mut zt).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{struct}\ yt^* \qquad yt^*[i] = \mathsf{mut}\ zt}{C \vdash \mathsf{struct.set}\ x\ i : (\mathsf{ref}\ \mathsf{null}\ x)\ \mathsf{unpack}(zt) \to \epsilon}$$

#### array.new x

The instruction (array.new x) is valid with the instruction type t is x o (ref x) if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (array (mut<sup>?</sup> zt)).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array} \; (\mathsf{mut}^? \; zt)}{C \vdash \mathsf{array}.\mathsf{new} \; x : \mathsf{unpack}(zt) \; \mathsf{i32} \to (\mathsf{ref} \; x)}$$

## array.new\_default $\boldsymbol{x}$

The instruction (array.new\_default x) is valid with the instruction type i32  $\rightarrow$  (ref x) if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (array (mut<sup>?</sup> zt)).
- A default value for the value type unpack(zt) is defined.

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array}\;(\mathsf{mut}^?\;zt) \qquad \mathsf{default}_{\mathsf{unpack}(zt)} \neq \epsilon}{C \vdash \mathsf{array}.\mathsf{new}\;\;\mathsf{default}\;x : \mathsf{i32} \to \mathsf{(ref}\;x)}$$

## $\mathsf{array}.\mathsf{new\_fixed}\ x\ n$

The instruction (array.new\_fixed x n) is valid with the instruction type  $t^n \to (\text{ref } x)$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types[x] is the composite type (array (mut<sup>?</sup> zt)).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array} \; (\mathsf{mut}^? \; zt)}{C \vdash \mathsf{array}.\mathsf{new\_fixed} \; x \; n : \mathsf{unpack}(zt)^n \to (\mathsf{ref} \; x)}$$

#### array.new elem x y

The instruction (array.new\_elem x y) is valid with the instruction type i32 i32  $\rightarrow$  (ref x) if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (array (mut<sup>?</sup> rt)).
- The element type C.elems[y] exists.
- The reference type C.elems[y] matches the reference type rt.

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array}\;(\mathsf{mut}^?\;rt) \qquad C \vdash C.\mathsf{elems}[y] \leq rt}{C \vdash \mathsf{array}.\mathsf{new}\;\;\mathsf{elem}\;x\;y : \mathsf{i32}\;\mathsf{i32} \to (\mathsf{ref}\;x)}$$

## array.new\_data $x\ y$

The instruction (array.new\_data x y) is valid with the instruction type i32 i32  $\rightarrow$  (ref x) if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (array (mut<sup>?</sup> zt)).
- The value type unpack(zt) is of the form numtype or unpack(zt) is of the form vectype.
- The data type  $C.\mathsf{datas}[y]$  exists.
- The data type  $C.\mathsf{datas}[y]$  is of the form ok.

## $array.get_sx^? x$

The instruction (array.get\_ $sx^2$  x) is valid with the instruction type (ref null x) i32  $\rightarrow t$  if:

- The defined type C.types [x] exists.
- The expansion of the defined type C.types[x] is the composite type (array (mut<sup>?</sup> zt)).
- The signedness  $sx^2$  is absent if and only if the storage type zt is of the form unpack(zt).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array}\; (\mathsf{mut}^?\; zt) \qquad sx^? = \epsilon \Leftrightarrow zt = \mathsf{unpack}(zt)}{C \vdash \mathsf{array}.\mathsf{get}\_sx^?\; x : (\mathsf{ref}\; \mathsf{null}\; x) \; \mathsf{i32} \to \mathsf{unpack}(zt)}$$

#### array.set x

The instruction (array.set x) is valid with the instruction type (ref null x) i32  $t \to \epsilon$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (array (mut zt)).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array}\; (\mathsf{mut}\; zt)}{C \vdash \mathsf{array}.\mathsf{set}\; x: (\mathsf{ref}\; \mathsf{null}\; x) \; \mathsf{i32}\; \mathsf{unpack}(zt) \to \epsilon}$$

#### array.len

The instruction array.len is valid with the instruction type (ref null array)  $\rightarrow$  i32.

$$\overline{C \vdash \mathsf{array}.\mathsf{len} : (\mathsf{ref} \; \mathsf{null} \; \mathsf{array}) o \mathsf{i32}}$$

## $\mathsf{array}.\mathsf{fill}\ x$

The instruction (array.fill x) is valid with the instruction type (ref null x) is t is  $t = \epsilon$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C-types [x] is the composite type (array (mut zt)).
- Let t be the value type unpack(zt).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array} \; (\mathsf{mut} \; zt)}{C \vdash \mathsf{array}.\mathsf{fill} \; x : (\mathsf{ref} \; \mathsf{null} \; x) \; \mathsf{i32} \; \mathsf{unpack}(zt) \; \mathsf{i32} \to \epsilon}$$

#### array.copy x y

The instruction (array.copy  $x_1$   $x_2$ ) is valid with the instruction type (ref null  $x_1$ ) is (ref null  $x_2$ ) is is is:  $\epsilon$  if:

- The defined type C.types[ $x_1$ ] exists.
- The expansion of the defined type C.types $[x_1]$  is the composite type (array (mut  $zt_1$ )).
- The defined type C.types  $[x_2]$  exists.
- The expansion of the defined type C-types  $[x_2]$  is the composite type (array (mut?  $zt_2$ )).
- The storage type  $zt_2$  matches the storage type  $zt_1$ .

$$\frac{C.\mathsf{types}[x_1] \approx \mathsf{array}\; (\mathsf{mut}\; zt_1) \qquad C.\mathsf{types}[x_2] \approx \mathsf{array}\; (\mathsf{mut}^?\; zt_2) \qquad C \vdash zt_2 \leq zt_1}{C \vdash \mathsf{array}.\mathsf{copy}\; x_1\; x_2 : (\mathsf{ref}\; \mathsf{null}\; x_1) \; \mathsf{i32}\; (\mathsf{ref}\; \mathsf{null}\; x_2) \; \mathsf{i32}\; \mathsf{i32} \to \epsilon}$$

 $array.init\_elem x y$ 

The instruction (array.init\_elem x y) is valid with the instruction type (ref null x) is is is is  $\epsilon$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (array (mut zt)).
- The element type C.elems[y] exists.
- The element type C.elems[y] matches the storage type zt.

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array}\; (\mathsf{mut}\; zt) \qquad C \vdash C.\mathsf{elems}[y] \leq zt}{C \vdash \mathsf{array}.\mathsf{init\_elem}\; x\; y: (\mathsf{ref}\; \mathsf{null}\; x) \; \mathsf{i32}\; \mathsf{i32} \; \to \epsilon}$$

 $array.init\_data \ x \ y$ 

The instruction (array.init\_data x y) is valid with the instruction type (ref null x) is 2 is 2 is 2 is  $\epsilon$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (array (mut zt)).
- The value type unpack(zt) is of the form numtype or unpack(zt) is of the form vectype.
- The data type  $C.\mathsf{datas}[y]$  exists.
- The data type  $C.\mathsf{datas}[y]$  is of the form  $\mathsf{ok}.$

$$\frac{C.\mathsf{types}[x] \approx \mathsf{array}\;(\mathsf{mut}\; zt) \qquad \mathsf{unpack}(zt) = \mathit{numtype} \lor \mathsf{unpack}(zt) = \mathit{vectype} \qquad C.\mathsf{datas}[y] = \mathsf{ok}}{C \vdash \mathsf{array}.\mathsf{init\_data}\; x\; y : (\mathsf{ref}\; \mathsf{null}\; x) \; \mathsf{i32}\; \mathsf{i32} \; \to \epsilon}$$

## 3.4.5 Scalar Reference Instructions

ref.i31

The instruction ref.i31 is valid with the instruction type i32  $\rightarrow$  (ref i31).

$$\overline{C \vdash \mathsf{ref}.\mathsf{i31} : \mathsf{i32} \to (\mathsf{ref}\;\mathsf{i31})}$$

i31.get sx

The instruction (i31.get\_sx) is valid with the instruction type (ref null i31)  $\rightarrow$  i32.

$$C \vdash \mathsf{i31.get} \ sx : (\mathsf{ref} \ \mathsf{null} \ \mathsf{i31}) \to \mathsf{i32}$$

### 3.4.6 External Reference Instructions

any.convert\_extern

The instruction any.convert\_extern is valid with the instruction type (ref null $\frac{?}{1}$  extern)  $\rightarrow$  (ref null $\frac{?}{2}$  any) if:

• null; is of the form null?

$$\frac{\mathsf{null}_1^2 = \mathsf{null}_2^2}{C \vdash \mathsf{any.convert\_extern} : (\mathsf{ref} \ \mathsf{null}_1^2 \ \mathsf{extern}) \to (\mathsf{ref} \ \mathsf{null}_2^2 \ \mathsf{any})}$$

extern.convert any

The instruction extern.convert\_any is valid with the instruction type (ref null $\frac{?}{1}$  any)  $\rightarrow$  (ref null $\frac{?}{2}$  extern) if:

• null<sub>1</sub>? is of the form null<sub>2</sub>?

$$\frac{\mathsf{null}_1^? = \mathsf{null}_2^?}{C \vdash \mathsf{extern.convert\_any} : (\mathsf{ref} \ \mathsf{null}_1^? \ \mathsf{any}) \to (\mathsf{ref} \ \mathsf{null}_2^? \ \mathsf{extern})}$$

## 3.4.7 Vector Instructions

Vector instructions can have a prefix to describe the shape of the operand. Packed numeric types, is and i16, are not value types. An auxiliary function maps such packed type shapes to value types:

$$unpack(iN \times N) = unpack(iN)$$

v128.const  $\it c$ 

The instruction (v128.const c) is valid with the instruction type  $\epsilon \to \text{v128}$ .

$$C \vdash \mathsf{v}_{128}.\mathsf{const}\ c : \epsilon \to \mathsf{v}_{128}$$

v128.vvunop

The instruction (v128. vvunop) is valid with the instruction type v128  $\rightarrow$  v128.

$$\overline{C \vdash \mathsf{v128}.vvunop} : \mathsf{v128} \to \mathsf{v128}$$

 $\verb"v128." vvbinop"$ 

The instruction (v128.vvbinop) is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$C \vdash \mathsf{v128}.vvbinop : \mathsf{v128} \ \mathsf{v128} \to \mathsf{v128}$$

v128.vvternop

The instruction (v128.vvternop) is valid with the instruction type v128 v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash \mathsf{v128}.vvternop : \mathsf{v128}\ \mathsf{v128}\ \mathsf{v128} \to \mathsf{v128}}$$

v128.vvtestop

The instruction (v128.vvtestop) is valid with the instruction type v128  $\rightarrow$  i32.

$$C \vdash v_{128}.vvtestop : v_{128} \rightarrow i_{32}$$

shape.vunop

The instruction (sh.vunop) is valid with the instruction type v128  $\rightarrow$  v128.

$$\overline{C \vdash sh.vunop : v128 \rightarrow v128}$$

shape.vbinop

The instruction (sh.vbinop) is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash sh.vbinop} : v128 \ v128 \rightarrow v128$$

shape.vternop

The instruction (sh.vternop) is valid with the instruction type v128 v128 v128  $\rightarrow$  v128.

$$C \vdash sh.vternop : v128 v128 v128 \rightarrow v128$$

shape.vtestop

The instruction (sh.vtestop) is valid with the instruction type  $v_{128} \rightarrow i_{32}$ .

$$C \vdash sh.vtestop : v_{128} \rightarrow i_{32}$$

shape.vrelop

The instruction (sh.vrelop) is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash sh.vrelop : v128 \ v128 \rightarrow v128}$$

ishape.vishiftop

The instruction (sh.vshiftop) is valid with the instruction type v128 i32  $\rightarrow$  v128.

$$\overline{C \vdash sh.vshiftop} : v128 i32 \rightarrow v128$$

ishape.bitmask

The instruction (sh.bitmask) is valid with the instruction type v128  $\rightarrow$  i32.

$$C \vdash sh.\mathsf{bitmask} : \mathsf{v}_{128} \to \mathsf{i}_{32}$$

i8x16. vswizzlop

The instruction (sh.vswizzlop) is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash sh.vswizzlop : v128 \ v128 \rightarrow v128}$$

i8x16.shuffle  $laneidx^{16}$ 

The instruction (sh.shuffle  $i^*$ ) is valid with the instruction type v128 v128  $\rightarrow$  v128 if:

- For all i in  $i^*$ :
  - The lane index i is less than  $2 \cdot \dim(sh)$ .

$$\frac{(i < 2 \cdot \dim(sh))^*}{C \vdash sh.\mathsf{shuffle}\ i^* : \mathsf{v128}\ \mathsf{v128} \to \mathsf{v128}}$$

 $shape. {\sf splat}$ 

The instruction (sh.splat) is valid with the instruction type  $t \to v_{128}$  if:

• Let t be the number type unpack(sh).

$$\overline{C \vdash sh.\mathsf{splat} : \mathsf{unpack}(sh) \to \mathsf{v128}}$$

shape.extract lane sx? laneidx

The instruction (sh.extract\_lane\_ $sx^?i$ ) is valid with the instruction type v<sub>128</sub>  $\rightarrow t$  if:

- The lane index i is less than  $\dim(sh)$ .
- Let t be the number type unpack(sh).

$$\frac{i < \dim(sh)}{C \vdash sh.\mathsf{extract\_lane\_} sx^? \ i : \mathsf{vi28} \to \mathsf{unpack}(sh)}$$

shape.replace\_lane laneidx

The instruction (sh.replace\_lane i) is valid with the instruction type v128  $t \rightarrow$  v128 if:

- The lane index i is less than  $\dim(sh)$ .
- Let t be the number type unpack(sh).

$$\frac{i < \dim(sh)}{C \vdash sh.\mathsf{replace\_lane}\; i : \mathsf{v128}\; \mathsf{unpack}(sh) \to \mathsf{v128}}$$

 $ishape_1.vextunop\_ishape_2$ 

The instruction  $(sh_1.vextunop\_sh_2)$  is valid with the instruction type v128  $\rightarrow$  v128.

$$\overline{C \vdash sh_1.vextunop\_sh_2 : v_{128} \rightarrow v_{128}}$$

 $ishape_1.vextbinop\_ishape_2$ 

The instruction  $(sh_1.vextbinop\_sh_2)$  is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash sh_1.vextbinop \ sh_2 : v128 \ v128 \rightarrow v128}$$

 $ishape_1.vextternop\_ishape_2$ 

The instruction  $(sh_1.vextternop\_sh_2)$  is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash sh_1.vextternop \ sh_2 : v128 \ v128 \ v128 \ v128} \rightarrow v128$$

 $ishape_1.\mathsf{narrow}\_ishape_2\_sx$ 

The instruction  $(sh_1.narrow\_sh_2\_sx)$  is valid with the instruction type v128 v128  $\rightarrow$  v128.

$$\overline{C \vdash sh_1.\mathsf{narrow}\_sh_2\_sx} : \mathsf{v128}\ \mathsf{v128} \to \mathsf{v128}$$

 $shape.vcvtop\_half?\_shape\_sx?\_zero?$ 

The instruction  $(sh_1.vcvtop\_zero^?\_sh_2\_half^?)$  is valid with the instruction type v128  $\rightarrow$  v128.

$$\overline{C \vdash sh_1.vcvtop\_zero?\_sh_2\_half?} : \forall 128 \rightarrow \forall 128$$

## 3.4.8 Variable Instructions

local.get x

The instruction (local.get x) is valid with the instruction type  $\epsilon \to t$  if:

- The local type C.locals[x] exists.
- The local type C.locals[x] is of the form (set t).

$$\frac{C.\mathsf{locals}[x] = \mathsf{set}\; t}{C \vdash \mathsf{local.get}\; x : \epsilon \to t}$$

local.set x

The instruction (local.set x) is valid with the instruction type  $t \to_x \epsilon$  if:

- The local type C.locals[x] exists.
- The local type C.locals[x] is of the form  $(init\ t)$ .

$$\frac{C.\mathsf{locals}[x] = init\ t}{C \vdash \mathsf{local.set}\ x : t \to_x \epsilon}$$

local.tee x

The instruction (local.tee x) is valid with the instruction type  $t \rightarrow_x t$  if:

- The local type C.locals[x] exists.
- The local type C.locals[x] is of the form (init t).

$$\frac{C.\mathsf{locals}[x] = init \ t}{C \vdash \mathsf{local.tee} \ x : t \to_x t}$$

## $\mathsf{global}.\mathsf{get}\ x$

The instruction (global.get x) is valid with the instruction type  $\epsilon \rightarrow t$  if:

- The global type C.globals [x] exists.
- The global type C.globals [x] is of the form (mut<sup>?</sup> t).

$$\frac{C.\mathsf{globals}[x] = \mathsf{mut}^?\ t}{C \vdash \mathsf{global.get}\ x : \epsilon \to t}$$

## $\mathsf{global}.\mathsf{set}\ x$

The instruction (global.set x) is valid with the instruction type  $t \to \epsilon$  if:

- The global type C.globals[x] exists.
- The global type C.globals[x] is of the form (mut t).

$$\frac{C.\mathsf{globals}[x] = \mathsf{mut}\ t}{C \vdash \mathsf{global.set}\ x : t \to \epsilon}$$

### 3.4.9 Table Instructions

## $\mathsf{table}.\mathsf{get}\; x$

The instruction (table.get x) is valid with the instruction type  $at \rightarrow rt$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form ( $at \ lim \ rt$ ).

$$\frac{C.\mathsf{tables}[x] = at \ lim \ rt}{C \vdash \mathsf{table.get} \ x : at \to rt}$$

#### table.set x

The instruction (table.set x) is valid with the instruction type at  $rt \rightarrow \epsilon$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form  $(at \ lim \ rt)$ .

$$\frac{C.\mathsf{tables}[x] = at \ lim \ rt}{C \vdash \mathsf{table.set} \ x : at \ rt \to \epsilon}$$

#### table.size x

The instruction (table.size x) is valid with the instruction type  $\epsilon \rightarrow at$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form  $(at \ lim \ rt)$ .

$$\frac{C.\mathsf{tables}[x] = at \ lim \ rt}{C \vdash \mathsf{table.size} \ x : \epsilon \to at}$$

## table.grow x

The instruction (table.grow x) is valid with the instruction type rt  $at \rightarrow at$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form ( $at \ lim \ rt$ ).

$$\frac{C.\mathsf{tables}[x] = at \ lim \ rt}{C \vdash \mathsf{table.grow} \ x : rt \ at \rightarrow at}$$

#### table.fill x

The instruction (table.fill x) is valid with the instruction type at rt at  $\rightarrow \epsilon$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form ( $at \ lim \ rt$ ).

$$\frac{C.\mathsf{tables}[x] = at \ lim \ rt}{C \vdash \mathsf{table.fill} \ x : at \ rt \ at \to \epsilon}$$

#### table.copy x y

The instruction (table.copy  $x_1 x_2$ ) is valid with the instruction type  $at_1 at_2 t \rightarrow \epsilon$  if:

- The table type C.tables[ $x_1$ ] exists.
- The table type C.tables $[x_1]$  is of the form  $(at_1 \ lim_1 \ rt_1)$ .
- The table type C.tables  $[x_2]$  exists.
- The table type C.tables[ $x_2$ ] is of the form ( $at_2 \ lim_2 \ rt_2$ ).
- The reference type  $rt_2$  matches the reference type  $rt_1$ .
- Let t be the address type  $\min(at_1, at_2)$ .

$$\frac{C.\mathsf{tables}[x_1] = \mathit{at}_1 \; \mathit{lim}_1 \; \mathit{rt}_1 \qquad C.\mathsf{tables}[x_2] = \mathit{at}_2 \; \mathit{lim}_2 \; \mathit{rt}_2 \qquad C \vdash \mathit{rt}_2 \leq \mathit{rt}_1}{C \vdash \mathsf{table.copy} \; x_1 \; x_2 : \mathit{at}_1 \; \mathit{at}_2 \; \min(\mathit{at}_1, \mathit{at}_2) \rightarrow \epsilon}$$

#### table.init x y

The instruction (table init x y) is valid with the instruction type at is t is t if:

- The table type C.tables[x] exists.
- The table type C.tables [x] is of the form  $(at \ lim \ rt_1)$ .
- The element type C.elems[y] exists.
- The reference type C.elems[y] is of the form  $rt_2$ .
- The reference type  $rt_2$  matches the reference type  $rt_1$ .

$$\frac{C.\mathsf{tables}[x] = \mathit{at\ lim\ } rt_1 \qquad C.\mathsf{elems}[y] = \mathit{rt}_2 \qquad C \vdash \mathit{rt}_2 \leq \mathit{rt}_1}{C \vdash \mathsf{table.init}\ x\ y : \mathit{at\ i32\ i32} \rightarrow \epsilon}$$

### $\operatorname{elem.drop} x$

The instruction (elem.drop x) is valid with the instruction type  $\epsilon \to \epsilon$  if:

- The element type C.elems[x] exists.
- The reference type C.elems[x] is of the form rt.

$$\frac{C.\mathsf{elems}[x] = rt}{C \vdash \mathsf{elem.drop}\ x : \epsilon \to \epsilon}$$

## 3.4.10 Memory Instructions

#### $t.\mathsf{load}\ x\ memarg$

The instruction (nt.load x memarg) is valid with the instruction type  $at \rightarrow nt$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to |nt|/8.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page}}{C \vdash \mathit{nt}.\mathsf{load}\ x\ \mathit{memarg}: \mathit{at} \to \mathit{nt}} \leq |\mathit{nt}|/8$$

### $t.loadN_sx\ x\ memarg$

The instruction (in.load $M_sx \ x \ memarg$ ) is valid with the instruction type  $at \rightarrow iN$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to M/8.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page}}{C \vdash \mathsf{i} \mathit{N}.\mathsf{load} M\_\mathit{sx\ x\ memarg} : \mathit{at} \rightarrow \mathsf{i} \mathit{N}}$$

#### $t.\mathsf{store}\ x\ memarg$

The instruction (nt.store x memorg) is valid with the instruction type at  $nt \rightarrow \epsilon$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to |nt|/8.

$$\frac{C.\mathsf{mems}[x] = at \ lim \ \mathsf{page} \qquad 2^{memarg.\mathsf{align}} \leq |nt|/8}{C \vdash nt.\mathsf{store} \ x \ memarg: at \ nt \to \epsilon}$$

## $t.storeN \ x \ memarg$

The instruction (in.store M x memorg) is valid with the instruction type at in  $\rightarrow \epsilon$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form (at lim page).
- $2^{memarg.align}$  is less than or equal to M/8.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page} }{C \vdash \mathsf{i} \mathit{N}.\mathsf{store} M\ \mathit{x\ memarg} : \mathit{at\ i} \mathit{N} \rightarrow \epsilon}$$

### v128.load *x memarg*

The instruction (v128.load  $x\ memarg$ ) is valid with the instruction type  $at \to v$ 128 if:

- The memory type C.mems[x] exists.
- The memory type  $C.\mathsf{mems}[x]$  is of the form  $(at\ lim\ \mathsf{page}).$
- $2^{memarg.align}$  is less than or equal to  $|v_{128}|/8$ .

$$\frac{C.\mathsf{mems}[x] = at \ lim \ \mathsf{page} \qquad 2^{memarg.\mathsf{align}} \leq |\mathsf{v128}|/8}{C \vdash \mathsf{v128}.\mathsf{load} \ x \ memarg: at \to \mathsf{v128}}$$

## v128.load $N \times M \_sx \ x \ memarg$

The instruction (v128.load $M \times N_s x \ x \ memarg$ ) is valid with the instruction type  $at \rightarrow v$ 128 if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form (at lim page).
- $2^{memarg.align}$  is less than or equal to  $M/8 \cdot N$ .

$$\frac{C.\mathsf{mems}[x] = at \ lim \ \mathsf{page}}{C \vdash \mathsf{v128.load} M \times N\_sx \ x \ memarg : at} \leq M/8 \cdot N$$

## v128.loadN\_splat x memarg

The instruction (v128.loadN\_splat  $x \ memarg$ ) is valid with the instruction type  $at \rightarrow$  v128 if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to N/8.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page}}{C \vdash \mathsf{v128.load}N\_\mathsf{splat}\ x\ \mathit{memarg} : \mathit{at} \to \mathsf{v128}}$$

## v128.loadN\_zero x memarg

The instruction (v128.load N\_zero x memorg) is valid with the instruction type  $at \rightarrow v128$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to N/8.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page}}{C \vdash \mathsf{v128}.\mathsf{load}N\_\mathsf{zero}\ x\ \mathit{memarg} : \mathit{at} \to \mathsf{v128}}$$

## v128.loadN\_lane x memarg laneidx

The instruction (v128.load  $N_{\text{lane}} x \ memarg \ i$ ) is valid with the instruction type  $at \ v128 \rightarrow v128 \ if$ :

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to N/8.
- i is less than 128/N.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page} \qquad 2^{\mathit{memarg.align}} \leq N/8 \qquad i < 128/N}{C \vdash \mathsf{v128.load}N\_\mathsf{lane}\ x\ \mathit{memarg\ i}: \mathit{at\ v128} \to \mathsf{v128}}$$

#### v128.store x memarg

The instruction (v128.store x memarg) is valid with the instruction type at v128  $\rightarrow \epsilon$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to  $|v_{128}|/8$ .

$$\frac{C.\mathsf{mems}[x] = at \ lim \ \mathsf{page} \qquad 2^{memarg.\mathsf{align}} \leq |\mathsf{v}_{128}|/8}{C \vdash \mathsf{v}_{128}.\mathsf{store} \ x \ memarg : at \ \mathsf{v}_{128} \to \epsilon}$$

## v128.storeN\_lane x memarg laneidx

The instruction (v128.store N\_lane  $x \ memarg \ i$ ) is valid with the instruction type  $at \ v128 \rightarrow \epsilon$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .
- $2^{memarg.align}$  is less than or equal to N/8.
- i is less than 128/N.

$$\frac{C.\mathsf{mems}[x] = at \ lim \ \mathsf{page} \qquad 2^{memarg.\mathsf{align}} \leq N/8 \qquad i < 128/N}{C \vdash \mathsf{v128.store} N\_\mathsf{lane} \ x \ memarg \ i : at \ \mathsf{v128} \rightarrow \epsilon}$$

#### memory.size x

The instruction (memory.size x) is valid with the instruction type  $\epsilon \rightarrow at$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page}}{C \vdash \mathsf{memory.size}\ x : \epsilon \to \mathit{at}}$$

### ${\it memory.grow} \,\, x$

The instruction (memory.grow x) is valid with the instruction type  $at \rightarrow at$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim\ page}}{C \vdash \mathsf{memory.grow}\ x : \mathit{at} \to \mathit{at}}$$

### memory.fill x

The instruction (memory.fill x) is valid with the instruction type at i32 at  $\rightarrow \epsilon$  if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form  $(at \ lim \ page)$ .

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim}\ \mathsf{page}}{C \vdash \mathsf{memory.fill}\ x : \mathit{at\ i32}\ \mathit{at} \to \epsilon}$$

#### memory.copy x y

The instruction (memory.copy  $x_1 x_2$ ) is valid with the instruction type  $at_1 at_2 t \rightarrow \epsilon$  if:

- The memory type C.mems $[x_1]$  exists.
- The memory type C.mems[ $x_1$ ] is of the form ( $at_1 \ lim_1 \ page$ ).
- The memory type C.mems $[x_2]$  exists.
- The memory type C.mems $[x_2]$  is of the form  $(at_2 \ lim_2 \ page)$ .
- Let t be the address type  $\min(at_1, at_2)$ .

$$\frac{C.\mathsf{mems}[x_1] = \mathit{at}_1 \; \mathit{lim}_1 \; \mathsf{page}}{C \vdash \mathsf{memory.copy} \; x_1 \; x_2 : \mathit{at}_1 \; \mathit{at}_2 \; \min(\mathit{at}_1, \mathit{at}_2) \to \epsilon}$$

## ${\it memory.init} \; x \; y$

- The memory type C.mems[x] exists.
- The memory type  $C.\mathsf{mems}[x]$  is of the form  $(at\ lim\ \mathsf{page}).$
- The data type  $C.\mathsf{datas}[y]$  exists.
- The data type  $C.\mathsf{datas}[y]$  is of the form ok.

$$\frac{C.\mathsf{mems}[x] = \mathit{at\ lim}\ \mathsf{page} \qquad C.\mathsf{datas}[y] = \mathsf{ok}}{C \vdash \mathsf{memory.init}\ x\ y : \mathit{at\ i32\ i32} \to \epsilon}$$

#### data.drop x

The instruction (data.drop x) is valid with the instruction type  $\epsilon \to \epsilon$  if:

- The data type  $C.\mathsf{datas}[x]$  exists.
- The data type  $C.\mathsf{datas}[x]$  is of the form ok.

$$\frac{C.\mathsf{datas}[x] = \mathsf{ok}}{C \vdash \mathsf{data.drop}\ x : \epsilon \to \epsilon}$$

## 3.4.11 Control Instructions

block  $blocktype\ instr^*$  end

The instruction (block bt  $instr^*$ ) is valid with the instruction type  $t_1^* \rightarrow t_2^*$  if:

- The block type bt is valid as the instruction type  $t_1^* \to t_2^*$ .
- Let C' be the same context as C, but with the result type sequence sequence  $t_2^*$  prepended to the field labels.
- Under the context C', the instruction sequence sequence  $instr^*$  is valid with the instruction type  $t_1^* \to_{x^*} t_2^*$ .

$$\frac{C \vdash bt: t_1^* \rightarrow t_2^* \quad \{ \text{labels } (t_2^*) \} \oplus C \vdash instr^*: t_1^* \rightarrow_{x^*} t_2^*}{C \vdash \text{block } bt \ instr^*: t_1^* \rightarrow t_2^*}$$

#### Note

The notation  $\{\text{labels }(t^*)\} \oplus C$  inserts the new label type at index 0, shifting all others. The same applies to all other block instructions.

loop blocktype instr\* end

The instruction (loop  $bt\ instr^*$ ) is valid with the instruction type  $t_1^* \to t_2^*$  if:

- The block type bt is valid as the instruction type  $t_1^* \rightarrow t_2^*$ .
- Let C' be the same context as C, but with the result type sequence sequence  $t_1^*$  prepended to the field labels.
- Under the context C', the instruction sequence sequence  $instr^*$  is valid with the instruction type  $t_1^* \to_{x^*} t_2^*$ .

$$\frac{C \vdash bt: t_1^* \rightarrow t_2^* \quad \{ \text{labels } (t_1^*) \} \oplus C \vdash instr^*: t_1^* \rightarrow_{x^*} t_2^*}{C \vdash \text{loop } bt \; instr^*: t_1^* \rightarrow t_2^*}$$

if  $blocktype \ instr_1^*$  else  $instr_2^*$  end

The instruction (if  $bt \ instr_1^*$  else  $instr_2^*$ ) is valid with the instruction type  $t_1^*$  is  $t_2^* = t_2^*$  if:

- The block type bt is valid as the instruction type  $t_1^* \to t_2^*$ .
- Let C' be the same context as C, but with the result type sequence sequence  $t_2^*$  prepended to the field labels.
- Under the context C', the instruction sequence sequence  $instr_1^*$  is valid with the instruction type  $t_1^* \to_{x_1^*} t_2^*$ .
- Under the context C', the instruction sequence sequence  $instr_2^*$  is valid with the instruction type  $t_1^* \to_{x_2^*} t_2^*$ .

$$\frac{C \vdash bt: t_1^* \rightarrow t_2^* \qquad \{\mathsf{labels}\,(t_2^*)\} \oplus C \vdash instr_1^*: t_1^* \rightarrow_{x_1^*} t_2^* \qquad \{\mathsf{labels}\,(t_2^*)\} \oplus C \vdash instr_2^*: t_1^* \rightarrow_{x_2^*} t_2^*}{C \vdash \mathsf{if}\,\,bt\,\,instr_1^*\,\,\mathsf{else}\,\,instr_2^*: t_1^*\,\,\mathsf{is2} \rightarrow t_2^*}$$

try\_table blocktype catch\* instr\* end

The instruction (try\_table  $bt \ catch^* \ instr^*$ ) is valid with the instruction type  $t_1^* \to t_2^*$  if:

- The block type bt is valid as the instruction type  $t_1^* \to t_2^*$ .
- Let C' be the same context as C, but with the result type sequence sequence  $t_2^*$  prepended to the field labels.
- Under the context C', the instruction sequence sequence  $instr^*$  is valid with the instruction type  $t_1^* \to_{x^*} t_2^*$ .
- For all catch in catch\*:
  - The catch clause catch is valid.

$$\frac{C \vdash bt: t_1^* \rightarrow t_2^* \qquad \{ \text{labels } (t_2^*) \} \oplus C \vdash instr^*: t_1^* \rightarrow_{x^*} t_2^* \qquad (C \vdash catch: \text{ok})^*}{C \vdash \text{try\_table } bt \ catch^* \ instr^*: t_1^* \rightarrow t_2^*}$$

#### $\operatorname{catch} x l$

The catch clause (catch x l) is valid if:

- The tag type C.tags[x] exists.
- The expansion of the defined type  $C.\mathsf{tags}[x]$  is the composite type (func  $t^* \to \epsilon$ ).
- The result type C.labels[l] exists.
- The result type  $t^*$  matches the result type C.labels[l].

$$\frac{C.\mathsf{tags}[x] \approx \mathsf{func}\; (t^* \to \epsilon) \qquad C \vdash t^* \leq C.\mathsf{labels}[l]}{C \vdash \mathsf{catch}\; x\; l : \mathsf{ok}}$$

## $\mathsf{catch\_ref}\ x\ l$

The catch clause (catch\_ref x l) is valid if:

- The tag type C.tags[x] exists.
- The expansion of the defined type  $C.\mathsf{tags}[x]$  is the composite type (func  $t^* \to \epsilon$ ).
- The result type C.labels[l] exists.
- The result type  $t^*$  (ref exn) matches the result type C.labels[l].

$$\frac{C.\mathsf{tags}[x] \approx \mathsf{func}\; (t^* \to \epsilon) \qquad C \vdash t^* \; (\mathsf{ref}\; \mathsf{exn}) \leq C.\mathsf{labels}[l]}{C \vdash \mathsf{catch\_ref}\; x\; l : \mathsf{ok}}$$

## $\mathsf{catch\_all}\ l$

The catch clause (catch\_all l) is valid if:

- The result type C.labels[l] exists.
- The result type  $\epsilon$  matches the result type C.labels[l].

$$\frac{C \vdash \epsilon \leq C. \mathsf{labels}[l]}{C \vdash \mathsf{catch\_all} \; l : \mathsf{ok}}$$

## ${\sf catch\_all\_ref}\ l$

The catch clause (catch\_all\_ref *l*) is valid if:

- The result type C.labels[l] exists.
- The result type (ref exn) matches the result type C.labels[l].

$$\frac{C \vdash (\mathsf{ref}\;\mathsf{exn}) \leq C.\mathsf{labels}[l]}{C \vdash \mathsf{catch\_all\_ref}\;l:\mathsf{ok}}$$

#### br l

The instruction (br l) is valid with the instruction type  $t_1^* t^* \rightarrow t_2^*$  if:

- The result type C.labels[l] exists.
- The result type  $C.\mathsf{labels}[l]$  is of the form  $t^*$ .
- The instruction type  $t_1^* \rightarrow t_2^*$  is valid.

$$\frac{C.\mathsf{labels}[l] = t^* \qquad C \vdash t_1^* \to t_2^* : \mathsf{ok}}{C \vdash \mathsf{br} \ l : t_1^* \ t^* \to t_2^*}$$

#### Note

The label index space in the context C contains the most recent label first, so that C labels [l] performs a relative lookup as expected. This applies to other branch instructions as well.

The br instruction is stack-polymorphic.

## $br_if l$

The instruction (br\_if l) is valid with the instruction type  $t^*$  is:

- The result type C.labels[l] exists.
- The result type C.labels [l] is of the form  $t^*$ .

$$\frac{C.\mathsf{labels}[l] = t^*}{C \vdash \mathsf{br} \text{ if } l : t^* \text{ is } 2 \to t^*}$$

## br\_table $l^*$ $l_N$

The instruction (br\_table  $l^*$  l') is valid with the instruction type  $t_1^*$   $t^*$  is  $t_2^*$  if:

- For all *l* in *l*\*:
  - The result type C.labels[l] exists.
- For all l in  $l^*$ :
  - The result type  $t^*$  matches the result type C.labels[l].
- The result type C.labels[l'] exists.
- The result type  $t^*$  matches the result type C.labels[l'].
- The instruction type  $t_1^* \to t_2^*$  is valid.

$$\frac{(C \vdash t^* \leq C. \mathsf{labels}[l])^* \qquad C \vdash t^* \leq C. \mathsf{labels}[l'] \qquad C \vdash t_1^* \to t_2^* : \mathsf{ok}}{C \vdash \mathsf{br\_table} \ l^* \ l' : t_1^* \ t^* \ \mathsf{i32} \to t_2^*}$$

### Note

The br\_table instruction is stack-polymorphic.

Furthermore, the result type  $t^*$  is also chosen non-deterministically in this rule. Although it may seem necessary to compute  $t^*$  as the greatest lower bound of all label types in practice, a simple sequential algorithm does not require this.

## $br_on_null\ l$

The instruction (br\_on\_null l) is valid with the instruction type  $t^*$  (ref null ht)  $\to t^*$  (ref ht) if:

- The result type C.labels[l] exists.
- The result type C.labels[l] is of the form  $t^*$ .
- The heap type ht is valid.

$$\frac{C.\mathsf{labels}[l] = t^* \qquad C \vdash ht : \mathsf{ok}}{C \vdash \mathsf{br\_on\_null} \ l : t^* \ (\mathsf{ref} \ \mathsf{null} \ ht) \to t^* \ (\mathsf{ref} \ ht)}$$

## $br_on_non_null\ l$

The instruction (br\_on\_non\_null l) is valid with the instruction type  $t^*$  (ref null ht)  $\to t^*$  if:

- The result type C.labels[l] exists.
- The result type C.labels[l] is of the form  $t^*$  (ref ht).

$$\frac{C.\mathsf{labels}[l] = t^* \; (\mathsf{ref} \; ht)}{C \vdash \mathsf{br\_on\_non\_null} \; l : t^* \; (\mathsf{ref} \; \mathsf{null} \; ht) \to t^*}$$

## $br_on_cast \ l \ rt_1 \ rt_2$

The instruction (br\_on\_cast l  $rt_1$   $rt_2$ ) is valid with the instruction type  $t^*$   $rt_1 \rightarrow t^*$  t' if:

- The result type C.labels[l] exists.
- The result type C.labels[l] is of the form  $t^*$  rt.
- The reference type  $rt_1$  is valid.
- The reference type  $rt_2$  is valid.
- The reference type  $rt_2$  matches the reference type  $rt_1$ .
- The reference type  $rt_2$  matches the reference type rt.
- Let t' be the reference type  $rt_1 \setminus rt_2$ .

$$\frac{C.\mathsf{labels}[l] = t^* \ rt \qquad C \vdash rt_1 : \mathsf{ok} \qquad C \vdash rt_2 : \mathsf{ok} \qquad C \vdash rt_2 \leq rt_1 \qquad C \vdash rt_2 \leq rt}{C \vdash \mathsf{br\_on\_cast} \ l \ rt_1 \ rt_2 : t^* \ rt_1 \rightarrow t^* \ (rt_1 \setminus rt_2)}$$

## $br\_on\_cast\_fail \ l \ rt_1 \ rt_2$

The instruction (br\_on\_cast\_fail  $l \ rt_1 \ rt_2$ ) is valid with the instruction type  $t^* \ rt_1 \ \to \ t^* \ rt_2$  if:

- $\bullet$  The result type  $C.\mathsf{labels}[l]$  exists.
- The result type C.labels[l] is of the form  $t^*$  rt.
- The reference type  $rt_1$  is valid.
- The reference type  $rt_2$  is valid.
- The reference type  $rt_2$  matches the reference type  $rt_1$ .
- The reference type  $rt_1 \setminus rt_2$  matches the reference type rt.

$$\frac{C.\mathsf{labels}[l] = t^* \ rt \qquad C \vdash rt_1 : \mathsf{ok} \qquad C \vdash rt_2 : \mathsf{ok} \qquad C \vdash rt_2 \leq rt_1 \qquad C \vdash rt_1 \setminus rt_2 \leq rt}{C \vdash \mathsf{br\_on\_cast\_fail} \ l \ rt_1 \ rt_2 : t^* \ rt_1 \rightarrow t^* \ rt_2}$$

#### $\operatorname{call} x$

The instruction (call x) is valid with the instruction type  $t_1^* \rightarrow t_2^*$  if:

- The defined type C.funcs[x] exists.
- The expansion of the defined type C.funcs[x] is the composite type (func  $t_1^* \to t_2^*$ ).

$$\frac{C.\mathsf{funcs}[x] \approx \mathsf{func}\; (t_1^* \to t_2^*)}{C \vdash \mathsf{call}\; x: t_1^* \to t_2^*}$$

# $\operatorname{call\_ref} x$

The instruction (call\_ref x) is valid with the instruction type  $t_1^*$  (ref null x)  $\to$   $t_2^*$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (func  $t_1^* \to t_2^*$ ).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{func}\; (t_1^* \to t_2^*)}{C \vdash \mathsf{call\_ref}\; x: t_1^* \; (\mathsf{ref}\; \mathsf{null}\; x) \to t_2^*}$$

# call\_indirect x y

The instruction (call\_indirect x y) is valid with the instruction type  $t_1^*$   $at \rightarrow t_2^*$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form ( $at \ lim \ rt$ ).
- The reference type rt matches the reference type (ref null func).
- The defined type C.types[y] exists.
- The expansion of the defined type C.types[y] is the composite type (func  $t_1^* \to t_2^*$ ).

$$\frac{C.\mathsf{tables}[x] = \mathit{at\ lim\ rt} \qquad C \vdash \mathit{rt} \leq (\mathsf{ref\ null\ func}) \qquad C.\mathsf{types}[y] \approx \mathsf{func\ } (t_1^* \to t_2^*)}{C \vdash \mathsf{call\_indirect}\ x\ y : t_1^*\ \mathit{at} \to t_2^*}$$

#### return

The instruction return is valid with the instruction type  $t_1^* t^* \rightarrow t_2^*$  if:

- The result type C return is of the form  $t^*$ .
- The instruction type  $t_1^* \to t_2^*$  is valid.

$$\frac{C.\mathsf{return} = (t^*) \qquad C \vdash t_1^* \to t_2^* : \mathsf{ok}}{C \vdash \mathsf{return} : t_1^* \ t^* \to t_2^*}$$

# Note

The return instruction is stack-polymorphic.

C.return is absent (set to  $\epsilon$ ) when validating an expression that is not a function body. This differs from it being set to the empty result type  $[\epsilon]$ , which is the case for functions not returning anything.

# $\mathsf{return\_call}\ x$

The instruction (return\_call x) is valid with the instruction type  $t_3^*$   $t_1^*$   $\to$   $t_4^*$  if:

- The defined type C.funcs[x] exists.
- The expansion of the defined type C.funcs[x] is the composite type (func  $t_1^* \to t_2^*$ ).
- The result type C. return is of the form  $t_2^*$ .
- The result type  $t_2^*$  matches the result type  $t_2^*$ .

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• The instruction type  $t_3^* \to t_4^*$  is valid.

$$\frac{C.\mathsf{funcs}[x] \approx \mathsf{func}\; (t_1^* \to t_2^*) \qquad C.\mathsf{return} = (t_2'') \qquad C \vdash t_2^* \leq t_2'' \qquad C \vdash t_3^* \to t_4^* : \mathsf{ok}}{C \vdash \mathsf{return\_call}\; x : t_3^* \; t_1^* \to t_4^*}$$

#### Note

The return\_call instruction is stack-polymorphic.

### $\mathsf{return\_call\_ref}\ x$

The instruction (return\_call\_ref x) is valid with the instruction type  $t_3^* t_1^*$  (ref null x)  $\to t_4^*$  if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (func  $t_1^* \to t_2^*$ ).
- The result type C.return is of the form  $t'_2^*$ .
- The result type  $t_2^*$  matches the result type  $t_2^*$ .
- The instruction type  $t_3^* \to t_4^*$  is valid.

$$\frac{C.\mathsf{types}[x] \approx \mathsf{func}\; (t_1^* \to t_2^*) \qquad C.\mathsf{return} = (t_2'') \qquad C \vdash t_2^* \leq t_2'' \qquad C \vdash t_3^* \to t_4^* : \mathsf{ok}}{C \vdash \mathsf{return\_call\_ref}\; x: t_3^*\; t_1^* \; (\mathsf{ref}\; \mathsf{null}\; x) \to t_4^*}$$

#### Note

The return\_call\_ref instruction is stack-polymorphic.

### return\_call\_indirect x y

The instruction (return\_call\_indirect  $x\ y$ ) is valid with the instruction type  $t_3^*\ t_1^*\ at\ \to\ t_4^*$  if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form (at  $\lim_{x \to \infty} rt$ ).
- The reference type rt matches the reference type (ref null func).
- The defined type C.types[y] exists.
- The expansion of the defined type C.types[y] is the composite type (func  $t_1^* \to t_2^*$ ).
- The result type C. return is of the form  $t_2^*$ .
- The result type  $t_2^*$  matches the result type  $t_2^*$ .
- The instruction type  $t_3^* \rightarrow t_4^*$  is valid.

$$\frac{C.\mathsf{tables}[x] = at \ lim \ rt \qquad C \vdash rt \leq (\mathsf{ref \ null \ func})}{C.\mathsf{types}[y] \approx \mathsf{func} \ (t_1^* \to t_2^*) \qquad C.\mathsf{return} = (t'_2^*) \qquad C \vdash t_2^* \leq t'_2^* \qquad C \vdash t_3^* \to t_4^* : \mathsf{ok}}{C \vdash \mathsf{return\_call\_indirect} \ x \ y : t_3^* \ t_1^* \ at \to t_4^*}$$

### Note

The return\_call\_indirect instruction is stack-polymorphic.

#### throw x

The instruction (throw x) is valid with the instruction type  $t_1^* t^* \rightarrow t_2^*$  if:

- The tag type C.tags[x] exists.
- The expansion of the defined type  $C.\mathsf{tags}[x]$  is the composite type (func  $t^* \to \epsilon$ ).
- The instruction type  $t_1^* \to t_2^*$  is valid.

$$\frac{C.\mathsf{tags}[x] \approx \mathsf{func}\; (t^* \to \epsilon) \qquad C \vdash t_1^* \to t_2^* : \mathsf{ok}}{C \vdash \mathsf{throw}\; x : t_1^* \; t^* \to t_2^*}$$

#### Note

The throw instruction is stack-polymorphic.

#### throw ref

The instruction throw\_ref is valid with the instruction type  $t_1^*$  (ref null exn)  $\to t_2^*$  if:

• The instruction type  $t_1^* \to t_2^*$  is valid.

$$\frac{C \vdash t_1^* \to t_2^* : \mathsf{ok}}{C \vdash \mathsf{throw\_ref} : t_1^* \ (\mathsf{ref} \ \mathsf{null} \ \mathsf{exn}) \to t_2^*}$$

#### Note

The throw\_ref instruction is stack-polymorphic.

# 3.4.12 Instruction Sequences

Typing of instruction sequences is defined recursively.

# **Empty Instruction Sequence:** $\epsilon$

The instruction sequence sequence  $instr'^*$  is valid with the instruction type it'' if:

- Either:
  - The instruction sequence sequence  $instr'^*$  is empty.
  - The instruction type it'' is of the form  $\epsilon \to \epsilon$ .
- Or:
  - The instruction sequence sequence  $instr'^*$  is of the form  $instr_1 \ instr_2^*$ .
  - The instruction type it'' is of the form  $t_1^* \to_{x_1^*} x_2^* t_3^*$ .
  - The instruction  $instr_1$  is valid with the instruction type  $t_1^* \rightarrow_{x_1^*} t_2^*$ .
  - The length of  $init^*$  is equal to the length of  $t^*$ .
  - The length of  $init^*$  is equal to the length of  $x_1^*$ .
  - For all  $x_1$  in  $x_1^*$ :
    - \* The local type C.locals[ $x_1$ ] exists.
  - For all init in init\*, and corresponding t in t\*, and corresponding  $x_1$  in  $x_1^*$ :
    - \* The local type C.locals[ $x_1$ ] is of the form (init t).
  - Under the context  $C[.local[x_1^*] = (\text{set } t)^*]$ , the instruction sequence sequence  $instr_2^*$  is valid with the instruction type  $t_2^* \to_{x_2^*} t_3^*$ .

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- Or:
  - The instruction sequence sequence  $instr'^*$  is of the form  $instr^*$ .
  - The instruction type it'' is of the form it'.
  - The instruction sequence sequence  $instr^*$  is valid with the instruction type it.
  - The instruction type it matches the instruction type it'.
  - The instruction type it' is valid.
- Or:
  - The instruction sequence sequence  $instr'^*$  is of the form  $instr^*$ .
  - The instruction type it'' is of the form  $t^* t_1^* \rightarrow_{x^*} t^* t_2^*$ .
  - The instruction sequence sequence instr\* is valid with the instruction type  $t_1^* \to_{x^*} t_2^*$ .
  - The result type  $t^*$  is valid.

#### Note

In combination with the previous rule, subsumption allows to compose instructions whose types would not directly fit otherwise. For example, consider the instruction sequence

To type this sequence, its subsequence (i32.const 2) (i32.add) needs to be valid with an intermediate type. But the direct type of (i32.const 2) is  $\epsilon \to i32$ , not matching the two inputs expected by i32.add. The subsumption rule allows to weaken the type of (const i32 2) to the supertype i32  $\to$  i32 i32, such that it can be composed with i32.add and yields the intermediate type i32  $\to$  i32 i32 for the subsequence. That can in turn be composed with the first constant.

Furthermore, subsumption allows to drop init variables  $x^*$  from the instruction type in a context where they are not needed, for example, at the end of the body of a block.

# 3.4.13 Expressions

Expressions expr are classified by result types  $t^*$ .

The expression  $instr^*$  is valid with the result type  $t^*$  if:

• The instruction sequence sequence  $instr^*$  is valid with the instruction type  $\epsilon \to t^*$ .

$$\frac{C \vdash instr^* : \epsilon \to_{\epsilon} t^*}{C \vdash instr^* : t^*}$$

# **Constant Expressions**

In a *constant* expression, all instructions must be constant.

 $instr^*$  is constant if:

- For all *instr* in *instr*\*:
  - instr is constant.

```
val is constant if:
   • Either:
         - The value val is of the form (nt.const c_{nt}).
   • Or:
         - The value val is of the form (vt.const c_{vt}).
   • Or:
         - The value val is of the form (ref.null ht).
   • Or:
         - The value val is of the form ref.i31.
   • Or:
         - The value val is of the form (ref.func x).
   • Or:
         - The value val is of the form (struct.new x).
   • Or:
         - The value val is of the form (struct.new_default x).
   • Or:
         - The value val is of the form (array.new x).
   • Or:
         - The value val is of the form (array.new_default x).
   • Or:
         - The value val is of the form (array.new_fixed x n).
   • Or:
         - The value val is of the form any.convert_extern.
   • Or:
         - The value val is of the form extern.convert_any.
   • Or:
         - The value val is of the form (global.get x).
```

– The global type C.globals[x] exists.

- The value val is of the form (in. binop).

- binop is contained in [add; sub; mul].

- iN is contained in [i32; i64].

• Or:

- The global type C.globals[x] is of the form  $(\epsilon t)$ .

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 $\frac{(C \vdash instr \mathsf{const})^*}{C \vdash instr^* \mathsf{const}}$ 

#### Note

Currently, constant expressions occurring in globals are further constrained in that contained global.get instructions are only allowed to refer to imported or previously defined globals. Constant expressions occurring in tables may only have global.get instructions that refer to imported globals. This is enforced in the validation rule for modules by constraining the context C accordingly.

The definition of constant expression may be extended in future versions of WebAssembly.

# 3.5 Modules

Modules are valid when all the components they contain are valid. To verify this, most definitions are themselves classified with a suitable type.

# 3.5.1 **Types**

The sequence of types defined in a module is validated incrementally, yielding a sequence of defined types representing them individually.

The type definition (type rectype) is valid with the defined type sequence sequence  $dt^*$  if:

- The length of C.types is equal to x.
- The defined type sequence sequence  $dt^*$  is of the form  $\operatorname{roll}_x^*(rectype)$ .
- Let C' be the same context as C, but with the defined type sequence sequence  $dt^*$  appended to the field types.
- Under the context C', the recursive type rectype is valid for (ok(x)).

$$\frac{x = |C.\mathsf{types}| \qquad dt^* = \mathrm{roll}_x^*(\mathit{rectype}) \qquad C \oplus \{\mathsf{types}\ dt^*\} \vdash \mathit{rectype} : \mathsf{ok}((x))}{C \vdash \mathsf{type}\ \mathit{rectype} : dt^*}$$

The type definition sequence sequence  $type'^*$  is valid with the defined type sequence sequence  $deftype^*$  if:

- Either:
  - The type definition sequence sequence  $type'^*$  is empty.
  - The defined type sequence sequence deftype\* is empty.
- Or:
  - The type definition sequence sequence  $type'^*$  is of the form  $type_1$   $type^*$ .
  - The defined type sequence sequence  $deftype^*$  is of the form  $dt_1^* dt^*$ .
  - The type definition  $type_1$  is valid with the defined type sequence sequence  $dt_1^*$ .
  - Let C' be the same context as C, but with the defined type sequence sequence  $dt_1^*$  appended to the field types.

- Under the context C', the type definition sequence sequence  $type^*$  is valid with the defined type sequence sequence  $dt^*$ .

$$\frac{C \vdash type_1 : dt_1^* \qquad C \oplus \{ \text{types } dt_1^* \} \vdash type^* : dt^*}{C \vdash type_1 \ type^* : dt_1^* \ dt^*}$$

# 3.5.2 Functions

Functions func are classified by defined types that expand to function types of the form func  $(t_1^* \to t_2^*)$ .

The function (func  $x \ local^* \ expr$ ) is valid with the defined type C.types[x] if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (func  $t_1^* o t_2^*$ ).
- The length of  $lt^*$  is equal to the length of  $local^*$ .
- For all lt in  $lt^*$ , and corresponding local in  $local^*$ :
  - The local local is valid with the local type lt.
- Under the context  $C[.locals = \oplus (set t_1)^* lt^*][.labels = \oplus t_2^*][.return = \oplus t_2^*]$ , the expression expr is valid with the result type  $t_2^*$ .

#### **Todo**

below is the official specification

- The defined type  $C.\mathsf{types}[x]$  must be a function type.
- Let func  $[t_1^*] o [t_2^*]$  be the expansion of the defined type C.types[x].
- For each local declared by a value type t in  $t^*$ :
  - The local for type t must be valid with local type  $local type_i$ .
- Let *localtype*\* be the concatenation of all *localtype*<sub>i</sub>.
- Let C' be the same context as C, but with:
  - locals set to the sequence of value types (set  $t_1$ )\* localtype\*, concatenating parameters and locals,
  - labels set to the singular sequence containing only result type  $[t_2^*]$ .
  - return set to the result type  $[t_2^*]$ .
- Under the context C', the expression expr must be valid with type  $[t_2^*]$ .
- Then the function definition is valid with type C.types[x].

$$\frac{C.\mathsf{types}[x] \approx \mathsf{func}\; (t_1^* \to t_2^*) \qquad (C \vdash local: \mathit{lt})^* \qquad C \oplus \{\mathsf{locals}\; (\mathsf{set}\; t_1)^* \; \mathit{lt}^*, \; \mathsf{labels}\; (t_2^*), \; \mathsf{return}\; (t_2^*)\} \vdash \mathit{expr}: t_2^*}{C \vdash \mathsf{func}\; x \; \mathit{local}^* \; \mathit{expr}: C.\mathsf{types}[x]}$$

# **3.5.3 Locals**

Locals *local* are classified with local types.

The local (local t) is valid with the local type (init t) if:

- Either:
  - The initialization status *init* is of the form set.
  - A default value for the value type t is defined.

• Or:

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- The initialization status *init* is of the form unset.
- A default value for the value type t is not defined.

$$\frac{\operatorname{default}_t \neq \epsilon}{C \vdash \operatorname{local} t : \operatorname{set} t} \qquad \frac{\operatorname{default}_t = \epsilon}{C \vdash \operatorname{local} t : \operatorname{unset} t}$$

#### Note

For cases where both rules are applicable, the former yields the more permissable type.

# **3.5.4 Tables**

Tables table are classified by table types.

The table (table tabletype expr) is valid with the table type tabletype if:

- The table type tabletype is valid.
- The table type table type is of the form  $(at \ lim \ rt)$ .
- The expression expr is valid with the value type rt.
- *expr* is constant.

$$\frac{C \vdash tabletype : \mathsf{ok} \qquad tabletype = at \ lim \ rt \qquad C \vdash expr : rt \ \mathsf{const}}{C \vdash \mathsf{table} \ tabletype \ expr : tabletype}$$

# 3.5.5 Memories

Memories mem are classified by memory types.

The memory (memory memtype) is valid with the memory type memtype if:

• The memory type memtype is valid.

$$\frac{C \vdash memtype : \mathsf{ok}}{C \vdash \mathsf{memory} \ memtype : memtype}$$

# 3.5.6 Globals

Globals global are classified by global types.

The global (global globaltype expr) is valid with the global type globaltype if:

- $\bullet\,$  The global type gt is valid.
- The global type global type is of the form (mut<sup>?</sup> t).
- The expression expr is valid with the value type t.
- expr is constant.

$$\frac{C \vdash \mathit{gt} : \mathsf{ok} \qquad \mathit{globaltype} = \mathsf{mut}^? \ t \qquad C \vdash \mathit{expr} : \mathit{t} \ \mathsf{const}}{C \vdash \mathsf{global} \ \mathit{globaltype} \ \mathit{expr} : \mathit{globaltype}}$$

Sequences of globals are handled incrementally, such that each definition has access to previous definitions.

The global sequence sequence  $global'^*$  is valid with the global type sequence sequence  $globaltype^*$  if:

- Either:
  - The global sequence sequence global'\* is empty.
  - The global type sequence sequence  $global type^*$  is empty.
- Or:

- The global sequence sequence global<sup>\*</sup> is of the form global<sub>1</sub> global<sup>\*</sup>.
- The global type sequence sequence  $global type^*$  is of the form  $gt_1$   $gt^*$ .
- The global  $global_1$  is valid with the global type  $gt_1$ .
- Let C' be the same context as C, but with the global type sequence sequence  $gt_1$  appended to the field globals.
- Under the context C', the global sequence sequence  $global^*$  is valid with the global type sequence sequence  $gt^*$ .

$$\frac{C \vdash global_1 : gt_1 \qquad C \oplus \{\mathsf{globals} \ gt_1\} \vdash global^* : gt^*}{C \vdash global_1 \ global^* : gt_1 \ gt^*}$$

# 3.5.7 Tags

Tags tag are classified by their tag types, which are defined types expanding to function types.

The tag (tag x) is valid with the tag type C.types[x] if:

- The defined type C.types[x] exists.
- The expansion of the defined type C.types[x] is the composite type (func functype).

$$\frac{C.\mathsf{types}[x] \approx \mathsf{func}\,\mathit{functype}}{C \vdash \mathsf{tag}\,x : C.\mathsf{types}[x]}$$

# 3.5.8 Element Segments

Element segments *elem* are classified by their element type.

The element segment (elem elemtype expr\* elemmode) is valid with the element type elemtype if:

- The reference type *elemtype* is valid.
- For all expr in  $expr^*$ :
  - The expression expr is valid with the value type elemtype.
  - expr is constant.
- ullet The element mode elemmode is valid with the element type elemtype.

$$\frac{C \vdash elemtype : \mathsf{ok} \qquad (C \vdash expr : elemtype \; \mathsf{const})^* \qquad C \vdash elemmode : elemtype}{C \vdash \mathsf{elem} \; elemtype \; expr^* \; elemmode : elemtype}$$

The element mode elemmode is valid with the element type rt if:

- Either:
  - The element mode elemmode is of the form (active  $x \ expr$ ).
  - The table type C.tables[x] exists.
  - The table type C.tables[x] is of the form  $(at \ lim \ rt')$ .
  - The reference type rt matches the reference type rt'.
  - The expression expr is valid with the value type i32.
  - expr is constant.
- Or:
  - The element mode *elemmode* is of the form passive.
- Or:
  - The element mode *elemmode* is of the form declare.

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$$\frac{C. \mathsf{tables}[x] = \mathit{at\ lim\ rt'} \qquad C \vdash \mathit{rt} \leq \mathit{rt'} \qquad C \vdash \mathit{expr} : \mathsf{i32\ const}}{C \vdash \mathsf{active}\ x\ \mathit{expr} : \mathit{rt}} \qquad \frac{C}{C} \vdash \mathsf{passive} : \mathit{rt}} \qquad \frac{C}{C} \vdash \mathsf{declare} : \mathit{rt}$$

# 3.5.9 Data Segments

Data segments data are classified by the singleton data type, which merely expresses well-formedness.

The data segment (data  $b^*$  datamode) is valid with the data type ok if:

• The data mode datamode is valid with the data type ok.

$$\frac{C \vdash datamode : \mathsf{ok}}{C \vdash \mathsf{data}\ b^*\ datamode : \mathsf{ok}}$$

The data mode datamode is valid with the data type ok if:

- Either:
  - The data mode data mode is of the form (active  $x \ expr$ ).
  - The memory type C.mems[x] exists.
  - The memory type C.mems[x] is of the form mt.
  - The expression expr is valid with the value type i32.
  - expr is constant.
- Or:
  - The data mode datamode is of the form passive.

$$\frac{C.\mathsf{mems}[x] = \mathit{mt} \qquad C \vdash \mathit{expr} : \mathsf{i32} \ \mathsf{const}}{C \vdash \mathsf{active} \ \mathit{x} \ \mathit{expr} : \mathsf{ok}} \qquad \qquad \frac{C \vdash \mathsf{passive} : \mathsf{ok}}{C \vdash \mathsf{passive} : \mathsf{ok}}$$

### 3.5.10 Start Function

The start function (start x) is valid if:

- The defined type C.funcs[x] exists.
- The expansion of the defined type C.funcs[x] is the composite type (func  $\epsilon \to \epsilon$ ).

$$\frac{C.\mathsf{funcs}[x] \approx \mathsf{func}\; (\epsilon \to \epsilon)}{C \vdash \mathsf{start}\; x : \mathsf{ok}}$$

# **3.5.11 Exports**

Exports export are classified by their external type.

The export (export name externidx) is valid with the name name and the external type xt if:

• The external index externidx is valid with the external type xt.

$$\frac{C \vdash externidx : xt}{C \vdash export \ name \ externidx : name \ xt}$$

func x

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The external index (func x) is valid with the external type (func dt) if:

- The defined type C.funcs[x] exists.
- The defined type C.funcs[x] is of the form dt.

$$\frac{C.\mathsf{funcs}[x] = dt}{C \vdash \mathsf{func}\; x : \mathsf{func}\; dt}$$

#### table x

The external index (table x) is valid with the external type (table tt) if:

- The table type C.tables[x] exists.
- The table type C.tables[x] is of the form tt.

$$\frac{C.\mathsf{tables}[x] = tt}{C \vdash \mathsf{table}\; x : \mathsf{table}\; tt}$$

#### mem x

The external index (memory x) is valid with the external type (mem mt) if:

- The memory type C.mems[x] exists.
- The memory type C.mems[x] is of the form mt.

$$\frac{C.\mathsf{mems}[x] = mt}{C \vdash \mathsf{memory} \; x : \mathsf{mem} \; mt}$$

# $\operatorname{\mathsf{global}} x$

The external index (global x) is valid with the external type (global gt) if:

- The global type C.globals[x] exists.
- The global type C.globals [x] is of the form gt.

$$\frac{C.\mathsf{globals}[x] = gt}{C \vdash \mathsf{global}\ x : \mathsf{global}\ gt}$$

#### tag x

The external index (tag x) is valid with the external type (tag jt) if:

- The tag type C.tags[x] exists.
- The tag type C.tags[x] is of the form jt.

$$\frac{C.\mathsf{tags}[x] = jt}{C \vdash \mathsf{tag}\; x : \mathsf{tag}\; it}$$

# **3.5.12 Imports**

Imports import are classified by external types.

The import (import  $name_1$   $name_2$  xt) is valid with the external type xt if:

• The external type xt is valid.

$$\frac{C \vdash xt : \mathsf{ok}}{C \vdash \mathsf{import} \ name_1 \ name_2 \ xt : xt}$$

# **3.5.13 Modules**

Modules are classified by their mapping from the external types of their imports to those of their exports.

A module is entirely closed, that is, its components can only refer to definitions that appear in the module itself. Consequently, no initial context is required. Instead, the context C for validation of the module's content is constructed from the definitions in the module.

The module (module  $type^*$   $import^*$   $func^*$   $global^*$   $table^*$   $mem^*$   $tag^*$   $elem^*$   $data^*$   $start^?$   $export^*$ ) is valid with the module type t if:

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- Under the context {return  $\epsilon$ }, the type definition sequence sequence type\* is valid with the defined type sequence sequence  $dt'^*$ .
- The length of  $import^*$  is equal to the length of  $xt_i^*$ .
- For all *import* in *import*\*, and corresponding  $xt_i$  in  $xt_i^*$ :
  - Under the context {types  $dt'^*$ , return  $\epsilon$ }, the import import is valid with the external type  $xt_i$ .
- Under the context C', the global sequence sequence  $global^*$  is valid with the global type sequence  $gt^*$ .
- The length of  $table^*$  is equal to the length of  $tt^*$ .
- For all table in table\*, and corresponding tt in tt\*:
  - Under the context C', the table table is valid with the table type tt.
- The length of  $mem^*$  is equal to the length of  $mt^*$ .
- For all mem in  $mem^*$ , and corresponding mt in  $mt^*$ :
  - Under the context C', the memory mem is valid with the memory type mt.
- The length of  $jt^*$  is equal to the length of  $tag^*$ .
- For all jt in  $jt^*$ , and corresponding tag in  $tag^*$ :
  - Under the context C', the tag tag is valid with the tag type jt.
- The length of  $dt^*$  is equal to the length of  $func^*$ .
- For all dt in  $dt^*$ , and corresponding func in func\*:
  - The function func is valid with the defined type dt.
- The length of  $elem^*$  is equal to the length of  $rt^*$ .
- For all elem in  $elem^*$ , and corresponding rt in  $rt^*$ :
  - The element segment elem is valid with the element type rt.
- The length of  $data^*$  is equal to the length of  $ok^*$ .
- For all data in data\*, and corresponding ok in ok\*:
  - The data segment data is valid.
- If *start* is defined, then:
  - The start function *start* is valid.
- The length of  $export^*$  is equal to the length of  $nm^*$ .
- The length of  $export^*$  is equal to the length of  $xt_e^*$ .
- For all export in export\*, and corresponding nm in  $nm^*$ , and corresponding  $xt_e$  in  $xt_e^*$ :
  - The export export is valid with the name nm and the external type  $xt_e$ .
- $nm^*$  disjoint is of the form true.
- The context C is of the form  $C'[.globals = \oplus gt^*][.tables = \oplus tt^*_i tt^*][.mems = \oplus mt^*_i mt^*][.tags = \oplus jt^*_i jt^*][.elems = \oplus rt^*][.datas = \oplus ok^*].$
- The context C' is of the form {types  $dt'^*$ , funcs  $dt_i^*$   $dt^*$ , globals  $gt_i^*$ , return  $\epsilon$ , refs  $x^*$ }.
- The function index sequence sequence  $x^*$  is of the form funcidx( $global^*$   $table^*$   $mem^*$   $elem^*$   $data^*$ ).
- The defined type sequence sequence  $dt_i^*$  is of the form funcs $(xt_i^*)$ .
- The global type sequence sequence  $gt_i^*$  is of the form globals  $(xt_i^*)$ .
- The table type sequence sequence  $tt_i^*$  is of the form tables  $(xt_i^*)$ .
- The memory type sequence sequence  $mt_i^*$  is of the form mems $(xt_i^*)$ .

- The tag type sequence sequence  $jt_i^*$  is of the form  $tags(xt_i^*)$ .
- Let t be the module type  $\operatorname{clos}_C(xt_i^* \to xt_e^*)$ .

#### Todo

below is the official specification

- Let *module* be the module to validate.
- The types module types must be valid yielding a context  $C_0$ .
- Let C be a context where:
  - C.types is  $C_0$ .types,
  - C.funcs is funcs( $it^*$ ) concatenated with  $dt^*$ , with the import's external types  $it^*$  and the internal defined types  $dt^*$  as determined below,
  - C.tables is tables( $it^*$ ) concatenated with  $tt^*$ , with the import's external types  $it^*$  and the internal table types  $tt^*$  as determined below,
  - C.mems is  $mems(it^*)$  concatenated with  $mt^*$ , with the import's external types  $it^*$  and the internal memory types  $mt^*$  as determined below,
  - C.globals is globals( $it^*$ ) concatenated with  $gt^*$ , with the import's external types  $it^*$  and the internal global types  $gt^*$  as determined below,
  - C.tags is tags( $it^*$ ) concatenated with  $ht^*$ , with the import's external types  $it^*$  and the internal tag types  $ht^*$  as determined below,
  - C.elems is  $rt^*$  as determined below,
  - C.datas is  $ok^*$  as determined below,
  - C.locals is empty,
  - C.labels is empty,
  - C.return is empty.
  - C.refs is the set  $\operatorname{funcidx}(module \text{ with } \operatorname{funcs} = \epsilon \text{ with } \operatorname{start} = \epsilon)$ , i.e., the set of function indices occurring in the module, except in its functions or start function.
- Let C' be the context where:
  - C'.globals is the sequence globals( $it^*$ ),
  - C'.types is the same as C.types,
  - C'.funcs is the same as C.funcs,
  - C'.tables is the same as C.tables,
  - C'.mems is the same as C.mems,
  - C'.refs is the same as C.refs,
  - all other fields are empty.
- Under the context C':
  - The sequence module.globals of globals must be valid with a sequence  $gt^*$  of global types.
  - For each  $table_i$  in module.tables, the definition  $table_i$  must be valid with a table type  $tt_i$ .
  - For each  $mem_i$  in module mems, the definition  $mem_i$  must be valid with a memory type  $mt_i$ .
- Under the context C:
  - For each  $func_i$  in module funcs, the definition  $func_i$  must be valid with a defined type  $dt_i$ .

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- For each  $tag_i$  in module tags, the definition  $tag_i$  must be valid with a tag type  $ht_i$ .
- For each  $elem_i$  in module elems, the segment  $elem_i$  must be valid with reference type  $rt_i$ .
- For each  $data_i$  in module.datas, the segment  $data_i$  must be valid with data type  $ok_i$ .
- If *module*.start is non-empty, then *module*.start must be valid.
- For each  $import_i$  in module imports, the segment  $import_i$  must be valid with an external type  $it_i$ .
- For each  $export_i$  in module.exports, the segment  $export_i$  must be valid with external type  $et_i$ .
- Let  $dt^*$  be the concatenation of the internal function types  $dt_i$ , in index order.
- Let  $tt^*$  be the concatenation of the internal table types  $tt_i$ , in index order.
- Let  $mt^*$  be the concatenation of the internal memory types  $mt_i$ , in index order.
- $\bullet$  Let  $gt^{\ast}$  be the concatenation of the internal global types  $gt_{i},$  in index order.
- Let  $ht^*$  be the concatenation of the internal tag types  $ht_i$ , in index order.
- Let  $rt^*$  be the concatenation of the reference types  $rt_i$ , in index order.
- Let  $ok^*$  be the concatenation of the data types  $ok_i$ , in index order.
- Let  $it^*$  be the concatenation of external types  $it_i$  of the imports, in index order.
- Let  $et^*$  be the concatenation of external types  $et_i$  of the exports, in index order.
- All export names *export*<sub>i</sub>.name must be different.
- Then the module is valid with external types  $it^* \to et^*$ .

```
\{\} \vdash type^* : dt'^* \quad (\{\mathsf{types}\ dt'^*\} \vdash import : xt_{\mathsf{i}})^* \\ C' \vdash global^* : gt^* \quad (C' \vdash table : tt)^* \quad (C' \vdash mem : mt)^* \quad (C' \vdash tag : jt)^* \quad (C \vdash func : dt)^* \\ (C \vdash elem : rt)^* \quad (C \vdash data : ok)^* \quad (C \vdash start : ok)^? \quad (C \vdash export : nm \ xt_{\mathsf{e}})^* \quad nm^* \ disjoint \\ C = C' \oplus \{\mathsf{globals}\ gt^*,\ \mathsf{tables}\ tt^*_{\mathsf{i}}\ tt^*,\ \mathsf{mems}\ mt^*_{\mathsf{i}}\ mt^*,\ \mathsf{tags}\ jt^*_{\mathsf{i}}\ jt^*,\ \mathsf{elems}\ rt^*,\ \mathsf{datas}\ ok^*\} \\ C' = \{\mathsf{types}\ dt'^*,\ \mathsf{funcs}\ dt^*_{\mathsf{i}}\ dt^*,\ \mathsf{globals}\ gt^*_{\mathsf{i}},\ \mathsf{refs}\ x^*\} \quad x^* = \mathsf{funcidx}(global^*\ table^*\ mem^*\ elem^*\ data^*) \\ dt^*_{\mathsf{i}} = \mathsf{funcs}(xt^*_{\mathsf{i}}) \quad gt^*_{\mathsf{i}} = \mathsf{globals}(xt^*_{\mathsf{i}}) \quad tt^*_{\mathsf{i}} = \mathsf{tables}(xt^*_{\mathsf{i}}) \quad mt^*_{\mathsf{i}} = \mathsf{mems}(xt^*_{\mathsf{i}}) \quad jt^*_{\mathsf{i}} = \mathsf{tags}(xt^*_{\mathsf{i}}) \\ \vdash \mathsf{module}\ type^*\ import^*\ func^*\ global^*\ table^*\ mem^*\ tag^*\ elem^*\ data^*\ start^?\ export^*: \mathsf{clos}_C(xt^*_{\mathsf{i}} \to xt^*_{\mathsf{e}}) \\ \end{cases}
```

#### Todo

Check refs; check export names

### Note

All functions in a module are mutually recursive. Consequently, the definition of the context C in this rule is recursive: it depends on the outcome of validation of the function, table, memory, and global definitions contained in the module, which itself depends on C. However, this recursion is just a specification device. All types needed to construct C can easily be determined from a simple pre-pass over the module that does not perform any actual validation.

Globals, however, are not recursive but evaluated sequentially, such that each constant expressions only has access to imported or previously defined globals.

# CHAPTER 4

Execution

# 4.1 Conventions

WebAssembly code is *executed* when instantiating a module or invoking an exported function on the resulting module instance.

Execution behavior is defined in terms of an *abstract machine* that models the *program state*. It includes a *stack*, which records operand values and control constructs, and an abstract *store* containing global state.

For each instruction, there is a rule that specifies the effect of its execution on the program state. Furthermore, there are rules describing the instantiation of a module. As with validation, all rules are given in two *equivalent* forms:

- 1. In *prose*, describing the execution in intuitive form.
- 2. In *formal notation*, describing the rule in mathematical form. <sup>18</sup>

# Note

As with validation, the prose and formal rules are equivalent, so that understanding of the formal notation is *not* required to read this specification. The formalism offers a more concise description in notation that is used widely in programming languages semantics and is readily amenable to mathematical proof.

# 4.1.1 Prose Notation

Execution is specified by stylised, step-wise rules for each instruction of the abstract syntax. The following conventions are adopted in stating these rules.

- ullet The execution rules implicitly assume a given store S.
- The execution rules also assume the presence of an implicit stack that is modified by *pushing* or *popping* values, labels, and frames.
- Certain rules require the stack to contain at least one frame. The most recent frame is referred to as the *current* frame.

<sup>&</sup>lt;sup>18</sup> The semantics is derived from the following article: Andreas Haas, Andreas Rossberg, Derek Schuff, Ben Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman. Bringing the Web up to Speed with WebAssembly<sup>19</sup>. Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017). ACM 2017.

<sup>19</sup> https://dl.acm.org/citation.cfm?doid=3062341.3062363

- Both the store and the current frame are mutated by *replacing* some of their components. Such replacement is assumed to apply globally.
- The execution of an instruction may *trap*, in which case the entire computation is aborted and no further modifications to the store are performed by it. (Other computations can still be initiated afterwards.)
- The execution of an instruction may also end in a *jump* to a designated target, which defines the next instruction to execute.
- Execution can enter and exit instruction sequences that form blocks.
- Instruction sequences are implicitly executed in order, unless a trap, jump, or exception occurs.
- In various places the rules contain assertions expressing crucial invariants about the program state.

#### 4.1.2 Formal Notation

#### Note

This section gives a brief explanation of the notation for specifying execution formally. For the interested reader, a more thorough introduction can be found in respective text books. <sup>20</sup>

The formal execution rules use a standard approach for specifying operational semantics, rendering them into *reduction rules*. Every rule has the following general form:

$$configuration \hookrightarrow configuration$$

A *configuration* is a syntactic description of a program state. Each rule specifies one *step* of execution. As long as there is at most one reduction rule applicable to a given configuration, reduction – and thereby execution – is *deterministic*. WebAssembly has only very few exceptions to this, which are noted explicitly in this specification.

For WebAssembly, a configuration typically is a tuple  $(s; f; instr^*)$  consisting of the current store s, the call frame f of the current function, and the sequence of instructions that is to be executed. (A more precise definition is given later.)

To avoid unnecessary clutter, the store s and the frame f are often combined into a *state* z, which is a pair (s; f). Moreover, z is omitted from reduction rules that do not touch them.

There is no separate representation of the stack. Instead, it is conveniently represented as part of the configuration's instruction sequence. In particular, values are defined to coincide with const and ref instructions, and a sequence of such instructions can be interpreted as an operand "stack" that grows to the right.

#### Note

For example, the reduction rule for the i32.add instruction can be given as follows:

(i32.const 
$$n_1$$
) (i32.const  $n_2$ ) (i32.add)  $\hookrightarrow$  (i32.const  $(n_1 + n_2) \bmod 2^{32}$ )

Per this rule, two const instructions and the add instruction itself are removed from the instruction stream and replaced with one new const instruction. This can be interpreted as popping two values off the stack and pushing the result.

When no result is produced, an instruction reduces to the empty sequence:

$$\mathsf{nop} \hookrightarrow \epsilon$$

Labels and frames are similarly defined to be part of an instruction sequence.

<sup>&</sup>lt;sup>20</sup> For example: Benjamin Pierce. Types and Programming Languages<sup>21</sup>. The MIT Press 2002

<sup>21</sup> https://www.cis.upenn.edu/~bcpierce/tapl/

The order of reduction is determined by the details of the reduction rules. Usually, the left-most instruction that is not a constant will be the subject of the next reduction *step*.

Reduction *terminates* when no more reduction rules are applicable. Soundness of the WebAssembly type system guarantees that this is only the case when the original instruction sequence has either been reduced to a sequence of value instructions, which can be interpreted as the values of the resulting operand stack, or if an exception or trap occurred.

#### Note

# 4.2 Runtime Structure

Store, stack, and other *runtime structure* forming the WebAssembly abstract machine, such as values or module instances, are made precise in terms of additional auxiliary syntax.

#### **4.2.1 Values**

WebAssembly computations manipulate *values* of either the four basic number types, i.e., integers and floating-point data of 32 or 64 bit width each, or vectors of 128 bit width, or of reference type.

In most places of the semantics, values of different types can occur. In order to avoid ambiguities, values are therefore represented with an abstract syntax that makes their type explicit. It is convenient to reuse the same notation as for the const instructions and ref.null producing them.

References other than null are represented with additional administrative instructions. They either are *scalar references*, containing a 31-bit integer, *structure references*, pointing to a specific structure address, *array references*, pointing to a specific array address, *function references*, pointing to a specific function address, *exception references*, pointing to a specific exception address, or *host references* pointing to an uninterpreted form of host address defined by the embedder. Any of the aformentioned references can furthermore be wrapped up as an *external reference*.

```
val ::= num \mid vec \mid ref
num ::= numtype.const num_{numtype}
vec ::= vectype.const vec_{vectype}
ref ::= addrref
\mid ref.null \ heaptype
addrref ::= ref.is1 \ us1
\mid ref.struct \ structaddr
\mid ref.array \ arrayaddr
\mid ref.exen \ exnaddr
\mid ref.extern \ addrref
```

#### Note

Future versions of WebAssembly may add additional forms of values.

Value types can have an associated *default value*; it is the respective value 0 for number types, 0 for vector types, and null for nullable reference types. For other references, no default value is defined, default<sub>t</sub> hence is an optional value  $val^2$ .

```
\begin{array}{lll} \operatorname{default}_{iN} & = & (i \text{N.const } 0) \\ \operatorname{default}_{fN} & = & (f \text{N.const } + 0) \\ \operatorname{default}_{vN} & = & (v \text{N.const } 0) \\ \operatorname{default}_{\text{ref null } ht} & = & (\text{ref.null } ht) \\ \operatorname{default}_{\text{ref } ht} & = & \epsilon \end{array}
```

# Convention

ullet The meta variable r ranges over reference values where clear from context.

# 4.2.2 Results

A result is the outcome of a computation. It is either a sequence of values, a thrown exception, or a trap.

```
result ::= val^* \mid (ref.exn \ exnaddr) \ throw\_ref \mid trap
```

#### 4.2.3 Store

The *store* represents all global state that can be manipulated by WebAssembly programs. It consists of the runtime representation of all *instances* of functions, tables, memories, globals, tags, element segments, data segments, and structures, arrays or exceptions that have been allocated during the life time of the abstract machine.

It is an invariant of the semantics that no element or data instance is addressed from anywhere else but the owning module instances.

Syntactically, the store is defined as a record listing the existing instances of each category:

#### Note

In practice, implementations may apply techniques like garbage collection or reference counting to remove objects from the store that are no longer referenced. However, such techniques are not semantically observable, and hence outside the scope of this specification.

# Convention

ullet The meta variable s ranges over stores where clear from context.

# 4.2.4 Addresses

Function instances, table instances, memory instances, global instances, tag instances, element instances, data instances and structure, array or exception instances in the store are referenced with abstract *addresses*. These are simply indices into the respective store component. In addition, an embedder may supply an uninterpreted set of *host addresses*.

```
\begin{array}{rcl} addr & ::= & 0 \mid 1 \mid 2 \mid \dots \\ funcaddr & ::= & addr \\ tableaddr & ::= & addr \\ memaddr & ::= & addr \\ globaladdr & ::= & addr \\ tagaddr & ::= & addr \\ elemaddr & ::= & addr \\ dataaddr & ::= & addr \\ structaddr & ::= & addr \\ arrayaddr & ::= & addr \\ hostaddr & ::= & addr \end{array}
```

An embedder may assign identity to exported store objects corresponding to their addresses, even where this identity is not observable from within WebAssembly code itself (such as for function instances or immutable globals).

#### Note

Addresses are *dynamic*, globally unique references to runtime objects, in contrast to indices, which are *static*, module-local references to their original definitions. A *memory address memaddr* denotes the abstract address *of* a memory *instance* in the store, not an offset *inside* a memory instance.

There is no specific limit on the number of allocations of store objects, hence logical addresses can be arbitrarily large natural numbers.

# **Conventions**

• The notation addr(A) denotes the set of addresses from address space addr occurring free in A. We sometimes reinterpret this set as the list of its elements, without assuming any particular order.

### 4.2.5 External Addresses

An *external address* is the runtime address of an entity that can be imported or exported. It is an address denoting either a function instance, global instance, table instance, memory instance, or tag instance in the shared store.

```
externaddr ::= func funcaddr \mid global global global ddr \mid table tableaddr \mid mem memaddr \mid tag tagaddr
```

#### 4.2.6 Module Instances

A *module instance* is the runtime representation of a module. It is created by instantiating a module, and collects runtime representations of all entities that are imported, defined, or exported by the module.

```
moduleinst ::= {types deftype* funcs funcaddr* globals globaladdr* tables tableaddr* mems memaddr* tags tagaddr* elems elemaddr* datas dataaddr* exports exportinst*}
```

Each component references runtime instances corresponding to respective declarations from the original module – whether imported or defined – in the order of their static indices. Function instances, table instances, memory instances, global instances, and tag instances are denoted by their respective addresses in the store.

It is an invariant of the semantics that all export instances in a given module instance have different names.

#### Note

All record fields except exports are to be considered *private* components of a module instance. They are not accessible to other modules, only to function instances originating from the same module.

# 4.2.7 Function Instances

A *function instance* is the runtime representation of a function. It effectively is a *closure* of the original function over the runtime module instance of its originating module. The module instance is used to resolve references to other definitions during execution of the function.

```
funcinst ::= \{ type \ deftype, module \ module inst, code \ code \} 
code ::= func \mid hostfunc
```

A *host function* is a function expressed outside WebAssembly but passed to a module as an import. The definition and behavior of host functions are outside the scope of this specification. For the purpose of this specification, it is assumed that when invoked, a host function behaves non-deterministically, but within certain constraints that ensure the integrity of the runtime.

#### Note

Function instances are immutable, and their identity is not observable by WebAssembly code. However, an embedder might provide implicit or explicit means for distinguishing their addresses.

#### 4.2.8 Table Instances

A table instance is the runtime representation of a table. It records its type and holds a sequence of reference values.

```
tableinst ::= \{ type \ table type, elem \ ref^* \}
```

Table elements can be mutated through table instructions, the execution of an active element segment, or by external means provided by the embedder.

It is an invariant of the semantics that all table elements have a type matching the element type of *tabletype*. It also is an invariant that the length of the element sequence never exceeds the maximum size of *tabletype*.

### 4.2.9 Memory Instances

A *memory instance* is the runtime representation of a linear memory. It records its type and holds a sequence of bytes.

```
meminst ::= \{ type memtype, bytes byte^* \}
```

The length of the sequence always is a multiple of the WebAssembly *page size*, which is defined to be the constant 65536 – abbreviated 64 Ki.

A memory's bytes can be mutated through memory instructions, the execution of an active data segment, or by external means provided by the embedder.

It is an invariant of the semantics that the length of the byte sequence, divided by page size, never exceeds the maximum size of *memtype*.

#### 4.2.10 Global Instances

A *global instance* is the runtime representation of a global variable. It records its type and holds an individual value.

```
globalinst ::= \{type globaltype, value val\}
```

The value of mutable globals can be mutated through variable instructions or by external means provided by the embedder.

It is an invariant of the semantics that the value has a type matching the value type of *globaltype*.

# 4.2.11 Tag Instances

A tag instance is the runtime representation of a tag definition. It records the defined type of the tag.

```
taginst ::= \{type \ tagtype\}
```

# 4.2.12 Element Instances

An element instance is the runtime representation of an element segment. It holds a list of references and its type.

```
eleminst ::= \{ type \ elemtype, elem \ ref^* \}
```

It is an invariant of the semantics that all elements of a segment have a type matching *elemtype*.

#### 4.2.13 Data Instances

An data instance is the runtime representation of a data segment. It holds a list of bytes.

```
datainst ::= \{bytes \ byte^*\}
```

# 4.2.14 Export Instances

An *export instance* is the runtime representation of an export. It defines the export's name and the associated external address.

```
exportinst ::= \{name \ name, addr \ externaddr\}
```

# **Conventions**

The following auxiliary functions are assumed on sequences of external addresses. They extract addresses of a specific kind in an order-preserving fashion:

- funcs $(xa^*)$  extracts all function addresses from  $xa^*$ ,
- tables( $xa^*$ ) extracts all table addresses from  $xa^*$ ,
- mems $(xa^*)$  extracts all memory addresses from  $xa^*$ ,
- globals $(xa^*)$  extracts all global addresses from  $xa^*$ ,
- $tags(xa^*)$  extracts all tag addresses from  $xa^*$ .

# 4.2.15 Aggregate Instances

A *structure instance* is the runtime representation of a heap object allocated from a structure type. Likewise, an *array instance* is the runtime representation of a heap object allocated from an array type. Both record their respective defined type and hold a list of the values of their *fields*.

```
structinst ::= {type deftype, fields fieldval^*} arrayinst ::= {type deftype, fields fieldval^*} fieldval ::= val \mid packval packval ::= packtype.pack iN
```

#### **Conventions**

• Conversion of a regular value to a field value is defined as follows:

```
\operatorname{pack}_{valtype}(val) = val

\operatorname{pack}_{packtype}(i32.\mathsf{const}\ i) = packtype.\mathsf{pack}\ \operatorname{wrap}_{32,|packtype|}(i)
```

• The inverse conversion of a field value to a regular value is defined as follows:

```
\begin{array}{lll} \operatorname{unpack}_{valtype}^{\epsilon}(val) & = & val \\ \operatorname{unpack}_{packtype}^{sx}(packtype.\mathsf{pack}\ i) & = & \operatorname{i32.const}\ \operatorname{extend}_{|packtype|,32}^{sx}(i) \end{array}
```

# 4.2.16 Exception Instances

An *exception instance* is the runtime representation of an exception produced by a throw instruction. It holds the address of the respective tag and the argument values.

```
exninst ::= \{ tag \ tagaddr, fields \ val^* \}
```

#### 4.2.17 Stack

Besides the store, most instructions interact with an implicit stack. The stack contains the two kinds of entries:

- Values: the operands of instructions.
- Control Frames: currently active control flow structures.

The latter can in turn be one of the following:

- Labels: active structured control instructions that can be targeted by branches.
- (Call) Frames: the activation records of active function calls.
- *Handlers*: active exception handlers.

#### Note

Where clear from context, call frame is abbreviated to just frame.

All these entries can occur on the stack in any order during the execution of a program. Stack entries are described by abstract syntax as follows.

# Note

It is possible to model the WebAssembly semantics using separate stacks for operands, control constructs, and calls. However, because the stacks are interdependent, additional book keeping about associated stack heights would be required. For the purpose of this specification, an interleaved representation is simpler.

#### **Values**

Values are represented by themselves.

#### Lahele

Labels carry an argument arity n and their associated branch target, which is expressed syntactically as an instruction sequence:

$$label ::= label_n \{instr^*\}$$

Intuitively,  $instr^*$  is the *continuation* to execute when the branch is taken, in place of the original control construct.

#### Note

For example, a loop label has the form

$$label_n\{(loop\ bt\ \dots)\}$$

When performing a branch to this label, this executes the loop, effectively restarting it from the beginning. Conversely, a simple block label has the form

$$label_n\{\epsilon\}$$

When branching, the empty continuation ends the targeted block, such that execution can proceed with consecutive instructions.

### **Call Frames**

Call frames carry the return arity n of the respective function, hold the values of its locals (including arguments) in the order corresponding to their static local indices, and a reference to the function's own module instance:

```
callframe ::= frame_n\{frame\}
frame ::= \{locals (val^?)^*, module module inst\}
```

Locals may be uninitialized, in which case they are empty. Locals are mutated by respective variable instructions.

# **Exception Handlers**

Exception handlers are installed by try\_table instructions and record the corresponding list of catch clauses:

$$handler ::= handler_n\{catch^*\}$$

The handlers on the stack are searched when an exception is thrown.

### Conventions

- ullet The meta variable L ranges over labels where clear from context.
- ullet The meta variable f ranges over frame states where clear from context.
- ullet The meta variable H ranges over exception handlers where clear from context.
- The following auxiliary definition takes a block type and looks up the instruction type that it denotes in the current frame:

$$\text{instrtype}_z(x) = ft \quad \text{if } z. \text{types}[x] \approx \text{func } ft \\ \text{instrtype}_z(t^?) = \epsilon \rightarrow t^?$$

# 4.2.18 Administrative Instructions

#### Note

This section is only relevant for the formal notation.

In order to express the reduction of traps, calls, exception handling, and control instructions, the syntax of instructions is extended to include the following *administrative instructions*:

```
\begin{array}{cccc} instr & ::= & \dots \\ & | & addrref \\ & | & label_n\{instr^*\} \ instr^* \\ & | & frame_n\{frame\} \ instr^* \\ & | & handler_n\{catch^*\} \ instr^* \\ & | & trap \end{array}
```

An address reference represents an allocated reference value of respective form "on the stack".

The label, frame, and handler instructions model labels, frames, and active exception handlers, respectively, "on the stack". Moreover, the administrative syntax maintains the nesting structure of the original structured control instruction or function body and their instruction sequences.

The trap instruction represents the occurrence of a trap. Traps are bubbled up through nested instruction sequences, ultimately reducing the entire program to a single trap instruction, signalling abrupt termination.

#### Note

For example, the reduction rule for block is:

```
(\operatorname{block}\ bt\ instr^*) \hookrightarrow (\operatorname{label}_n\{\epsilon\}\ instr^*)
```

if the block type bt denotes a function type  $t_1^m \to t_2^n$ , such that n is the block's result arity. This rule replaces the block with a label instruction, which can be interpreted as "pushing" the label on the stack. When its end is reached, i.e., the inner instruction sequence has been reduced to the empty sequence – or rather, a sequence of n values representing the results – then the label instruction is eliminated courtesy of its own reduction rule:

$$(label_n\{instr^*\}\ val^*) \hookrightarrow val^*$$

This can be interpreted as removing the label from the stack and only leaving the locally accumulated operand values. Validation guarantees that n matches the number  $|val^*|$  of resulting values at this point.

# **Configurations**

A *configuration* describes the current computation. It consists of the computations's *state* and the sequence of instructions left to execute. The state in turn consists of a global store and a current frame referring to the module instance in which the computation runs, i.e., where the current function originates from.

```
config ::= state; instr^*

state ::= store; frame
```

#### Note

The current version of WebAssembly is single-threaded, but configurations with multiple threads may be supported in the future.

# 4.3 Numerics

Numeric primitives are defined in a generic manner, by operators indexed over a bit width N.

Some operators are *non-deterministic*, because they can return one of several possible results (such as different NaN values). Technically, each operator thus returns a *set* of allowed values. For convenience, deterministic results are expressed as plain values, which are assumed to be identified with a respective singleton set.

Some operators are *partial*, because they are not defined on certain inputs. Technically, an empty set of results is returned for these inputs.

In formal notation, each operator is defined by equational clauses that apply in decreasing order of precedence. That is, the first clause that is applicable to the given arguments defines the result. In some cases, similar clauses are combined into one by using the notation  $\pm$  or  $\mp$ . When several of these placeholders occur in a single clause, then they must be resolved consistently: either the upper sign is chosen for all of them or the lower sign.

#### Note

For example, the fcopysign operator is defined as follows:

$$\begin{array}{lcl} \text{fcopysign}_N(\pm p_1, \pm p_2) & = & \pm p_1 \\ \text{fcopysign}_N(\pm p_1, \mp p_2) & = & \mp p_1 \end{array}$$

This definition is to be read as a shorthand for the following expansion of each clause into two separate ones:

$$\begin{array}{llll} \operatorname{fcopysign}_N(+p_1,+p_2) & = & +p_1 \\ \operatorname{fcopysign}_N(-p_1,-p_2) & = & -p_1 \\ \operatorname{fcopysign}_N(+p_1,-p_2) & = & -p_1 \\ \operatorname{fcopysign}_N(-p_1,+p_2) & = & +p_1 \end{array}$$

Numeric operators are lifted to input sequences by applying the operator element-wise, returning a sequence of results. When there are multiple inputs, they must be of equal length.

$$op(c_1^n, \dots, c_k^n) = op(c_1^n[0], \dots, c_k^n[0]) \dots op(c_1^n[n-1], \dots, c_k^n[n-1])$$

#### Note

For example, the unary operator fabs, when given a sequence of floating-point values, return a sequence of floating-point results:

$$fabs_N(z^n) = fabs_N(z[0]) \dots fabs_N(z[n])$$

The binary operator iadd, when given two sequences of integers of the same length, n, return a sequence of integer results:

$$iadd_N(i_1^n, i_2^n) = iadd_N(i_1[0], i_2[0]) \dots iadd_N(i_1[n], i_2[n])$$

# Conventions:

- The meta variable d is used to range over single bits.
- The meta variable p is used to range over (signless) magnitudes of floating-point values, including nan and  $\infty$ .
- The meta variable q is used to range over (signless) rational magnitudes, excluding nan or  $\infty$ .
- The notation  $f^{-1}$  denotes the inverse of a bijective function f.
- Truncation of rational values is written  $trunc(\pm q)$ , with the usual mathematical definition:

$$\operatorname{trunc}(\pm q) = \pm i \quad (\text{if } i \in \mathbb{N} \land +q-1 < i \leq +q)$$

• Saturation of integers is written  $\operatorname{sat\_u}_N(i)$  and  $\operatorname{sat\_s}_N(i)$ . The arguments to these two functions range over arbitrary signed integers.

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- Unsigned saturation, sat\_ $u_N(i)$  clamps i to between 0 and  $2^N - 1$ :

$$\begin{array}{lcl} {\rm sat\_u}_N(i) & = & 0 & \quad & ({\rm if} \ i < 0) \\ {\rm sat\_u}_N(i) & = & 2^N - 1 & \quad & ({\rm if} \ i > 2^N - 1) \\ {\rm sat\_u}_N(i) & = & i & \quad & ({\rm otherwise}) \end{array}$$

- Signed saturation, sat\_ $s_N(i)$  clamps i to between  $-2^{N-1}$  and  $2^{N-1}-1$ :

$$\begin{array}{lll} \mathrm{sat\_s}_N(i) & = & -2^{N-1} & \quad \text{(if } i < -2^{N-1}) \\ \mathrm{sat\_s}_N(i) & = & 2^{N-1} - 1 & \quad \text{(if } i > 2^{N-1} - 1) \\ \mathrm{sat\_s}_N(i) & = & i & \quad \text{(otherwise)} \end{array}$$

# 4.3.1 Representations

Numbers and numeric vectors have an underlying binary representation as a sequence of bits:

$$\operatorname{bits}_{iN}(i) = \operatorname{ibits}_{N}(i)$$
  
 $\operatorname{bits}_{fN}(z) = \operatorname{fbits}_{N}(z)$   
 $\operatorname{bits}_{vN}(i) = \operatorname{ibits}_{N}(i)$ 

The first case of these applies to representations of both integer value types and packed types.

Each of these functions is a bijection, hence they are invertible.

### **Integers**

Integers are represented as base two unsigned numbers:

$$ibits_N(i) = d_{N-1} \dots d_0 \qquad (i = 2^{N-1} \cdot d_{N-1} + \dots + 2^0 \cdot d_0)$$

Boolean operators like  $\land$ ,  $\lor$ , or  $\lor$  are lifted to bit sequences of equal length by applying them pointwise.

# **Floating-Point**

Floating-point values are represented in the respective binary format defined by IEEE 754<sup>22</sup> (Section 3.4):

```
\begin{array}{lll} \mathrm{fbits}_N(\pm(1+m\cdot 2^{-M})\cdot 2^e) & = & \mathrm{fsign}(\pm) \, \mathrm{ibits}_E(e+\mathrm{fbias}_N) \, \mathrm{ibits}_M(m) \\ \mathrm{fbits}_N(\pm(0+m\cdot 2^{-M})\cdot 2^e) & = & \mathrm{fsign}(\pm) \, (0)^E \, \mathrm{ibits}_M(m) \\ \mathrm{fbits}_N(\pm\infty) & = & \mathrm{fsign}(\pm) \, (1)^E \, (0)^M \\ \mathrm{fbits}_N(\pm \mathrm{nan}(n)) & = & \mathrm{fsign}(\pm) \, (1)^E \, \mathrm{ibits}_M(n) \\ & = & \mathrm{fsign}(\pm) \, (1)^E \, \mathrm{ibits}_M(n) \\ & = & 2^{E-1} - 1 \\ \mathrm{fsign}(+) & = & 0 \\ \mathrm{fsign}(-) & = & 1 \end{array}
```

where  $M = \operatorname{signif}(N)$  and  $E = \operatorname{expon}(N)$ .

#### **Vectors**

Numeric vectors of type  $\forall N$  have the same underlying representation as an iN. They can also be interpreted as a sequence of numeric values packed into a  $\forall N$  with a particular  $shape\ t\times M$ , provided that  $N=|t|\cdot M$ .

lanes<sub>t×M</sub>(c) = 
$$c_0 \dots c_{M-1}$$
  
(where  $w = |t|/8$   
 $\land b^* = \text{bytes}_{iN}(c)$   
 $\land c_i = \text{bytes}_i^{-1}(b^*[i \cdot w : w]))$ 

This function is a bijection on iN, hence it is invertible.

<sup>&</sup>lt;sup>22</sup> https://ieeexplore.ieee.org/document/8766229

#### Todo

pack/unpacknum

### **Storage**

When a number is stored into memory, it is converted into a sequence of bytes in little endian<sup>23</sup> byte order:

```
\begin{array}{lll} \mathrm{bytes}_t(i) & = & \mathrm{littleendian}(\mathrm{bits}_t(i)) \\ \mathrm{littleendian}(\epsilon) & = & \epsilon \\ \mathrm{littleendian}(d^8 \, {d'}^* \,) & = & \mathrm{littleendian}({d'}^*) \, \mathrm{ibits}_8^{-1}(d^8) \end{array}
```

Again these functions are invertible bijections.

# 4.3.2 Integer Operations

### **Sign Interpretation**

Integer operators are defined on *iN* values. Operators that use a signed interpretation convert the value using the following definition, which takes the two's complement when the value lies in the upper half of the value range (i.e., its most significant bit is 1):

$$\operatorname{signed}_{N}(i) = i \qquad (0 \le i < 2^{N-1})$$
  
 $\operatorname{signed}_{N}(i) = i - 2^{N} \qquad (2^{N-1} \le i < 2^{N})$ 

This function is bijective, and hence invertible.

# **Boolean Interpretation**

The integer result of predicates – i.e., tests and relational operators – is defined with the help of the following auxiliary function producing the value 1 or 0 depending on a condition.

$$bool(C) = 1$$
 (if  $C$ )  
 $bool(C) = 0$  (otherwise)

 $iadd_N(i_1, i_2)$ 

• Return the result of adding  $i_1$  and  $i_2$  modulo  $2^N$ .

$$iadd_N(i_1, i_2) = (i_1 + i_2) \bmod 2^N$$

 $isub_N(i_1, i_2)$ 

• Return the result of subtracting  $i_2$  from  $i_1$  modulo  $2^N$ .

$$isub_N(i_1, i_2) = (i_1 - i_2 + 2^N) \bmod 2^N$$

 $imul_N(i_1, i_2)$ 

• Return the result of multiplying  $i_1$  and  $i_2$  modulo  $2^N$ .

$$\operatorname{imul}_N(i_1, i_2) = (i_1 \cdot i_2) \bmod 2^N$$

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<sup>&</sup>lt;sup>23</sup> https://en.wikipedia.org/wiki/Endianness#Little-endian

# $idiv_u_N(i_1, i_2)$

- If  $i_2$  is 0, then the result is undefined.
- Else, return the result of dividing  $i_1$  by  $i_2$ , truncated toward zero.

$$\operatorname{idiv}_{u_N}(i_1, 0) = \{\}$$
  
 $\operatorname{idiv}_{u_N}(i_1, i_2) = \operatorname{trunc}(i_1/i_2)$ 

#### Note

This operator is partial.

# $idiv_s_N(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$ .
- Let  $j_2$  be the signed interpretation of  $i_2$ .
- If  $j_2$  is 0, then the result is undefined.
- Else if  $j_1$  divided by  $j_2$  is  $2^{N-1}$ , then the result is undefined.
- Else, return the result of dividing  $j_1$  by  $j_2$ , truncated toward zero.

```
\begin{array}{lll} \operatorname{idiv\_s}_N(i_1,0) &=& \{ \} \\ \operatorname{idiv\_s}_N(i_1,i_2) &=& \{ \} \\ \operatorname{idiv\_s}_N(i_1,i_2) &=& \operatorname{signed}_N^{-1}(\operatorname{trunc}(\operatorname{signed}_N(i_1)/\operatorname{signed}_N(i_2)) = 2^{N-1}) \end{array}
```

#### Note

This operator is partial. Besides division by 0, the result of  $(-2^{N-1})/(-1) = +2^{N-1}$  is not representable as an N-bit signed integer.

#### irem\_ $\mathbf{u}_N(i_1,i_2)$

- If  $i_2$  is 0, then the result is undefined.
- Else, return the remainder of dividing  $i_1$  by  $i_2$ .

#### Note

This operator is partial.

As long as both operators are defined, it holds that  $i_1 = i_2 \cdot \text{idiv}_u(i_1, i_2) + \text{irem}_u(i_1, i_2)$ .

#### irem\_s<sub>N</sub> $(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$ .
- Let  $j_2$  be the signed interpretation of  $i_2$ .
- If  $i_2$  is 0, then the result is undefined.
- Else, return the remainder of dividing  $j_1$  by  $j_2$ , with the sign of the dividend  $j_1$ .

#### Note

This operator is partial.

As long as both operators are defined, it holds that  $i_1 = i_2 \cdot \text{idiv\_s}(i_1, i_2) + \text{irem\_s}(i_1, i_2)$ .

# $inot_N(i)$

• Return the bitwise negation of i.

$$\operatorname{inot}_N(i) = \operatorname{ibits}_N^{-1}(\operatorname{ibits}_N(i) \vee \operatorname{ibits}_N(2^N - 1))$$

# $irev_N(i)$

• Return the bitwise reversal of i.

$$\operatorname{irev}_N(i) = \operatorname{ibits}_N^{-1}((d^N[N-i])^{i \le N}) \quad (\text{if } d^N = \operatorname{ibits}_N(i))$$

# $iand_N(i_1, i_2)$

• Return the bitwise conjunction of  $i_1$  and  $i_2$ .

$$\operatorname{iand}_{N}(i_{1}, i_{2}) = \operatorname{ibits}_{N}^{-1}(\operatorname{ibits}_{N}(i_{1}) \wedge \operatorname{ibits}_{N}(i_{2}))$$

### $iandnot_N(i_1, i_2)$

• Return the bitwise conjunction of  $i_1$  and the bitwise negation of  $i_2$ .

$$iandnot_N(i_1, i_2) = iand_N(i_1, inot_N(i_2))$$

# $ior_N(i_1,i_2)$

• Return the bitwise disjunction of  $i_1$  and  $i_2$ .

$$ior_N(i_1, i_2) = ibits_N^{-1}(ibits_N(i_1) \vee ibits_N(i_2))$$

# $ixor_N(i_1, i_2)$

• Return the bitwise exclusive disjunction of  $i_1$  and  $i_2$ .

$$ixor_N(i_1, i_2) = ibits_N^{-1}(ibits_N(i_1) \vee ibits_N(i_2))$$

# $ishl_N(i_1,i_2)$

- Let k be  $i_2$  modulo N.
- Return the result of shifting  $i_1$  left by k bits, modulo  $2^N$ .

$$ishl_N(i_1, i_2) = ibits_N^{-1}(d_2^{N-k} 0^k)$$
 (if  $ibits_N(i_1) = d_1^k d_2^{N-k} \wedge k = i_2 \mod N$ )

 $ishr_u_N(i_1,i_2)$ 

- Let k be  $i_2$  modulo N.
- Return the result of shifting  $i_1$  right by k bits, extended with 0 bits.

$$ishr_u_N(i_1, i_2) = ibits_N^{-1}(0^k d_1^{N-k})$$
 (if  $ibits_N(i_1) = d_1^{N-k} d_2^k \wedge k = i_2 \mod N$ )

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 $ishr_s_N(i_1, i_2)$ 

- Let k be  $i_2$  modulo N.
- Return the result of shifting  $i_1$  right by k bits, extended with the most significant bit of the original value.

$$\mathrm{ishr\_s}_N(i_1,i_2) \ = \ \mathrm{ibits}_N^{-1}(d_0^{k+1} \ d_1^{N-k-1}) \quad (\mathrm{if} \ \mathrm{ibits}_N(i_1) = d_0 \ d_1^{N-k-1} \ d_2^k \wedge k = i_2 \ \mathrm{mod} \ N)$$

 $irotl_N(i_1, i_2)$ 

- Let k be  $i_2$  modulo N.
- Return the result of rotating  $i_1$  left by k bits.

$$irotl_N(i_1, i_2) = ibits_N^{-1}(d_2^{N-k} d_1^k)$$
 (if  $ibits_N(i_1) = d_1^k d_2^{N-k} \wedge k = i_2 \mod N$ )

 $irotr_N(i_1, i_2)$ 

- Let k be  $i_2$  modulo N.
- Return the result of rotating  $i_1$  right by k bits.

$$irotr_N(i_1, i_2) = ibits_N^{-1}(d_2^k d_1^{N-k})$$
 (if  $ibits_N(i_1) = d_1^{N-k} d_2^k \wedge k = i_2 \mod N$ )

 $iclz_N(i)$ 

• Return the count of leading zero bits in i; all bits are considered leading zeros if i is 0.

$$iclz_N(i) = k \quad (if ibits_N(i) = 0^k (1 d^*)^?)$$

 $ictz_N(i)$ 

• Return the count of trailing zero bits in i; all bits are considered trailing zeros if i is 0.

$$ictz_N(i) = k$$
 (if  $ibits_N(i) = (d^* 1)^? 0^k$ )

 $ipopcnt_N(i)$ 

• Return the count of non-zero bits in i.

$$ipopcnt_N(i) = k \quad (if ibits_N(i) = (0^* 1)^k 0^*)$$

 $ieqz_N(i)$ 

• Return 1 if i is zero, 0 otherwise.

$$ieqz_N(i) = bool(i = 0)$$

 $inez_N(i)$ 

• Return 0 if i is zero, 1 otherwise.

$$inez_N(i) = bool(i = / = 0)$$

 $ieq_N(i_1,i_2)$ 

• Return 1 if  $i_1$  equals  $i_2$ , 0 otherwise.

$$ieq_N(i_1, i_2) = bool(i_1 = i_2)$$

# $ine_N(i_1,i_2)$

• Return 1 if  $i_1$  does not equal  $i_2$ , 0 otherwise.

$$\operatorname{ine}_N(i_1, i_2) = \operatorname{bool}(i_1 \neq i_2)$$

# $ilt_u_N(i_1, i_2)$

• Return 1 if  $i_1$  is less than  $i_2$ , 0 otherwise.

$$ilt_u_N(i_1, i_2) = bool(i_1 < i_2)$$

# ilt\_s<sub>N</sub> $(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$ .
- Let  $j_2$  be the signed interpretation of  $i_2$ .
- Return 1 if  $j_1$  is less than  $j_2$ , 0 otherwise.

$$ilt_s_N(i_1, i_2) = bool(signed_N(i_1) < signed_N(i_2))$$

# $\operatorname{igt}_{\mathbf{u}_N}(i_1, i_2)$

• Return 1 if  $i_1$  is greater than  $i_2$ , 0 otherwise.

$$\operatorname{igt\_u}_N(i_1, i_2) = \operatorname{bool}(i_1 > i_2)$$

# $\operatorname{igt\_s}_N(i_1,i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$ .
- Let  $j_2$  be the signed interpretation of  $i_2$ .
- Return 1 if  $j_1$  is greater than  $j_2$ , 0 otherwise.

$$igt_s_N(i_1, i_2) = bool(signed_N(i_1) > signed_N(i_2))$$

# $ile_u_N(i_1, i_2)$

• Return 1 if  $i_1$  is less than or equal to  $i_2$ , 0 otherwise.

$$ile_u_N(i_1, i_2) = bool(i_1 \leq i_2)$$

# ile\_ $s_N(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$ .
- Let  $j_2$  be the signed interpretation of  $i_2$ .
- Return 1 if  $j_1$  is less than or equal to  $j_2$ , 0 otherwise.

$$ile_s_N(i_1, i_2) = bool(signed_N(i_1) \le signed_N(i_2))$$

# $ige_u_N(i_1, i_2)$

• Return 1 if  $i_1$  is greater than or equal to  $i_2$ , 0 otherwise.

$$ige_u_N(i_1, i_2) = bool(i_1 \ge i_2)$$

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# $ige\_s_N(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$ .
- Let  $j_2$  be the signed interpretation of  $i_2$ .
- Return 1 if  $j_1$  is greater than or equal to  $j_2$ , 0 otherwise.

$$ige_s_N(i_1, i_2) = bool(signed_N(i_1) \ge signed_N(i_2))$$

# iextend $M_s_N(i)$

- Let j be the result of computing  $\operatorname{wrap}_{N,M}(i)$ .
- Return extend  $_{M,N}(j)$ .

$$\operatorname{iextend} M_{s_N}(i) = \operatorname{extend}_{M,N}(\operatorname{wrap}_{N,M}(i))$$

# ibitselect<sub>N</sub> $(i_1, i_2, i_3)$

- Let  $j_1$  be the bitwise conjunction of  $i_1$  and  $i_3$ .
- Let  $j_3'$  be the bitwise negation of  $i_3$ .
- Let  $j_2$  be the bitwise conjunction of  $i_2$  and  $j_3'$ .
- Return the bitwise disjunction of  $j_1$  and  $j_2$ .

$$ibitselect_N(i_1, i_2, i_3) = ior_N(iand_N(i_1, i_3), iand_N(i_2, inot_N(i_3)))$$

# $iabs_N(i)$

- Let j be the signed interpretation of i.
- If j is greater than or equal to 0, then return i.
- Else return the negation of j, modulo  $2^N$ .

$$iabs_N(i) = i$$
 (if  $signed_N(i) \ge 0$ )  
 $iabs_N(i) = -signed_N(i) \mod 2^N$  (otherwise)

# $ineg_N(i)$

• Return the result of negating i, modulo  $2^N$ .

$$\operatorname{ineg}_N(i) = (2^N - i) \mod 2^N$$

# $\min_{\mathbf{u}} \mathbf{u}_N(i_1, i_2)$

• Return  $i_1$  if ilt\_ $u_N(i_1, i_2)$  is 1, return  $i_2$  otherwise.

$$\begin{aligned} & \min_{\mathbf{u}_N}(i_1,i_2) &= i_1 & (\text{if } \mathrm{ilt}_{\mathbf{u}_N}(i_1,i_2) = 1) \\ & \min_{\mathbf{u}_N}(i_1,i_2) &= i_2 & (\text{otherwise}) \end{aligned}$$

### $\min_{s_N(i_1, i_2)}$

• Return  $i_1$  if ilt\_s<sub>N</sub> $(i_1, i_2)$  is 1, return  $i_2$  otherwise.

$$\underset{i \in S_N(i_1, i_2)}{\min_s_N(i_1, i_2)} = i_1 \quad (\text{if } ilt_s_N(i_1, i_2) = 1) \\
\underset{i \in S_N(i_1, i_2)}{\min_s_N(i_1, i_2)} = i_2 \quad (\text{otherwise})$$

# $\max_{\mathbf{u}} \mathbf{u}_N(i_1, i_2)$

• Return  $i_1$  if  $igt_u_N(i_1, i_2)$  is 1, return  $i_2$  otherwise.

$$\begin{array}{lcl} \mathrm{imax\_u}_N(i_1,i_2) &=& i_1 & (\mathrm{if} \ \mathrm{igt\_u}_N(i_1,i_2) = 1) \\ \mathrm{imax\_u}_N(i_1,i_2) &=& i_2 & (\mathrm{otherwise}) \end{array}$$

# $\max_{s_N(i_1, i_2)}$

• Return  $i_1$  if  $igt_s_N(i_1, i_2)$  is 1, return  $i_2$  otherwise.

$$\max_{S_N(i_1, i_2)} = i_1$$
 (if  $\operatorname{igt\_s_N}(i_1, i_2) = 1$ )  
 $\max_{S_N(i_1, i_2)} = i_2$  (otherwise)

### $iadd\_sat\_u_N(i_1, i_2)$

- Let i be the result of adding  $i_1$  and  $i_2$ .
- Return  $\operatorname{sat}_{\mathbf{u}_N}(i)$ .

$$iadd_sat_u_N(i_1, i_2) = sat_u_N(i_1 + i_2)$$

# $iadd\_sat\_s_N(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$
- Let  $j_2$  be the signed interpretation of  $i_2$
- Let j be the result of adding  $j_1$  and  $j_2$ .
- Return the value whose signed interpretation is  $\operatorname{sat\_s}_N(j)$ .

$$iadd\_sat\_s_N(i_1, i_2) = signed_N^{-1}(sat\_s_N(signed_N(i_1) + signed_N(i_2)))$$

### $isub\_sat\_u_N(i_1, i_2)$

- Let i be the result of subtracting  $i_2$  from  $i_1$ .
- Return  $\operatorname{sat}_{\mathbf{u}_N}(i)$ .

isub sat 
$$u_N(i_1, i_2) = \text{sat } u_N(i_1 - i_2)$$

# $isub\_sat\_s_N(i_1, i_2)$

- Let  $j_1$  be the signed interpretation of  $i_1$
- Let  $j_2$  be the signed interpretation of  $i_2$
- Let j be the result of subtracting  $j_2$  from  $j_1$ .
- Return the value whose signed interpretation is  $\operatorname{sat\_s}_N(j)$ .

$$\operatorname{isub\_sat\_s}_N(i_1, i_2) = \operatorname{signed}_N^{-1}(\operatorname{sat\_s}_N(\operatorname{signed}_N(i_1) - \operatorname{signed}_N(i_2)))$$

### $iavgr_u_N(i_1, i_2)$

- Let j be the result of adding  $i_1$ ,  $i_2$ , and 1.
- Return the result of dividing j by 2, truncated toward zero.

$$iavgr_u_N(i_1, i_2) = trunc((i_1 + i_2 + 1)/2)$$

# $iq15mulrsat\_s_N(i_1, i_2)$

• Return the whose signed interpretation is the result of  $sat_s_N(ishr_s_N(i_1 \cdot i_2 + 2^{14}, 15))$ .

```
iq15mulrsat_s<sub>N</sub>(i_1, i_2) = signed_N^{-1}(sat_s_N(ishr_s_N(i_1 \cdot i_2 + 2^{14}, 15)))
```

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# 4.3.3 Floating-Point Operations

Floating-point arithmetic follows the IEEE 754<sup>24</sup> standard, with the following qualifications:

- All operators use round-to-nearest ties-to-even, except where otherwise specified. Non-default directed rounding attributes are not supported.
- Following the recommendation that operators propagate NaN payloads from their operands is permitted but not required.
- All operators use "non-stop" mode, and floating-point exceptions are not otherwise observable. In particular, neither alternate floating-point exception handling attributes nor operators on status flags are supported. There is no observable difference between quiet and signalling NaNs.

#### Note

Some of these limitations may be lifted in future versions of WebAssembly.

### Rounding

Rounding always is round-to-nearest ties-to-even, in correspondence with IEEE 754<sup>25</sup> (Section 4.3.1).

An exact floating-point number is a rational number that is exactly representable as a floating-point number of given bit width N.

A *limit* number for a given floating-point bit width N is a positive or negative number whose magnitude is the smallest power of 2 that is not exactly representable as a floating-point number of width N (that magnitude is  $2^{128}$  for N=32 and  $2^{1024}$  for N=64).

A *candidate* number is either an exact floating-point number or a positive or negative limit number for the given bit width N.

A candidate pair is a pair  $z_1, z_2$  of candidate numbers, such that no candidate number exists that lies between the two.

A real number r is converted to a floating-point value of bit width N as follows:

- If r is 0, then return +0.
- Else if r is an exact floating-point number, then return r.
- Else if r greater than or equal to the positive limit, then return  $+\infty$ .
- Else if r is less than or equal to the negative limit, then return  $-\infty$ .
- Else if  $z_1$  and  $z_2$  are a candidate pair such that  $z_1 < r < z_2$ , then:
  - If  $|r z_1| < |r z_2|$ , then let z be  $z_1$ .
  - Else if  $|r z_1| > |r z_2|$ , then let z be  $z_2$ .
  - Else if  $|r-z_1|=|r-z_2|$  and the significand of  $z_1$  is even, then let z be  $z_1$ .
  - Else, let z be  $z_2$ .
- If z is 0, then:
  - If r < 0, then return -0.
  - Else, return +0.
- Else if z is a limit number, then:
  - If r < 0, then return −∞.
  - Else, return  $+\infty$ .

<sup>&</sup>lt;sup>24</sup> https://ieeexplore.ieee.org/document/8766229

<sup>&</sup>lt;sup>25</sup> https://ieeexplore.ieee.org/document/8766229

• Else, return z.

```
float_N(0)
                                  = +0
float_N(r)
                                                                          (if r \in \operatorname{exact}_N)
                                  = r
float_N(r)
                                                                          (if r \geq + \text{limit}_N)
                                  = +\infty
float_N(r)
                                                                          (if r \leq -limit_N)
                                  = -\infty
float_N(r)
                                  = \operatorname{closest}_N(r, z_1, z_2)
                                                                          (if z_1 < r < z_2 \land (z_1, z_2) \in \text{candidatepair}_N)
\operatorname{closest}_N(r, z_1, z_2) = \operatorname{rectify}_N(r, z_1)
                                                                          (if |r-z_1| < |r-z_2|)
                                                                          (if |r - z_1| > |r - z_2|)
\operatorname{closest}_N(r, z_1, z_2) = \operatorname{rectify}_N(r, z_2)
                                                                          (if |r - z_1| = |r - z_2| \wedge even_N(z_1))
                                 = \operatorname{rectify}_{N}(r, z_1)
\operatorname{closest}_N(r,z_1,z_2)
                                                                          (if |r - z_1| = |r - z_2| \wedge even_N(z_2))
\operatorname{closest}_N(r,z_1,z_2)
                                  = rectify _N(r,z_2)
\operatorname{rectify}_{N}(r, \pm \operatorname{limit}_{N}) = \pm \infty
\operatorname{rectify}_{N}(r,0)
                                 = +0
                                                    (r \ge 0)
\operatorname{rectify}_{N}(r,0)
                                 = -0
                                                    (r < 0)
\operatorname{rectify}_{N}(r,z)
```

#### where:

```
\begin{array}{lll} \operatorname{exact}_N & = & fN \cap \mathbb{Q} \\ \operatorname{limit}_N & = & 2^{2^{\operatorname{expon}(N)-1}} \\ \operatorname{candidate}_N & = & \operatorname{exact}_N \cup \{+\operatorname{limit}_N, -\operatorname{limit}_N\} \\ \operatorname{candidatepair}_N & = & \{(z_1, z_2) \in \operatorname{candidate}_N^2 \mid z_1 < z_2 \wedge \forall z \in \operatorname{candidate}_N, z \leq z_1 \vee z \geq z_2\} \\ \operatorname{even}_N((d+m \cdot 2^{-M}) \cdot 2^e) & \Leftrightarrow & m \operatorname{mod} 2 = 0 \\ \operatorname{even}_N(\pm \operatorname{limit}_N) & \Leftrightarrow & \operatorname{true} \end{array}
```

### **NaN Propagation**

When the result of a floating-point operator other than fneg, fabs, or fcopysign is a NaN, then its sign is non-deterministic and the payload is computed as follows:

- If the payload of all NaN inputs to the operator is canonical (including the case that there are no NaN inputs), then the payload of the output is canonical as well.
- Otherwise the payload is picked non-deterministically among all arithmetic NaNs; that is, its most significant bit is 1 and all others are unspecified.
- In the deterministic profile, however, a positive canonical NaNs is reliably produced in the latter case.

The non-deterministic result is expressed by the following auxiliary function producing a set of allowed outputs from a set of inputs:

```
\begin{array}{rcl} & \operatorname{nans}_N\{z^*\} &=& \{+\operatorname{nan}(\operatorname{canon}_N)\} \\ \text{[!DET]} & \operatorname{nans}_N\{z^*\} &=& \{+\operatorname{nan}(n), -\operatorname{nan}(n) \mid n = \operatorname{canon}_N\} \\ \text{[!DET]} & \operatorname{nans}_N\{z^*\} &=& \{+\operatorname{nan}(n), -\operatorname{nan}(n) \mid n \geq \operatorname{canon}_N\} \\ \end{array} \quad \begin{array}{rcl} & \text{(if } \{z^*\} \subseteq \{+\operatorname{nan}(\operatorname{canon}_N), -\operatorname{nan}(\operatorname{canon}_N)\} \\ & \text{(if } \{z^*\} \not\subseteq \{+\operatorname{nan}(\operatorname{canon}_N), -\operatorname{nan}(\operatorname{canon}_N)\} \\ \end{array}
```

#### $fadd_N(z_1,z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if both  $z_1$  and  $z_2$  are infinities of opposite signs, then return an element of  $nans_N\{\}$ .
- Else if both  $z_1$  and  $z_2$  are infinities of equal sign, then return that infinity.
- Else if either  $z_1$  or  $z_2$  is an infinity, then return that infinity.
- Else if both  $z_1$  and  $z_2$  are zeroes of opposite sign, then return positive zero.
- Else if both  $z_1$  and  $z_2$  are zeroes of equal sign, then return that zero.
- Else if either  $z_1$  or  $z_2$  is a zero, then return the other operand.
- Else if both  $z_1$  and  $z_2$  are values with the same magnitude but opposite signs, then return positive zero.
- Else return the result of adding  $z_1$  and  $z_2$ , rounded to the nearest representable value.

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```
fadd_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
fadd_N(z_1, \pm nan(n)) = nans_N\{\pm nan(n), z_1\}
fadd_N(\pm \infty, \mp \infty) = nans_N\{\}
fadd_N(\pm\infty,\pm\infty)
                          = \pm \infty
fadd_N(z_1,\pm\infty)
                          = \pm \infty
fadd_N(\pm\infty,z_2)
                          = \pm \infty
fadd_N(\pm 0, \mp 0)
                         = +0
fadd_N(\pm 0, \pm 0)
                         = \pm 0
fadd_N(z_1,\pm 0)
                         = z_1
fadd_N(\pm 0, z_2)
                          = z_2
                          = +0
fadd_N(\pm q, \mp q)
fadd_N(z_1, z_2)
                          = \operatorname{float}_N(z_1 + z_2)
```

### $fsub_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if both  $z_1$  and  $z_2$  are infinities of equal signs, then return an element of  $nans_N\{\}$ .
- Else if both  $z_1$  and  $z_2$  are infinities of opposite sign, then return  $z_1$ .
- Else if  $z_1$  is an infinity, then return that infinity.
- Else if  $z_2$  is an infinity, then return that infinity negated.
- Else if both  $z_1$  and  $z_2$  are zeroes of equal sign, then return positive zero.
- Else if both  $z_1$  and  $z_2$  are zeroes of opposite sign, then return  $z_1$ .
- Else if  $z_2$  is a zero, then return  $z_1$ .
- Else if  $z_1$  is a zero, then return  $z_2$  negated.
- Else if both  $z_1$  and  $z_2$  are the same value, then return positive zero.
- Else return the result of subtracting  $z_2$  from  $z_1$ , rounded to the nearest representable value.

```
\operatorname{fsub}_N(\pm \operatorname{nan}(n), z_2) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_2\}
\operatorname{fsub}_N(z_1, \pm \operatorname{nan}(n)) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_1\}
fsub_N(\pm \infty, \pm \infty) = nans_N\{\}
fsub_N(\pm\infty, \mp\infty) = \pm\infty
fsub_N(z_1, \pm \infty) = \mp \infty
fsub_N(\pm\infty,z_2)
                              = \pm \infty
fsub_N(\pm 0, \pm 0)
                              = +0
                              = \pm 0
fsub_N(\pm 0, \mp 0)
                                = z_1
fsub_N(z_1,\pm 0)
fsub_N(\pm 0, \pm q_2)
                                = \mp q_2
fsub_N(\pm q, \pm q)
                                = +0
                               = \operatorname{float}_N(z_1 - z_2)
\mathrm{fsub}_N(z_1,z_2)
```

#### Note

Up to the non-determinism regarding NaNs, it always holds that  $fsub_N(z_1, z_2) = fadd_N(z_1, fneg_N(z_2))$ .

#### $\operatorname{fmul}_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if one of  $z_1$  and  $z_2$  is a zero and the other an infinity, then return an element of  $nans_N\{\}$ .
- Else if both  $z_1$  and  $z_2$  are infinities of equal sign, then return positive infinity.
- Else if both  $z_1$  and  $z_2$  are infinities of opposite sign, then return negative infinity.
- Else if either  $z_1$  or  $z_2$  is an infinity and the other a value with equal sign, then return positive infinity.

- Else if either  $z_1$  or  $z_2$  is an infinity and the other a value with opposite sign, then return negative infinity.
- Else if both  $z_1$  and  $z_2$  are zeroes of equal sign, then return positive zero.
- Else if both  $z_1$  and  $z_2$  are zeroes of opposite sign, then return negative zero.
- Else return the result of multiplying  $z_1$  and  $z_2$ , rounded to the nearest representable value.

```
\operatorname{fmul}_N(\pm \operatorname{nan}(n), z_2) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_2\}
\operatorname{fmul}_N(z_1, \pm \operatorname{nan}(n)) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_1\}
\operatorname{fmul}_N(\pm \infty, \pm 0) = \operatorname{nans}_N\{\}
\text{fmul}_N(\pm\infty,\mp0)
                                       = \operatorname{nans}_{N}\{\}
\text{fmul}_N(\pm 0, \pm \infty)
                                      = \operatorname{nans}_N\{\}
\operatorname{fmul}_N(\pm 0, \mp \infty)
                                         = \operatorname{nans}_{N}\{\}
\text{fmul}_N(\pm\infty,\pm\infty)
                                         = +\infty
\operatorname{fmul}_N(\pm\infty,\mp\infty)
                                         = -\infty
\operatorname{fmul}_N(\pm q_1, \pm \infty)
                                          = +\infty
\text{fmul}_N(\pm q_1, \mp \infty)
\text{fmul}_N(\pm\infty,\pm q_2)
                                         = +\infty
\text{fmul}_N(\pm\infty,\mp q_2)
                                         = -\infty
                                         = +0
\operatorname{fmul}_N(\pm 0, \pm 0)
\text{fmul}_N(\pm 0, \mp 0)
                                         = -0
\mathrm{fmul}_N(z_1,z_2)
                                         = \operatorname{float}_N(z_1 \cdot z_2)
```

## $fdiv_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if both  $z_1$  and  $z_2$  are infinities, then return an element of  $nans_N\{\}$ .
- Else if both  $z_1$  and  $z_2$  are zeroes, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if  $z_1$  is an infinity and  $z_2$  a value with equal sign, then return positive infinity.
- Else if  $z_1$  is an infinity and  $z_2$  a value with opposite sign, then return negative infinity.
- ullet Else if  $z_2$  is an infinity and  $z_1$  a value with equal sign, then return positive zero.
- Else if  $z_2$  is an infinity and  $z_1$  a value with opposite sign, then return negative zero.
- Else if  $z_1$  is a zero and  $z_2$  a value with equal sign, then return positive zero.
- Else if  $z_1$  is a zero and  $z_2$  a value with opposite sign, then return negative zero.
- Else if  $z_2$  is a zero and  $z_1$  a value with equal sign, then return positive infinity.
- Else if  $z_2$  is a zero and  $z_1$  a value with opposite sign, then return negative infinity.
- Else return the result of dividing  $z_1$  by  $z_2$ , rounded to the nearest representable value.

 $fdiv_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}$  $fdiv_N(z_1, \pm nan(n)) = nans_N \{\pm nan(n), z_1\}$  $fdiv_N(\pm \infty, \pm \infty) = nans_N\{\}$  $fdiv_N(\pm\infty,\mp\infty)$  $= \operatorname{nans}_{N}\{\}$  $fdiv_N(\pm 0, \pm 0)$  $= \operatorname{nans}_{N}\{\}$  $fdiv_N(\pm 0, \mp 0)$  $= \operatorname{nans}_{N}\{\}$  $fdiv_N(\pm\infty,\pm q_2)$ =  $+\infty$  $fdiv_N(\pm\infty,\mp q_2)$  $-\infty$  $fdiv_N(\pm q_1,\pm\infty)$ = +0 $fdiv_N(\pm q_1, \mp \infty)$ -0 $fdiv_N(\pm 0, \pm q_2)$ = +0= -0 $fdiv_N(\pm 0, \mp q_2)$  $fdiv_N(\pm q_1,\pm 0)$ =  $+\infty$  $fdiv_N(\pm q_1, \mp 0)$ =  $-\infty$  $fdiv_N(z_1, z_2)$  $= \operatorname{float}_N(z_1/z_2)$ 

```
fma_N(z_1, z_2, z_3)
```

The function fma is the same as *fusedMultiplyAdd* defined by IEEE 754<sup>26</sup> (Section 5.4.1). It computes  $(z_1 \cdot z_2) + z_3$  as if with unbounded range and precision, rounding only once for the final result.

- If either  $z_1$  or  $z_2$  or  $z_3$  is a NaN, return an element of  $nans_N z_1, z_2, z_3$ .
- Else if either  $z_1$  or  $z_2$  is a zero and the other is an infinity, then return an element of  $nans_N$  {}.
- Else if both  $z_1$  or  $z_2$  are infinities of equal sign, and  $z_3$  is a negative infinity, then return an element of  $nans_N\{\}$ .
- Else if both z<sub>1</sub> or z<sub>2</sub> are infinities of opposite sign, and z<sub>3</sub> is a positive infinity, then return an element of nans<sub>N</sub>{}.
- Else if either  $z_1$  or  $z_2$  is an infinity and the other is a value of the same sign, and  $z_3$  is a negative infinity, then return an element of  $nans_N\{\}$ .
- Else if either  $z_1$  or  $z_2$  is an infinity and the other is a value of the opposite sign, and  $z_3$  is a positive infinity, then return an element of  $nans_N\{\}$ .
- Else if both  $z_1$  and  $z_2$  are zeroes of the same sign and  $z_3$  is a zero, then return positive zero.
- Else if both  $z_1$  and  $z_2$  are zeroes of the opposite sign and  $z_3$  is a positive zero, then return positive zero.
- Else if both  $z_1$  and  $z_2$  are zeroes of the opposite sign and  $z_3$  is a negative zero, then return negative zero.
- Else return the result of multiplying  $z_1$  and  $z_2$ , adding  $z_3$  to the intermediate, and the final result ref: rounded < aux-ieee> to the nearest representable value.

```
fma_N(\pm nan(n), z_2, z_3) = nans_N\{\pm nan(n), z_2, z_3\}
\operatorname{fma}_N(z_1, \pm \operatorname{\mathsf{nan}}(n), z_3) = \operatorname{nans}_N\{\pm \operatorname{\mathsf{nan}}(n), z_1, z_3\}
\operatorname{fma}_N(z_1, z_2, \pm \operatorname{nan}(n)) = \operatorname{nans}_N\{\pm \operatorname{nan}(n), z_1, z_2\}
\begin{array}{lll} \operatorname{fma}_N(\pm\infty,\pm0,z_3) & = & \operatorname{nans}_N\{\} \\ \operatorname{fma}_N(\pm\infty,\mp0,z_3) & = & \operatorname{nans}_N\{\} \end{array}
\operatorname{fma}_N(\pm\infty,\pm\infty,-\infty) = \operatorname{nans}_N\{\}
\operatorname{fma}_N(\pm\infty, \mp\infty, +\infty) = \operatorname{nans}_N\{\}
\operatorname{fma}_N(\pm q_1, \pm \infty, -\infty) = \operatorname{nans}_N\{\}
\operatorname{fma}_N(\pm q_1, \mp \infty, +\infty) = \operatorname{nans}_N\{\}
\operatorname{fma}_N(\pm \infty, \pm q_1, -\infty) = \operatorname{nans}_N\{\}
\operatorname{fma}_N(\mp\infty, \pm q_1, +\infty) = \operatorname{nans}_N\{\}
fma_N(\pm 0, \pm 0, \mp 0)
                                                = +0
fma_N(\pm 0, \pm 0, \pm 0)
                                                = +0
fma_N(\pm 0, \mp 0, +0)
                                                = +0
fma_N(\pm 0, \mp 0, -0)
                                                 = -0
                                                 = \text{float}_N(z_1 \cdot z_2 + z_3)
fma_N(z_1, z_2, z_3)
```

#### $fmin_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if either  $z_1$  or  $z_2$  is a negative infinity, then return negative infinity.
- Else if either  $z_1$  or  $z_2$  is a positive infinity, then return the other value.
- Else if both  $z_1$  and  $z_2$  are zeroes of opposite signs, then return negative zero.
- Else return the smaller value of  $z_1$  and  $z_2$ .

<sup>&</sup>lt;sup>26</sup> https://ieeexplore.ieee.org/document/8766229

```
fmin_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
fmin_N(z_1, \pm nan(n)) = nans_N\{\pm nan(n), z_1\}
fmin_N(+\infty, z_2)
                        = z_2
fmin_N(-\infty, z_2)
                        = -\infty
fmin_N(z_1, +\infty)
                        = z_1
fmin_N(z_1, -\infty)
fmin_N(\pm 0, \mp 0)
                        = -0
fmin_N(z_1, z_2)
                                                       (if z_1 \leq z_2)
                        = z_1
                                                       (if z_2 \le z_1)
fmin_N(z_1,z_2)
```

### $fmax_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return an element of  $nans_N\{z_1, z_2\}$ .
- Else if either  $z_1$  or  $z_2$  is a positive infinity, then return positive infinity.
- Else if either  $z_1$  or  $z_2$  is a negative infinity, then return the other value.
- Else if both  $z_1$  and  $z_2$  are zeroes of opposite signs, then return positive zero.
- Else return the larger value of  $z_1$  and  $z_2$ .

```
fmax_N(\pm nan(n), z_2) = nans_N\{\pm nan(n), z_2\}
fmax_N(z_1, \pm nan(n)) = nans_N\{\pm nan(n), z_1\}
fmax_N(+\infty, z_2)
                       = +\infty
                         = z_2
fmax_N(-\infty, z_2)
fmax_N(z_1, +\infty)
                         = +\infty
\mathrm{fmax}_N(z_1,-\infty)
                          = z_1
fmax_N(\pm 0, \mp 0)
                         = +0
\operatorname{fmax}_N(z_1, z_2)
                                                            (if z_1 \geq z_2)
                         = z_1
\operatorname{fmax}_N(z_1, z_2)
                                                           (if z_2 \ge z_1)
```

### $fcopysign_N(z_1, z_2)$

- If  $z_1$  and  $z_2$  have the same sign, then return  $z_1$ .
- Else return  $z_1$  with negated sign.

```
fcopysign<sub>N</sub>(\pm p_1, \pm p_2) = \pm p_1
fcopysign<sub>N</sub>(\pm p_1, \mp p_2) = \mp p_1
```

### $fabs_N(z)$

- If z is a NaN, then return z with positive sign.
- Else if z is an infinity, then return positive infinity.
- ullet Else if z is a zero, then return positive zero.
- Else if z is a positive value, then z.
- $\bullet$  Else return z negated.

```
fabs_N(\pm nan(n)) = +nan(n)
fabs_N(\pm \infty) = +\infty
fabs_N(\pm 0) = +0
fabs_N(\pm q) = +q
```

#### $fneg_N(z)$

- If z is a NaN, then return z with negated sign.
- Else if z is an infinity, then return that infinity negated.
- Else if z is a zero, then return that zero negated.
- Else return z negated.

```
\begin{array}{lll} \operatorname{fneg}_N(\pm \operatorname{nan}(n)) & = & \mp \operatorname{nan}(n) \\ \operatorname{fneg}_N(\pm \infty) & = & \mp \infty \\ \operatorname{fneg}_N(\pm 0) & = & \mp 0 \\ \operatorname{fneg}_N(\pm q) & = & \mp q \end{array}
```

## $fsqrt_N(z)$

- If z is a NaN, then return an element of  $nans_N\{z\}$ .
- Else if z is negative infinity, then return an element of  $nans_N$ {}.
- Else if z is positive infinity, then return positive infinity.
- Else if z is a zero, then return that zero.
- Else if z has a negative sign, then return an element of  $nans_N$ {}.
- Else return the square root of z.

```
\begin{array}{lll} \operatorname{fsqrt}_N(\pm \operatorname{nan}(n)) & = & \operatorname{nans}_N\{\pm \operatorname{nan}(n)\} \\ \operatorname{fsqrt}_N(-\infty) & = & \operatorname{nans}_N\{\} \\ \operatorname{fsqrt}_N(+\infty) & = & +\infty \\ \operatorname{fsqrt}_N(\pm 0) & = & \pm 0 \\ \operatorname{fsqrt}_N(-q) & = & \operatorname{nans}_N\{\} \\ \operatorname{fsqrt}_N(+q) & = & \operatorname{float}_N\left(\sqrt{q}\right) \end{array}
```

### $fceil_N(z)$

- If z is a NaN, then return an element of  $nans_N\{z\}$ .
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is smaller than 0 but greater than -1, then return negative zero.
- Else return the smallest integral value that is not smaller than z.

```
\begin{array}{lll} \operatorname{fceil}_N(\pm \operatorname{nan}(n)) & = & \operatorname{nans}_N\{\pm \operatorname{nan}(n)\} \\ \operatorname{fceil}_N(\pm \infty) & = & \pm \infty \\ \operatorname{fceil}_N(\pm 0) & = & \pm 0 \\ \operatorname{fceil}_N(-q) & = & -0 \\ \operatorname{fceil}_N(\pm q) & = & \operatorname{float}_N(i) \end{array} \qquad \begin{array}{ll} (\operatorname{if} -1 < -q < 0) \\ (\operatorname{if} \pm q \leq i < \pm q + 1) \end{array}
```

## $ffloor_N(z)$

- If z is a NaN, then return an element of  $nans_N\{z\}$ .
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- ullet Else if z is greater than 0 but smaller than 1, then return positive zero.
- Else return the largest integral value that is not larger than z.

```
\begin{array}{lll} \operatorname{ffloor}_N(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N\{\pm \operatorname{nan}(n)\} \\ \operatorname{ffloor}_N(\pm \infty) &=& \pm \infty \\ \operatorname{ffloor}_N(\pm 0) &=& \pm 0 \\ \operatorname{ffloor}_N(+q) &=& +0 \\ \operatorname{ffloor}_N(\pm q) &=& \operatorname{float}_N(i) & (\text{if } 0 < +q < 1) \\ \operatorname{ffloor}_N(\pm q) &=& \operatorname{float}_N(i) & (\text{if } \pm q - 1 < i \leq \pm q) \end{array}
```

### $ftrunc_N(z)$

- If z is a NaN, then return an element of  $nans_N\{z\}$ .
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is greater than 0 but smaller than 1, then return positive zero.
- Else if z is smaller than 0 but greater than -1, then return negative zero.
- Else return the integral value with the same sign as z and the largest magnitude that is not larger than the magnitude of z.

```
\begin{array}{lll} {\rm ftrunc}_N(\pm {\rm nan}(n)) & = & {\rm nans}_N\{\pm {\rm nan}(n)\} \\ {\rm ftrunc}_N(\pm \infty) & = & \pm \infty \\ & {\rm ftrunc}_N(\pm 0) & = & \pm 0 \\ & {\rm ftrunc}_N(+q) & = & +0 & ({\rm if}\ 0 < +q < 1) \\ {\rm ftrunc}_N(-q) & = & -0 & ({\rm if}\ -1 < -q < 0) \\ & {\rm ftrunc}_N(\pm q) & = & {\rm float}_N(\pm i) & ({\rm if}\ +q - 1 < i \le +q) \end{array}
```

#### $fnearest_N(z)$

- If z is a NaN, then return an element of  $nans_N\{z\}$ .
- Else if z is an infinity, then return z.
- Else if z is a zero, then return z.
- Else if z is greater than 0 but smaller than or equal to 0.5, then return positive zero.
- Else if z is smaller than 0 but greater than or equal to -0.5, then return negative zero.
- Else return the integral value that is nearest to z; if two values are equally near, return the even one.

```
\operatorname{fnearest}_N(\pm \operatorname{\mathsf{nan}}(n)) = \operatorname{nans}_N\{\pm \operatorname{\mathsf{nan}}(n)\}
\text{fnearest}_N(\pm \infty)
                                 = \pm \infty
fnearest_N(\pm 0)
                                 = \pm 0
fnearest_N(+q)
                                = +0
                                                                      (if 0 < +q \le 0.5)
                                 = -0
                                                                      (if -0.5 \le -q < 0)
\text{fnearest}_N(-q)
\text{fnearest}_N(\pm q)
                                = \operatorname{float}_N(\pm i)
                                                                     (if |i - q| < 0.5)
fnearest_N(\pm q)
                                 = \operatorname{float}_N(\pm i)
                                                                     (if |i - q| = 0.5 \wedge i even)
```

### $feq_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return 0.
- Else if both  $z_1$  and  $z_2$  are zeroes, then return 1.
- Else if both  $z_1$  and  $z_2$  are the same value, then return 1.
- Else return 0.

```
\begin{array}{lcl} \mathrm{feq}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ \mathrm{feq}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{feq}_N(\pm 0, \mp 0) & = & 1 \\ \mathrm{feq}_N(z_1, z_2) & = & \mathrm{bool}(z_1 = z_2) \end{array}
```

### $fne_N(z_1,z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return 1.
- Else if both  $z_1$  and  $z_2$  are zeroes, then return 0.
- Else if both  $z_1$  and  $z_2$  are the same value, then return 0.
- Else return 1.

```
\begin{array}{llll} & \operatorname{fine}_N(\pm \operatorname{nan}(n), z_2) & = & 1 \\ & \operatorname{fine}_N(z_1, \pm \operatorname{nan}(n)) & = & 1 \\ & \operatorname{fine}_N(\pm 0, \mp 0) & = & 0 \\ & \operatorname{fine}_N(z_1, z_2) & = & \operatorname{bool}(z_1 \neq z_2) \end{array}
```

#### $\operatorname{flt}_N(z_1,z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return 0.
- Else if  $z_1$  and  $z_2$  are the same value, then return 0.
- Else if  $z_1$  is positive infinity, then return 0.
- Else if  $z_1$  is negative infinity, then return 1.
- Else if  $z_2$  is positive infinity, then return 1.
- Else if  $z_2$  is negative infinity, then return 0.
- Else if both  $z_1$  and  $z_2$  are zeroes, then return 0.
- Else if  $z_1$  is smaller than  $z_2$ , then return 1.
- Else return 0.

```
\operatorname{flt}_N(\pm \operatorname{\mathsf{nan}}(n), z_2) = 0
\operatorname{flt}_N(z_1, \pm \operatorname{\mathsf{nan}}(n)) =
                                         0
                                         0
\mathrm{flt}_N(z,z)
\mathrm{flt}_N(+\infty,z_2)
                                  = 0
\mathrm{flt}_N(-\infty,z_2)
\mathrm{flt}_N(z_1,+\infty)
                                  = 1
                                  = 0
\mathrm{flt}_N(z_1,-\infty)
\mathrm{flt}_N(\pm 0, \mp 0)
                                  = 0
                                  = bool(z_1 < z_2)
\mathrm{flt}_N(z_1,z_2)
```

## $fgt_N(z_1,z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return 0.
- Else if  $z_1$  and  $z_2$  are the same value, then return 0.
- Else if  $z_1$  is positive infinity, then return 1.
- Else if  $z_1$  is negative infinity, then return 0.
- Else if  $z_2$  is positive infinity, then return 0.
- Else if  $z_2$  is negative infinity, then return 1.
- Else if both  $z_1$  and  $z_2$  are zeroes, then return 0.
- Else if  $z_1$  is larger than  $z_2$ , then return 1.
- Else return 0.

```
\begin{array}{llll} \mathrm{fgt}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ \mathrm{fgt}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{fgt}_N(z, z) & = & 0 \\ \mathrm{fgt}_N(+\infty, z_2) & = & 1 \\ \mathrm{fgt}_N(-\infty, z_2) & = & 0 \\ \mathrm{fgt}_N(z_1, +\infty) & = & 0 \\ \mathrm{fgt}_N(z_1, -\infty) & = & 1 \\ \mathrm{fgt}_N(\pm 0, \mp 0) & = & 0 \\ \mathrm{fgt}_N(z_1, z_2) & = & \mathrm{bool}(z_1 > z_2) \end{array}
```

## $fle_N(z_1,z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return 0.
- Else if  $z_1$  and  $z_2$  are the same value, then return 1.
- Else if  $z_1$  is positive infinity, then return 0.
- Else if  $z_1$  is negative infinity, then return 1.
- Else if  $z_2$  is positive infinity, then return 1.
- Else if  $z_2$  is negative infinity, then return 0.
- Else if both  $z_1$  and  $z_2$  are zeroes, then return 1.
- Else if  $z_1$  is smaller than or equal to  $z_2$ , then return 1.
- Else return 0.

```
\begin{array}{lll} \mathrm{fle}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ \mathrm{fle}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ \mathrm{fle}_N(z, z) & = & 1 \\ \mathrm{fle}_N(+\infty, z_2) & = & 0 \\ \mathrm{fle}_N(-\infty, z_2) & = & 1 \\ \mathrm{fle}_N(z_1, +\infty) & = & 1 \\ \mathrm{fle}_N(z_1, -\infty) & = & 0 \\ \mathrm{fle}_N(\pm 0, \mp 0) & = & 1 \\ \mathrm{fle}_N(z_1, z_2) & = & \mathrm{bool}(z_1 \leq z_2) \end{array}
```

#### $fge_N(z_1, z_2)$

- If either  $z_1$  or  $z_2$  is a NaN, then return 0.
- Else if  $z_1$  and  $z_2$  are the same value, then return 1.
- Else if  $z_1$  is positive infinity, then return 1.
- Else if  $z_1$  is negative infinity, then return 0.
- Else if  $z_2$  is positive infinity, then return 0.
- Else if  $z_2$  is negative infinity, then return 1.
- Else if both  $z_1$  and  $z_2$  are zeroes, then return 1.
- Else if  $z_1$  is smaller than or equal to  $z_2$ , then return 1.
- Else return 0.

```
\begin{array}{llll} & \mathrm{fge}_N(\pm \mathrm{nan}(n), z_2) & = & 0 \\ & \mathrm{fge}_N(z_1, \pm \mathrm{nan}(n)) & = & 0 \\ & \mathrm{fge}_N(z, z) & = & 1 \\ & \mathrm{fge}_N(+\infty, z_2) & = & 1 \\ & \mathrm{fge}_N(-\infty, z_2) & = & 0 \\ & \mathrm{fge}_N(z_1, +\infty) & = & 0 \\ & \mathrm{fge}_N(z_1, -\infty) & = & 1 \\ & \mathrm{fge}_N(\pm 0, \mp 0) & = & 1 \\ & \mathrm{fge}_N(z_1, z_2) & = & \mathrm{bool}(z_1 \geq z_2) \end{array}
```

### $fpmin_N(z_1, z_2)$

- If  $z_2$  is less than  $z_1$  then return  $z_2$ .
- Else return  $z_1$ .

```
\begin{array}{lcl} \mathrm{fpmin}_N(z_1,z_2) & = & z_2 & (\mathrm{if} \ \mathrm{flt}_N(z_2,z_1) = 1) \\ \mathrm{fpmin}_N(z_1,z_2) & = & z_1 & (\mathrm{otherwise}) \end{array}
```

 $fpmax_N(z_1, z_2)$ 

- If  $z_1$  is less than  $z_2$  then return  $z_2$ .
- Else return  $z_1$ .

$$\begin{array}{lcl} \mathrm{fpmax}_N(z_1,z_2) & = & z_2 & (\mathrm{if} \ \mathrm{flt}_N(z_1,z_2) = 1) \\ \mathrm{fpmax}_N(z_1,z_2) & = & z_1 & (\mathrm{otherwise}) \end{array}$$

#### 4.3.4 Conversions

#### Todo

ext or extend?

## $\operatorname{extend}^{\mathsf{u}}_{M,N}(i)$

• Return i.

$$\operatorname{extend}^{\mathsf{u}}_{M,N}(i) = i$$

#### Note

In the abstract syntax, unsigned extension just reinterprets the same value.

 $\operatorname{extend}^{\mathsf{s}}_{M,N}(i)$ 

- Let j be the signed interpretation of i of size M.
- Return the two's complement of j relative to size N.

$$\operatorname{extend}^{\mathsf{s}}_{M,N}(i) = \operatorname{signed}_{N}^{-1}(\operatorname{signed}_{M}(i))$$

 $\operatorname{wrap}_{M,N}(i)$ 

• Return  $i \mod 2^N$ .

$$\operatorname{wrap}_{M,N}(i) = i \operatorname{mod} 2^N$$

 $\operatorname{trunc}^{\mathsf{u}}_{M,N}(z)$ 

- If z is a NaN, then the result is undefined.
- Else if z is an infinity, then the result is undefined.
- Else if z is a number and trunc(z) is a value within range of the target type, then return that value.
- Else the result is undefined.

```
\begin{array}{lll} \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm \operatorname{nan}(n)) & = & \{\} \\ \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm \infty) & = & \{\} \\ \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm q) & = & \operatorname{trunc}(\pm q) & & (\operatorname{if} -1 < \operatorname{trunc}(\pm q) < 2^N) \\ \operatorname{trunc}^{\operatorname{u}}{}_{M,N}(\pm q) & = & \{\} & & (\operatorname{otherwise}) \end{array}
```

## Note

This operator is partial. It is not defined for NaNs, infinities, or values for which the result is out of range.

## $\operatorname{trunc}^{\mathsf{s}}_{M,N}(z)$

- If z is a NaN, then the result is undefined.
- Else if z is an infinity, then the result is undefined.
- If z is a number and trunc(z) is a value within range of the target type, then return that value.
- Else the result is undefined.

```
\begin{array}{lll} {\rm trunc}^{\rm s}{}_{M,N}(\pm {\rm nan}(n)) & = & \{ \} \\ {\rm trunc}^{\rm s}{}_{M,N}(\pm \infty) & = & \{ \} \\ {\rm trunc}^{\rm s}{}_{M,N}(\pm q) & = & {\rm trunc}(\pm q) & ({\rm if} -2^{N-1} - 1 < {\rm trunc}(\pm q) < 2^{N-1}) \\ {\rm trunc}^{\rm s}{}_{M,N}(\pm q) & = & \{ \} & ({\rm otherwise}) \end{array}
```

#### Note

This operator is partial. It is not defined for NaNs, infinities, or values for which the result is out of range.

#### trunc\_sat\_ $\mathbf{u}_{M,N}(z)$

- If z is a NaN, then return 0.
- Else if z is negative infinity, then return 0.
- Else if z is positive infinity, then return  $2^N 1$ .
- Else, return  $\operatorname{sat}_{\mathbf{u}N}(\operatorname{trunc}(z))$ .

```
\begin{array}{llll} \operatorname{trunc\_sat\_u}_{M,N}(\pm \operatorname{nan}(n)) & = & 0 \\ \operatorname{trunc\_sat\_u}_{M,N}(-\infty) & = & 0 \\ \operatorname{trunc\_sat\_u}_{M,N}(+\infty) & = & 2^N - 1 \\ \operatorname{trunc\_sat\_u}_{M,N}(z) & = & \operatorname{sat\_u}_{N}(\operatorname{trunc}(z)) \end{array}
```

### trunc\_sat\_s $_{M,N}(z)$

- If z is a NaN, then return 0.
- Else if z is negative infinity, then return  $-2^{N-1}$ .
- Else if z is positive infinity, then return  $2^{N-1} 1$ .
- Else, return the value whose signed interpretation is  $\operatorname{sat\_s}_N(\operatorname{trunc}(z))$ .

```
\begin{array}{lll} \operatorname{trunc\_sat\_s}_{M,N}(\pm \operatorname{nan}(n)) & = & 0 \\ \operatorname{trunc\_sat\_s}_{M,N}(-\infty) & = & -2^{N-1} \\ \operatorname{trunc\_sat\_s}_{M,N}(+\infty) & = & 2^{N-1} - 1 \\ \operatorname{trunc\_sat\_s}_{M,N}(z) & = & \operatorname{signed}_N^{-1}(\operatorname{sat\_s}_N(\operatorname{trunc}(z))) \end{array}
```

#### $promote_{M,N}(z)$

- If z is a canonical NaN, then return an element of  $nans_N\{\}$  (i.e., a canonical NaN of size N).
- Else if z is a NaN, then return an element of  $nans_N\{\pm nan(1)\}\$  (i.e., any arithmetic NaN of size N).
- Else, return z.

```
\begin{array}{llll} \operatorname{promote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N \{\} & & (\text{if } n = \operatorname{canon}_N) \\ \operatorname{promote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N \{+\operatorname{nan}(1)\} & & (\text{otherwise}) \\ \operatorname{promote}_{M,N}(z) &=& z & & \end{array}
```

## $demote_{M,N}(z)$

- If z is a canonical NaN, then return an element of  $nans_N\{\}$  (i.e., a canonical NaN of size N).
- Else if z is a NaN, then return an element of  $nans_N\{\pm nan(1)\}\$  (i.e., any NaN of size N).
- Else if z is an infinity, then return that infinity.
- Else if z is a zero, then return that zero.
- Else, return  $float_N(z)$ .

```
\begin{array}{lll} \operatorname{demote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N\{\} & \quad \text{(if } n = \operatorname{canon}_N) \\ \operatorname{demote}_{M,N}(\pm \operatorname{nan}(n)) &=& \operatorname{nans}_N\{+\operatorname{nan}(1)\} & \quad \text{(otherwise)} \\ \operatorname{demote}_{M,N}(\pm \infty) &=& \pm \infty \\ \operatorname{demote}_{M,N}(\pm 0) &=& \pm 0 \\ \operatorname{demote}_{M,N}(\pm q) &=& \operatorname{float}_N(\pm q) \end{array}
```

## $\operatorname{convert}^{\mathsf{u}}_{M,N}(i)$

• Return float N(i).

$$\operatorname{convert}^{\mathsf{u}}_{M,N}(i) = \operatorname{float}_{N}(i)$$

## $\operatorname{convert}^{\mathsf{s}}_{M,N}(i)$

- Let j be the signed interpretation of i.
- Return float $_N(j)$ .

$$\operatorname{convert}^{s}_{M,N}(i) = \operatorname{float}_{N}(\operatorname{signed}_{M}(i))$$

## reinterpret<sub> $t_1,t_2$ </sub> (c)

- Let  $d^*$  be the bit sequence  $\operatorname{bits}_{t_1}(c)$ .
- Return the constant c' for which  $\operatorname{bits}_{t_2}(c') = d^*$ .

$$reinterpret_{t_1,t_2}(c) = bits_{t_2}^{-1}(bits_{t_1}(c))$$

## $\operatorname{narrow}^{\mathsf{s}}_{M,N}(i)$

- Let j be the signed interpretation of i of size M.
- Return the value whose signed interpretation is  $\operatorname{sat\_s}_N(j)$ .

$$\operatorname{narrow}^{s}_{M,N}(i) = \operatorname{signed}_{N}^{-1}(\operatorname{sat}_{s}_{N}(\operatorname{signed}_{M}(i)))$$

### $\operatorname{narrow}^{\mathsf{u}}_{M,N}(i)$

- Let j be the signed interpretation of i of size M.
- Return  $\operatorname{sat}_{\mathbf{u}_N}(j)$ .

$$\operatorname{narrow}^{\mathsf{u}}_{M,N}(i) = \operatorname{sat}_{\mathsf{u}}_{N}(\operatorname{signed}_{M}(i))$$

## 4.3.5 Vector Operations

Most vector operations are performed by applying numeric operations lanewise. However, some operators consider multiple lanes at once.

## ivbitmask $_N(i^m)$

- 1. For each  $i_k$  in  $i^m$ , let  $b_k$  be the result of computing ilt\_s<sub>N</sub>(i, 0).
- 2. Let  $b^m$  be the concatenation of all  $b_k$ .
- 3. Return the result of computing ibits $_{32}^{-1}((0)^{32-m}b^m)$ .

$$ivbitmask_N(i^m) = ibits_{32}^{-1}((0)^{32-m} ilt_s_N(i,0)^m)$$

### ivswizzle $(i^n, j^n)$

- 1. For each  $j_k$  in  $j^n$ , let  $r_k$  be the value ivswizzle\_lane $(i^n, j_k)$ .
- 2. Let  $r^n$  be the concatenation of all  $r_k$ .
- 3. Return  $r^n$ .

ivswizzle
$$(i^n, j^n)$$
 = ivswizzle\_lane $(i^n, j)^n$ 

where:

$$\begin{array}{lll} {\rm ivswizzle\_lane}(i^n,j) & = & i^n[j] & ({\rm if} \ j < n) \\ {\rm ivswizzle\_lane}(i^n,j) & = & 0 & ({\rm otherwise}) \end{array}$$

## ivshuffle $(j^n, i_1^n, i_2^n)$

- 1. Let  $i^*$  ne the concatenation of  $i_1^n$  and  $i_2^n$ .
- 2. For each  $j_k$  in  $j^n$ , let  $r_k$  be  $i^*[j_k]$ .
- 3. Let  $r^n$  be the concatenation of all  $r_k$ .
- 4. Return  $r^n$ .

ivshuffle
$$(j^n, i_1^n, i_2^n) = ((i_1^n i_2^n)[j])^n$$
 (if  $(j < 2 \cdot n)^n$ )

## ivadd pairwise<sub>N</sub> $(i^{2m})$

- 1. Let  $(i_1 i_2)^m$  be  $i^{2m}$ , decomposed into pairwise elements.
- 2. For each  $i_{1k}$  in  $i_1^m$  and corresponding  $i_{2k}$  in  $i_2^m$ , let  $r_k$  be  $iadd_N(i_{1k}, i_{2k})$ .
- 3. Let  $r^m$  be the concatenation of all  $r_k$ .
- 4. Return  $r^m$ .

ivadd\_pairwise<sub>N</sub>
$$(i^{2m}) = (iadd_N(i_1, i_2))^m$$
 (if  $i^{2m} = (i_1 i_2)^m$ )

### $\mathrm{ivmul}_N(i_1^m, i_2^m)$

- 1. For each  $i_{1k}$  in  $i_1^m$  and corresponding  $i_{2k}$  in  $i_2^m$ , let  $r_k$  be  $\mathrm{imul}_N(i_{1k}, i_{2k})$ .
- 2. Let  $r^m$  be the concatenation of all  $r_k$ .
- 3. Return  $r^m$ .

$$\mathrm{ivmul}_N(i_1^m, i_2^m) = (\mathrm{imul}_N(i_1, i_2))^m$$

## $ivdot_N(i_1^{2m}, i_2^{2m})$

- 1. For each  $i_{1k}$  in  $i_1^{2m}$  and corresponding  $i_{2k}$  in  $i_2^{2m}$ , let  $j_k$  be  $\mathrm{imul}_N(i_{1k},i_{2k})$ .
- 2. Let  $j^{2m}$  be the concatenation of all  $j_k$ .
- 3. Let  $(j_1 \ j_2)^m$  be  $j^{2m}$ , decomposed into pairwise elements.
- 4. For each  $i_{1k}$  in  $i_1^m$  and corresponding  $i_{2k}$  in  $i_2^m$ , let  $r_k$  be  $iadd_N(i_{1k}, i_{2k})$ .
- 5. Let  $r^m$  be the concatenation of all  $r_k$ .

6. Return  $r^m$ .

$$ivdot_N(i_1^{2m}, i_2^{2m}) = (iadd_N(j_1, j_2))^m \quad (if (imul_N(i_1, i_2))^{2m} = (j_1 j_2)^m)$$

 $ivdotsat_N(i_1^m, i_2^m)$ 

- 1. For each  $i_{1k}$  in  $i_1^{2m}$  and corresponding  $i_{2k}$  in  $i_2^{2m}$ , let  $j_k$  be  $\mathrm{imul}_N(i_{1k},i_{2k})$ .
- 2. Let  $j^{2m}$  be the concatenation of all  $j_k$ .
- 3. Let  $(j_1 \ j_2)^m$  be  $j^{2m}$ , decomposed into pairwise elements.
- 4. For each  $i_{1k}$  in  $i_1^m$  and corresponding  $i_{2k}$  in  $i_2^m$ , let  $r_k$  be iadd\_sat $N(i_{1k}, i_{2k})$ .
- 5. Let  $r^m$  be the concatenation of all  $r_k$ .
- 6. Return  $r^m$ .

$$ivdotsat_N(i_1^{2m}, i_2^{2m}) = (iadd\_sat_N(j_1, j_2))^m \quad (if (imul_N(i_1, i_2))^{2m} = (j_1 \ j_2)^m)$$

The previous operators are lifted to operators on arguments of vector type by wrapping them in corresponding lane projections and injections and intermediate extension operations:

$$vextunop_{sh_1,sh_2}(c)$$

$$\begin{array}{lll} \mathsf{extadd\_pairwise\_} sx_{\mathsf{i}N_1 \times M_1, \mathsf{i}N_2 \times M_2}(c) &=& \mathsf{lanes}_{\mathsf{i}N_2 \times M_2}^{-1}(j^*) & (\mathsf{if}\ i^* = \mathsf{lanes}_{\mathsf{i}N_1 \times M_1}(c) \\ & & \wedge i'^* = \mathsf{extend}_{N_1, N_2}^{sx}(i)^* \\ & & \wedge j^* = \mathsf{ivadd\_pairwise}_{N_2}(i'^*) \end{array}$$

 $vextbinop_{sh_1,sh_2}(c_1,c_2)$ 

$$vextbinop_{iN_{1}\times M_{1}, iN_{2}\times M_{2}}(c_{1}, c_{2}) = lanes_{iN_{2}\times M_{2}}^{-1}(j^{*}) \quad (if \ i_{1}^{*} = lanes_{iN_{1}\times M_{1}}(c_{1})[h:k] \\ \wedge \ i_{2}^{*} = lanes_{iN_{1}\times M_{1}}(c_{2})[h:k] \\ \wedge \ i_{1}^{'} = extend_{N_{1},N_{2}}^{sx}(i_{1})^{*} \\ \wedge \ i_{2}^{'} = extend_{N_{1},N_{2}}^{sx}(i_{2})^{*} \\ \wedge \ j^{*} = f_{N_{2}}(i_{1}^{'}, i_{1}^{'})^{*}$$

where f,  $sx_1$ ,  $sx_2$ , h, and k are instantiated as follows, depending on the operator:

vextbinop	f	$sx_1$	$sx_2$	h	k
extmul_low_sx	ivmul	sx	sx	0	$\overline{M_2}$
extmul_high_ $sx$	ivmul	sx	sx	$M_2$	$M_2$
dot_s	ivdot	S	S	0	$M_1$
relaxed_dot_s	ivdotsat	S	$\operatorname{relaxed}(R_{\operatorname{idot}})[s,u]$	0	$M_1$

#### Note

Relaxed operations and the paramater  $R_{idot}$  are introduced below.

$$\begin{aligned} \textit{vextternop}_{\mathit{sh}_1,\mathit{sh}_2}(c_1,c_2,c_3) &= c & (\text{if } N = 2 \cdot N_1 \\ & \land M = 2 \cdot M_2 \\ & \land c' = \mathsf{relaxed\_dot\_s}_{\mathsf{i}N_1 \times M_1,\mathsf{i}N_2 \times M_2}(c_1,c_2) \\ & \land c'' = \mathsf{extadd\_pairwise\_s}_{\mathsf{i}N_1 \times M_1,\mathsf{i}N_2 \times M_2}(c') \\ & \land c \in \mathsf{add}_{\mathsf{i}N_2 \times M_2}(c'',c_3) \end{aligned}$$

$$\begin{split} \text{narrow}\_sx_{sh_1,sh_2}(c_1,c_2) &= \text{lanes}_{\mathsf{i}N_2 \times M_2}^{-1}(j^*) & \text{ (if } i_1^* = \text{lanes}_{\mathsf{i}N_1 \times M_1}(c_1) \\ & \wedge i_2^* = \text{lanes}_{\mathsf{i}N_1 \times M_1}(c_2) \\ & \wedge i_1'^* = \text{narrow}_{N_1,N_2}^{sx}(i_1)^* \\ & \wedge i_2'^* = \text{narrow}_{N_1,N_2}^{sx}(i_2)^* \\ & \wedge j^* = i_1'^* \oplus i_1'^* \end{split}$$

where h, k, n, and *condition* are instantiated as follows, depending on the operator:

half?	zero?	h	k	n	condition
$\epsilon$	$\epsilon$	0	$M_1$	0	$(M_1 = M_2)$
low	$\epsilon$	0	$M_2$	0	$(M_1 = 2 \cdot M_2)$
high	$\epsilon$	$M_2$	$M_2$	0	$(M_1 = 2 \cdot M_2)$
$\epsilon$	zero	0	$M_1$	$M_1$	$(2 \cdot M_1 = M_2)$

while  $\times \{x^*\}^N$  transforms a sequence of N sets of non-deterministic values into a set of non-deterministic sequences of N values by computing the set product:

$$\times (S_1 \dots S_N) = \{x_1 \dots x_N \mid x_1 \in S_1 \wedge \dots \wedge x_N \in S_N\}$$

## 4.3.6 Relaxed Operations

The result of *relaxed* operators are *implementation-dependent*, because the set of possible results may depend on properties of the host environment, such as its hardware. Technically, their behaviour is controlled by a set of *global parameters* to the semantics that an implementation can instantiate in different ways. These choices are fixed, that is, parameters are constant during the execution of any given program.

Every such parameter is an index into a sequence of possible sets of results and must be instantiated to a defined index. In the deterministic profile, every parameter is prescribed to be 0. This behaviour is expressed by the following auxiliary function, where R is a global parameter selecting one of the allowed outcomes:

[!DET] relaxed
$$(R)[A_0, \dots, A_n] = A_R$$
  
relaxed $(R)[A_0, \dots, A_n] = A_0$ 

### Note

Each parameter can be thought of as inducing a family of operations that is fixed to one particular choice by an implementation. The fixed operation itself can still be non-deterministic or partial.

Implementations are expected to either choose the behaviour that is the most efficient on the underlying hardware, or the behaviour of the deterministic profile.

frelaxed  $\operatorname{madd}_N(z_1, z_2, z_3)$ 

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{\text{fmadd}} \in \{0, 1\}$ .

• Return relaxed $(R_{\text{fmadd}})$ [fadd $_N(\text{fmul}_N(z_1, z_2), z_3)$ , fma $_N(z_1, z_2, z_3)$ ]. frelaxed\_madd $_N(z_1, z_2, z_3)$  = relaxed $(R_{\text{fmadd}})$ [fadd $_N(\text{fmul}_N(z_1, z_2), z_3)$ , fma $_N(z_1, z_2, z_3)$ ]

#### Note

Relaxed multiply-add allows for fused or unfused results, which leads to implementation-dependent rounding behaviour. In the deterministic profile, the unfused behaviour is used.

```
frelaxed\_nmadd_N(z_1, z_2, z_3)
```

• Return frelaxed\_madd( $-z_1, z_2, z_3$ ).

```
frelaxed\_nmadd_N(z_1, z_2, z_3) = frelaxed\_madd_N(-z_1, z_2, z_3)
```

#### Note

This operation is implementation-dependent because frelaxed madd is implementation-dependent.

```
frelaxed \min_{N}(z_1, z_2)
```

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{\text{fmin}} \in \{0,1,2,3\}$ .

- If  $z_1$  is a NaN, then return relaxed  $(R_{\text{fmin}})[\text{fmin}_N(z_1, z_2), \text{nan}(n), z_2, z_2]$ .
- If  $z_2$  is a NaN, then return relaxed  $(R_{\text{fmin}})[\text{fmin}_N(z_1, z_2), z_1, \text{nan}(n), z_1]$ .
- If both  $z_1$  and  $z_2$  are zeroes of opposite sign, then return relaxed  $(R_{\text{fmin}})[\text{fmin}_N(z_1, z_2), \text{pm 0, mp 0, -0}]$ .
- Return  $fmin_N(z_1, z_2)$ .

```
\begin{array}{lll} \operatorname{frelaxed\_min}_N(\pm \operatorname{nan}(n), z_2) & = & \operatorname{relaxed}(R_{\operatorname{fmin}})[\operatorname{fmin}_N(\pm \operatorname{nan}(n), z_2), \operatorname{nan}(n), z_2, z_2] \\ \operatorname{frelaxed\_min}_N(z_1, \pm \operatorname{nan}(n)) & = & \operatorname{relaxed}(R_{\operatorname{fmin}})[\operatorname{fmin}_N(z_1, \pm \operatorname{nan}(n)), z_1, \operatorname{nan}(n), z_1] \\ \operatorname{frelaxed\_min}_N(\pm 0, \mp 0) & = & \operatorname{relaxed}(R_{\operatorname{fmin}})[\operatorname{fmin}_N(\pm 0, \mp 0), \pm 0, \mp 0, -0] \\ \operatorname{frelaxed\_min}_N(z_1, z_2) & = & \operatorname{fmin}_N(z_1, z_2) \end{array} \tag{otherwise}
```

#### Note

Relaxed minimum is implementation-dependent for NaNs and for zeroes with different signs. In the deterministic profile, it behaves like regular fmin.

```
frelaxed_max_N(z_1, z_2)
```

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{\text{fmax}} \in \{0, 1, 2, 3\}$ .

- If  $z_1$  is a NaN, then return relaxed  $(R_{\text{fmax}})[\text{fmax}_N(z_1, z_2), \text{nan}(n), z_2, z_2]$ .
- If  $z_2$  is a NaN, then return relaxed  $(R_{\text{fmax}})[\text{fmax}_N(z_1, z_2), z_1, \text{nan}(n), z_1]$ .
- If both  $z_1$  and  $z_2$  are zeroes of opposite sign, then return relaxed  $(R_{\text{fmax}})[\text{fmax}_N(z_1, z_2), \text{pm 0, mp 0, +0}]$ .
- Return  $\max_N(z_1, z_2)$ .

```
\begin{array}{lll} \operatorname{frelaxed\_max}_N(\pm \mathsf{nan}(n), z_2) & = & \operatorname{relaxed}(R_{\mathrm{fmax}})[\operatorname{fmax}_N(\pm \mathsf{nan}(n), z_2), \mathsf{nan}(n), z_2, z_2] \\ \operatorname{frelaxed\_max}_N(z_1, \pm \mathsf{nan}(n)) & = & \operatorname{relaxed}(R_{\mathrm{fmax}})[\operatorname{fmax}_N(z_1, \pm \mathsf{nan}(n)), z_1, \mathsf{nan}(n), z_1] \\ \operatorname{frelaxed\_max}_N(\pm 0, \mp 0) & = & \operatorname{relaxed}(R_{\mathrm{fmax}})[\operatorname{fmax}_N(\pm 0, \mp 0), \pm 0, \mp 0, + 0] \\ \operatorname{frelaxed\_max}_N(z_1, z_2) & = & \operatorname{fmax}_N(z_1, z_2) \end{array}
```

#### Note

Relaxed maximum is implementation-dependent for NaNs and for zeroes with different signs. In the deterministic profile, it behaves like regular fmax.

### $irelaxed_q15mulr_s_N(i_1, i_2)$

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{iq15mulr} \in \{0, 1\}$ .

- If both  $i_1$  and  $i_2$  equal (signed  $N = (-2^{N-1})$ , then return relaxed  $(R_{iq15\text{mulr}})[2^{N-1} 1, \text{signed}_N^{-1}(-2^{N-1})]$ .
- Return iq15mulrsat\_s $(i_1, i_2)$

#### Note

Relaxed Q15 multiplication is implementation-dependent when the result overflows. In the deterministic profile, it behaves like regular  $iq15mulrsat\_s$ .

## relaxed\_trunc $_{M,N}^u(z)$

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{\text{trunc\_u}} \in \{0, 1, 2, 3\}$ .

- If z is normal or subnormal and  $\operatorname{trunc}(z)$  is non-negative and less than  $2^N$ , then return  $\operatorname{trunc}^u_{M,N}(z)$ .
- Else, return relaxed  $(R_{\text{trunc u}})[\text{trunc\_sat\_u}_{M,N}(z), 2^N 1, 2^N 2, 2^N 1)].$

```
 \begin{array}{lcl} \operatorname{relaxed\_trunc}_{M,N}^u(\pm q) & = & \operatorname{trunc}^{\operatorname{u}}_{M,N}(\pm q) & & \text{ (if } 0 \leq \operatorname{trunc}(\pm q) < 2^N \\ \operatorname{relaxed\_trunc}_{M,N}^u(z) & = & \operatorname{relaxed}(R_{\operatorname{trunc\_u}})[\operatorname{trunc\_sat\_u}_{M,N}(z), 2^N - 1, 2^N - 2, 2^{N-1}] & \text{ (otherwise)} \\ \end{array}
```

#### Note

Relaxed unsigned truncation is implementation-dependent for NaNs and out-of-range values. In the deterministic profile, it behaves like regular trunc\_sat\_u.

```
\operatorname{relaxed\_trunc}_{M,N}^{s}(z)
```

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{trunc\_s} \in \{0, 1\}$ .

- If z is normal or subnormal and  $\operatorname{trunc}(z)$  is greater than or equal to  $-2^{N-1}$  and less than  $2^{N-1}$ , then return  $\operatorname{trunc}_{M,N}(z)$ .
- Else, return relaxed  $(R_{\text{trunc\_s}})[\text{trunc\_sat\_s}_{M,N}(z), 2^N 1, 2^N 2, 2^N 1)].$

```
 \begin{array}{lcl} \operatorname{relaxed\_trunc}_{M,N}^s(\pm q) & = & \operatorname{trunc}_{M,N}^s(\pm q) & & (\operatorname{if} - 2^{N-1} \leq \operatorname{trunc}(\pm q) < 2^{N-1}) \\ \operatorname{relaxed\_trunc}_{M,N}^s(z) & = & \operatorname{relaxed}(R_{\operatorname{trunc\_s}})[\operatorname{trunc\_sat\_s}_{M,N}(z), \operatorname{signed}_N^{-1}(-2^{N-1})] & (\operatorname{otherwise}) \\ \end{array}
```

#### Note

Relaxed signed truncation is implementation-dependent for NaNs and out-of-range values. In the deterministic profile, it behaves like regular trunc\_sat\_s.

```
ivrelaxed swizzle(i^n, j^n)
```

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{\text{swizzle}} \in \{0, 1\}$ .

- For each  $j_k$  in  $j^n$ , let  $r_k$  be the value ivrelaxed\_swizzle\_lane $(i^n, j_k)$ .
- Let  $r^n$  be the concatenation of all  $r_k$ .
- Return  $r^n$ .

```
ivrelaxed_swizzle(i^n, j^n) = ivrelaxed_swizzle_lane(i^n, j)<sup>n</sup>
```

where:

```
\begin{array}{lll} \text{ivrelaxed\_swizzle\_lane}(i^n,j) &=& i[j] & \text{(if } j<16) \\ \text{ivrelaxed\_swizzle\_lane}(i^n,j) &=& 0 & \text{(if signed}_8(j)<0) \\ \text{ivrelaxed\_swizzle\_lane}(i^n,j) &=& \text{relaxed}(R_{\text{swizzle}})[0,i^n[j \bmod n]] & \text{(otherwise)} \end{array}
```

#### Note

Relaxed swizzle is implementation-dependent if the signed interpretation of any of the 8-bit indices in  $j^n$  is larger than or equal to 16. In the deterministic profile, it behaves like regular ivswizzle.

```
\mathsf{relaxed\_dot}(i_1, i_2)
```

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{idot} \in \{0, 1\}$ . It also affects the behaviour of relaxed\_dot\_add.

Its definition is part of the definition of vextbinop specified above.

#### Note

Relaxed dot product is implementation-dependent when the second operand is negative in a signed interpretation. In the deterministic profile, it behaves like signed dot product.

```
irelaxed\_laneselect_N(i_1, i_2, i_3)
```

The implementation-specific behaviour of this operation is determined by the global parameter  $R_{laneselect} \in \{0, 1\}$ .

- If  $i_3$  is smaller than  $2^{N-1}$ , then let  $i_3'$  be the value 0, otherwise  $2^N 1$ .
- Let  $i_3''$  be relaxed  $(R_{laneselect})[i_3, i_3']$ .
- Return ibitselect<sub>N</sub> $(i_1, i_2, i_3'')$ .

```
irelaxed\_laneselect_N(i_1, i_2, i_3) = ibitselect_N(i_1, i_2, relaxed(R_{laneselect})[i_3, extend_{1,N}^s(ishr\_u_N(i_3, N-1))])
```

## Note

Relaxed lane selection is non-deterministic when the mask mixes set and cleared bits, since the value of the high bit may or may not be expanded to all bits. In the deterministic profile, it behaves like ibitselect.

# 4.4 Types

Execution has to check and compare types in a few places, such as executing call\_indirect or instantiating modules. It is an invariant of the semantics that all types occurring during execution are closed.

### Note

Runtime type checks generally involve types from multiple modules or types not defined by a module at all, such that any module-local type indices occurring inside them would not geenrally be meaningful.

### 4.4.1 Instantiation

Any form of type can be *instantiated* into a closed type inside a module instance by substituting each type index x occurring in it with the corresponding defined type moduleinst.types[x].

$$clos_{moduleinst}(t) = t[:= dt^*]$$
 if  $dt^* = moduleinst.types$ 

#### Note

This is the runtime equivalent to type closure, which is applied at validation time.

## 4.5 Values

## 4.5.1 Value Typing

For the purpose of checking argument values against the parameter types of exported functions, values are classified by value types. The following auxiliary typing rules specify this typing relation relative to a store S in which possibly referenced addresses live.

#### **Numeric Values**

The number value (nt.const c) is valid with the number type nt.

#### Todo

below is the official specification

• The value is valid with number type t.

$$s \vdash nt.\mathsf{const}\ c : nt$$

### **Vector Values**

The vector value (vt.const c) is valid with the vector type vt.

#### Todo

below is the official specification

ullet The value is valid with vector type t.

$$s \vdash vt.\mathsf{const}\ c : vt$$

## **Null References**

The reference value (ref.null ht) is valid with the reference type (ref null ht') if:

• The heap type ht' matches the heap type ht.

## Todo

below is the official specification

- The heap type must be valid under the empty context.
- Then the value is valid with reference type (ref null t'), where the heap type t' is the least type that matches t.

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$$\frac{\{\} \vdash ht' \leq ht}{s \vdash \mathsf{ref.null}\ ht : (\mathsf{ref}\ \mathsf{null}\ ht')}$$

#### Note

A null reference can be typed with any smaller type. In particular, that allows it to be typed with the least type in its respective hierarchy. That ensures that the value is compatible with any nullable type in that hierarchy.

#### **Scalar References**

The reference value (ref.i31 i) is valid with the reference type (ref i31).

#### Todo

below is the official specification

• The value is valid with reference type (ref i31).

$$s \vdash \mathsf{ref}.\mathsf{i}\mathsf{31}\ i : (\mathsf{ref}\ \mathsf{i}\mathsf{31})$$

#### **Structure References**

The reference value (ref.struct a) is valid with the reference type (ref dt) if:

- The structure instance s.structs[a] exists.
- The defined type s.structs [a] type is of the form dt.

#### Todo

below is the official specification

- ullet The structure address a must exist in the store.
- Let structinst be the structure instance S.structs[a].
- Let *deftype* be the defined type *structinst*.type.
- The expansion of deftype must be a struct type.
- Then the value is valid with reference type (ref deftype).

$$\frac{s.\mathsf{structs}[a].\mathsf{type} = dt}{s \vdash \mathsf{ref}.\mathsf{struct}\; a : (\mathsf{ref}\; dt)}$$

## **Array References**

The reference value (ref.array a) is valid with the reference type (ref dt) if:

- The array instance s.arrays[a] exists.
- The defined type s.arrays[a].type is of the form dt.

## Todo

below is the official specification

- The array address a must exist in the store.
- Let arrayinst be the array instance S.arrays[a].
- Let deftype be the defined type arrayinst.type.

- The expansion of deftype must be an array type.
- Then the value is valid with reference type (ref arraytype).

$$\frac{s.\mathsf{arrays}[a].\mathsf{type} = dt}{s \vdash \mathsf{ref.array}\; a : (\mathsf{ref}\; dt)}$$

## **Exception References**

The reference value (ref.exn a) is valid with the reference type (ref exn).

#### **Todo**

below is the official specification

- The store entry S.exns[a] must exist.
- Then the value is valid with reference type exnref.

$$s \vdash \text{ref.exn } a : (\text{ref exn})$$

#### **Function References**

The reference value (ref.func a) is valid with the reference type (ref dt) if:

- The function instance s.funcs[a] exists.
- The defined type s.funcs[a].type is of the form dt.

#### **Todo**

below is the official specification

- The function address a must exist in the store.
- Let funcinst be the function instance S.funcs[a].
- Let deftype be the defined type funcinst.type.
- The expansion of deftype must be a function type.
- Then the value is valid with reference type (ref functype).

$$\frac{s.\mathsf{funcs}[a].\mathsf{type} = dt}{s \vdash \mathsf{ref}.\mathsf{func}\; a : (\mathsf{ref}\; dt)}$$

### **Host References**

The reference value (ref.host a) is valid with the reference type (ref any).

#### Todo

below is the official specification

• The value is valid with reference type (ref any).

$$s \vdash \mathsf{ref.host}\ a : (\mathsf{ref\ any})$$

### Note

A bare host reference is considered to be internalized.

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#### **External References**

The reference value (ref.extern addrref) is valid with the reference type (ref extern).

#### Todo

below is the official specification

- The reference value ref must be valid with some reference type (ref null? t).
- The heap type t must match the heap type any.
- Then the value is valid with reference type (ref null? extern).

$$s \vdash \text{ref.extern } addref : (\text{ref extern})$$

### **Subsumption**

The reference value ref is valid with the reference type rt if:

- Under the context s, the reference value ref is valid with the reference type rt'.
- The reference type rt' matches the reference type rt.

#### Todo

below is the official specification

- The value must be valid with some value type t.
- The value type t matches another valid type t'.
- Then the value is valid with type t'.

$$\frac{s \vdash \mathit{ref} : \mathit{rt'} \quad \{\} \vdash \mathit{rt'} \leq \mathit{rt}}{s \vdash \mathit{ref} : \mathit{rt}}$$

## 4.5.2 External Typing

For the purpose of checking external address against imports, such values are classified by external types. The following auxiliary typing rules specify this typing relation relative to a store S in which the referenced instances live.

#### **Functions**

The external address (func a) is valid with the external type (func funcinst.type) if:

- ullet The function instance  $s.\mathsf{funcs}[a]$  exists.
- The function instance s.funcs[a] is of the form funcinst.

### Todo

below is the official specification

- The store entry S.funcs[a] must exist.
- Then func a is valid with external type func S.funcs[a].type.

$$\frac{s.\mathsf{funcs}[a] = \mathit{funcinst}}{s \vdash \mathsf{func}\ a : \mathsf{func}\ \mathit{funcinst}.\mathsf{type}}$$

#### **Tables**

The external address (table a) is valid with the external type (table tableinst.type) if:

- The table instance s.tables[a] exists.
- The table instance s.tables[a] is of the form tableinst.

#### Todo

below is the official specification

- The store entry S.tables[a] must exist.
- Then table a is valid with external type table S.tables[a].type.

$$\frac{s. \mathsf{tables}[a] = \mathit{tableinst}}{s \vdash \mathsf{table} \ a : \mathsf{table} \ \mathit{tableinst}. \mathsf{type}}$$

#### **Memories**

The external address (mem a) is valid with the external type (mem meminst.type) if:

- The memory instance  $s.\mathsf{mems}[a]$  exists.
- The memory instance s.mems[a] is of the form meminst.

#### **Todo**

below is the official specification

- The store entry  $S.\mathsf{mems}[a]$  must exist.
- Then mem a is valid with external type mem S.mems[a].type.

$$\frac{s.\mathsf{mems}[a] = meminst}{s \vdash \mathsf{mem} \ a : \mathsf{mem} \ meminst.\mathsf{type}}$$

#### **Globals**

The external address (global a) is valid with the external type (global globalinst.type) if:

- The global instance s.globals[a] exists.
- The global instance s.globals[a] is of the form globalinst.

#### Todo

below is the official specification

- The store entry  $S.\mathsf{globals}[a]$  must exist.
- Then global a is valid with external type global S.globals[a].type.

$$\frac{s.\mathsf{globals}[a] = \mathit{globalinst}}{s \vdash \mathsf{global}\ a : \mathsf{global}\ \mathit{globalinst}.\mathsf{type}}$$

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#### **Tags**

The external address (tag a) is valid with the external type (tag taginst.type) if:

- The tag instance s.tags[a] exists.
- The tag instance s.tags[a] is of the form taginst.

#### **Todo**

below is the official specification

- The store entry  $S.\mathsf{tags}[a]$  must exist.
- Let tagtype be the function type S.tags[a].type.
- Then tag a is valid with external type tag tagtype.

$$\frac{s.\mathsf{tags}[a] = taginst}{s \vdash \mathsf{tag}\ a : \mathsf{tag}\ taginst.\mathsf{type}}$$

## **Subsumption**

The external address externaldr is valid with the external type xt if:

- Under the context s, the external address externaddr is valid with the external type xt'.
- The external type xt' matches the external type xt.

### Todo

below is the official specification

- The external address must be valid with some external type et.
- The external type et matches another valid type et'.
- Then the external address is valid with type et'.

$$\frac{s \vdash externaddr : xt' \quad \{\} \vdash xt' \leq xt}{s \vdash externaddr : xt}$$

## 4.6 Instructions

WebAssembly computation is performed by executing individual instructions.

## 4.6.1 Parametric Instructions

nop

1. Do nothing.

$$\mathsf{nop} \ \hookrightarrow \ \epsilon$$

unreachable

1. Trap.

unreachable 
$$\hookrightarrow$$
 trap

#### drop

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.

#### Todo

(1) Remove trailing "Do nothing."

$$val \ \mathsf{drop} \ \hookrightarrow \ \epsilon$$

select  $(t^*)$ ?

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const c) from the stack.
- 3. Assert: Due to validation, a value is on the top of the stack.
- 4. Pop the value  $val_2$  from the stack.
- 5. Assert: Due to validation, a value is on the top of the stack.
- 6. Pop the value  $val_1$  from the stack.
- 7. If  $c \neq 0$ , then:
  - a. Push the value  $val_1$  to the stack.
- 8. Else:
  - a. Push the value  $val_2$  to the stack.

```
val_1 \ val_2 \ (\text{i32.const} \ c) \ (\text{select} \ (t^*)^?) \ \hookrightarrow \ val_1 \ \ \text{if} \ c \neq 0 val_1 \ val_2 \ (\text{i32.const} \ c) \ (\text{select} \ (t^*)^?) \ \hookrightarrow \ val_2 \ \ \text{if} \ c = 0
```

#### Note

In future versions of WebAssembly, select may allow more than one value per choice.

## 4.6.2 Numeric Instructions

Numeric instructions are defined in terms of the generic numeric operators. The mapping of numeric instructions to their underlying operators is expressed by the following definition:

$$\begin{array}{rcl} op_{\mathrm{i}N}(i_1,\ldots,i_k) & = & \mathrm{i}\,op_{\,N}(i_1,\ldots,i_k) \\ op_{\,\mathrm{f}N}(z_1,\ldots,z_k) & = & \mathrm{f}\,op_{\,N}(z_1,\ldots,z_k) \end{array}$$

And for conversion operators:

$$cvtop_{t_1,t_2}^{sx^?}(c) = cvtop_{|t_1|,|t_2|}^{sx^?}(c)$$

Where the underlying operators are partial, the corresponding instruction will trap when the result is not defined. Where the underlying operators are non-deterministic, because they may return one of multiple possible NaN values, so are the corresponding instructions.

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#### Note

For example, the result of instruction i32.add applied to operands  $i_1, i_2$  invokes  $\operatorname{add}_{i32}(i_1, i_2)$ , which maps to the generic  $\operatorname{iadd}_{32}(i_1, i_2)$  via the above definition. Similarly, i64.trunc\_f32\_s applied to z invokes  $\operatorname{trunc}_{f32,i64}^s(z)$ , which maps to the generic  $\operatorname{trunc}_{32,64}^s(z)$ .

#### t.const c

1. Push the value t.const c to the stack.

#### Note

No formal reduction rule is required for this instruction, since const instructions already are values.

#### nt.unop

- 1. Assert: Due to validation, a value of number type nt is on the top of the stack.
- 2. Pop the value ( $numtype_0$ .const  $c_1$ ) from the stack.
- 3. If  $unop_{nt}(c_1)$  is empty, then:
  - a. Trap.
- 4. Let c be an element of  $unop_{nt}(c_1)$ .
- 5. Push the value (nt.const c) to the stack.

```
(nt.\mathsf{const}\ c_1)\ (nt.unop) \hookrightarrow (nt.\mathsf{const}\ c) \quad \text{if}\ c \in unop_{nt}(c_1) \\ (nt.\mathsf{const}\ c_1)\ (nt.unop) \hookrightarrow \mathsf{trap} \quad \quad \text{if}\ unop_{nt}(c_1) = \epsilon
```

#### nt.binop

- 1. Assert: Due to validation, a value of number type nt is on the top of the stack.
- 2. Pop the value ( $numtype_0$ .const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a number value is on the top of the stack.
- 4. Pop the value ( $numtype_0$ .const  $c_1$ ) from the stack.
- 5. If  $binop_{nt}(c_1, c_2)$  is empty, then:
  - a. Trap.
- 6. Let c be an element of  $binop_{nt}(c_1, c_2)$ .
- 7. Push the value (nt.const c) to the stack.

```
(nt.\mathsf{const}\ c_1)\ (nt.\mathsf{const}\ c_2)\ (nt.\mathit{binop}) \hookrightarrow (nt.\mathsf{const}\ c) \quad \text{if}\ c \in binop_{nt}(c_1,c_2) \\ (nt.\mathsf{const}\ c_1)\ (nt.\mathsf{const}\ c_2)\ (nt.\mathit{binop}) \hookrightarrow \quad \text{trap} \quad \quad \text{if}\ binop_{nt}(c_1,c_2) = \epsilon
```

#### nt.testop

- 1. Assert: Due to validation, a value of number type nt is on the top of the stack.
- 2. Pop the value ( $numtype_0$ .const  $c_1$ ) from the stack.
- 3. Let c be  $testop_{nt}(c_1)$ .
- 4. Push the value (i32.const c) to the stack.

```
(nt.\mathsf{const}\ c_1)\ (nt.testop) \hookrightarrow (\mathsf{i32.const}\ c) \quad \mathsf{if}\ c = testop_{nt}(c_1)
```

#### nt.relop

- 1. Assert: Due to validation, a value of number type nt is on the top of the stack.
- 2. Pop the value ( $numtype_0$ .const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a number value is on the top of the stack.
- 4. Pop the value ( $numtype_0$ .const  $c_1$ ) from the stack.
- 5. Let c be  $relop_{nt}(c_1, c_2)$ .
- 6. Push the value (i32.const c) to the stack.

```
(nt.\mathsf{const}\ c_1)\ (nt.\mathsf{const}\ c_2)\ (nt.\mathit{relop}) \ \hookrightarrow \ (\mathsf{i32.const}\ c) \ \mathsf{if}\ c = \mathit{relop}_{nt}(c_1,c_2)
```

## $nt_2.cvtop\_nt_1$

- 1. Assert: Due to validation, a value of number type  $nt_1$  is on the top of the stack.
- 2. Pop the value ( $numtype_0$ .const  $c_1$ ) from the stack.
- 3. If  $cvtop_{nt_1,nt_2}(c_1)$  is empty, then:
  - a. Trap.
- 4. Let c be an element of  $\operatorname{cvtop}_{nt_1,nt_2}(c_1)$ .
- 5. Push the value  $(nt_2.\mathsf{const}\ c)$  to the stack.

```
\begin{array}{lll} (nt_1.\mathsf{const}\ c_1)\ (nt_2.\mathit{cvtop\_nt_1}) &\hookrightarrow & (nt_2.\mathsf{const}\ c) & \text{if}\ c \in \mathit{cvtop}_{nt_1,nt_2}(c_1) \\ (nt_1.\mathsf{const}\ c_1)\ (nt_2.\mathit{cvtop\_nt_1}) &\hookrightarrow & \text{trap} & \text{if}\ \mathit{cvtop}_{nt_1,nt_2}(c_1) = \epsilon \end{array}
```

### 4.6.3 Reference Instructions

#### ref.null x

- 1. Let *F* be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let deftype be the defined type F.module.types[x].
- 4. Push the value ref.null deftype to the stack.

```
z; (ref.null x) \hookrightarrow (ref.null z.types[x])
```

#### Note

No formal reduction rule is required for the case ref.null *absheaptype*, since the instruction form is already a value.

### $\mathsf{ref}.\mathsf{func}\; x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, x < |z| module.funcs.
- 3. Push the value (ref.func z.module.funcs[x]) to the stack.

```
z; (ref.func x) \hookrightarrow (ref.func z.module.funcs[x])
```

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### ref.is\_null

- 1. Assert: Due to validation, a reference value is on the top of the stack.
- 2. Pop the value *ref* from the stack.
- 3. If *ref* is ref.null, then:
  - a. Push the value (i32.const 1) to the stack.
- 4. Else:
  - a. Push the value (i32.const 0) to the stack.

#### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
ref 	ext{ ref.is\_null } \hookrightarrow 	ext{ (i32.const 1)} 	ext{ if } ref = 	ext{ (ref.null } ht) ref 	ext{ ref.is\_null } \hookrightarrow 	ext{ (i32.const 0)} 	ext{ otherwise}
```

### ref.as\_non\_null

- 1. Assert: Due to validation, a reference value is on the top of the stack.
- 2. Pop the value *ref* from the stack.
- 3. If *ref* is ref.null, then:
  - a. Trap.
- 4. Push the value *ref* to the stack.

#### **Todo**

(3) Introduce if-let instruction instead of "is of the case".

```
ref 	ext{ ref.as_non_null } \hookrightarrow 	ext{ trap } 	ext{ if } ref = (	ext{ref.null } ht) ref 	ext{ ref.as_non_null } \hookrightarrow 	ext{ ref } 	ext{ otherwise}
```

### ref.eq

- 1. Assert: Due to validation, a reference value is on the top of the stack.
- 2. Pop the value  $ref_2$  from the stack.
- 3. Assert: Due to validation, a reference value is on the top of the stack.
- 4. Pop the value  $ref_1$  from the stack.
- 5. If  $ref_1$  is ref.null, then:
  - a. If  $ref_2$  is ref.null, then:
    - 1) Push the value (i32.const 1) to the stack.
  - b. Else if  $ref_1 = ref_2$ , then:
    - 1) Push the value (i32.const 1) to the stack.
  - c. Else:
    - 1) Push the value (i32.const 0) to the stack.

- 6. Else if  $ref_1 = ref_2$ , then:
  - a. Push the value (i32.const 1) to the stack.
- 7. Else:
  - a. Push the value (i32.const 0) to the stack.

#### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
\begin{array}{lll} \mathit{ref}_1 \; \mathit{ref}_2 \; \mathit{ref}.\mathsf{eq} & \hookrightarrow & (\mathsf{i32.const}\; 1) & \mathsf{if} \; \mathit{ref}_1 = (\mathsf{ref}.\mathsf{null}\; \mathit{ht}_1) \wedge \mathit{ref}_2 = (\mathsf{ref}.\mathsf{null}\; \mathit{ht}_2) \\ \mathit{ref}_1 \; \mathit{ref}_2 \; \mathit{ref}.\mathsf{eq} & \hookrightarrow & (\mathsf{i32.const}\; 1) & \mathsf{otherwise}, \mathsf{if} \; \mathit{ref}_1 = \mathit{ref}_2 \\ \mathit{ref}_1 \; \mathit{ref}_2 \; \mathit{ref}.\mathsf{eq} & \hookrightarrow & (\mathsf{i32.const}\; 0) & \mathsf{otherwise} \end{array}
```

#### ref.test rt

- 1. Let F be the topmost frame.
- 2. Assert: Due to validation, a reference value is on the top of the stack.
- 3. Pop the value *ref* from the stack.
- 4. Assert: Due to validation, ref is valid.
- 5. Let rt' be the type of ref.
- 6. If rt' matches  $\operatorname{clos}_{f.\mathsf{module}}(rt)$ , then:
  - a. Push the value (i32.const 1) to the stack.
- 7. Else:
  - a. Push the value (i32.const 0) to the stack.

#### Todo

- (9) Need to handle RulePr s |- ref: rt properly in prose instead of \$ref\_type\_of Below is the actual prose.
- 1. Let F be the current frame.
- 2. Let  $rt_1$  be the reference type  $clos_{F.module}(rt)$ .
- 3. Assert: due to validation,  $rt_1$  is closed.
- 4. Assert: due to validation, a reference value is on the top of the stack.
- 5. Pop the value *ref* from the stack.
- 6. Assert: due to validation, the reference value is valid with some reference type.
- 7. Let  $rt_2$  be the reference type of ref.
- 8. If the reference type  $rt_2$  matches  $rt_1$ , then:
  - a. Push the value i32.const 1 to the stack.
- 9. Else:
  - a. Push the value i32.const 0 to the stack.

```
\begin{array}{lll} s;f;\mathit{ref}\;(\mathsf{ref}.\mathsf{test}\;rt) &\hookrightarrow & (\mathsf{i32.const}\;1) & \mathsf{if}\;s \vdash \mathit{ref}:\mathit{rt'} \\ & & \land \{\} \vdash \mathit{rt'} \leq \mathsf{clos}_{f.\mathsf{module}}(\mathit{rt}) \\ s;f;\mathit{ref}\;(\mathsf{ref}.\mathsf{test}\;\mathit{rt}) &\hookrightarrow & (\mathsf{i32.const}\;0) & \mathsf{otherwise} \end{array}
```

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#### ref.cast rt

- 1. Let F be the topmost frame.
- 2. Assert: Due to validation, a reference value is on the top of the stack.
- 3. Pop the value *ref* from the stack.
- 4. Assert: Due to validation, ref is valid.
- 5. Let rt' be the type of ref.
- 6. If rt' does not match  $clos_{f.module}(rt)$ , then:
  - a. Trap.
- 7. Push the value *ref* to the stack.

#### Todo

- (9) Need to handle RulePr s |- ref: rt properly in prose instead of \$ref\_type\_of Below is the actual prose.
- 1. Let *F* be the current frame.
- 2. Let  $rt_1$  be the reference type  $clos_{F.module}(rt)$ .
- 3. Assert: due to validation,  $rt_1$  is closed.
- 4. Assert: due to validation, a reference value is on the top of the stack.
- 5. Pop the value *ref* from the stack.
- 6. Assert: due to validation, the reference value is valid with some reference type.
- 7. Let  $rt_2$  be the reference type of ref.
- 8. If the reference type  $rt_2$  matches  $rt_1$ , then:
  - a. Push the value ref back to the stack.
- 9. Else:
  - a. Trap.

```
s; f; ref (ref. cast rt) \hookrightarrow ref \quad \text{if } s \vdash ref : rt' \\ \land \{\} \vdash rt' \leq \operatorname{clos}_{f. \mathsf{module}}(rt) \\ s; f; ref (ref. cast rt) \hookrightarrow \mathsf{trap} \quad \mathsf{otherwise}
```

#### ref.i31

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const i) from the stack.
- 3. Push the value (ref.i31  $\operatorname{wrap}_{32,31}(i))$  to the stack.

```
(i32.const i) ref.i31 \hookrightarrow (ref.i31 \operatorname{wrap}_{32,31}(i))
```

### iз1.get $\_sx$

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If *val* is ref.null, then:
  - a. Trap.
- 4. If val is ref.i31, then:
  - a. Let (ref.i31 i) be val.

b. Push the value (i32.const  $\operatorname{extend}_{31,32}^{sx}(i)$ ) to the stack.

#### Todo

- (3) Introduce if-let instruction instead of "is of the case". (4) Guarantees from validation can help simplify the prose. Below is the actual prose.
- 1. Assert: due to validation, a value of type (ref null i31) is on the top of the stack.
- 2. Pop the value *ref* from the stack.
- 3. If *ref* is ref.null *t*, then:
  - a. Trap.
- 4. Assert: due to validation, a ref is a scalar reference.
- 5. Let ref.i31 i be the reference value ref.
- 6. Let j be the result of computing extend $_{31,32}^{sx}(i)$ .
- 7. Push the value i32.const j to the stack.

```
\begin{array}{lll} (\mathsf{ref.null}\; ht)\; (\mathsf{i31.get}\_sx) &\hookrightarrow & \mathsf{trap} \\ & (\mathsf{ref.i31}\; i)\; (\mathsf{i31.get}\_sx) &\hookrightarrow & (\mathsf{i32.const}\; \mathrm{extend}_{31,32}^{sx}(i)) \end{array}
```

#### struct.new x

- 1. Let z be the current state.
- 2. Assert: Due to validation, the expansion of z.types[x] is struct.
- 3. Let (struct  $structtype_0$ ) be the expansion of z.types[x].
- 4. Let  $(\text{mut}^? zt)^n$  be  $structtype_0$ .
- 5. Let a be the length of z.structs.
- 6. Assert: Due to validation, there are at least n values on the top of the stack.
- 7. Pop the values  $val^n$  from the stack.
- 8. Let si be {type z.types[x], fields  $pack_{zt}(val)^n$  }.
- 9. Push the value (ref.struct a) to the stack.
- 10. Perform  $z[.structs = \oplus si]$ .

#### Todo

- (3') Introduce let binding instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let *F* be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let *deftype* be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is a structure type.
- 5. Let struct  $ft^*$  be the expanded structure type of deftype.
- 6. Let n be the length of the field type sequence  $ft^*$ .
- 7. Assert: due to validation, n values are on the top of the stack.
- 8. Pop the n values  $val^*$  from the stack.
- 9. For every value  $val_i$  in  $val^*$  and corresponding field type  $ft_i$  in  $ft^*$ :

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- a. Let  $fieldval_i$  be the result of computing  $pack_{ft_i}(val_i)$ ).
- 10. Let fieldval\* the concatenation of all field values fieldval<sub>i</sub>.
- 11. Let si be the structure instance {type deftype, fields  $fieldval^*$  }.
- 12. Let a be the length of S.structs.
- 13. Append si to S.structs.
- 14. Push the structure reference ref. struct a to the stack.

```
z; val^n \text{ (struct.new } x) \hookrightarrow z[\text{.structs} = \oplus si]; \text{ (ref.struct } a) \text{ if } z. \text{types}[x] \approx \text{struct (mut}^? zt)^n \\ \wedge a = |z. \text{structs}| \\ \wedge si = \{\text{type } z. \text{types}[x], \text{ fields } (\text{pack}_{zt}(val))^n \}
```

### $\mathsf{struct}.\mathsf{new\_default}\ x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, the expansion of z.types[x] is struct.
- 3. Let (struct  $structtype_0$ ) be the expansion of z.types[x].
- 4. Let  $(\text{mut}^? zt)^*$  be  $structtype_0$ .
- 5. Assert: Due to validation, for all zt in  $zt^*$ , default<sub>unpack(zt)</sub> is defined.
- 6. Let  $val^*$  be default  $\underset{\text{unpack}(zt)}{*}$ .
- 7. Assert: Due to validation, |val\*| = |zt\*|.
- 8. Push the values  $val^*$  to the stack.
- 9. Execute the instruction (struct.new x).

#### Todo

- (3') Introduce let binding instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let deftype be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is a structure type.
- 5. Let struct  $ft^*$  be the expanded structure type of deftype.
- 6. Let n be the length of the field type sequence  $ft^*$ .
- 7. For every field type  $ft_i$  in  $ft^*$ :
  - a. Let  $t_i$  be the value type unpack $(ft_i)$ .
  - b. Assert: due to validation, default $_{t_i}$  is defined.
  - c. Push the value  $default_{t_i}$  to the stack.
- 8. Execute the instruction (struct.new x).

```
z; (struct.new_default x) \hookrightarrow val^* (struct.new x) if z.types[x] \approx struct (mut<sup>?</sup> xt)* \land (default_{unpack(xt)} = val)*
```

## $struct.get\_sx^? x i$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value *val* from the stack.
- 4. If *val* is ref.null, then:
  - a. Trap.
- 5. If *val* is ref.struct, then:
  - a. Let (ref.struct a) be val.
  - b. If i < |z.structs[a].fields| and a < |z.structs|, then:
    - 1) Assert: Due to validation, the expansion of z.types[x] is struct.
    - 2) Let (struct  $structtype_0$ ) be the expansion of z.types[x].
    - 3) Let  $(\text{mut}^? zt)^*$  be  $structtype_0$ .
    - 4) If  $i < |zt^*|$ , then:
      - a) Push the value  $\operatorname{unpack}^{sx^2}_{zt^*[i]}(z.\mathsf{structs}[a].\mathsf{fields}[i])$  to the stack.

#### Todo

- (3) Introduce if-let instruction instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let *deftype* be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is a structure type with at least y+1 fields.
- 5. Let struct  $ft^*$  be the expanded structure type of deftype.
- 6. Let  $ft_y$  be the y-th field type of  $ft^*$ .
- 7. Assert: due to validation, a value of type (ref null x) is on the top of the stack.
- 8. Pop the value *ref* from the stack.
- 9. If ref is ref.null t, then:
  - a. Trap.
- 10. Assert: due to validation, a ref is a structure reference.
- 11. Let ref.struct a be the reference value ref.
- 12. Assert: due to validation, the structure instance S.structs[a] exists and has at least y + 1 fields.
- 13. Let fieldval be the field value S.structs[a].fields[y].
- 14. Let val be the result of computing unpack  $f_{H_n}^{sx^2}$  (fieldval)).
- 15. Push the value *val* to the stack.

```
 z; (\mathsf{ref.null}\ ht)\ (\mathsf{struct.get}\_sx^?\ x\ i) \ \hookrightarrow \ \mathsf{trap} \\ z; (\mathsf{ref.struct}\ a)\ (\mathsf{struct.get}\_sx^?\ x\ i) \ \hookrightarrow \ \mathsf{unpack}^{sx^?}_{zt^*[i]}(z.\mathsf{structs}[a].\mathsf{fields}[i]) \ \mathsf{if}\ z.\mathsf{types}[x] \approx \mathsf{struct}\ (\mathsf{mut}^?\ zt)^*
```

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#### struct.set x i

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value *val* from the stack.
- 4. Assert: Due to validation, a value is on the top of the stack.
- 5. Pop the value val' from the stack.
- 6. If val' is ref.null, then:
  - a. Trap.
- 7. If val' is ref.struct, then:
  - a. Let (ref.struct a) be val'.
  - b. Assert: Due to validation, the expansion of z.types[x] is struct.
  - c. Let (struct  $structtype_0$ ) be the expansion of z.types[x].
  - d. Let  $(mut^? zt)^*$  be  $structtype_0$ .
  - e. If  $i < |zt^*|$ , then:
    - 1) Perform  $z[.structs[a].fields[i] = pack_{zt*[i]}(val)].$

#### Todo

- (3) Introduce if-let instruction instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let *deftype* be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is a structure type with at least y+1 fields.
- 5. Let struct  $ft^*$  be the expanded structure type of deftype.
- 6. Let  $ft_y$  be the y-th field type of  $ft^*$ .
- 7. Assert: due to validation, a value is on the top of the stack.
- 8. Pop the value *val* from the stack.
- 9. Assert: due to validation, a value of type (ref null x) is on the top of the stack.
- 10. Pop the value ref from the stack.
- 11. If ref is ref.null t, then:
- a. Trap.
- 12. Assert: due to validation, a ref is a structure reference.
- 13. Let ref.struct a be the reference value ref.
- 14. Assert: due to validation, the structure instance S.structs[a] exists and has at least y + 1 fields.
- 15. Let *fieldval* be the result of computing  $pack_{ft_n}(val)$ ).
- 16. Replace the field value S.structs[a].fields[y] with fieldval.

```
 \begin{array}{lll} z; (\text{ref.null } ht) \ val \ (\text{struct.set } x \ i) & \hookrightarrow & z; \text{trap} \\ z; (\text{ref.struct } a) \ val \ (\text{struct.set } x \ i) & \hookrightarrow & z[.\text{structs}[a].\text{fields}[i] = \text{pack}_{zt^*[i]}(val)]; \epsilon & \text{if } z. \text{types}[x] \approx \text{struct } (\text{mut}^? \ zt)^* \\ \end{array}
```

#### array.new x

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const n) from the stack.
- 3. Assert: Due to validation, a value is on the top of the stack.
- 4. Pop the value *val* from the stack.
- 5. Push the values  $val^n$  to the stack.
- 6. Execute the instruction (array.new\_fixed x n).

```
val (i32.const n) (array.new x) \hookrightarrow val^n (array.new_fixed x n)
```

### ${\sf array.new\_default}\ x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, the expansion of z-types[x] is array.
- 5. Let (array  $array type_0$ ) be the expansion of z.types[x].
- 6. Let (mut<sup>?</sup> zt) be  $arraytype_0$ .
- 7. Assert: Due to validation,  $default_{unpack(zt)}$  is defined.
- 8. Let val be default<sub>unpack(zt)</sub>.
- 9. Push the values  $val^n$  to the stack.
- 10. Execute the instruction (array.new\_fixed x n).

#### Todo

- (3') Introduce let binding instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F.module.types[x] exists.
- 3. Let deftype be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is an array type.
- 5. Let array ft be the expanded array type of deftype.
- 6. Assert: due to validation, a value of type i32 is on the top of the stack.
- 7. Pop the value i32.const n from the stack.
- 8. Let t be the value type unpack(ft).
- 9. Assert: due to validation, default<sub>t</sub> is defined.
- 10. Push the value default<sub>t</sub> to the stack n times.
- 11. Execute the instruction (array.new\_fixed x n).

```
z; (i32.const n) (array.new_default x) \hookrightarrow val^n (array.new_fixed x n) if z.types[x] \approx array (mut^2 x) \land default_{unpack(xt)} = val
```

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#### array.new fixed x n

- 1. Let z be the current state.
- 2. Assert: Due to validation, the expansion of z.types[x] is array.
- 3. Let (array  $array type_0$ ) be the expansion of z.types[x].
- 4. Let (mut? zt) be  $arraytype_0$ .
- 5. Let a be the length of z.arrays.
- 6. Assert: Due to validation, there are at least n values on the top of the stack.
- 7. Pop the values  $val^n$  from the stack.
- 8. Let ai be {type z.types[x], fields  $pack_{zt}(val)^n$  }.
- 9. Push the value (ref.array a) to the stack.
- 10. Perform  $z[.arrays = \oplus ai]$ .

#### Todo

- (3') Introduce let binding instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let *deftype* be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is a array type.
- 5. Let array ft be the expanded array type of deftype.
- 6. Assert: due to validation, n values are on the top of the stack.
- 7. Pop the n values  $val^*$  from the stack.
- 8. For every value  $val_i$  in  $val^*$ :
  - a. Let fieldval<sub>i</sub> be the result of computing  $pack_{ft}(val_i)$ ).
- 9. Let  $fieldval^*$  be the concatenation of all field values  $fieldval_i$ .
- 10. Let ai be the array instance {type deftype, fields  $fieldval^*$  }.
- 11. Let a be the length of S.arrays.
- 12. Append ai to S.arrays.
- 13. Push the array reference ref. array a to the stack.

```
z; val^n \text{ (array.new\_fixed } x n) \hookrightarrow z[\text{.arrays} = \oplus ai]; (\text{ref.array } a)  if z. \text{types}[x] \approx \text{array (mut}^? zt)  \land a = |z. \text{arrays}| \land ai = \{\text{type } z. \text{types}[x], \text{ fields } (\text{pack}_{zt}(val))^n\}
```

#### array.new\_data x y

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const i) from the stack.
- 6. Assert: Due to validation, the expansion of z.types[x] is array.

- 7. Let (array  $array type_0$ ) be the expansion of z.types[x].
- 8. Let (mut<sup>?</sup> zt) be  $arraytype_0$ .
- 9. If  $i + n \cdot |zt|/8 > |z.\mathsf{datas}[y].\mathsf{bytes}|$ , then:
  - a. Trap.
- 10. Let  $byte^{**}$  be the result for which  $\bigoplus byte^{**} = z.datas[y].bytes[i:n\cdot|zt|/8].$
- 11. Let  $c^n$  be the result for which  $(bytes_{zt}(c^n) = byte^*)^*$ .
- 12. Push the values  $\operatorname{unpack}(zt)$ .const  $\operatorname{unpack}_{zt}(c)^n$  to the stack.
- 13. Execute the instruction (array.new fixed x n).

### Todo

- (7) Render \$inverse\_ with display hint. Below is the actual prose.
- 1. Let *F* be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let deftype be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is an array type.
- 5. Let array ft be the expanded array type of deftype.
- 6. Assert: due to validation, the data address F.module.datas[y] exists.
- 7. Let da be the data address F.module.datas[y].
- 8. Assert: due to validation, the data instance S.datas[da] exists.
- 9. Let datainst be the data instance S.datas[da].
- 10. Assert: due to validation, two values of type i32 are on the top of the stack.
- 11. Pop the value i32.const n from the stack.
- 12. Pop the value i32.const s from the stack.
- 13. Assert: due to validation, the field type ft has a defined bit width.
- 14. Let z be the bit width of field type ft divided by eight.
- 15. If the sum of s and n times z is larger than the length of datainst.bytes, then:
  - a. Trap.
- 16. Let  $b^*$  be the byte sequence datainst.bytes $[s:n\cdot z]$ .
- 17. Let t be the value type unpack(ft).
- 18. For each of the n consecutive subsequences  $b'^z$  of  $b^*$ :
  - a. Assert: due to validation, by  $tes_{ft}$  is defined.
  - b. Let  $c_i$  be the constant for which by  $tes_{ft}(c_i)$  is  $b'^z$ .
  - c. Push the value t.const  $c_i$  to the stack.
- 19. Execute the instruction (array.new\_fixed x n).

```
z; (\mathsf{i32.const}\ i)\ (\mathsf{i32.const}\ n)\ (\mathsf{array.new\_data}\ x\ y) \quad \hookrightarrow \quad \mathsf{trap} \\ \qquad \qquad \mathsf{if}\ z.\mathsf{types}[x] \approx \mathsf{array}\ (\mathsf{mut}^{?}\ zt) \\ \qquad \qquad \land i + n \cdot |zt|/8 > |z.\mathsf{datas}[y].\mathsf{bytes}| \\ z; (\mathsf{i32.const}\ i)\ (\mathsf{i32.const}\ n)\ (\mathsf{array.new\_data}\ x\ y) \quad \hookrightarrow \quad (\mathsf{unpack}(zt).\mathsf{const}\ \mathsf{unpack}_{zt}(c))^n\ (\mathsf{array.new\_fixed}\ x\ n) \\ \qquad \qquad \mathsf{if}\ z.\mathsf{types}[x] \approx \mathsf{array}\ (\mathsf{mut}^{?}\ zt) \\ \qquad \qquad \land \bigoplus \mathsf{bytes}_{zt}(c)^n = z.\mathsf{datas}[y].\mathsf{bytes}[i:n \cdot |zt|/8]
```

4.6. Instructions

### array.new\_elem $x\ y$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const i) from the stack.
- 6. If i + n > |z.elems[y].elem|, then:
  - a. Trap.
- 7. Let  $ref^n$  be z.elems[y].elem[i:n].
- 8. Push the values  $ref^n$  to the stack.
- 9. Execute the instruction (array.new fixed x n).

```
z; (i32.const i) (i32.const n) (array.new_elem x y) \hookrightarrow trap if i+n > |z.elems[y].elem| z; (i32.const i) (i32.const n) (array.new_elem x y) \hookrightarrow ref^n (array.new_fixed x n) if ref^n = z.elems[y].elem[i:n]
```

## $\mathsf{array.get}\_sx?\ x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const i) from the stack.
- 4. Assert: Due to validation, a value is on the top of the stack.
- 5. Pop the value *val* from the stack.
- 6. If *val* is ref.null, then:
  - a. Trap.
- 7. If *val* is ref.array, then:
  - a. Let (ref.array a) be val.
  - b. If a < |z| and  $i \ge |z|$  arrays [a]. fields, then:
    - 1) Trap.
  - c. If i < |z.arrays[a].fields| and a < |z.arrays|, then:
    - 1) Assert: Due to validation, the expansion of z.types[x] is array.
    - 2) Let (array  $array type_0$ ) be the expansion of z.types[x].
    - 3) Let  $(mut^? zt)$  be  $arraytype_0$ .
    - 4) Push the value  $\operatorname{unpack}_{zt}^{sx^{?}}(z.\operatorname{arrays}[a].\operatorname{fields}[i])$  to the stack.

#### Todo

- (3) Introduce if-let instruction instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let *deftype* be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is an array type.

- 5. Let array ft be the expanded array type of deftype.
- 6. Assert: due to validation, a value of type i32 is on the top of the stack.
- 7. Pop the value i32.const i from the stack.
- 8. Assert: due to validation, a value of type (ref null x) is on the top of the stack.
- 9. Pop the value *ref* from the stack.
- 10. If ref is ref.null t, then:
- a. Trap.
- 11. Assert: due to validation, ref is an array reference.
- 12. Let ref.array a be the reference value ref.
- 13. Assert: due to validation, the array instance S.arrays[a] exists.
- 14. If n is larger than or equal to the length of S-arrays[a].fields, then:
  - a. Trap.
- 15. Let fieldval be the field value S.arrays[a].fields[i].
- 16. Let val be the result of computing unpack  $_{tt}^{sx^2}$  (fieldval)).
- 17. Push the value *val* to the stack.

```
z; (ref.null ht) (i32.const i) (array.get_sx^?x) \hookrightarrow trap z; (ref.array a) (i32.const i) (array.get_sx^?x) \hookrightarrow trap if i \ge |z.arrays[a].fields| z; (ref.array a) (i32.const i) (array.get_sx^?x) \hookrightarrow unpack _{zt}^{sx^?}(z.arrays[a].fields[i]) if z.types[x] z array (mutx)
```

### array.set x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value *val* from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const i) from the stack.
- 6. Assert: Due to validation, a value is on the top of the stack.
- 7. Pop the value val' from the stack.
- 8. If val' is ref.null, then:
  - a. Trap.
- 9. If val' is ref.array, then:
  - a. Let (ref.array a) be val'.
  - b. If a < |z| arrays and  $i \ge |z|$  arrays [a]. fields, then:
    - 1) Trap.
  - c. Assert: Due to validation, the expansion of z.types[x] is array.
  - d. Let (array  $array type_0$ ) be the expansion of z.types[x].
  - e. Let (mut? zt) be  $arraytype_0$ .
  - f. Perform  $z[.arrays[a].fields[i] = pack_{zt}(val)]$ .

### Todo

(3) Introduce if-let instruction instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. Below is the actual prose.

- 1. Let *F* be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[x] exists.
- 3. Let deftype be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is an array type.
- 5. Let array ft be the expanded array type of deftype.
- 6. Assert: due to validation, a value is on the top of the stack.
- 7. Pop the value val from the stack.
- 8. Assert: due to validation, a value of type i32 is on the top of the stack.
- 9. Pop the value i32.const i from the stack.
- 10. Assert: due to validation, a value of type (ref null x) is on the top of the stack.
- 11. Pop the value *ref* from the stack.
- 12. If ref is ref.null t, then:
- a. Trap.
- 13. Assert: due to validation, ref is an array reference.
- 14. Let ref.array a be the reference value ref.
- 15. Assert: due to validation, the array instance S-arrays[a] exists.
- 16. If n is larger than or equal to the length of S.arrays[a].fields, then:
  - a. Trap.
- 17. Let *fieldval* be the result of computing  $pack_{ft}(val)$ ).
- 18. Replace the field value S.arrays[a].fields[i] with fieldval.

```
 \begin{array}{lll} z; (\text{ref.null } ht) \text{ (i32.const } i) \ val \ (\text{array.set } x) & \hookrightarrow & z; \text{trap} \\ z; (\text{ref.array } a) \ (\text{i32.const } i) \ val \ (\text{array.set } x) & \hookrightarrow & z; \text{trap} \\ z; (\text{ref.array } a) \ (\text{i32.const } i) \ val \ (\text{array.set } x) & \hookrightarrow & z[\text{.arrays}[a].\text{fields}[i] = \operatorname{pack}_{zt}(val)]; \epsilon \\ & & \text{if } z.\text{types}[x] \approx \operatorname{array} \ (\text{mut}^? \ zt) \\ \end{array}
```

## array.len

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value *val* from the stack.
- 4. If *val* is ref.null, then:
  - a. Trap.
- 5. If *val* is ref.array, then:
  - a. Let (ref.array a) be val.
  - b. If a < |z| arrays, then:
    - 1) Push the value (i32.const |z.arrays[a].fields|) to the stack.

### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
z; (\mathsf{ref.null}\ ht) \ \mathsf{array.len} \ \hookrightarrow \ \mathsf{trap} \ z; (\mathsf{ref.array}\ a) \ \mathsf{array.len} \ \hookrightarrow \ (\mathsf{i32.const}\ |z.\mathsf{arrays}[a].\mathsf{fields}|)
```

### array.fill x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value is on the top of the stack.
- 5. Pop the value val from the stack.
- 6. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 7. Pop the value (i32.const i) from the stack.
- 8. Assert: Due to validation, a value is on the top of the stack.
- 9. Pop the value val' from the stack.
- 10. If val' is ref.null, then:
  - a. Trap.
- 11. If val' is ref.array, then:
  - a. Let (ref.array a) be val'.
  - b. If  $a \ge |z.arrays|$ , then:
    - 1) Do nothing.
  - c. Else if i + n > |z.arrays[a].fields|, then:
    - 1) Trap.
  - d. If n = 0, then:
    - 1) Do nothing.
  - e. Else:
    - 1) Push the value (ref.array a) to the stack.
    - 2) Push the value (i32.const i) to the stack.
    - 3) Push the value *val* to the stack.
    - 4) Execute the instruction (array.set x).
    - 5) Push the value (ref.array a) to the stack.
    - 6) Push the value (i32.const i + 1) to the stack.
    - 7) Push the value *val* to the stack.
    - 8) Push the value (i32.const n-1) to the stack.
    - 9) Execute the instruction (array.fill x).

# Todo

(3) Introduce if-let instruction instead of "is of the case".

```
\begin{array}{lll} z; (\text{ref.null } ht) \text{ (i32.const } i) \text{ } val \text{ (i32.const } n) \text{ (array.fill } x) & \hookrightarrow & \text{trap} \\ z; (\text{ref.array } a) \text{ (i32.const } i) \text{ } val \text{ (i32.const } n) \text{ (array.fill } x) & \hookrightarrow & \text{trap} & \text{if } i+n > |z.\text{arrays}[a].\text{fields}| \\ z; (\text{ref.array } a) \text{ (i32.const } i) \text{ } val \text{ (i32.const } n) \text{ (array.fill } x) & \hookrightarrow & \text{otherwise, if } n=0 \\ z; (\text{ref.array } a) \text{ (i32.const } i) \text{ } val \text{ (i32.const } n) \text{ (array.fill } x) & \hookrightarrow & \text{otherwise} \\ \text{ (ref.array } a) \text{ (i32.const } i) \text{ } val \text{ (array.set } x) & \text{otherwise} \\ \text{ (ref.array } a) \text{ (i32.const } i+1) \text{ } val \text{ (i32.const } n-1) \text{ (array.fill } x) \\ \end{array}
```

### array.copy $x_1 x_2$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const  $i_2$ ) from the stack.
- 6. Assert: Due to validation, a value is on the top of the stack.
- 7. Pop the value *val* from the stack.
- 8. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 9. Pop the value (i32.const  $i_1$ ) from the stack.
- 10. Assert: Due to validation, a value is on the top of the stack.
- 11. Pop the value val' from the stack.
- 12. If val' is ref.null and val is reference value, then:
  - a. Trap.
- 13. If val is ref.null and val' is reference value, then:
  - a. Trap.
- 14. If val' is ref.array, then:
  - a. Let (ref.array  $a_1$ ) be val'.
  - b. If val is ref.array, then:
    - 1) If  $a_1 < |z|$  arrays and  $i_1 + n > |z|$  arrays  $[a_1]$  fields, then:
      - a) Trap.
    - 2) Let (ref.array  $a_2$ ) be val.
    - 3) If  $a_2 \geq |z.arrays|$ , then:
      - a) Do nothing.
    - 4) Else if  $i_2 + n > |z|$  arrays  $[a_2]$  fields, then:
      - a) Trap.
    - 5) If n = 0, then:
      - a) Do nothing.
    - 6) Else:
      - a) Assert: Due to validation, the expansion of z.types[ $x_2$ ] is array.
      - b) Let (array  $array type_0$ ) be the expansion of z.types[ $x_2$ ].

- c) Let  $(mut^? zt_2)$  be  $arraytype_0$ .
- d) Let sx? be  $sx(zt_2)$ .
- e) Push the value (ref.array  $a_1$ ) to the stack.
- f) If  $i_1 \leq i_2$ , then:
  - 1. Push the value (i32.const  $i_1$ ) to the stack.
  - 2. Push the value (ref.array  $a_2$ ) to the stack.
  - 3. Push the value (i32.const  $i_2$ ) to the stack.
  - 4. Execute the instruction (array.get\_ $sx^? x_2$ ).
  - 5. Execute the instruction (array.set  $x_1$ ).
  - 6. Push the value (ref.array  $a_1$ ) to the stack.
  - 7. Push the value (i32.const  $i_1 + 1$ ) to the stack.
  - 8. Push the value (ref.array  $a_2$ ) to the stack.
  - 9. Push the value (i32.const  $i_2 + 1$ ) to the stack.
- g) Else:
  - 1. Push the value (i32.const  $i_1 + n 1$ ) to the stack.
  - 2. Push the value (ref.array  $a_2$ ) to the stack.
  - 3. Push the value (i32.const  $i_2 + n 1$ ) to the stack.
  - 4. Execute the instruction (array.get\_ $sx^? x_2$ ).
  - 5. Execute the instruction (array.set  $x_1$ ).
  - 6. Push the value (ref.array  $a_1$ ) to the stack.
  - 7. Push the value (i32.const  $i_1$ ) to the stack.
  - 8. Push the value (ref.array  $a_2$ ) to the stack.
  - 9. Push the value (i32.const  $i_2$ ) to the stack.
- h) Push the value (i32.const n-1) to the stack.
- i) Execute the instruction (array.copy  $x_1 x_2$ ).

## Todo

- (3) Introduce if-let instruction instead of "is of the case". (5) Use "the expansion of" instead of \$expand function application. + Was too deeply nested Below is the actual prose.
- 1. Let *F* be the current frame.
- 2. Assert: due to validation, the defined type F-module.types[y] exists.
- 3. Let deftype be the defined type F.module.types[y].
- 4. Assert: due to validation, the expansion of deftype is an array type.
- 5. Let array  $mut\ st$  be the expanded array type deftype.
- 6. Assert: due to validation, a value of type i32 is on the top of the stack.
- 7. Pop the value i32.const n from the stack.
- 8. Assert: due to validation, a value of type i32 is on the top of the stack.
- 9. Pop the value i32.const s from the stack.
- 10. Assert: due to validation, a value of type (ref null y) is on the top of the stack.

- 11. Pop the value  $ref_2$  from the stack.
- 12. Assert: due to validation, a value of type i32 is on the top of the stack.
- 13. Pop the value i32.const d from the stack.
- 14. Assert: due to validation, a value of type (ref null x) is on the top of the stack.
- 15. Pop the value  $ref_1$  from the stack.
- 16. If  $ref_1$  is ref.null t, then:
- a. Trap.
- 17. Assert: due to validation,  $ref_1$  is an array reference.
- 18. Let ref.array  $a_1$  be the reference value  $ref_1$ .
- 19. If  $ref_2$  is ref.null t, then:
- a. Trap.
- 20. Assert: due to validation,  $ref_2$  is an array reference.
- 21. Let ref.array  $a_2$  be the reference value  $ref_2$ .
- 22. Assert: due to validation, the array instance S-arrays[ $a_1$ ] exists.
- 23. Assert: due to validation, the array instance S-arrays[ $a_2$ ] exists.
- 24. If d + n is larger than the length of S.arrays[ $a_1$ ].fields, then:
  - a. Trap.
- 25. If s + n is larger than the length of S.arrays[ $a_2$ ].fields, then:
  - a. Trap.
- 26. If n = 0, then:
  - a. Return.
- 27. If  $d \leq s$ , then:
  - a. Push the value ref.array  $a_1$  to the stack.
  - b. Push the value i32.const d to the stack.
  - c. Push the value ref.array  $a_2$  to the stack.
  - d. Push the value i32.const s to the stack.
  - e. Execute getfield(st).
  - f. Execute the instruction array.set x.
  - g. Push the value ref.array  $a_1$  to the stack.
  - h. Assert: due to the earlier check against the array size,  $d+1 < 2^{32}$ .
  - i. Push the value i32.const (d+1) to the stack.
  - j. Push the value ref.array  $a_2$  to the stack.
  - k. Assert: due to the earlier check against the array size,  $s + 1 < 2^{32}$ .
  - 1. Push the value i32.const (s+1) to the stack.
- 28. Else:
  - a. Push the value ref.array  $a_1$  to the stack.
  - b. Assert: due to the earlier check against the array size,  $d + n 1 < 2^{32}$ .
  - c. Push the value i32.const (d + n 1) to the stack.
  - d. Push the value ref.array  $a_2$  to the stack.

- e. Assert: due to the earlier check against the array size,  $s + n 1 < 2^{32}$ .
- f. Push the value i32.const (s + n 1) to the stack.
- g. Execute getfield(st).
- h. Execute the instruction array.set x.
- i. Push the value ref. array  $a_1$  to the stack.
- j. Push the value i32.const d to the stack.
- k. Push the value ref.array  $a_2$  to the stack.
- 1. Push the value i32.const s to the stack.
- 29. Push the value i32.const (n-1) to the stack.
- 30. Execute the instruction array.copy x y.

```
z; (ref.null ht_1) (i32.const i_1) ref (i32.const i_2) (i32.const i_3) (array.copy i_1 i_2) i_3 trap
            z; ref (i32.const i_1) (ref.null ht_2) (i32.const i_2) (i32.const n) (array.copy x_1 x_2) \hookrightarrow trap
z; (ref.array a_1) (i32.const i_1) (ref.array a_2) (i32.const i_2) (i32.const n) (array.copy x_1 x_2) \hookrightarrow trap
     if i_1 + n > |z.arrays[a_1].fields|
z; (ref.array a_1) (i32.const i_1) (ref.array a_2) (i32.const i_2) (i32.const n) (array.copy x_1 x_2) \hookrightarrow trap
     if i_2 + n > |z.arrays[a_2].fields|
z; (ref.array a_1) (i32.const i_1) (ref.array a_2) (i32.const i_2) (i32.const n) (array.copy x_1 x_2) \leftrightarrow \epsilon
     otherwise, if n = 0
z; (ref.array a_1) (i32.const i_1) (ref.array a_2) (i32.const i_2) (i32.const i_2) (array.copy x_1 x_2) \hookrightarrow
   (ref.array a_1) (i32.const i_1)
   (ref.array a_2) (i32.const i_2)
   (array.get_sx^? x_2) (array.set x_1)
   (ref.array a_1) (i32.const i_1 + 1) (ref.array a_2) (i32.const i_2 + 1) (i32.const n - 1) (array.copy x_1 x_2)
        otherwise, if z.types[x_2] \approx array (mut? zt_2)
        \wedge i_1 \leq i_2 \wedge sx^? = sx(zt_2)
z; (ref.array a_1) (i32.const i_1) (ref.array a_2) (i32.const i_2) (i32.const i_3) (array.copy x_1 x_2) \hookrightarrow
   (ref.array a_1) (i32.const i_1 + n - 1)
   (ref.array a_2) (i32.const i_2+n-1)
   (array.get_sx^? x_2) (array.set x_1)
   (ref.array a_1) (i32.const i_1) (ref.array a_2) (i32.const i_2) (i32.const i_2) (array.copy i_1 i_2)
        otherwise, if z.types[x_2] \approx array (mut? zt_2)
        \wedge sx^? = sx(zt_2)
```

Where:

```
sx(consttype) = \epsilon

sx(packtype) = s
```

## array.init\_data x y

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const j) from the stack.
- 6. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 7. Pop the value (i32.const i) from the stack.
- 8. Assert: Due to validation, a value is on the top of the stack.
- 9. Pop the value *val* from the stack.

- 10. If *val* is ref.null, then:
  - a. Trap.
- 11. If val is ref.array, then:
  - a. Let (ref.array a) be val.
  - b. If a < |z| and i + n > |z| arrays[a]. fields], then:
    - 1) Trap
  - c. If the expansion of z.types[x] is array, then:
    - 1) Let (array  $array type_0$ ) be the expansion of z.types[x].
    - 2) Let (mut? zt) be  $arraytype_0$ .
    - 3) If  $j + n \cdot |zt|/8 > |z.\mathsf{datas}[y].\mathsf{bytes}|$ , then:
      - a) Trap.
    - 4) If n = 0, then:
      - a) Do nothing.
    - 5) Else:
      - a) Let c be the result for which by  $tes_{zt}(c) = z.datas[y]$ . by tes[j:|zt|/8].
      - b) Push the value (ref.array a) to the stack.
      - c) Push the value (i32.const i) to the stack.
      - d) Push the value  $\operatorname{unpack}(zt)$ .const  $\operatorname{unpack}_{zt}(c)$  to the stack.
      - e) Execute the instruction (array.set x).
      - f) Push the value (ref.array a) to the stack.
      - g) Push the value (i32.const i + 1) to the stack.
      - h) Push the value (i32.const j + |zt|/8) to the stack.
      - i) Push the value (i32.const n-1) to the stack.
      - j) Execute the instruction (array.init\_data x y).
  - d. Else if n = 0, then:
    - 1) Do nothing.

# Todo

- (7) Render \$inverse\_ with display hint. Below is the actual prose.
- 1. Let F be the current frame.
- 2. Assert: due to validation, the defined type F.module.types[x] exists.
- 3. Let *deftype* be the defined type F.module.types[x].
- 4. Assert: due to validation, the expansion of deftype is an array type.
- 5. Let array ft be the expanded array type deftype.
- 6. Assert: due to validation, the data address F.module.datas[y] exists.
- 7. Let da be the data address F.module.datas[y].
- 8. Assert: due to validation, the data instance S.datas[da] exists.
- 9. Let datainst be the data instance S.datas[da].

- 10. Assert: due to validation, three values of type i32 are on the top of the stack.
- 11. Pop the value i32.const n from the stack.
- 12. Pop the value i32.const s from the stack.
- 13. Pop the value i32.const d from the stack.
- 14. Assert: due to validation, a value of type (ref null x) is on the top of the stack.
- 15. Pop the value *ref* from the stack.
- 16. If ref is ref.null t, then:
- a. Trap.
- 17. Assert: due to validation, ref is an array reference.
- 18. Let ref.array a be the reference value ref.
- 19. Assert: due to validation, the array instance S-arrays[a] exists.
- 20. Assert: due to validation, the field type ft has a defined bit width.
- 21. Let z be the bit width of field type ft divided by eight.
- 22. If d + n is larger than the length of S.arrays[a].fields, or the sum of s and n times z is larger than the length of datainst.bytes, then:
  - a. Trap.
- 23. If n = 0, then:
  - a. Return.
- 24. Let  $b^*$  be the byte sequence datainst.bytes[s:z].
- 25. Let t be the value type unpack(ft).
- 26. Assert: due to validation, bytes $_{tt}$  is defined.
- 27. Let c be the constant for which by  $tes_{tt}(c)$  is  $b^*$ .
- 28. Push the value ref. array a to the stack.
- 29. Push the value i32.const d to the stack.
- 30. Push the value t.const c to the stack.
- 31. Execute the instruction array.set x.
- 32. Push the value ref. array a to the stack.
- 33. Push the value i32.const (d+1) to the stack.
- 34. Push the value i32.const (s+z) to the stack.
- 35. Push the value i32.const (n-1) to the stack.
- 36. Execute the instruction array.init\_data x y.

```
 z; (\text{ref.null } ht) \ (\text{i32.const } i) \ (\text{i32.const } j) \ (\text{i32.const } n) \ (\text{array.init\_data } x \ y) \ \hookrightarrow \ \text{trap}   z; (\text{ref.array } a) \ (\text{i32.const } i) \ (\text{i32.const } j) \ (\text{i32.const } n) \ (\text{array.init\_data } x \ y) \ \hookrightarrow \ \text{trap}   \text{if } i+n>|z.\text{arrays}[a].\text{fields}|   z; (\text{ref.array } a) \ (\text{i32.const } i) \ (\text{i32.const } j) \ (\text{i32.const } n) \ (\text{array.init\_data } x \ y) \ \hookrightarrow \ \text{trap}   \text{if } z.\text{types}[x] \approx \text{array } (\text{mut}^2 \ zt)   \land j+n\cdot|zt|/8>|z.\text{datas}[y].\text{bytes}|   z; (\text{ref.array } a) \ (\text{i32.const } i) \ (\text{i32.const } j) \ (\text{i32.const } n) \ (\text{array.init\_data } x \ y) \ \hookrightarrow \ \epsilon   \text{otherwise, if } n=0   z; (\text{ref.array } a) \ (\text{i32.const } i) \ (\text{i32.const } j) \ (\text{i32.const } n) \ (\text{array.init\_data } x \ y) \ \hookrightarrow   (\text{ref.array } a) \ (\text{i32.const } i) \ (\text{inpack}(zt).\text{const unpack}_{zt}(c)) \ (\text{array.set } x)   (\text{ref.array } a) \ (\text{i32.const } i+1) \ (\text{i32.const } j+|zt|/8) \ (\text{i32.const } n-1) \ (\text{array.init\_data } x \ y)   \text{otherwise, if } z.\text{types}[x] \approx \text{array } (\text{mut}^2 \ zt)   \land \text{bytes}_{zt}(c) = z.\text{datas}[y].\text{bytes}[j:|zt|/8]
```

# $array.init\_elem x y$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const j) from the stack.
- 6. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 7. Pop the value (i32.const i) from the stack.
- 8. Assert: Due to validation, a value is on the top of the stack.
- 9. Pop the value *val* from the stack.
- 10. If *val* is ref.null, then:
  - a. Trap.
- 11. If *val* is ref.array, then:
  - a. Let (ref.array a) be val.
  - b. If a < |z| and i + n > |z| arrays[a]. fields, then:
    - 1) Trap.
  - c. If j + n > |z.elems[y].elem|, then:
    - 1) Trap.
  - d. If n = 0, then:
    - 1) Do nothing.
  - e. Else if j < |z.elems[y].elem|, then:
    - 1) Let ref be z.elems[y].elem[j].
    - 2) Push the value (ref. array a) to the stack.
    - 3) Push the value (i32.const i) to the stack.
    - 4) Push the value *ref* to the stack.
    - 5) Execute the instruction (array.set x).
    - 6) Push the value (ref.array a) to the stack.
    - 7) Push the value (i32.const i + 1) to the stack.
    - 8) Push the value (i32.const j + 1) to the stack.
    - 9) Push the value (i32.const n-1) to the stack.

10) Execute the instruction (array.init\_elem x y).

### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
 \begin{aligned} z; &(\text{ref.null } ht) \text{ (i32.const } i) \text{ (i32.const } j) \text{ (i32.const } n) \text{ (array.init\_elem } x \text{ } y) &\hookrightarrow \text{ trap } \\ z; &(\text{ref.array } a) \text{ (i32.const } i) \text{ (i32.const } j) \text{ (i32.const } n) \text{ (array.init\_elem } x \text{ } y) &\hookrightarrow \text{ trap } \\ &\text{if } i+n>|z.\text{arrays}[a].\text{fields}| \\ z; &(\text{ref.array } a) \text{ (i32.const } i) \text{ (i32.const } j) \text{ (i32.const } n) \text{ (array.init\_elem } x \text{ } y) &\hookrightarrow \text{ trap } \\ &\text{if } j+n>|z.\text{elems}[y].\text{elem}| \\ z; &(\text{ref.array } a) \text{ (i32.const } i) \text{ (i32.const } j) \text{ (i32.const } n) \text{ (array.init\_elem } x \text{ } y) &\hookrightarrow \epsilon \\ &\text{otherwise, if } n=0 \\ z; &(\text{ref.array } a) \text{ (i32.const } i) \text{ (i32.const } j) \text{ (i32.const } n) \text{ (array.init\_elem } x \text{ } y) &\hookrightarrow \epsilon \\ &\text{(ref.array } a) \text{ (i32.const } i) \text{ ref (array.set } x) \\ &\text{(ref.array } a) \text{ (i32.const } i+1) \text{ (i32.const } j+1) \text{ (i32.const } n-1) \text{ (array.init\_elem } x \text{ } y) \\ &\text{otherwise, if } ref = z.\text{elems}[y].\text{elem}[j] \end{aligned}
```

### any.convert extern

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value val from the stack.
- 3. If *val* is ref.null, then:
  - a. Push the value (ref.null any) to the stack.
- 4. If *val* is ref.extern, then:
  - a. Let (ref.extern addrref) be val.
  - b. Push the value addrref to the stack.

# Todo

(3) Introduce if-let instruction instead of "is of the case".

# $extern.convert\_any$

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If *val* is ref.null, then:
  - a. Push the value (ref.null extern) to the stack.
- 4. If *val* is address value, then:
  - a. Let addrref be val.
  - b. Push the value (ref.extern addrref) to the stack.

### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
(ref.null ht) extern.convert_any \hookrightarrow (ref.null extern) addrref extern.convert_any \hookrightarrow (ref.extern addrref)
```

# 4.6.4 Vector Instructions

Vector instructions that operate bitwise are handled as integer operations of respective bit width.

$$op_{\forall N}(i_1,\ldots,i_k) = iop_N(i_1,\ldots,i_k)$$

Most other vector instructions are defined in terms of numeric operators that are applied lane-wise according to the given shape.

$$op_{t \times N}(n_1, \dots, n_k) = \operatorname{lanes}_{t \times N}^{-1}(op_t(i_1, \dots, i_k)^*)$$
 (if  $i_1^* = \operatorname{lanes}_{t \times N}(n_1) \wedge \dots \wedge i_k^* = \operatorname{lanes}_{t \times N}(n_k)$ 

#### Note

For example, the result of instruction i32x4.add applied to operands  $v_1, v_2$  invokes  $\mathsf{add}_{\mathsf{i32x4}}(v_1, v_2)$ , which maps to  $\mathsf{lanes}_{\mathsf{i32x4}}^{-1}(\mathsf{add}_{\mathsf{i32}}(i_1, i_2)^*)$ , where  $i_1^*$  and  $i_2^*$  are sequences resulting from invoking  $\mathsf{lanes}_{\mathsf{i32x4}}(v_1)$  and  $\mathsf{lanes}_{\mathsf{i32x4}}(v_2)$  respectively.

For non-deterministic operators this definition is generalized to sets:

$$op_{t \times N}(n_1, \dots, n_k) = \{\operatorname{lanes}_{t \times N}^{-1}(i^*) \mid i^* \in \times op_t(i_1, \dots, i_k)^* \wedge i_1^* = \operatorname{lanes}_{t \times N}(n_1) \wedge \dots \wedge i_k^* = \operatorname{lanes}_{t \times N}(n_k)\}$$

where  $\times \{x^*\}^N$  transforms a sequence of N sets of values into a set of sequences of N values by computing the set product:

$$\times (S_1 \dots S_N) = \{x_1 \dots x_N \mid x_1 \in S_1 \wedge \dots \wedge x_N \in S_N\}$$

The remaining vector operators use individual definitions.

## v<sub>128</sub>.const c

1. Push the value  $v_{128}$ .const c to the stack.

## Note

No formal reduction rule is required for this instruction, since const instructions coincide with values.

### v128.vvunop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v<sub>128</sub>.const  $c_1$ ) from the stack.
- 3. Assert: Due to validation,  $|vvunop_{v128}(c_1)| > 0$ .
- 4. Let c be an element of  $vvunop_{v128}(c_1)$ .
- 5. Push the value ( $v_{128}$ .const c) to the stack.

```
(\texttt{v128.const}\ c_1)\ (\texttt{v128}.vvunop) \ \hookrightarrow \ (\texttt{v128.const}\ c) \ \ \text{if}\ c \in vvunop_{\texttt{v128}}(c_1)
```

### v128.vvbinop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Assert: Due to validation,  $|vvbinop_{v128}(c_1, c_2)| > 0$ .
- 6. Let c be an element of  $vvbinop_{v128}(c_1, c_2)$ .
- 7. Push the value ( $v_{128}$ .const c) to the stack.

```
(\texttt{v128.const}\ c_1)\ (\texttt{v128.const}\ c_2)\ (\texttt{v128}.vvbinop) \ \hookrightarrow \ (\texttt{v128.const}\ c) \ \text{if}\ c \in vvbinop_{\texttt{v128}}(c_1,c_2)
```

### v128.vvternop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value ( $v_{128}$ .const  $c_3$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_2$ ) from the stack.
- 5. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 6. Pop the value (v128.const  $c_1$ ) from the stack.
- 7. Assert: Due to validation,  $|vvternop_{\vee 128}(c_1, c_2, c_3)| > 0$ .
- 8. Let c be an element of  $vvternop_{v128}(c_1, c_2, c_3)$ .
- 9. Push the value ( $v_{128}$ .const c) to the stack.

```
 (\text{v128.const } c_1) \ (\text{v128.const } c_2) \ (\text{v128.const } c_3) \ (\text{v128.} vvternop) \quad \hookrightarrow \quad (\text{v128.const } c)   \text{if } c \in vvternop_{\text{v128}}(c_1, c_2, c_3)
```

### v128.any\_true

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. Let c be  $ine_{|v|128|}(c_1, 0)$ .
- 4. Push the value (i32.const c) to the stack.

```
(v128.const c_1) (v128.any_true) \hookrightarrow (i32.const c) if c = \mathrm{ine}_{|v|28|}(c_1,0)
```

## sh.vunop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. If  $vunop_{sh}(c_1)$  is empty, then:
  - a. Trap.
- 4. Let c be an element of  $vunop_{sh}(c_1)$ .
- 5. Push the value ( $v_{128}$ .const c) to the stack.

## sh.vbinop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. If  $vbinop_{sh}(c_1, c_2)$  is empty, then:
  - a. Trap.
- 6. Let c be an element of  $vbinop_{sh}(c_1, c_2)$ .
- 7. Push the value ( $v_{128}$ .const c) to the stack.

```
       \text{(v128.const } c_1 \text{) (v128.const } c_2 \text{) } (sh.vbinop) \quad \hookrightarrow \quad \text{(v128.const } c) \quad \text{if } c \in vbinop_{sh}(c_1,c_2) \\        \text{(v128.const } c_1 \text{) (v128.const } c_2 \text{) } (sh.vbinop) \quad \hookrightarrow \quad \text{trap} \qquad \qquad \text{if } vbinop_{sh}(c_1,c_2) = \epsilon
```

### sh.vternop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v<sub>128</sub>.const  $c_3$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_2$ ) from the stack.
- 5. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 6. Pop the value ( $v_{128}$ .const  $c_1$ ) from the stack.
- 7. If  $vternop_{sh}(c_1, c_2, c_3)$  is empty, then:
  - a. Trap.
- 8. Let c be an element of  $vternop_{sh}(c_1, c_2, c_3)$ .
- 9. Push the value ( $v_{128}$ .const c) to the stack.

```
      \text{(v128.const } c_1 \text{) (v128.const } c_2 \text{) (v128.const } c_3 \text{) } (sh.vternop) \ \hookrightarrow \ \text{(v128.const } c) \ \text{if } c \in vternop_{sh}(c_1,c_2,c_3) \\       \text{(v128.const } c_1 \text{) (v128.const } c_2 \text{) (v128.const } c_3 \text{) } (sh.vternop) \ \hookrightarrow \ \text{trap} \ \text{if } vternop_{sh}(c_1,c_2,c_3) = \epsilon
```

### sh.vtestop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. Let i be  $vtestop_{sh}(c_1)$ .
- 4. Push the value (i32.const i) to the stack.

```
(v128.const c_1) (sh.vtestop) \hookrightarrow (i32.const i) if i = vtestop_{sh}(c_1)
```

### sh.vrelop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Let c be  $vrelop_{sh}(c_1, c_2)$ .
- 6. Push the value ( $v_{128}$ .const c) to the stack.

```
(v_{128}.const\ c_1)\ (v_{128}.const\ c_2)\ (sh.vrelop) \hookrightarrow (v_{128}.const\ c) \ \ if\ c=v_{relop} \ _{sh}(c_1,c_2)
```

## sh.vshiftop

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const i) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Let c be  $vshiftop_{sh}(c_1, i)$ .
- 6. Push the value ( $v_{128}$ .const c) to the stack.

```
(v128.const c_1) (i32.const i) (sh.vshiftop) \hookrightarrow (v128.const c) if c = vshiftop_{sh}(c_1, i)
```

#### sh.bitmask

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. Let c be bitmask<sub>sh</sub> $(c_1)$ .
- 4. Push the value (i32.const c) to the stack.

```
(v128.const c_1) (sh.bitmask) \hookrightarrow (i32.const c) if c = \mathsf{bitmask}_{sh}(c_1)
```

### sh.vswizzlop

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Let c be  $vswizzlop_{sh}(c_1, c_2)$ .
- 6. Push the value ( $v_{128}$ .const c) to the stack.

```
(v_{128}.const\ c_1)\ (v_{128}.const\ c_2)\ (sh.vswizzlop)\ \hookrightarrow\ (v_{128}.const\ c)\ if\ c=vswizzlop_{sh}(c_1,c_2)
```

### $sh.\mathsf{shuffle}\ i^*$

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Let c be shuffle<sub>sh</sub> $(i^*, c_1, c_2)$ .
- 6. Push the value ( $v_{128}$ .const c) to the stack.

```
(v128.const c_1) (v128.const c_2) (sh.shuffle i^*) \hookrightarrow (v128.const c) if c = \mathsf{shuffle}_{sh}(i^*, c_1, c_2)
```

## $iN \times M.splat$

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value  $(numtype_0.const c_1)$  from the stack.
- 3. Assert: Due to validation,  $numtype_0 = unpack(iN)$ .
- 4. Let c be  $\operatorname{lanes}_{iN\times M}^{-1}(\operatorname{pack}_{iN}(c_1)^M)$ .
- 5. Push the value (v128.const c) to the stack.

$$(\operatorname{unpack}(\mathsf{i} \mathsf{v}).\mathsf{const}\, c_1)\,(\mathsf{i} \mathsf{v} \mathsf{x} M.\mathsf{splat}) \ \hookrightarrow \ (\mathsf{v} \mathsf{128}.\mathsf{const}\, c) \ \mathsf{if}\, c = \operatorname{lanes}_{\mathsf{i} \mathcal{V} \mathsf{x} M}^{-1}(\operatorname{pack}_{\mathsf{i} \mathcal{V}}(c_1)^M)$$

# $lanetype \times M.extract\_lane\_sx'^? i$

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. If sx'? is not defined and *lanetype* is number type, then:
  - a. Let nt be lanetype.
  - b. If  $i < |\text{lanes}_{nt \times M}(c_1)|$ , then:
    - 1) Let  $c_2$  be lanes $_{nt\times M}(c_1)[i]$ .
    - 2) Push the value  $(nt.const c_2)$  to the stack.
- 4. If *lanetype* is packed type, then:
  - a. Let pt be lanetype.
  - b. If sx'? is defined, then:
    - 1) Let sx be sx'?.
    - 2) If  $i < |\text{lanes}_{pt \times M}(c_1)|$ , then:
      - a) Let  $c_2$  be extend $_{pt|,32}^{sx}(lanes_{pt\times M}(c_1)[i])$ .
      - b) Push the value (i32.const  $c_2$ ) to the stack.

### iNxM.replace lane i

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value  $(numtype_0.const c_2)$  from the stack.
- 3. Assert: Due to validation,  $numtype_0 = unpack(iN)$ .
- 4. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 5. Pop the value (v128.const  $c_1$ ) from the stack.
- 6. Let c be lanes $_{iN\times M}^{-1}(\text{lanes}_{iN\times M}(c_1)[[i] = \text{pack}_{iN}(c_2)])$ .
- 7. Push the value ( $v_{128}$ .const c) to the stack.

```
 (\text{v128.const } c_1) \text{ (unpack(in).const } c_2) \text{ (inx} M. \text{replace\_lane } i) \quad \hookrightarrow \quad (\text{v128.const } c) \\ \text{if } c = \text{lanes}_{\text{iN} \times M}^{-1} \text{ (lanes}_{\text{iN} \times M} (c_1) [[i] = \text{pack}_{\text{iN}} (c_2)])
```

## $sh_2.vextunop\_sh_1$

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. Let c be  $vextunop_{sh_1,sh_2}(c_1)$ .
- 4. Push the value ( $v_{128}$ .const c) to the stack.

```
(v_{128.const} c_1) (sh_2.vextunop\_sh_1) \hookrightarrow (v_{128.const} c) \text{ if } vextunop_{sh_1,sh_2}(c_1) = c
```

# $sh_2.vextbinop\_sh_1$

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Let c be  $vextbinop_{sh_1,sh_2}(c_1,c_2)$ .
- 6. Push the value ( $v_{128}$ .const c) to the stack.

```
(v_{128}.const\ c_1)\ (v_{128}.const\ c_2)\ (sh_2.vextbinop\_sh_1) \ \hookrightarrow \ (v_{128}.const\ c) \ if\ vextbinop_{sh_1,sh_2}(c_1,c_2) = c
```

# $sh_2.vextternop\_sh_1$

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value ( $v_{128}$ .const  $c_3$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v<sub>128</sub>.const  $c_2$ ) from the stack.
- 5. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 6. Pop the value (v128.const  $c_1$ ) from the stack.
- 7. Let *c* be  $vextternop_{sh_1,sh_2}(c_1, c_2, c_3)$ .
- 8. Push the value ( $v_{128}$ .const c) to the stack.

```
(\texttt{v128.const}\ c_1)\ (\texttt{v128.const}\ c_2)\ (\texttt{v128.const}\ c_3)\ (sh_2.vextternop\_sh_1) \quad \hookrightarrow \quad (\texttt{v128.const}\ c) \quad \text{if}\ vextternop\_sh_1, sh_2}(c_1, c_2, c_3) = c
```

# $\mathit{sh}_2.\mathsf{narrow}\_\mathit{sh}_1\_\mathit{sx}$

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_2$ ) from the stack.
- 3. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 4. Pop the value (v128.const  $c_1$ ) from the stack.
- 5. Let c be narrow $_{sh_1,sh_2}^{sx}(c_1,c_2)$ .
- 6. Push the value ( $v_{128}$ .const c) to the stack.

```
(\texttt{v128.const}\ c_1)\ (\texttt{v128.const}\ c_2)\ (sh_2.\mathsf{narrow}\_sh_1\_sx) \quad \hookrightarrow \quad (\texttt{v128.const}\ c) \quad \text{if}\ c = \mathsf{narrow}^{sx}_{sh_1,sh_2}(c_1,c_2)
```

# $sh_2.vcvtop\_zero$ ? $\_sh_1\_half$ ?

- 1. Assert: Due to validation, a value of vector type v128 is on the top of the stack.
- 2. Pop the value (v128.const  $c_1$ ) from the stack.
- 3. Let c be  $vcvtop_{sh_1,sh_2}(vcvtop, half^?, zero^?, c_1)$ .
- 4. Push the value ( $v_{128}$ .const c) to the stack.

```
(\texttt{v128.const}\ c_1)\ (sh_2.vcvtop\_zero^?\_sh_1\_half^?) \ \hookrightarrow \ (\texttt{v128.const}\ c) \ \ \text{if}\ c = vcvtop_{sh_1,sh_2}(vcvtop,half^?,zero^?,c_1)
```

# 4.6.5 Variable Instructions

# local.get x

- 1. Let z be the current state.
- 2. Assert: Due to validation, z.locals[x] is defined.
- 3. Let val be z.locals[x].
- 4. Push the value *val* to the stack.

```
z; (\mathsf{local.get}\ x) \ \hookrightarrow \ val \ \mathsf{if}\ z.\mathsf{locals}[x] = val
```

### local.set x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value val from the stack.
- 4. Perform z[.locals[x] = val].

```
z; val \text{ (local.set } x) \hookrightarrow z[.locals[x] = val]; \epsilon
```

### local.tee x

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. Push the value *val* to the stack.
- 4. Push the value val to the stack.
- 5. Execute the instruction (local.set x).

```
val 	ext{ (local.tee } x) 	ext{ } \hookrightarrow 	ext{ } val 	ext{ (local.set } x)
```

# $\mathsf{global}.\mathsf{get}\ x$

- 1. Let z be the current state.
- 2. Let val be z.globals[x].value.
- 3. Push the value *val* to the stack.

```
z; (global.get x) \hookrightarrow val if z.globals[x].value = val
```

# global.set x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value *val* from the stack.
- 4. Perform z[.globals[x].value = val].

```
z; val \text{ (global.set } x) \hookrightarrow z[.globals[x].value = val]; \epsilon
```

# 4.6.6 Table Instructions

### table.get x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at.const i) from the stack.
- 4. If  $i \geq |z.\mathsf{tables}[x].\mathsf{elem}|$ , then:
  - a. Trap.
- 5. Push the value z.tables[x].elem[i] to the stack.

```
z; (at.\mathsf{const}\ i) (table.get x) \hookrightarrow trap if i \ge |z.\mathsf{tables}[x].\mathsf{elem}| z; (at.\mathsf{const}\ i) (table.get x) \hookrightarrow z.\mathsf{tables}[x].\mathsf{elem}[i] if i < |z.\mathsf{tables}[x].\mathsf{elem}|
```

#### table.set x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a reference value is on the top of the stack.
- 3. Pop the value *ref* from the stack.
- 4. Assert: Due to validation, a number value is on the top of the stack.
- 5. Pop the value (at.const i) from the stack.
- 6. If  $i \ge |z.\mathsf{tables}[x].\mathsf{elem}|$ , then:
  - a. Trap.
- 7. Perform z[.tables[x].elem[i] = ref].

```
z; (at. {\sf const}\ i)\ ref\ ({\sf table.set}\ x) \hookrightarrow z; {\sf trap} if i \ge |z. {\sf tables}[x]. {\sf elem}| z; (at. {\sf const}\ i)\ ref\ ({\sf table.set}\ x) \hookrightarrow z[. {\sf tables}[x]. {\sf elem}[i] = ref]; \epsilon if i < |z. {\sf tables}[x]. {\sf elem}[i]
```

# table.size x

- 1. Let z be the current state.
- 2. Let  $(at \ lim \ rt)$  be z.tables[x].type.
- 3. Let n be the length of z.tables[x].elem.
- 4. Push the value (at.const n) to the stack.

```
 z; (\mathsf{table.size}\ x) \ \hookrightarrow \ (at.\mathsf{const}\ n) \ \ \mathsf{if}\ |z.\mathsf{tables}[x].\mathsf{elem}| = n \\ \wedge \ z.\mathsf{tables}[x].\mathsf{type} = at\ lim\ rt
```

## table.grow x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at.const n) from the stack.
- 4. Assert: Due to validation, a reference value is on the top of the stack.
- 5. Pop the value *ref* from the stack.
- 6. Either:
  - a. Let ti be growtable(z.tables[x], n, ref).
  - b. Push the value (at.const | z.tables[x].elem|) to the stack.
  - c. Perform z[.tables[x] = ti].

### 7. Or:

a. Push the value  $(at. const signed_{|at|}^{-1}(-1))$  to the stack.

```
 z; \mathit{ref} \ (\mathit{at}.\mathsf{const} \ \mathit{n}) \ (\mathsf{table}.\mathsf{grow} \ \mathit{x}) \ \hookrightarrow \ z[.\mathsf{tables}[x] = \mathit{ti}]; (\mathit{at}.\mathsf{const} \ | \mathit{z}.\mathsf{tables}[x].\mathsf{elem}|) \\  \qquad \qquad \mathsf{if} \ \mathit{ti} = \mathsf{growtable}(z.\mathsf{tables}[x], \mathit{n}, \mathit{ref}) \\ z; \mathit{ref} \ (\mathit{at}.\mathsf{const} \ \mathit{n}) \ (\mathsf{table}.\mathsf{grow} \ \mathit{x}) \ \hookrightarrow \ z; (\mathit{at}.\mathsf{const} \ \mathsf{signed}_{|\mathit{at}|}^{-1}(-1))
```

### Note

The table grow instruction is non-deterministic. It may either succeed, returning the old table size sz, or fail, returning -1. Failure must occur if the referenced table instance has a maximum size defined that would be exceeded. However, failure can occur in other cases as well. In practice, the choice depends on the resources available to the embedder.

### table.fill x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at.const n) from the stack.
- 4. Assert: Due to validation, a value is on the top of the stack.
- 5. Pop the value *val* from the stack.
- 6. Assert: Due to validation, a value of number type at is on the top of the stack.
- 7. Pop the value  $(numtype_0.const i)$  from the stack.
- 8. If i + n > |z.tables[x].elem|, then:
  - a. Trap.
- 9. If n = 0, then:
  - a. Do nothing.
- 10. Else:
  - a. Push the value (at.const i) to the stack.
  - b. Push the value val to the stack.
  - c. Execute the instruction (table.set x).
  - d. Push the value (at.const i + 1) to the stack.
  - e. Push the value *val* to the stack.
  - f. Push the value (at.const n-1) to the stack.
  - g. Execute the instruction (table.fill x).

```
\begin{array}{lll} z; (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ n)\ (\mathsf{table.fill}\ x) &\hookrightarrow &\mathsf{trap} &\mathsf{if}\ i+n > |z.\mathsf{tables}[x].\mathsf{elem}| \\ z; (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ n)\ (\mathsf{table.fill}\ x) &\hookrightarrow &\epsilon &\mathsf{otherwise}, \mathsf{if}\ n=0 \\ z; (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ n)\ (\mathsf{table.fill}\ x) &\hookrightarrow &\mathsf{otherwise} \\ (at.\mathsf{const}\ i)\ val\ (\mathsf{table.set}\ x) &\mathsf{otherwise} \\ (at.\mathsf{const}\ i+1)\ val\ (at.\mathsf{const}\ n-1)\ (\mathsf{table.fill}\ x) \end{array}
```

### table.copy $x_1 x_2$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at'.const n) from the stack.

- 4. Assert: Due to validation, a number value is on the top of the stack.
- 5. Pop the value ( $at_2$ .const  $i_2$ ) from the stack.
- 6. Assert: Due to validation, a number value is on the top of the stack.
- 7. Pop the value ( $at_1$ .const  $i_1$ ) from the stack.
- 8. If  $i_1 + n > |z.\mathsf{tables}[x_1].\mathsf{elem}|$ , then:
  - a. Trap.
- 9. If  $i_2 + n > |z.tables[x_2].elem|$ , then:
  - a. Trap.
- 10. If n = 0, then:
  - a. Do nothing.
- 11. Else:
  - a. If  $i_1 \leq i_2$ , then:
    - 1) Push the value  $(at_1.const i_1)$  to the stack.
    - 2) Push the value  $(at_2.const i_2)$  to the stack.
    - 3) Execute the instruction (table.get  $x_2$ ).
    - 4) Execute the instruction (table.set  $x_1$ ).
    - 5) Push the value  $(at_1.const i_1 + 1)$  to the stack.
    - 6) Push the value ( $at_2$ .const  $i_2 + 1$ ) to the stack.
  - b. Else:
    - 1) Push the value  $(at_1.const i_1 + n 1)$  to the stack.
    - 2) Push the value ( $at_2$ .const  $i_2 + n 1$ ) to the stack.
    - 3) Execute the instruction (table.get  $x_2$ ).
    - 4) Execute the instruction (table.set  $x_1$ ).
    - 5) Push the value  $(at_1.const i_1)$  to the stack.
    - 6) Push the value ( $at_2$ .const  $i_2$ ) to the stack.
  - c. Push the value (at'.const n 1) to the stack.
  - d. Execute the instruction (table.copy  $x_1$   $x_2$ ).

### table.init x y

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.

- 5. Pop the value (i32.const j) from the stack.
- 6. Assert: Due to validation, a number value is on the top of the stack.
- 7. Pop the value (at.const i) from the stack.
- 8. If i + n > |z.tables[x].elem|, then:
  - a. Trap.
- 9. If j + n > |z.elems[y].elem|, then:
  - a. Trap.
- 10. If n = 0, then:
  - a. Do nothing.
- 11. Else if j < |z.elems[y].elem|, then:
  - a. Push the value (at.const i) to the stack.
  - b. Push the value z.elems[y].elem[j] to the stack.
  - c. Execute the instruction (table.set x).
  - d. Push the value (at.const i + 1) to the stack.
  - e. Push the value (i32.const j + 1) to the stack.
  - f. Push the value (i32.const n-1) to the stack.
  - g. Execute the instruction (table.init x y).

```
\begin{array}{lll} z; (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ j)\ (\mathsf{i32}.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{init}\ x\ y) &\hookrightarrow &\mathsf{trap}\\ &\mathsf{if}\ i+n>|z.\mathsf{tables}[x].\mathsf{elem}|\ \lor j+n>|z.\mathsf{elems}[y].\mathsf{elem}|\\ z; (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{init}\ x\ y) &\hookrightarrow &\mathsf{\epsilon}\\ z; (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ j)\ (\mathsf{i32}.\mathsf{const}\ n)\ (\mathsf{table}.\mathsf{init}\ x\ y) &\hookrightarrow &\mathsf{\epsilon}\\ (at.\mathsf{const}\ i)\ z.\mathsf{elems}[y].\mathsf{elem}[j]\ (\mathsf{table}.\mathsf{set}\ x) &\mathsf{otherwise}\\ (at.\mathsf{const}\ i+1)\ (\mathsf{i32}.\mathsf{const}\ j+1)\ (\mathsf{i32}.\mathsf{const}\ n-1)\ (\mathsf{table}.\mathsf{init}\ x\ y) &\mathsf{otherwise} \end{array}
```

## elem.drop x

- 1. Let z be the current state.
- 2. Perform z[.elems[x].elem =  $\epsilon$ ].

```
z; (elem.drop x) \hookrightarrow z[.elems[x].elem = \epsilon]; \epsilon
```

# 4.6.7 Memory Instructions

# Note

The alignment memarg.align in load and store instructions does not affect the semantics. It is a hint that the offset ea at which the memory is accessed is intended to satisfy the property  $ea \mod 2^{memarg.align} = 0$ . A WebAssembly implementation can use this hint to optimize for the intended use. Unaligned access violating that property is still allowed and must succeed regardless of the annotation. However, it may be substantially slower on some hardware.

### nt'.loadloadop? x ao

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at.const i) from the stack.

- 4. If *loadop*? is not defined, then:
  - a. Let nt be nt'.
  - b. If i + ao.offset + |nt|/8 > |z.mems[x].bytes|, then:
    - 1) Trap.
  - c. Let c be the result for which by  $tes_{nt}(c) = z$ . mems[x]. by tes[i + ao.offset : |nt|/8].
  - d. Push the value (nt.const c) to the stack.
- 5. If nt' is iN, then:
  - a. If loadop? is defined, then:
    - 1) Let *loadop\_o* be *loadop*?.
    - 2) Let  $n\_sx$  be  $loadop\_o$ .
    - 3) If i + ao.offset + n/8 > |z.mems[x].bytes|, then:
      - a) Trap.
  - b. Let in be nt'.
  - c. If *loadop*? is defined, then:
    - 1) Let *loadop\_o* be *loadop*?.
    - 2) Let  $n\_sx$  be  $loadop\_o$ .
    - 3) Let c be the result for which  $\operatorname{bytes}_{\operatorname{in}}(c)=z.\operatorname{mems}[x].\operatorname{bytes}[i+ao.\operatorname{offset}:n/8].$
    - 4) Push the value (in.const extend  $_{n,|iN|}^{sx}(c)$ ) to the stack.

### Todo

- (7) Render \$inverse\_of\_nbytes with display hint. Below is the actual prose.
- 1. Let *F* be the current frame.
- 2. Assert: due to validation, F.module.mems[x] exists.
- 3. Let a be the memory address F.module.mems[x].
- 4. Assert: due to validation, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of some address type at is on the top of the stack.
- 7. Pop the value at.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If N is not part of the instruction, then:
  - a. Let N be the bit width |t| of number type t.
- 10. If ea + N/8 is larger than the length of mem.bytes, then:
  - a. Trap.
- 11. Let  $b^*$  be the byte sequence mem.bytes[ea: N/8].
- 12. If N and sx are part of the instruction, then:
  - a. Let n be the integer for which bytes<sub>iN</sub> $(n) = b^*$ .
  - b. Let c be the result of computing extend  $_{N,|t|}^{sx}(n)$ .
- 13. Else:

- a. Let c be the constant for which bytes<sub>t</sub>(c) =  $b^*$ .
- 14. Push the value t.const c to the stack.

```
z; (at.\mathsf{const}\ i)\ (nt.\mathsf{load}\ x\ ao) \quad\hookrightarrow \quad \mathsf{trap} \\ \qquad \qquad \qquad \mathsf{if}\ i+ao.\mathsf{offset} + |nt|/8 > |z.\mathsf{mems}[x].\mathsf{bytes}| \\ z; (at.\mathsf{const}\ i)\ (nt.\mathsf{load}\ x\ ao) \quad\hookrightarrow \quad (nt.\mathsf{const}\ c) \\ \qquad \qquad \mathsf{if}\ \mathsf{bytes}_{nt}(c) = z.\mathsf{mems}[x].\mathsf{bytes}[i+ao.\mathsf{offset}:|nt|/8] \\ z; (at.\mathsf{const}\ i)\ (\mathsf{iN}.\mathsf{load}n\_sx\ x\ ao) \quad\hookrightarrow \quad \mathsf{trap} \\ \qquad \qquad \qquad \mathsf{if}\ i+ao.\mathsf{offset} + n/8 > |z.\mathsf{mems}[x].\mathsf{bytes}| \\ z; (at.\mathsf{const}\ i)\ (\mathsf{iN}.\mathsf{load}n\_sx\ x\ ao) \quad\hookrightarrow \quad (\mathsf{iN}.\mathsf{const}\ \mathsf{extend}_{n,|\mathsf{iN}|}^{sx}(c)) \\ \qquad \qquad \mathsf{if}\ \mathsf{bytes}_{\mathsf{in}}(c) = z.\mathsf{mems}[x].\mathsf{bytes}[i+ao.\mathsf{offset}:n/8]
```

v128.loadMxN\_sx x memarg

## Todo

- (\*) Rule and prose both not spliced.
- 1. Let F be the current frame.
- 2. Assert: due to validation, F.module.mems[x] exists.
- 3. Let a be the memory address F.module.mems[x].
- 4. Assert: due to validation, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of some address type at is on the top of the stack.
- 7. Pop the value at.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If  $ea + M \cdot N/8$  is larger than the length of mem bytes, then:
  - a. Trap.
- 10. Let  $b^*$  be the byte sequence  $mem.bytes[ea: M \cdot N/8]$ .
- 11. Let  $m_k$  be the integer for which by  $tes_{iM}(m_k) = b^*[k \cdot M/8 : M/8]$ .
- 12. Let W be the integer  $M \cdot 2$ .
- 13. Let  $n_k$  be the result of computing extend  $M_{M,W}^{sx}(m_k)$ .
- 14. Let c be the result of computing  $\operatorname{lanes}_{iW\times N}^{-1}(n_0\dots n_{N-1})$ .
- 15. Push the value  $v_{128}$ .const c to the stack.

```
S; F; (at. \mathsf{const}\ i) \ (\mathsf{vi28.load} M \times N\_sx \ x \ memarg) \ \hookrightarrow \ S; F; (\mathsf{vi28.const}\ c)   (\mathsf{if}\ ea = i + memarg. \mathsf{offset}   \land ea + M \cdot N/8 \le |S. \mathsf{mems}[F. \mathsf{module}. \mathsf{mems}[x]]. \mathsf{bytes}|   \land \mathsf{bytes}_{iM}(m_k) = S. \mathsf{mems}[F. \mathsf{module}. \mathsf{mems}[x]]. \mathsf{bytes}[ea + k \cdot M/8 : M/8])   \land W = M \cdot 2   \land c = \mathsf{lanes}_{\mathsf{iW} \times N}^{-1} (\mathsf{extend}_{M,W}^{sx}(m_0) \dots \mathsf{extend}_{M,W}^{sx}(m_{N-1})))   S; F; (at. \mathsf{const}\ i) \ (\mathsf{vi28.load} M \times N\_sx \ x \ memarg) \ \hookrightarrow \ S; F; \mathsf{trap}   (\mathsf{otherwise})   z; (at. \mathsf{const}\ i) \ (\mathsf{vi28.load} M \times K\_sx \ x \ ao) \ \hookrightarrow \ \mathsf{trap} \qquad \mathsf{if}\ i + ao. \mathsf{offset} + M \cdot K/8 > |z. \mathsf{mems}[x]. \mathsf{bytes}|   z; (at. \mathsf{const}\ i) \ (\mathsf{vi28.load} M \times K\_sx \ x \ ao) \ \hookrightarrow \ (\mathsf{vi28.const}\ c)   \mathsf{if} \ (\mathsf{bytes}_{\mathsf{iM}}(j) = z. \mathsf{mems}[x]. \mathsf{bytes}[i + ao. \mathsf{offset} + k \cdot M/8 : M/8])^{k < K}   \land c = \mathsf{lanes}_{\mathsf{iN} \times K}^{-1} (\mathsf{extend}_{M,N}^{sx}(j)^K) \land N = M \cdot 2
```

### v<sub>128</sub>.loadN\_splat x memarg

### **Todo**

- (\*) Rule and prose both not spliced.
- 1. Let *F* be the current frame.
- 2. Assert: due to validation, F.module.mems[x] exists.
- 3. Let a be the memory address F.module.mems[x].
- 4. Assert: due to validation, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of some address type at is on the top of the stack.
- 7. Pop the value at.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If ea + N/8 is larger than the length of mem.bytes, then:
  - a. Trap.
- 10. Let  $b^*$  be the byte sequence mem.bytes[ea: N/8].
- 11. Let n be the integer for which bytes<sub>iN</sub> $(n) = b^*$ .
- 12. Let L be the integer 128/N.
- 13. Let c be the result of computing lanes $_{iN\times L}^{-1}(n^L)$ .
- 14. Push the value  $v_{128}$ .const c to the stack.

```
S; F; (at.\mathsf{const}\ i) \ (\mathsf{v128.load}\ N_{-}\mathsf{splat}\ x\ memarg) \ \hookrightarrow \ S; F; (\mathsf{v128.const}\ c)  (\mathsf{if}\ ea = i + memarg.\mathsf{offset} \\ \land \ ea + N/8 \le |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{mems}[x]].\mathsf{bytes}| \\ \land \ \mathsf{bytes}_{iN}(n) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{mems}[x]].\mathsf{bytes}[ea : N/8] \\ \land \ c = \mathsf{lanes}_{\mathsf{iN} \times L}^{-1}(n^L)) \\ S; F; (at.\mathsf{const}\ i) \ (\mathsf{v128.load}\ N_{-}\mathsf{splat}\ x\ memarg) \ \hookrightarrow \ S; F; \mathsf{trap} \\ \ (\mathsf{otherwise}) \\ z; (at.\mathsf{const}\ i) \ (\mathsf{v128.load}\ N_{-}\mathsf{splat}\ x\ ao) \ \hookrightarrow \ \mathsf{trap} \\ \ \mathsf{if}\ i + \ ao.\mathsf{offset} + N/8 > |z.\mathsf{mems}[x].\mathsf{bytes}| \\ z; (at.\mathsf{const}\ i) \ (\mathsf{v128.load}\ N_{-}\mathsf{splat}\ x\ ao) \ \hookrightarrow \ (\mathsf{v128.const}\ c) \\ \ \mathsf{if}\ \mathsf{bytes}_{\mathsf{iN}}(j) = z.\mathsf{mems}[x].\mathsf{bytes}[i + \ ao.\mathsf{offset} : N/8] \\ \land \ N = |\mathsf{iN}| \\ \land \ N = |\mathsf{iN}| \\ \land \ N = |\mathsf{anes}_{\mathsf{iN} \times M}^{-1}(j^M) \\ \end{cases}
```

v128.loadN\_zero x memarg

## **Todo**

- (\*) Rule and prose both not spliced.
- 1. Let *F* be the current frame.
- 2. Assert: due to validation, F.module.mems[x] exists.
- 3. Let a be the memory address F.module.mems[x].
- 4. Assert: due to validation, S.mems[a] exists.

- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of some address type at is on the top of the stack.
- 7. Pop the value at.const i from the stack.
- 8. Let ea be the integer i + memarg.offset.
- 9. If ea + N/8 is larger than the length of mem.bytes, then:
  - a. Trap.
- 10. Let  $b^*$  be the byte sequence mem.bytes[ea: N/8].
- 11. Let n be the integer for which by  $tes_{iN}(n) = b^*$ .
- 12. Let c be the result of computing extend  $_{N,128}^{\mathsf{u}}(n)$ .
- 13. Push the value  $v_{128}$ .const c to the stack.

```
S; F; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{load}N\_\mathsf{zero}\ x\ memarg) \ \hookrightarrow \ S; F; (\mathsf{v128}.\mathsf{const}\ c) \\ (\text{if}\ ea = i + memarg.\mathsf{offset} \\ \land \ ea + N/8 \le |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{mems}[x]].\mathsf{bytes}| \\ \land \ \mathsf{bytes}_{iN}(n) = S.\mathsf{mems}[F.\mathsf{module}.\mathsf{mems}[x]].\mathsf{bytes}[ea : N/8]) \\ \land \ c = \mathsf{extend}^{\mathsf{u}}_{N,128}(n) \\ S; F; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{load}N\_\mathsf{zero}\ x\ memarg) \ \hookrightarrow \ S; F; \mathsf{trap} \\ (\mathsf{otherwise}) \\ z; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{load}N\_\mathsf{zero}\ x\ ao) \ \hookrightarrow \ \mathsf{trap} \qquad \text{if}\ i + ao.\mathsf{offset} + N/8 > |z.\mathsf{mems}[x].\mathsf{bytes}| \\ z; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{load}N\_\mathsf{zero}\ x\ ao) \ \hookrightarrow \ (\mathsf{v128}.\mathsf{const}\ c) \\ \text{if}\ \ \mathsf{bytes}_{iN}(j) = z.\mathsf{mems}[x].\mathsf{bytes}[i + ao.\mathsf{offset}: N/8] \\ \land \ c = \mathsf{extend}^{\mathsf{u}}_{N,128}(j) \\ \end{cases}
```

v128.loadN\_lane x memarg y

## Todo

- (\*) Rule and prose both not spliced.
- 1. Let F be the current frame.
- 2. Assert: due to validation, F.module.mems[x] exists.
- 3. Let a be the memory address F.module.mems[x].
- 4. Assert: due to validation, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 7. Pop the value  $v_{128}$ .const v from the stack.
- 8. Assert: due to validation, a value of some address type at is on the top of the stack.
- 9. Pop the value at.const i from the stack.
- 10. Let ea be the integer i + memarg.offset.
- 11. If ea + N/8 is larger than the length of mem.bytes, then:
  - a. Trap.
- 12. Let  $b^*$  be the byte sequence mem.bytes[ea: N/8].
- 13. Let r be the constant for which by  $tes_{iN}(r) = b^*$ .
- 14. Let L be 128/N.

```
15. Let j^* be the result of computing lanes<sub>iN×L</sub>(v).
  16. Let c be the result of computing lanes_{iN\times L}^{-1}(j^* \text{ with } [y] = r).
  17. Push the value v_{128}.const c to the stack.
          S; F; (at.\mathsf{const}\ i) \ (v_{128}.\mathsf{const}\ v) \ (v_{128}.\mathsf{load}N_{\mathsf{lane}}\ x\ memarg\ y) \ \hookrightarrow \ S; F; (v_{128}.\mathsf{const}\ c)
               (if ea = i + memarq.offset
               \land ea + N/8 \leq |S.mems[F.module.mems[x]].bytes|
               \land \text{ bytes}_{iN}(r) = S.\text{mems}[F.\text{module.mems}[x]].\text{bytes}[ea:N/8])
               \wedge L = 128/N
               \wedge c = \operatorname{lanes}_{i N \times L}^{-1}(\operatorname{lanes}_{i N \times L}(v) \text{ with } [y] = r))
          S; F; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{const}\ v)\ (\mathsf{v128}.\mathsf{load}N\_\mathsf{lane}\ x\ memarg\ y) \ \hookrightarrow \ S; F; \mathsf{trap}
               (otherwise)
z; (at.const i) (v128.const c_1) (v128.loadN_lane x \ ao \ j) \hookrightarrow trap
                                                                                                   if i + ao.offset + N/8 > |z.mems[x].bytes|
z; (at. const i) (v128.const c_1) (v128.loadN_lane x ao j) \hookrightarrow (v128.const c)
                                                                                   \text{if bytes}_{\mathrm{i}N}(k) = z.\mathsf{mems}[x].\mathsf{bytes}[i + ao.\mathsf{offset}:N/8]
                                                                                   \wedge N = |iN|
                                                                                   nt'.storestoreop? x ao
   1. Let z be the current state.
   2. Assert: Due to validation, a number value is on the top of the stack.
   3. Pop the value (nt'''.const c) from the stack.
   4. Assert: Due to validation, a number value is on the top of the stack.
   5. Pop the value (at.const i) from the stack.
   6. Let nt be nt'''.
   7. If i + ao.offset + |nt|/8 > |z.mems[x].bytes| and nt' = nt and storeop? is not defined, then:
          a. Trap.
   8. If nt' = nt and storeop? is not defined, then:
          a. Let b^* be bytes<sub>nt</sub>(c).
          b. Perform z[.mems[x].bytes[i + ao.offset : |nt|/8] = b^*].
   9. If nt''' is in, then:
          a. Let in be nt'''.
          b. If nt' = iN and storeop? is defined, then:
                1) Let n be storeop?.
```

4.6. Instructions

2) If i + ao. offset + n/8 > |z.mems[x].bytes|, then:

4) Perform  $z[.mems[x].bytes[i + ao.offset : n/8] = b^*].$ 

3) Let  $b^*$  be bytes<sub>in</sub>(wrap<sub>|iN|,n</sub>(c)).

a) Trap.

v<sub>128</sub>.storeN\_lane x memarg y

### Todo

(\*) Rule and prose both not spliced.

- 1. Let *F* be the current frame.
- 2. Assert: due to validation, F.module.mems[x] exists.
- 3. Let a be the memory address F.module.mems[x].
- 4. Assert: due to validation, S.mems[a] exists.
- 5. Let mem be the memory instance S.mems[a].
- 6. Assert: due to validation, a value of value type v128 is on the top of the stack.
- 7. Pop the value  $v_{128}$ .const c from the stack.
- 8. Assert: due to validation, a value of some address type at is on the top of the stack.
- 9. Pop the value at.const i from the stack.
- 10. Let ea be the integer i + memarg.offset.
- 11. If ea + N/8 is larger than the length of mem.bytes, then:
  - a. Trap.
- 12. Let L be 128/N.
- 13. Let  $j^*$  be the result of computing lanes<sub>iN×L</sub>(c).
- 14. Let  $b^*$  be the result of computing bytes<sub>iN</sub>  $(j^*[y])$ .
- 15. Replace the bytes mem.bytes [ea: N/8] with  $b^*$ .

```
S; F; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{const}\ c)\ (\mathsf{v128}.\mathsf{store}N\_\mathsf{lane}\ x\ memarg\ y) \ \hookrightarrow \ S'; F; \epsilon (\mathsf{if}\ ea = i + memarg.\mathsf{offset} \land ea + N \le |S.\mathsf{mems}[F.\mathsf{module}.\mathsf{mems}[x]].\mathsf{bytes}| \land L = 128/N \land S' = S\ \mathsf{with}\ \mathsf{mems}[F.\mathsf{module}.\mathsf{mems}[x]].\mathsf{bytes}[ea : N/8] = \mathsf{bytes}_{iN}(\mathsf{lanes}_{iN\times L}(c)[y])) S; F; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{const}\ c)\ (\mathsf{v128}.\mathsf{store}N\_\mathsf{lane}\ x\ memarg\ y) \ \hookrightarrow \ S; F; \mathsf{trap} (\mathsf{otherwise}) z; (at.\mathsf{const}\ i)\ (\mathsf{v128}.\mathsf{const}\ c)\ (\mathsf{v128}.\mathsf{store}N\_\mathsf{lane}\ x\ ao\ j) \ \hookrightarrow \ z; \mathsf{trap}
```

```
 z; (at.\mathsf{const}\ i)\ (\mathsf{v}_{128}.\mathsf{const}\ c)\ (\mathsf{v}_{128}.\mathsf{store}\ N\_\mathsf{lane}\ x\ ao\ j) \ \hookrightarrow \ z; \mathsf{trap} \\ z; (at.\mathsf{const}\ i)\ (\mathsf{v}_{128}.\mathsf{const}\ c)\ (\mathsf{v}_{128}.\mathsf{store}\ N\_\mathsf{lane}\ x\ ao\ j) \ \hookrightarrow \ z[.\mathsf{mems}[x].\mathsf{bytes}[i+ao.\mathsf{offset}:N/8] = b^*]; \epsilon \ \ \mathsf{if}\ if\ if\ N=|\mathsf{i}_N| \\ \wedge\ M=128/N \\ \wedge\ b^*=\mathsf{bytes}_{\mathsf{i}_N}(\mathsf{lane}\ x) \ \wedge\ b^*=\mathsf{bytes}_{\mathsf{i}_N}(\mathsf{lane}\ x) \ \ \mathsf{if}\ if\ if\ N=|\mathsf{i}_N| \ \ \mathsf{if}\ N=|\mathsf{i}_N| \ \ \mathsf{i}_N| \ \ \mathsf{if}\ N=|\mathsf{i}_N| \ \ \mathsf{if}\ N=|\mathsf{i}_N| \ \ \mathsf{if}\ N=|\mathsf{
```

### memory.size x

- 1. Let z be the current state.
- 2. Let  $(at \ lim \ page)$  be z.mems[x].type.
- 3. Let  $n \cdot 64 \, \text{Ki}$  be the length of z.mems[x].bytes.
- 4. Push the value (at.const n) to the stack.

```
z; (memory.size x) \hookrightarrow (at.const n) if n \cdot 64 \, \text{Ki} = |z.\text{mems}[x].\text{bytes}|
 \land z.\text{mems}[x].\text{type} = at \, lim \, \text{page}
```

### ${\it memory.grow} \,\, x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at.const n) from the stack.
- 4. Either:
  - a. Let mi be growmem $(z.\mathsf{mems}[x], n)$ .
  - b. Push the value (at.const |z.mems[x].bytes|/(64 Ki)) to the stack.
  - c. Perform z[.mems[x] = mi].
- 5. Or:
  - a. Push the value  $(at.\mathsf{const}\ \mathrm{signed}_{|at|}^{-1}(-1))$  to the stack.

```
\begin{array}{lll} z; (at.\mathsf{const}\ n)\ (\mathsf{memory.grow}\ x) &\hookrightarrow & z[.\mathsf{mems}[x] = mi]; (at.\mathsf{const}\ |z.\mathsf{mems}[x].\mathsf{bytes}|/64\,\mathrm{Ki}) \\ && \text{if}\ mi = \mathrm{growmem}(z.\mathsf{mems}[x], n) \\ z; (at.\mathsf{const}\ n)\ (\mathsf{memory.grow}\ x) &\hookrightarrow & z; (at.\mathsf{const}\ \mathrm{signed}_{|at|}^{-1}(-1)) \end{array}
```

# Note

The memory.grow instruction is non-deterministic. It may either succeed, returning the old memory size sz, or fail, returning -1. Failure *must* occur if the referenced memory instance has a maximum size defined that would be exceeded. However, failure *can* occur in other cases as well. In practice, the choice depends on the resources available to the embedder.

# memory.fill x

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at.const n) from the stack.
- 4. Assert: Due to validation, a value is on the top of the stack.
- 5. Pop the value *val* from the stack.
- 6. Assert: Due to validation, a value of number type at is on the top of the stack.
- 7. Pop the value  $(numtype_0.const i)$  from the stack.
- 8. If i + n > |z.mems[x].bytes|, then:
  - a. Trap.
- 9. If n = 0, then:
  - a. Do nothing.
- 10. Else:

- a. Push the value (at.const i) to the stack.
- b. Push the value *val* to the stack.
- c. Execute the instruction (i32.store8 x).
- d. Push the value (at.const i + 1) to the stack.
- e. Push the value val to the stack.
- f. Push the value (at.const n-1) to the stack.
- g. Execute the instruction (memory.fill x).

```
\begin{array}{lll} z; (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ n)\ (\mathsf{memory.fill}\ x) &\hookrightarrow &\mathsf{trap} &\mathsf{if}\ i+n > |z.\mathsf{mems}[x].\mathsf{bytes}| \\ z; (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ n)\ (\mathsf{memory.fill}\ x) &\hookrightarrow &\epsilon &\mathsf{otherwise}, \mathsf{if}\ n=0 \\ z; (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ n)\ (\mathsf{memory.fill}\ x) &\hookrightarrow &\mathsf{otherwise} \\ (at.\mathsf{const}\ i)\ val\ (at.\mathsf{const}\ x) &\mathsf{otherwise} \\ (at.\mathsf{const}\ i+1)\ val\ (at.\mathsf{const}\ n-1)\ (\mathsf{memory.fill}\ x) & \\ \end{array}
```

### memory.copy $x_1 x_2$

- 1. Let z be the current state.
- 2. Assert: Due to validation, a number value is on the top of the stack.
- 3. Pop the value (at'.const n) from the stack.
- 4. Assert: Due to validation, a number value is on the top of the stack.
- 5. Pop the value  $(at_2.\mathsf{const}\ i_2)$  from the stack.
- 6. Assert: Due to validation, a number value is on the top of the stack.
- 7. Pop the value  $(at_1.const i_1)$  from the stack.
- 8. If  $i_1 + n > |z.mems[x_1].bytes|$ , then:
  - a. Trap.
- 9. If  $i_2 + n > |z.mems[x_2].bytes|$ , then:
  - a. Trap.
- 10. If n = 0, then:
  - a. Do nothing.
- 11. Else:
  - a. If  $i_1 \leq i_2$ , then:
    - 1) Push the value ( $at_1$ .const  $i_1$ ) to the stack.
    - 2) Push the value  $(at_2.const i_2)$  to the stack.
    - 3) Execute the instruction (i32.load8\_u  $x_2$ ).
    - 4) Execute the instruction (i32.store8  $x_1$ ).
    - 5) Push the value  $(at_1.const i_1 + 1)$  to the stack.
    - 6) Push the value ( $at_2$ .const  $i_2 + 1$ ) to the stack.
  - b. Else:
    - 1) Push the value  $(at_1.const i_1 + n 1)$  to the stack.
    - 2) Push the value  $(at_2.const\ i_2 + n 1)$  to the stack.
    - 3) Execute the instruction (i32.load8\_u  $x_2$ ).
    - 4) Execute the instruction (i32.store8  $x_1$ ).
    - 5) Push the value  $(at_1.const i_1)$  to the stack.

- 6) Push the value ( $at_2$ .const  $i_2$ ) to the stack.
- c. Push the value (at'.const n 1) to the stack.
- d. Execute the instruction (memory.copy  $x_1 x_2$ ).

```
\begin{array}{lll} z; (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n)\ (\mathsf{memory.copy}\ x_1\ x_2) &\hookrightarrow \mathsf{trap} \\ & \text{if}\ i_1+n>|z.\mathsf{mems}[x_1].\mathsf{bytes}| \lor i_2+n>|z.\mathsf{mems}[x_2].\mathsf{bytes}| \\ z; (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n)\ (\mathsf{memory.copy}\ x_1\ x_2) &\hookrightarrow &\mathsf{c} \\ z; (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n)\ (\mathsf{memory.copy}\ x_1\ x_2) &\hookrightarrow \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (\mathsf{i32.load8\_u}\ x_2)\ (\mathsf{i32.store8}\ x_1) &\mathsf{otherwise}, \mathsf{if}\ i_1\leq i_2\\ (at_1.\mathsf{const}\ i_1+1)\ (at_2.\mathsf{const}\ i_2+1)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\hookrightarrow \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n)\ (\mathsf{memory.copy}\ x_1\ x_2) &\hookrightarrow \\ (at_1.\mathsf{const}\ i_1+n-1)\ (at_2.\mathsf{const}\ i_2+n-1)\ (\mathsf{i32.load8\_u}\ x_2)\ (\mathsf{i32.store8}\ x_1) &\mathsf{otherwise}\\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\hookrightarrow \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_1)\ (at_2.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ n-1)\ (\mathsf{memory.copy}\ x_1\ x_2) &\mathsf{otherwise} \\ (at_1.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\ i_2)\ (at'.\mathsf{const}\
```

### memory.init x y

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 3. Pop the value (i32.const n) from the stack.
- 4. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 5. Pop the value (i32.const j) from the stack.
- 6. Assert: Due to validation, a number value is on the top of the stack.
- 7. Pop the value (at.const i) from the stack.
- 8. If i + n > |z.mems[x].bytes|, then:
  - a. Trap.
- 9. If j + n > |z.datas[y].bytes|, then:
  - a. Trap.
- 10. If n = 0, then:
  - a. Do nothing.
- 11. Else if j < |z.datas[y].bytes|, then:
  - a. Push the value (at.const i) to the stack.
  - b. Push the value (i32.const z.datas[y].bytes[j]) to the stack.
  - c. Execute the instruction (i32.store8 x).
  - d. Push the value (at.const i + 1) to the stack.
  - e. Push the value (i32.const j + 1) to the stack.
  - f. Push the value (i32.const n-1) to the stack.
  - g. Execute the instruction (memory.init x y).

```
\begin{array}{lll} z; (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ j)\ (\mathsf{i32}.\mathsf{const}\ n)\ (\mathsf{memory.init}\ x\ y) &\hookrightarrow &\mathsf{trap} \\ &\mathsf{if}\ i+n>|z.\mathsf{mems}[x].\mathsf{bytes}| \lor j+n>|z.\mathsf{datas}[y].\mathsf{bytes}| \\ z; (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ j)\ (\mathsf{i32}.\mathsf{const}\ n)\ (\mathsf{memory.init}\ x\ y) &\hookrightarrow &\mathsf{\epsilon} \\ z; (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ j)\ (\mathsf{i32}.\mathsf{const}\ n)\ (\mathsf{memory.init}\ x\ y) &\hookrightarrow \\ (at.\mathsf{const}\ i)\ (\mathsf{i32}.\mathsf{const}\ z.\mathsf{datas}[y].\mathsf{bytes}[j])\ (\mathsf{i32}.\mathsf{store8}\ x) \\ (at.\mathsf{const}\ i+1)\ (\mathsf{i32}.\mathsf{const}\ j+1)\ (\mathsf{i32}.\mathsf{const}\ n-1)\ (\mathsf{memory.init}\ x\ y) \end{array}
```

## data.drop x

- 1. Let z be the current state.
- 2. Perform  $z[.datas[x].bytes = \epsilon]$ .

```
z; (data.drop x) \hookrightarrow z[.datas[x].bytes = \epsilon]; \epsilon
```

# 4.6.8 Control Instructions

### block bt instr\*

- 1. Let z be the current state.
- 2. Let  $t_1^m \to t_2^n$  be instrype<sub>z</sub>(bt).
- 3. Assert: Due to validation, there are at least m values on the top of the stack.
- 4. Pop the values  $val^m$  from the stack.
- 5. Let L be the label whose arity is n and whose continuation is the end of the block.
- 6. Enter the block  $val^m$   $instr^*$  with the label L.

```
z; val^m \text{ (block } bt \; instr^*) \; \hookrightarrow \; \text{ (label}_n\{\epsilon\} \; val^m \; instr^*) \; \text{ if } instrtype_z(bt) = t_1^m \to t_2^m
```

# loop bt instr\*

- 1. Let z be the current state.
- 2. Let  $t_1^m \to t_2^n$  be instrtype<sub>z</sub>(bt).
- 3. Assert: Due to validation, there are at least m values on the top of the stack.
- 4. Pop the values  $val^m$  from the stack.
- 5. Let L be the label whose arity is m and whose continuation is the start of the block.
- 6. Enter the block  $val^m$   $instr^*$  with the label L.

```
z; val^m \text{ (loop } bt \; instr^*) \; \hookrightarrow \; \text{ (label}_m \{ loop \; bt \; instr^* \} \; val^m \; instr^*) \; \text{ if } instrtype_z(bt) = t_1^m \to t_2^m
```

# if $bt \ instr_1^* \ instr_2^*$

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const c) from the stack.
- 3. If  $c \neq 0$ , then:
  - a. Execute the instruction (block bt  $instr_1^*$ ).
- 4. Else:
  - a. Execute the instruction (block  $bt instr_2^*$ ).

```
(i32.const c) (if bt\ instr_1^* else instr_2^*) \hookrightarrow (block bt\ instr_1^*) if c \neq 0 (i32.const c) (if bt\ instr_1^* else instr_2^*) \hookrightarrow (block bt\ instr_2^*) if c = 0
```

## br l

- 1. If the first non-value entry of the stack is a label, then:
  - a. Let L be the topmost label.
  - b. Let n be the arity of L
  - c. If l = 0, then:
    - 1) Assert: Due to validation, there are at least n values on the top of the stack.

- 2) Pop the values  $val^n$  from the stack.
- 3) Pop all values  $val'^*$  from the top of the stack.
- 4) Pop the label L from the stack.
- 5) Push the values  $val^n$  to the stack.
- 6) Jump to the continuation of L.
- d. Else:
  - 1) Pop all values  $val^*$  from the top of the stack.
  - 2) If l > 0, then:
    - a) Pop the label L from the stack.
    - b) Push the values  $val^*$  to the stack.
    - c) Execute the instruction (br l-1).
- 2. Else if the first non-value entry of the stack is a handler, then:
  - a. Pop all values  $val^*$  from the top of the stack.
  - b. Pop the handler H from the stack.
  - c. Push the values  $val^*$  to the stack.
  - d. Execute the instruction (br l).

# $br_if l$

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const c) from the stack.
- 3. If  $c \neq 0$ , then:
  - a. Execute the instruction (br l).
- 4. Else:
  - a. Do nothing.

```
\begin{array}{lll} \mbox{(i32.const $c$) (br_if $l$)} & \hookrightarrow & \mbox{(br $l$)} & \mbox{if $c \neq 0$} \\ \mbox{(i32.const $c$) (br_if $l$)} & \hookrightarrow & \epsilon & \mbox{if $c = 0$} \end{array}
```

# $br_table l^* l'$

- 1. Assert: Due to validation, a value of number type i32 is on the top of the stack.
- 2. Pop the value (i32.const i) from the stack.
- 3. If  $i < |l^*|$ , then:
  - a. Execute the instruction (br  $l^*[i]$ ).
- 4. Else:
  - a. Execute the instruction (br l').

```
\begin{array}{lll} \text{(i32.const $i$) (br\_table $l^*$ $l'$)} & \hookrightarrow & \text{(br $l^*[i]$)} & \text{if $i < |l^*|$} \\ \text{(i32.const $i$) (br\_table $l^*$ $l'$)} & \hookrightarrow & \text{(br $l'$)} & \text{if $i \ge |l^*|$} \\ \end{array}
```

# $br_on_null\ l$

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value val from the stack.
- 3. If *val* is ref.null, then:
  - a. Execute the instruction (br l).
- 4. Else:
  - a. Push the value val to the stack.

### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
val 	ext{ (br_on_null } l) \hookrightarrow 	ext{ (br } l) 	ext{ if } val = 	ext{ref.null } ht val 	ext{ (br_on_null } l) \hookrightarrow 	ext{ } val 	ext{ } 	ext{ otherwise}
```

# $br\_on\_non\_null \ \mathit{l}$

- 1. Assert: Due to validation, a value is on the top of the stack.
- 2. Pop the value *val* from the stack.
- 3. If *val* is ref.null, then:
  - a. Do nothing.
- 4. Else:
  - a. Push the value val to the stack.
  - b. Execute the instruction (br l).

### Todo

(3) Introduce if-let instruction instead of "is of the case".

```
\begin{array}{lll} \mathit{val} \; (\mathsf{br\_on\_non\_null} \; l) & \hookrightarrow & \epsilon & \text{if} \; \mathit{val} = \mathsf{ref.null} \; \mathit{ht} \\ \mathit{val} \; (\mathsf{br\_on\_non\_null} \; l) & \hookrightarrow & \mathit{val} \; (\mathsf{br} \; l) & \mathsf{otherwise} \end{array}
```

# $br_on_cast \ l \ rt_1 \ rt_2$

- 1. Let F be the topmost frame.
- 2. Assert: Due to validation, a reference value is on the top of the stack.
- 3. Pop the value *ref* from the stack.
- 4. Assert: Due to validation, ref is valid.
- 5. Let rt be the type of ref.
- 6. Push the value *ref* to the stack.
- 7. If rt matches  $clos_{f.module}(rt_2)$ , then:
  - a. Execute the instruction (br l).
- 8. Else:

a. Do nothing.

### Todo

- (9) Need to handle RulePr s |- ref: rt properly in prose instead of \$ref\_type\_of Below is the acutal prose.
- 1. Let *F* be the current frame.
- 2. Let  $rt'_2$  be the reference type  $clos_{F.module}(rt_2)$ .
- 3. Assert: due to validation,  $rt'_2$  is closed.
- 4. Assert: due to validation, a reference value is on the top of the stack.
- 5. Pop the value *ref* from the stack.
- 6. Assert: due to validation, the reference value is valid with some reference type.
- 7. Let rt be the reference type of ref.
- 8. Push the value ref back to the stack.
- 9. If the reference type rt matches  $rt_2'$ , then:
  - a. Execute the instruction (br l).

```
\begin{array}{lll} s;f;\mathit{ref}\;(\mathsf{br\_on\_cast}\;l\;\mathit{rt_1}\;\mathit{rt_2}) &\hookrightarrow &\mathit{ref}\;(\mathsf{br}\;l) & \mathsf{if}\;s\vdash\mathit{ref}\;:\mathit{rt}\\ &&& \land \{\}\vdash\mathit{rt}\leq \mathsf{clos}_{f.\mathsf{module}}(\mathit{rt_2})\\ s;f;\mathit{ref}\;(\mathsf{br\_on\_cast}\;l\;\mathit{rt_1}\;\mathit{rt_2}) &\hookrightarrow &\mathit{ref} & \mathsf{otherwise} \end{array}
```

# br\_on\_cast\_fail $l\ rt_1\ rt_2$

- 1. Let F be the topmost frame.
- 2. Assert: Due to validation, a reference value is on the top of the stack.
- 3. Pop the value *ref* from the stack.
- 4. Assert: Due to validation, ref is valid.
- 5. Let rt be the type of ref.
- 6. Push the value *ref* to the stack.
- 7. If rt matches  $clos_{f.module}(rt_2)$ , then:
  - a. Do nothing.
- 8. Else:
  - a. Execute the instruction (br l).

### Todo

- (9) Need to handle RulePr s |- ref: rt properly in prose instead of \$ref\_type\_of Below is the actual prose.
- 1. Let *F* be the current frame.
- 2. Let  $rt'_2$  be the reference type  $clos_{F.module}(rt_2)$ .
- 3. Assert: due to validation,  $rt'_2$  is closed.
- 4. Assert: due to validation, a reference value is on the top of the stack.
- 5. Pop the value *ref* from the stack.
- 6. Assert: due to validation, the reference value is valid with some reference type.
- 7. Let rt be the reference type of ref.

- 8. Push the value *ref* back to the stack.
- 9. If the reference type rt does not match  $rt'_2$ , then:
  - a. Execute the instruction (br l).

```
s; f; ref 	ext{ (br_on_cast_fail } l 	ext{ } rt_1 	ext{ } rt_2 	ext{)} 	ext{ } \hookrightarrow 	ext{ } ref 	ext{ } if 	ext{ } s \vdash ref : rt 	ext{ } \land \{\} \vdash rt \leq \operatorname{clos}_{f.\mathsf{module}}(rt_2)  s; f; ref 	ext{ (br_on_cast_fail } l 	ext{ } rt_1 	ext{ } rt_2 	ext{)} 	ext{ } \hookrightarrow 	ext{ } ref 	ext{ (br } l 	ext{)} 	ext{ } otherwise
```

### return

- 1. If the first non-value entry of the stack is a frame, then:
  - a. Let F be the topmost frame.
  - b. Let n be the arity of F
  - c. Assert: Due to validation, there are at least n values on the top of the stack.
  - d. Pop the values  $val^n$  from the stack.
  - e. Pop all values  $val'^*$  from the top of the stack.
  - f. Pop the frame F from the stack.
  - g. Push the values  $val^n$  to the stack.
- 2. Else if the first non-value entry of the stack is a label, then:
  - a. Pop all values  $val^*$  from the top of the stack.
  - b. Pop the label L from the stack.
  - c. Push the values  $val^*$  to the stack.
  - d. Execute the instruction return.
- 3. Else:
  - a. If the first non-value entry of the stack is a handler, then:
    - 1) Pop all values  $val^*$  from the top of the stack.
    - 2) Pop the handler H from the stack.
    - 3) Push the values  $val^*$  to the stack.
    - 4) Execute the instruction return.

```
\begin{array}{lll} \text{(frame}_n\{f\} \ val'^* \ val^n \ \text{return } instr^*) & \hookrightarrow & val^n \\ \text{(label}_n\{instr'^*\} \ val^* \ \text{return } instr^*) & \hookrightarrow & val^* \ \text{return} \\ \text{(handler}_n\{catch^*\} \ val^* \ \text{return } instr^*) & \hookrightarrow & val^* \ \text{return} \\ \end{array}
```

### $\mathsf{call}\ x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, x < |z| module.funcs.
- 3. Let a be z-module.funcs[x].
- 4. Assert: Due to validation, a < |z|.funcs.
- 5. Push the value (ref.func a) to the stack.
- 6. Execute the instruction (call\_ref z.funcs[a].type).

```
z; (call x) \hookrightarrow (ref.func a) (call_ref z.funcs[a].type) if z.module.funcs[x] = a
```

### $\mathsf{call}\_\mathsf{ref}\ x$

#### **Todo**

- (\*) Prose not spliced, for the prose merges the two cases of null and non-null references.
- 1. Assert: due to validation, a null or function reference is on the top of the stack.
- 2. Pop the reference value r from the stack.
- 3. If r is ref.null ht, then:
  - a. Trap.
- 4. Assert: due to validation, r is a function reference.
- 5. Let ref.func a be the reference r.
- 6. Invoke the function instance at address a.

$$z$$
; (ref.null  $ht$ ) (call\_ref  $y$ )  $\hookrightarrow$  trap

#### Note

The formal rule for calling a non-null function reference is described below.

```
call_indirect x y
```

- 1. Execute the instruction (table.get x).
- 2. Execute the instruction (ref.cast (ref null y)).
- 3. Execute the instruction (call\_ref y).

```
(\mathsf{call\_indirect}\ x\ y) \ \hookrightarrow \ (\mathsf{table.get}\ x)\ (\mathsf{ref.cast}\ (\mathsf{ref}\ \mathsf{null}\ y))\ (\mathsf{call\_ref}\ y)
```

### $\mathsf{return\_call}\ x$

- 1. Let z be the current state.
- 2. Assert: Due to validation, x < |z| module.funcs.
- 3. Let a be z-module.funcs[x].
- 4. Assert: Due to validation, a < |z|.funcs.
- 5. Push the value (ref.func *a*) to the stack.
- 6. Execute the instruction (return\_call\_ref z.funcs[a].type).

```
z; (return_call x) \hookrightarrow (ref.func a) (return_call_ref z.funcs[a].type) if z.module.funcs[x] = a
```

 $\mathsf{return\_call\_ref}\ x$ 

## $\mathsf{return\_call\_ref}\ y$

- 1. Let z be the current state.
- 2. If the first non-value entry of the stack is a label, then:
  - a. Pop all values  $val^*$  from the top of the stack.
  - b. Pop the label L from the stack.
  - c. Push the values  $val^*$  to the stack.
  - d. Execute the instruction (return\_call\_ref y).

4.6. Instructions

- 3. Else if the first non-value entry of the stack is a handler, then:
  - a. Pop all values  $val^*$  from the top of the stack.
  - b. Pop the handler H from the stack.
  - c. Push the values  $val^*$  to the stack.
  - d. Execute the instruction (return\_call\_ref y).
- 4. Else:
  - a. If the first non-value entry of the stack is a frame, then:
    - 1) Assert: Due to validation, a value is on the top of the stack.
    - 2) Pop the value val'' from the stack.
    - 3) If val'' is ref.null, then:
      - a) Pop all values  $val^*$  from the top of the stack.
      - b) Pop the frame F from the stack.
      - c) Trap.
    - 4) If val'' is ref.func, then:
      - a) Let (ref.func a) be val''.
      - b) If a < |z|, then:
        - 1. Assert: Due to validation, the expansion of z-funcs[a].type is func.
        - 2. Let (func  $functype_0$ ) be the expansion of z-funcs[a]-type.
        - 3. Let  $t_1^n \rightarrow t_2^m$  be  $functype_0$ .
        - 4. Assert: Due to validation, there are at least n values on the top of the stack.
        - 5. Pop the values  $val^n$  from the stack.
        - 6. Pop all values  $val'^*$  from the top of the stack.
        - 7. Pop the frame F from the stack.
        - 8. Push the values  $val^n$  to the stack.
        - 9. Push the value (ref.func a) to the stack.
      - 10. Execute the instruction (call\_ref y).

## Todo

- (\*) Prose not spliced, Sphinx cannot build the document with deeply nested ordered list. (mainly caused by spurious conditions that should be assertions)
- 1. Assert: due to validation, a function reference is on the top of the stack.
- 2. Pop the reference value r from the stack.
- 3. If r is ref.null ht, then:
  - a. Trap.
- 4. Assert: due to validation, r is a function reference.
- 5. Let ref.func a be the reference r.
- 6. Tail-invoke the function instance at address a.

#### return call indirect x y

- 1. Execute the instruction (table.get x).
- 2. Execute the instruction (ref.cast (ref null y)).
- 3. Execute the instruction (return\_call\_ref y).

```
(\text{return\_call\_indirect } x \ y) \ \hookrightarrow \ (\text{table.get } x) \ (\text{ref.cast } (\text{ref } \textbf{null } y)) \ (\text{return\_call\_ref } y)
```

#### throw x

- 1. Let z be the current state.
- 2. Assert: Due to validation, x < |z.tags|.
- 3. Assert: Due to validation, the expansion of z.tags[x].type is func.
- 4. Let (func  $functype_0$ ) be the expansion of z.tags[x].type.
- 5. Let  $t^n \rightarrow result type_1$  be  $functype_0$ .
- 6. Assert: Due to validation,  $result type_1 = \epsilon$ .
- 7. Let a be the length of z.exns.
- 8. Assert: Due to validation, there are at least n values on the top of the stack.
- 9. Pop the values  $val^n$  from the stack.
- 10. Let exn be  $\{ tag z.tags[x], fields <math>val^n \}$ .
- 11. Perform  $z[.exns = \oplus exn]$ .
- 12. Push the value (ref.exn a) to the stack.
- 13. Execute the instruction throw\_ref.

```
z; val^n \text{ (throw } x) \hookrightarrow z[.\mathsf{exns} = \oplus \mathit{exn}]; (\mathsf{ref.exn} \, a) \text{ throw\_ref} \quad \text{if } z.\mathsf{tags}[x].\mathsf{type} \approx \mathsf{func} \, (t^n \to \epsilon) \\ \wedge a = |z.\mathsf{exns}| \\ \wedge \mathit{exn} = \{\mathsf{tag} \, z.\mathsf{tags}[x], \, \mathsf{fields} \, \mathit{val}^n \}
```

## throw\_ref

- 1. Let z be the current state.
- 2. Assert: Due to validation, a value is on the top of the stack.
- 3. Pop the value val' from the stack.
- 4. If val' is ref.null, then:
  - a. Trap.
- 5. If val' is ref.exn, then:
  - a. Let (ref.exn a) be val'.
  - b. Pop all values  $val^*$  from the top of the stack.
  - c. If  $val^* \neq \epsilon$ , then:
    - 1) Push the value (ref.exn a) to the stack.
    - 2) Execute the instruction throw\_ref.
  - d. Else if the first non-value entry of the stack is a label, then:

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- 1) Pop the label L from the stack.
- 2) Push the value (ref.exn a) to the stack.
- 3) Execute the instruction throw\_ref.
- e. Else:
  - 1) If the first non-value entry of the stack is a frame, then:
    - a) Pop the frame F from the stack.
    - b) Push the value (ref.exn a) to the stack.
    - c) Execute the instruction throw ref.
  - 2) Else if not the first non-value entry of the stack is a handler, then:
    - a) Throw the exception val' as a result.
  - 3) Else:
    - a) Let H be the topmost handler.
    - b) Let n be the arity of H
    - c) Let catch"\* be the catch handler of H
    - d) If  $catch''^* = \epsilon$ , then:
      - 1. Pop the handler H from the stack.
      - 2. Push the value (ref.exn a) to the stack.
      - 3. Execute the instruction throw\_ref.
    - e) Else if  $a \ge |z.\text{exns}|$ , then:
      - 1. Let  $catch_0$   $catch'^*$  be  $catch''^*$ .
      - 2. If  $catch_0$  is catch\_all, then:
        - a. Let (catch\_all l) be  $catch_0$ .
        - b. Pop the handler H from the stack.
        - c. Execute the instruction (br l).
      - 3. Else if *catch*<sub>0</sub> is not catch\_all\_ref, then:
        - a. Let catch catch"\* be catch"\*.
        - b. Pop the handler H from the stack.
        - c. Let H be the handler whose arity is n and whose catch handler is  $catch'^*$ .
        - d. Push the handler H.
        - e. Push the value (ref.exn a) to the stack.
        - f. Execute the instruction throw\_ref.
      - 4. Else:
        - a. Let (catch\_all\_ref l) be  $catch_0$ .
        - b. Pop the handler H from the stack.
        - c. Push the value (ref.exn a) to the stack.
        - d. Execute the instruction (br l).
    - f) Else:
      - 1. Let  $val^*$  be z.exns[a].fields.
      - 2. Let  $catch_0$   $catch'^*$  be  $catch''^*$ .

- 3. If  $catch_0$  is catch, then:
  - a. Let (catch x l) be  $catch_0$ .
  - b. If  $x < |z.\mathsf{tags}|$  and  $z.\mathsf{exns}[a].\mathsf{tag} = z.\mathsf{tags}[x]$ , then:
    - 1) Pop the handler H from the stack.
    - 2) Push the values  $val^*$  to the stack.
    - 3) Execute the instruction (br l).
  - c. Else:
    - 1) Let catch catch" be catch".
    - 2) Pop the handler H from the stack.
    - 3) Let H be the handler whose arity is n and whose catch handler is  $catch'^*$ .
    - 4) Push the handler H.
    - 5) Push the value (ref.exn a) to the stack.
    - 6) Execute the instruction throw\_ref.
- 4. Else if  $catch_0$  is catch\_ref, then:
  - a. Let (catch\_ref x l) be  $catch_0$ .
  - b. If  $x \ge |z.\mathsf{tags}|$ , then:
    - 1) Let catch catch"\* be catch"\*.
    - 2) Pop the handler H from the stack.
    - 3) Let H be the handler whose arity is n and whose catch handler is  $catch'^*$ .
    - 4) Push the handler H.
    - 5) Push the value (ref.exn a) to the stack.
    - 6) Execute the instruction throw\_ref.
  - c. Else if  $z.exns[a].tag \neq z.tags[x]$ , then:
    - 1) Let catch catch" be catch".
    - 2) Pop the handler H from the stack.
    - 3) Let H be the handler whose arity is n and whose catch handler is  $catch'^*$ .
    - 4) Push the handler H.
    - 5) Push the value (ref.exn a) to the stack.
    - 6) Execute the instruction throw\_ref.
  - d. Else:
    - 1) Pop the handler H from the stack.
    - 2) Push the values  $val^*$  to the stack.
    - 3) Push the value (ref.exn a) to the stack.
    - 4) Execute the instruction (br l).
- 5. Else:
  - a. If  $catch_0$  is catch\_all, then:
    - 1) Let (catch\_all l) be  $catch_0$ .
    - 2) Pop the handler H from the stack.
    - 3) Execute the instruction (br l).

4.6. Instructions

- b. Else if *catch*<sub>0</sub> is not catch\_all\_ref, then:
  - 1) Let catch catch"\* be catch"\*.
  - 2) Pop the handler H from the stack.
  - 3) Let H be the handler whose arity is n and whose catch handler is  $catch'^*$ .
  - 4) Push the handler H.
  - 5) Push the value (ref.exn a) to the stack.
  - 6) Execute the instruction throw\_ref.
- c. Else:
  - 1) Let (catch\_all\_ref l) be  $catch_0$ .
  - 2) Pop the handler H from the stack.
  - 3) Push the value (ref.exn a) to the stack.
  - 4) Execute the instruction (br l).
- 6. Else if not the first non-value entry of the stack is a label and not the first non-value entry of the stack is a frame and not the first non-value entry of the stack is a handler, then:
  - a. Throw the exception val' as a result.

#### Todo

Was too deeply nested

- 1. Assert: due to validation, a reference is on the top of the stack.
- 2. Pop the reference *ref* from the stack.
- 3. If ref is ref.null ht, then:
  - a. Trap.
- 4. Assert: due to validation, ref is an exception reference.
- 5. Let ref.exn ea be ref.
- 6. Assert: due to validation, S.exns[ea] exists.
- 7. Let exn be the exception instance S.exns[ea].
- 8. Let a be the tag address exn.tag.
- 9. While the stack is not empty and the top of the stack is not an exception handler, do:
  - a. Pop the top element from the stack.
- 10. Assert: the stack is now either empty, or there is an exception handler on the top of the stack.
- 11. If the stack is empty, then:
- a. Return the exception (ref.exn a) as a result.
- 12. Assert: there is an exception handler on the top of the stack.
- 13. Pop the exception handler handler  $\{catch^*\}$  from the stack.
- 14. If  $catch^*$  is empty, then:
  - a. Push the exception reference ref.exn ea back to the stack.
  - b. Execute the instruction throw\_ref again.
- 15. Else:
  - a. Let F be the current frame.

- b. Let  $catch_1$  be the first catch clause in  $catch^*$  and  $catch'^*$  the remaining clauses.
- c. If  $catch_1$  is of the form catch x l and the tag address a equals F.module.tags[x], then:
  - i. Push the values exn.fields to the stack.
  - ii. Execute the instruction br l.
- d. Else if  $catch_1$  is of the form catch\_ref x l and the tag address a equals F.module.tags[x], then:
  - i. Push the values exn.fields to the stack.
  - ii. Push the exception reference ref.exn ea to the stack.
  - iii. Execute the instruction br l.
- e. Else if  $catch_1$  is of the form catch\_all l, then:
  - i. Execute the instruction br l.
- f. Else if  $catch_1$  is of the form catch\_all\_ref l, then:
  - i. Push the exception reference ref.exn ea to the stack.
  - ii. Execute the instruction br l.
- g. Else:
  - 1. Push the modified handler handler<sub>n</sub> $\{catch'^*\}$  back to the stack.
  - 2. Push the exception reference ref.exn ea back to the stack.
  - 3. Execute the instruction throw\_ref again.

```
z; (\mathsf{ref.null}\ ht) \ \mathsf{throw\_ref} \ \hookrightarrow \ \mathsf{trap} z; \mathit{val}^* \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref} \ \mathit{instr}^* \ \hookrightarrow \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref} z; (\mathsf{label}_n \{ \mathit{instr}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref} z; (\mathsf{frame}_n \{ f \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref} z; (\mathsf{handler}_n \{ \epsilon \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref} z; (\mathsf{handler}_n \{ (\mathsf{catch}\ x\ l) \ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ \mathit{val}^* \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref} if z.\mathsf{exns}[a].\mathsf{ta} \ \land \mathit{val}^* = z.\mathsf{ex} z; (\mathsf{handler}_n \{ (\mathsf{catch\_all}\ l) \ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ \mathit{val}^* \ (\mathsf{ref.exn}\ a) \ (\mathsf{br}\ l) if z.\mathsf{exns}[a].\mathsf{ta} \ \land \mathit{val}^* = z.\mathsf{ex} z; (\mathsf{handler}_n \{ (\mathsf{catch\_all}\ l) \ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{br}\ l) z; (\mathsf{handler}_n \{ (\mathsf{catch\_all}\ ref\ l) \ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{ref.exn}\ a) \ (\mathsf{br}\ l) z; (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^* \} \ (\mathsf{ref.exn}\ a) \ \mathsf{throw\_ref}) \ \hookrightarrow \ (\mathsf{handler}_n \{ \mathit{catch}\ \mathit{catch}'^*
```

try table bt catch\* instr\*

- 1. Let z be the current state.
- 2. Let  $t_1^m \to t_2^n$  be instrtype<sub>z</sub>(bt).
- 3. Assert: Due to validation, there are at least m values on the top of the stack.
- 4. Pop the values  $val^m$  from the stack.
- 5. Let H be the handler whose arity is n and whose catch handler is  $catch^*$ .
- 6. Push the handler H.
- 7. Let L be the label whose arity is n and whose continuation is the end of the block.
- 8. Enter the block  $val^m$   $instr^*$  with the label L.

```
z; val^m \text{ (try\_table } bt \ catch^* \ instr^*) \ \hookrightarrow \ \text{ (handler}_n\{catch^*\} \ (label_n\{\epsilon\} \ val^m \ instr^*)) \ \ \text{if } instrtype}_z(bt) = t_1^m \to t_2^m
```

4.6. Instructions

#### 4.6.9 Blocks

The following auxiliary rules define the semantics of executing an instruction sequence that forms a block.

### Entering $instr^*$ with label L

- 1. Push L to the stack.
- 2. Jump to the start of the instruction sequence  $instr^*$ .

#### Note

No formal reduction rule is needed for entering an instruction sequence, because the label L is embedded in the administrative instruction that structured control instructions reduce to directly.

## Exiting $instr^*$ with label L

When the end of a block is reached without a jump, exception, or trap aborting it, then the following steps are performed.

- 1. Pop all values  $val^*$  from the top of the stack.
- 2. Assert: due to validation, the label L is now on the top of the stack.
- 3. Pop the label from the stack.
- 4. Push  $val^*$  back to the stack.
- 5. Jump to the position after the end of the structured control instruction associated with the label L.

$$(label_n\{instr^*\}\ val^*) \hookrightarrow val^*$$

#### Note

This semantics also applies to the instruction sequence contained in a loop instruction. Therefore, execution of a loop falls off the end, unless a backwards branch is performed explicitly.

## 4.6.10 Exception Handling

The following auxiliary rules define the semantics of entering and exiting try\_table blocks.

#### Entering $instr^*$ with label L and exception handler H

- 1. Push H to the stack.
- 2. Push L onto the stack.
- 3. Jump to the start of the instruction sequence  $instr^*$ .

#### Note

No formal reduction rule is needed for entering an exception handler because it is an administrative instruction that the try\_table instruction reduces to directly.

### **Exiting an exception handler**

When the end of a try\_table block is reached without a jump, exception, or trap, then the following steps are performed.

1. Let m be the number of values on the top of the stack.

- 2. Pop the values  $val^m$  from the stack.
- 3. Assert: due to validation, a handler and a label are now on the top of the stack.
- 4. Pop the label from the stack.
- 5. Pop the handler H from the stack.
- 6. Push  $val^m$  back to the stack.
- 7. Jump to the position after the end of the administrative instruction associated with the handler H.

```
(\mathsf{handler}_n\{\mathit{catch}^*\}\ \mathit{val}^*) \hookrightarrow \mathit{val}^*
```

# 4.6.11 Function Calls

The following auxiliary rules define the semantics of invoking a function instance through one of the call instructions and returning from it.

## **Invocation of function reference** (ref.func a)

- 1. Assert: due to validation, S.funcs[a] exists.
- 2. Let f be the function instance, S.funcs[a].
- 3. Let func  $[t_1^n] \to [t_2^m]$  be the composite type expand $(f.\mathsf{type})$ .
- 4. Let  $local^*$  be the list of locals f.code.locals.
- 5. Let  $instr^*$  end be the expression f.code.body.
- 6. Assert: due to validation, n values are on the top of the stack.
- 7. Pop the values  $val^n$  from the stack.
- 8. Let F be the frame {module, locals  $val^n$  (default<sub>t</sub>)\*}.
- 9. Push the activation of F with arity m to the stack.
- 10. Let L be the label whose arity is m and whose continuation is the end of the function.
- 11. Enter the instruction sequence  $instr^*$  with label L.

```
\begin{aligned} z; \mathit{val}^n \; (\mathsf{ref.func} \; a) \; (\mathsf{call\_ref} \; y) &\hookrightarrow & (\mathsf{frame}_m\{f\} \; (\mathsf{label}_m\{\epsilon\} \; \mathit{instr}^*)) \\ & \quad \mathsf{if} \; z. \mathsf{funcs}[a] = \mathit{fi} \\ & \quad \land \mathit{fi}. \mathsf{type} \approx \mathsf{func} \; (t_1^n \to t_2^m) \\ & \quad \land \mathit{fi}. \mathsf{code} = \mathsf{func} \; x \; (\mathsf{local} \; t)^* \; (\mathit{instr}^*) \\ & \quad \land f = \{\mathsf{locals} \; \mathit{val}^n \; (\mathsf{default}_t)^*, \; \mathsf{module} \; \mathit{fi}. \mathsf{module} \} \end{aligned}
```

#### Note

For non-defaultable types, the respective local is left uninitialized by these rules.

### Returning from a function

When the end of a function is reached without a jump (including through return), or an exception or trap aborting it, then the following steps are performed.

- 1. Let F be the current frame.
- 2. Let n be the arity of the activation of F.
- 3. Assert: due to validation, there are n values on the top of the stack.
- 4. Pop the results  $val^n$  from the stack.
- 5. Assert: due to validation, the frame F is now on the top of the stack.

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- 6. Pop the frame from the stack.
- 7. Push  $val^n$  back to the stack.
- 8. Jump to the instruction after the original call.

```
(frame_n \{f\} val^n) \hookrightarrow val^n
```

#### **Host Functions**

Invoking a host function has non-deterministic behavior. It may either terminate with a trap, an exception, or return regularly. However, in the latter case, it must consume and produce the right number and types of WebAssembly values on the stack, according to its function type.

A host function may also modify the store. However, all store modifications must result in an extension of the original store, i.e., they must only modify mutable contents and must not have instances removed. Furthermore, the resulting store must be valid, i.e., all data and code in it is well-typed.

```
S; val^n \text{ (invoke } a) \hookrightarrow S'; result \\ \text{ (if } S. \text{funcs}[a] = \{ \text{type } deftype, \text{hostfunc } hf \} \\ \land \text{ expand} (deftype) = \text{func } [t_1^n] \rightarrow [t_2^m] \\ \land (S'; result) \in hf(S; val^n)) \\ S; val^n \text{ (invoke } a) \hookrightarrow S; val^n \text{ (invoke } a) \\ \text{ (if } S. \text{funcs}[a] = \{ \text{type } deftype, \text{hostfunc } hf \} \\ \land \text{ expand} (deftype) = \text{func } [t_1^n] \rightarrow [t_2^m] \\ \land \bot \in hf(S; val^n)) \\ \end{cases}
```

Here,  $hf(S; val^n)$  denotes the implementation-defined execution of host function hf in current store S with arguments  $val^n$ . It yields a set of possible outcomes, where each element is either a pair of a modified store S' and a result or the special value  $\bot$  indicating divergence. A host function is non-deterministic if there is at least one argument for which the set of outcomes is not singular.

For a WebAssembly implementation to be sound in the presence of host functions, every host function instance must be valid, which means that it adheres to suitable pre- and post-conditions: under a valid store S, and given arguments  $val^n$  matching the ascribed parameter types  $t_1^n$ , executing the host function must yield a non-empty set of possible outcomes each of which is either divergence or consists of a valid store S' that is an extension of S and a result matching the ascribed return types  $t_2^m$ . All these notions are made precise in the Appendix.

#### Note

A host function can call back into WebAssembly by invoking a function exported from a module. However, the effects of any such call are subsumed by the non-deterministic behavior allowed for the host function.

# 4.6.12 Expressions

An expression is evaluated relative to a current frame pointing to its containing module instance.

eval expr instr\*

- 1. Execute the sequence  $instr^*$ .
- 2. Pop the value *val* from the stack.
- 3. Return val.

#### Todo

This is the manual prose:

- 1. Jump to the start of the instruction sequence  $instr^*$  of the expression.
- 2. Execute the instruction sequence.
- 3. Assert: due to validation, the top of the stack contains a value.
- 4. Pop the value val from the stack.

The value val is the result of the evaluation.

```
z; instr^* \hookrightarrow^* z'; val^* \text{ if } z; instr^* \hookrightarrow^* z'; val^*
```

#### Note

Evaluation iterates this reduction rule until reaching a value. Expressions constituting function bodies are executed during function invocation.

# 4.7 Modules

For modules, the execution semantics primarily defines instantiation, which allocates instances for a module and its contained definitions, initializes tables and memories from contained element and data segments, and invokes the start function if present. It also includes invocation of exported functions.

## 4.7.1 Allocation

New instances of functions, tables, memories, globals, tags, element segments, and data segments are *allocated* in a store s, as defined by the following auxiliary functions.

### **Functions**

allocfunc(s, deftype, code, moduleinst)

- 1. Let funcinst be {type deftype, module moduleinst, code code}.
- 2. Let a be the length of s.funcs.
- 3. Append *funcinst* to *s*.funcs.
- 4. Return a.

```
allocfunc(s, deftype, code, moduleinst) = (s \oplus \{funcs funcinst\}, |s.funcs|)
if funcinst = \{type \ deftype, \ module \ moduleinst, \ code \ code\}
```

### **Tables**

```
alloctable(s, at [i ... j] rt, ref)
```

- 1. Let tableinst be {type (at [i ... j] rt), elem  $ref^i$  }.
- 2. Let a be the length of s.tables.
- 3. Append *tableinst* to *s*.tables.
- 4. Return a.

```
 alloctable(s, at [i..j] \ rt, ref) = (s \oplus \{tables \ tableinst\}, |s.tables|)  if  tableinst = \{type \ (at \ [i..j] \ rt), \ elem \ ref^i\}
```

### **Memories**

allocmem(s, at [i ... j] page)

- 1. Let meminst be {type (at [i ... j] page), bytes  $0x00^{i \cdot 64 \text{ Ki}}$  }.
- 2. Let a be the length of s.mems.
- 3. Append meminst to s.mems.
- 4. Return a.

```
\begin{array}{ll} \text{allocmem}(s,at~[i\mathinner{\ldotp\ldotp} j]~\text{page}) &= & (s\oplus \{\text{mems}~meminst\},|s.\text{mems}|)\\ \text{if}~meminst &= \{\text{type}~(at~[i\mathinner{\ldotp\ldotp} j]~\text{page}),~\text{bytes}~(\text{0x00})^{i\cdot 64~\text{Ki}}\} \end{array}
```

## **Tags**

alloctag(s, tagtype)

- 1. Let taginst be  $\{type\ tagtype\}$ .
- 2. Let a be the length of s.tags.
- 3. Append *taginst* to *s*.tags.
- 4. Return a.

```
\begin{array}{ll} \operatorname{alloctag}(s, tagtype) &= (s \oplus \{\operatorname{tags}\ taginst\}, |s.\operatorname{tags}|) \\ \operatorname{if}\ taginst = \{\operatorname{type}\ tagtype\} \end{array}
```

#### **Globals**

allocglobal(s, globaltype, val)

- 1. Let globalinst be {type globaltype, value val }.
- 2. Let a be the length of s.globals.
- 3. Append *globalinst* to *s*.globals.
- 4. Return a.

```
\begin{aligned} \text{allocglobal}(s, \textit{globaltype}, \textit{val}) &= (s \oplus \{\text{globals} \textit{globalinst}\}, |s.\text{globals}|) \\ \text{if } \textit{globalinst} &= \{\text{type } \textit{globaltype}, \text{ value } \textit{val}\} \end{aligned}
```

# **Element segments**

 $allocelem(s, elemtype, ref^*)$ 

- 1. Let eleminst be  $\{\text{type } elemtype, \text{ elem } ref^*\}.$
- 2. Let a be the length of s.elems.
- 3. Append *eleminst* to *s*.elems.
- 4. Return a.

```
allocelem(s, elemtype, ref^*) = (s \oplus \{elems \ eleminst\}, |s.elems|)
if eleminst = \{type \ elemtype, \ elem \ ref^*\}
```

### **Data segments**

 $allocdata(s, ok, byte^*)$ 

- 1. Let datainst be {bytes  $byte^*$ }.
- 2. Let a be the length of s.datas.
- 3. Append *datainst* to *s*.datas.
- 4. Return a.

```
allocdata(s, ok, byte^*) = (s \oplus \{datas \ datainst\}, |s.datas|)

if \ datainst = \{bytes \ byte^*\}
```

## **Growing tables**

growtable(tableinst, n, r)

- 1. Let  $\{\text{type } (at [i ... j] rt), \text{ elem } r'^*\} \text{ be } tableinst.$
- 2. If  $|r'^*| + n > j$ , then:
  - a. Fail.
- 3. Let i' be  $|r'^*| + n$ .
- 4. Let tableinst' be  $\{type\ (at\ [i'\ ..\ j\ ]\ rt),\ elem\ r'^*\ r^n\}.$
- 5. Return tableinst'.

```
growtable(tableinst, n, r) = tableinst' if tableinst = {type (at [i ...j] rt), elem r'^*}

\land tableinst' = {type (at <math>[i' ...j] rt), elem r'^* r^n}

\land i' = |r'^*| + n < j
```

# **Growing memories**

growmem(meminst, n)

- 1. Let  $\{\text{type } (at \ [i \ ... \ j] \ \text{page}), \ \text{bytes } b^*\} \ \text{be } meminst.$
- 2. If  $|b^*|/(64 \text{ Ki}) + n > j$ , then:
  - a. Fail.
- 3. Let i' be  $|b^*|/(64 \text{ Ki}) + n$ .
- 4. Let meminst' be {type (at [i' ... j] page), bytes  $b^*$   $0x00^{n\cdot64 \text{ Ki}}$  }.
- 5. Return meminst'.

## Modules

allocmodule(s, module,  $externaddr^*$ ,  $val_g^*$ ,  $ref_e^*$ )

- 1. Let (module type\* import\* func\* global\* table\* mem\* tag\* elem\* data\* start? export\*) be module.
- 2. Let  $fa_i^*$  be funcs( $externaddr^*$ ).
- 3. Let  $ga_i^*$  be globals( $externaddr^*$ ).
- 4. Let  $aa_i^*$  be tags( $externaddr^*$ ).
- 5. Let  $ma_i^*$  be mems( $externaddr^*$ ).
- 6. Let  $ta_i^*$  be tables  $(externaddr^*)$ .

34. Let  $elemaddr_0^*$  be allocelem\* $(s, elemtype[:= dt^*]^*, ref_e^{**})$ .

35. Assert: Due to validation,  $elemaddr_0^* = ea^*$ .

37. Assert: Due to validation,  $dataaddr_0^* = da^*$ .

36. Let  $dataaddr_0^*$  be allocdata\* $(s, ok^{|data^*|}, byte^{**})$ .

7. Let  $fa^*$  be  $(|s.\text{funcs}| + i_f)^{i_f < |func^*|}$ . 8. Let  $ga^*$  be ( $|s.globals| + i_g$ ) $^{i_g < |global^*|}$ . 9. Let  $ta^*$  be  $(|s.tables| + i_t)^{i_t < |table^*|}$ . 10. Let  $aa^*$  be  $(|s.\text{tags}| + i_a)^{i_a < |tag^*|}$ . 11. Let  $ma^*$  be  $(|s.mems| + i_m)^{i_m < |mem^*|}$ . 12. Let  $ea^*$  be ( $|s.\text{elems}| + i_e$ ) $^{i_e < |elem^*|}$ . 13. Let  $da^*$  be  $(|s.\mathsf{datas}| + i_\mathsf{d})^{i_\mathsf{d} < |data^*|}$ . 14. Let (memory memtype)\* be  $mem^*$ . 15. Let  $dt^*$  be alloctype\* $(type^*)$ . 16. Let  $(tag y)^*$  be  $tag^*$ . 17. Let (data byte\* datamode)\* be data\*. 18. Let (global globaltype  $expr_{\sigma}$ )\* be  $global^*$ . 19. Let (table tabletype  $expr_{t}$ )\* be table\*. 20. Let (elem elemtype  $expr_e^*$  elemmode)\* be  $elem^*$ . 21. Let (func  $x local^* expr_f$ )\* be  $func^*$ . 22. Let  $xi^*$  be allocexport\*({funcs  $fa_i^* fa^*$ , globals  $ga_i^* ga^*$ , tables  $ta_i^* ta^*$ , mems  $ma_i^* ma^*$ , tags  $aa_i^* aa^*$ }, export\*). 23. Let module inst be {types  $dt^*$ , funcs  $fa_i^* fa^*$ , globals  $ga_i^* ga^*$ , tables  $ta_i^* ta^*$ , mems  $ma_i^* ma^*$ , tags  $aa_i^* aa^*$ , elems  $ea^*$ , 24. Let  $funcaddr_0^*$  be allocfunc\* $(s, dt^*[x]^*, (func \ x \ local^* \ expr_f)^*, module inst^{|func^*|})$ . 25. Assert: Due to validation,  $funcaddr_0^* = fa^*$ . 26. Let  $globaladdr_0^*$  be allocglobal\* $(s, globaltype[:= dt^*]^*, val_{\sigma}^*)$ . 27. Assert: Due to validation,  $globaladdr_0^* = ga^*$ . 28. Let  $tableaddr_0^*$  be allocable  $(s, tabletype[:=dt^*]^*, ref_t^*)$ . 29. Assert: Due to validation,  $tableaddr_0^* = ta^*$ . 30. Let  $memaddr_0^*$  be allocmem\* $(s, memtype[:= dt^*]^*)$ . 31. Assert: Due to validation,  $memaddr_0^* = ma^*$ . 32. Let  $tagaddr_0^*$  be alloctag\* $(s, dt^*[y]^*)$ . 33. Assert: Due to validation,  $tagaddr_0^* = aa^*$ .

#### Todo

38. Return moduleinst.

Prose for Allocmodule was being skipped due to indentation error, which is fixed by now. Needs to check if the generated prose seems good.

The allocation function for modules requires a suitable list of external addresses that are assumed to match the import list of the module, a list of initialization values for the module's globals, and list of reference lists for the module's element segments.

- 1. Let module be the module to allocate and  $externaddr^*_{im}$  the list of external addresses providing the module's imports,  $val^*_g$  the initialization values of the module's globals,  $ref^*_t$  the initializer reference of the module's tables, and  $(ref^*_e)^*$  the reference lists of the module's element segments.
- 2. Let deftype\* be the sequence of defined types obtained by allocating the types from module.types.
- 3. For each function  $func_i$  in module.funcs, do:
  - a. Let  $funcaddr_i$  be the function address resulting from allocating  $func_i$  for the module instance module inst defined below.
- 4. For each table  $table_i$  in module.tables, do:
  - a. Let  $limits_i t_i$  be the table type obtained by instantiating  $table_i$  type in module inst defined below.
  - b. Let  $tableaddr_i$  be the table address resulting from allocating  $table_i$  type with initialization value  $ref_t^*[i]$ .
- 5. For each memory  $mem_i$  in module.mems, do:
  - a. Let  $memtype_i$  be the memory type obtained by instantiating  $mem_i$  type in module inst defined below.
  - b. Let  $memaddr_i$  be the memory address resulting from allocating  $memtype_i$ .
- 6. For each global global, in module.globals, do:
  - a. Let  $globaltype_i$  be the global type obtained by instantiating  $global_i$  type in module inst defined below.
  - b. Let  $globaladdr_i$  be the global address resulting from allocating  $globaltype_i$  with initializer value  $val_{\mathfrak{g}}^*[i]$ .
- 7. For each tag  $tag_i$  in module.tags, do:
  - a. Let tagtype be the tag type  $module.types[tag_i.type]$ .
  - b. Let  $tagaddr_i$  be the tag address resulting from allocating tagtype.
- 8. For each element segment  $elem_i$  in module.elems, do:
  - a. Let  $reftype_i$  be the element reference type obtained by instantiating  $elem_i$  type in module inst defined below.
  - b. Let  $elemaddr_i$  be the element address resulting from allocating a element instance of reference type  $reftype_i$  with contents  $(ref_e^*)^*[i]$ .
- 9. For each data segment  $data_i$  in module.datas, do:
  - a. Let  $dataaddr_i$  be the data address resulting from allocating a data instance with contents  $data_i$ .init.
- 10. Let  $deftype^*$  be the concatenation of the defined types  $deftype_i$  in index order.
- 11. Let  $funcaddr^*$  be the concatenation of the function addresses  $funcaddr_i$  in index order.
- 12. Let  $tableaddr^*$  be the concatenation of the table addresses  $tableaddr_i$  in index order.
- 13. Let  $memaddr^*$  be the concatenation of the memory addresses  $memaddr_i$  in index order.
- 14. Let  $globaladdr^*$  be the concatenation of the global addresses  $globaladdr_i$  in index order.
- 15. Let  $tagaddr^*$  be the concatenation of the tag addresses  $tagaddr_i$  in index order.
- 16. Let  $elemaddr^*$  be the concatenation of the element addresses  $elemaddr_i$  in index order.
- 17. Let  $dataaddr^*$  be the concatenation of the data addresses  $dataaddr_i$  in index order.
- 18. Let  $funcaddr_{mod}^*$  be the list of function addresses extracted from  $externaddr_{im}^*$ , concatenated with  $funcaddr^*$ .
- 19. Let  $tableaddr_{mod}^*$  be the list of table addresses extracted from  $externaddr_{im}^*$ , concatenated with  $tableaddr^*$ .
- 20. Let  $memaddr_{mod}^*$  be the list of memory addresses extracted from  $externaddr_{im}^*$ , concatenated with  $memaddr^*$ .
- 21. Let  $globaladdr^*_{mod}$  be the list of global addresses extracted from  $externaddr^*_{im}$ , concatenated with  $globaladdr^*$ .

- 22. Let  $tagaddr_{mod}^*$  be the list of tag addresses extracted from  $externaddr_{im}^*$ , concatenated with  $tagaddr^*$ .
- 23. For each export  $export_i$  in module.exports, do:
  - a. Let exportins  $t_i$  be the export instance resulting from allocating export<sub>i</sub>.
- 24. Let exportinst\* be the concatenation of the export instances exportins $t_i$  in index order.
- 25. Let module inst be the module instance {types  $deftype^*$ , funcs  $funcaddr^*_{mod}$ , tables  $table addr^*_{mod}$ , mems  $memaddr^*_{mod}$ , globals  $global addr^*_{mod}$ , tags  $tagaddr^*_{mod}$ , elems  $elemaddr^*$ , datas  $dataaddr^*$ , exports  $export inst^*$ }.
- 26. Return moduleinst.

```
allocmodule(s, module, externaddr^*, val_{\mathsf{g}}^*, ref_{\mathsf{t}}^*, (ref_{\mathsf{e}}^*)^*) = (s_7, module inst)
              if \ module = module \ type^* \ import^* \ func^* \ global^* \ table^* \ mem^* \ tag^* \ elem^* \ data^* \ start^? \ export^* \ data^* \ start^* \ export^* 
              \wedge func^* = (\text{func } x \ local^* \ expr_f)^*
              \land global^* = (global \ global type \ expr_g)^*
              \wedge table^* = (table \ table type \ expr_t)^*
              \land mem^* = (memory memtype)^*
              \wedge tag^* = (tag y)^*
              \wedge elem^* = (elem \ elem type \ expr_e^* \ elem mode)^*
              \wedge data^* = (data \ byte^* \ datamode)^*
              \wedge fa_{i}^{*} = \text{funcs}(externaddr^{*})
              \wedge ga_{i}^{*} = globals(externaddr^{*})
              \wedge ta_{i}^{*} = tables(externaddr^{*})
              \wedge ma_{i}^{*} = mems(externaddr^{*})
              \wedge aa_{i}^{*} = \operatorname{tags}(\operatorname{externaddr}^{*})
              \wedge \mathit{fa}^* = (|s.\mathsf{funcs}| + i_\mathsf{f})^{i_\mathsf{f} < |\mathit{func}^*|}
             \wedge \; ga^* = (|s.\mathsf{globals}| + i_{\mathsf{g}})^{i_{\mathsf{g}} < |global^*|}
             \wedge \ ta^* = (|s. \mathsf{tables}| + i_{\mathsf{t}})^{\widetilde{i_{\mathsf{t}}} < |table^*|}
              \wedge \ aa^* = (|s.\mathrm{tags}| + i_{\mathrm{a}})^{i_{\mathrm{a}} < |tag^*|}
             \wedge \ ma^* = (|s.\mathsf{mems}| + i_\mathsf{m})^{i_\mathsf{m} < |mem^*|}
              \wedge \ ea^* = (|s.\mathsf{elems}| + i_\mathsf{e})^{i_\mathsf{e} < |elem^*|}
              \wedge \ da^* = (|s.\mathsf{datas}| + i_\mathsf{d})^{i_\mathsf{d} < |\mathit{data}^*|}
              \wedge dt^* = \text{alloctype}^*(type^*)
              \wedge (s_1, fa^*) = \text{allocfunc}^*(s, dt^*[x]^*, (\text{func } x \ local^* \ expr_f)^*, module inst^{|func^*|})
              \wedge (s_2, ga^*) = \text{allocglobal}^*(s_1, globaltype[:= dt^*]^*, val_{\mathfrak{g}}^*)
              \wedge (s_3, ta^*) = \text{alloctable}^*(s_2, tabletype[:= dt^*]^*, ref_{\dagger}^*)
              \wedge (s_4, ma^*) = \text{allocmem}^*(s_3, memtype[:= dt^*]^*)
              \wedge (s_5, aa^*) = \text{alloctag}^*(s_4, dt^*[y]^*)
              \wedge (s_6, ea^*) = \text{allocelem}^*(s_5, elemtype[:= dt^*]^*, (ref_e^*)^*)
              \wedge (s_7, da^*) = \text{allocdata}^*(s_6, \mathsf{ok}^{|data^*|}, (byte^*)^*)
              \wedge xi^* = \text{allocexport}^*(\{\text{funcs } fa_i^* fa^*, \text{ globals } ga_i^* ga^*, \text{ tables } ta_i^* ta^*, \text{ mems } ma_i^* ma^*, \text{ tags } aa_i^* aa^*\}, export^*)
              \land moduleinst = \{ types dt^*, 
                                                                   funcs fa_i^* fa^*, globals ga_i^* ga^*,
                                                                   tables ta_i^* ta^*, mems ma_i^* ma^*,
                                                                   tags aa_i^* aa^*,
                                                                   elems ea^*, datas da^*,
                                                                   exports xi^*
```

Here, the notation allocx\* is shorthand for multiple allocations of object kind X, defined as follows:

```
\begin{array}{lll} {\rm allocX}^*(s,\epsilon,\epsilon) & = & (s,\epsilon) \\ {\rm allocX}^*(s,X\,{X'}^*,Y\,{Y'}^*) & = & (s_2,a\,{a'}^*) & {\rm if}\;(s_1,a) = {\rm allocX}(s,X,Y) \\ & & \wedge (s_2,{a'}^*) = {\rm allocX}^*(s_1,{X'}^*,{Y'}^*) \end{array}
```

For types, however, allocation is defined in terms of rolling and substitution of all preceding types to produce a list of closed defined types:

```
alloctype^*(type''^*)
   1. If type''^* = \epsilon, then:
        a. Return \epsilon.
   2. Let type'* type be type"*.
   3. Let (type rectype) be type.
   4. Let deftype'^* be alloctype(type'^*).
   5. Let x be the length of deftype'^*.
   6. Let deftype^* be roll_x^*(rectype)[:= deftype'^*].
   7. Return deftype'* deftype*.
        alloctype*(\epsilon)
        alloctype^*(type'^*type) = deftype'^* deftype^* \text{ if } deftype'^* = alloctype^*(type'^*)
                                                             \land type = type \ rectype
                                                             \land deftype^* = roll_x^*(rectype)[:= deftype'^*]
                                                             \wedge x = |deftype'^*|
Finally, export instances are produced with the help of the following definition:
allocexport(moduleinst, export name externidx)
   1. If externidx is func, then:
        a. Let (func x) be externidx.
        b. Return {name name, addr (func moduleinst.funcs[x])}.
   2. If externidx is global, then:
        a. Let (global x) be externidx.
        b. Return {name, addr (global moduleinst.globals[x]) }.
   3. If externidx is table, then:
        a. Let (table x) be externidx.
        b. Return {name name, addr (table moduleinst.tables[x])}.
   4. If externidx is memory, then:
        a. Let (memory x) be externidx.
        b. Return {name, addr (mem moduleinst.mems[x]) }.
   5. Assert: externidx is tag.
   6. Let (tag x) be externidx.
   7. Return {name, addr (tag moduleinst.tags[x])}.
allocexport(moduleinst, export name (func x))
                                                       = {name name, addr (func moduleinst.funcs[x])}
allocexport(moduleinst, export name (global x))
                                                       = {name name, addr (global moduleinst.globals[x])}
                                                       = \{\text{name } name, \text{ addr } (\text{table } module inst. \text{tables}[x])\}
allocexport(moduleinst, export name (table x))
allocexport(moduleinst, export\ name\ (memory\ x)) = \{name\ name, addr\ (mem\ moduleinst.mems[x])\}
```

### Note

allocexport(moduleinst, export name (tag x))

The definition of module allocation is mutually recursive with the allocation of its associated functions, because the resulting module instance is passed to the allocators as an argument, in order to form the necessary closures. In an implementation, this recursion is easily unraveled by mutating one or the other in a secondary step.

{name name, addr (tag moduleinst.tags[x])}

# 4.7.2 Instantiation

Given a store s, a module is instantiated with a list of external addresses  $externaddr^*$  supplying the required imports as follows.

Instantiation checks that the module is valid and the provided imports match the declared types, and may *fail* with an error otherwise. Instantiation can also result in an exception or trap when initializing a table or memory from an active segment or when executing the start function. It is up to the embedder to define how such conditions are reported.

```
instantiate(s, module, externaddr^*)
   1. If module is not valid, then:
         a. Fail.
   2. Let xt_i^* \rightarrow xt_e^* be the type of module.
   3. Let (module type* import* func* global* table* mem* tag* elem* data* start? export*) be module.
   4. If |externaddr^*| \neq |xt_i^*|, then:
         a. Fail.
   5. For all externaddr, and xt_i in (externaddr, xt_i)^*:
         a. If externaddr is not valid with type xt_i, then:
   6. Let instr_d^* be the concatenation of rundata_{i_d}(data^*[i_d])^{i_d < |data^*|}.
   7. Let instr_e^* be the concatenation of runelem_{i_e}(elem^*[i_e])^{i_e < |elem^*|}.
   8. Let (start x)? be start?.
   9. Let module inst_0 be {types alloctype*(type^*), funcs funcs(externaddr^*) (|s.funcs| + i_f)i_f < |func^*|, globals globals(externaddr^*)
  10. Let (table table type \ expr_{t})* be table*.
  11. Let (global globaltype expr_{\sigma})* be global*.
  12. Let (elem reftype expr* elemmode)* be elem*.
  13. Let instr_s^? be (call x)^?.
  14. Let z be (s, \{\text{module } module inst_0\}).
  15. Let F be the frame z.frame.
  16. Push the frame F.
  17. Let val_{\mathbf{g}}^* be evalglobal*(z, globaltype^*, expr_{\mathbf{g}}^*).
  18. Pop the frame F from the stack.
```

- 19. Let F be the frame f.
- 20. Push the frame F.
- 21. Let  $ref_t^*$  be the result of evaluating  $expr_t^*$  with state z.
- 22. Pop the frame F from the stack.
- 23. Let F be the frame f.
- 24. Push the frame F.
- 25. Let  $ref_e^{**}$  be the result of evaluating  $expr_e^{**}$  with state z.
- 26. Pop the frame F from the stack.
- 27. Let module inst be allocmodule  $(s, module, externaddr^*, val_{\mathfrak{g}}^*, ref_{\mathfrak{e}}^*, ref_{\mathfrak{e}}^*)$ .
- 28. Let f be {module module inst }.

- 29. Let F be the frame f.
- 30. Push the frame F.
- 31. Execute the sequence  $instr_e^*$ .
- 32. Execute the sequence  $instr_d^*$ .
- 33. If  $instr_s^?$  is defined, then:
  - a. Let  $instr_0$  be  $instr_s^?$ .
  - b. Execute the instruction  $instr_0$ .
- 34. Pop the frame F from the stack.
- 35. Return *f*.module.
- 1. If *module* is not valid, then:
  - a. Fail.
- 2. Assert: module is valid with external types  $externtype_{im}^{m}$  classifying its imports.
- 3. If the number m of imports is not equal to the number n of provided external addresses, then:
  - a. Fail.
- 4. For each external address  $external dr_i$  in  $external dr^n$  and external type  $externtype_i'$  in  $externtype_{im}^n$ , do:
  - a. If  $externaddr_i$  is not valid with an external type  $externtype_i$  in store S, then:
    - i. Fail.
  - b. Let  $externtype_i''$  be the external type obtained by instantiating  $externtype_i'$  in module inst defined below.
  - c. If  $externtype_i$  does not match  $externtype_i''$ , then:
    - i. Fail.
- 6. Let F be the auxiliary frame {module module inst, locals  $\epsilon$ }, that consists of the final module instance module inst, defined below.
- 7. Push the frame F to the stack.
- 8. Let  $val_g^*$  be the list of global initialization values determined by module and  $externaddr^n$ . These may be calculated as follows.
  - a. For each global global; in module.globals, do:
    - i. Let  $val_{gi}$  be the result of evaluating the initializer expression  $global_i$ .init.
  - b. Assert: due to validation, the frame F is now on the top of the stack.
  - c. Let  $val_g^*$  be the concatenation of  $val_{gi}$  in index order.
- 9. Let  $ref_t^*$  be the list of table initialization references determined by module and  $externaldr^n$ . These may be calculated as follows.
  - a. For each table  $table_i$  in module.tables, do:
    - i. Let  $val_{ti}$  be the result of evaluating the initializer expression  $table_i$ .init.
    - ii. Assert: due to validation,  $val_{ti}$  is a reference.
    - iii. Let  $ref_{ti}$  be the reference  $val_{ti}$ .
  - b. Assert: due to validation, the frame F is now on the top of the stack.
  - c. Let  $ref_t^*$  be the concatenation of  $ref_{ti}$  in index order.
- 10. Let  $(ref_e^*)^*$  be the list of reference lists determined by the element segments in *module*. These may be calculated as follows.

- a. For each element segment  $elem_i$  in module.elems, and for each element expression  $expr_{ij}$  in  $elem_i$ .init, do:
  - i. Let  $ref_{ij}$  be the result of evaluating the initializer expression  $expr_{ij}$ .
- b. Let  $ref_i^*$  be the concatenation of function elements  $ref_{ij}$  in order of index j.
- c. Let  $(ref_e^*)^*$  be the concatenation of function element lists  $ref_i^*$  in order of index i.
- 11. Let module inst be a new module instance allocated from module in store S with imports  $externaddr^n$ , global initializer values  $val_{\rm g}^*$ , table initializer values  $ref_{\rm t}^*$ , and element segment contents  $(ref_{\rm e}^*)^*$ , and let S' be the extended store produced by module allocation.
- 12. For each element segment  $elem_i$  in module.elems whose mode is of the form active {table  $tableidx_i$ , offset  $einstr_i^*$  end}, do:
  - a. Let n be the length of the list  $elem_i$ .init.
  - b. Execute the instruction sequence  $einstr_i^*$ .
  - c. Execute the instruction i32.const 0.
  - d. Execute the instruction i32.const n.
  - e. Execute the instruction table.init tableidx<sub>i</sub> i.
  - f. Execute the instruction elem.drop i.
- 13. For each element segment  $elem_i$  in module elems whose mode is of the form declare, do:
  - a. Execute the instruction elem.drop i.
- 14. For each data segment  $data_i$  in module.datas whose mode is of the form active {memory  $memidx_i$ , offset  $dinstr_i^*$  end}, do:
  - a. Let n be the length of the list  $data_i$ .init.
  - b. Execute the instruction sequence  $dinstr_i^*$ .
  - c. Execute the instruction i32.const 0.
  - d. Execute the instruction i32.const n.
  - e. Execute the instruction memory.init i.
  - f. Execute the instruction data.drop i.
- 15. If the start function *module*.start is not empty, then:
  - a. Let start be the start function module.start.
  - b. Execute the instruction call start.func.
- 16. Assert: due to validation, the frame F is now on the top of the stack.
- 17. Pop the frame F from the stack.

```
instantiate(s, module, externaddr^*) = s'; f; instr_e^* instr_d^* instr_s^?
           if \vdash module : xt_{\mathsf{i}}^* \to xt_{\mathsf{e}}^*
           \land (s \vdash externaddr : xt_i)^*
            \land \ module = \mathsf{module} \ type^* \ import^* \ func^* \ global^* \ table^* \ mem^* \ tag^* \ elem^* \ data^* \ start^? \ export^* 
           \land global^* = (global \ global type \ expr_{\sigma})^*
           \wedge \ table^* = (table \ table type \ expr_t)^*
           \land moduleinst_0 = \{ types alloctype^*(type^*), 
                                    funcs funcs(externaddr^*) (|s.funcs| + i_f)<sup>i_f < |func^*|</sup>,
                                   globals(externaddr^*)
           \land z = s; \{ \text{module} \ module inst_0 \}
           \wedge (z', val_{g}^{*}) = \text{evalglobal}^{*}(z, globaltype^{*}, expr_{g}^{*})
           \land (s', module inst) = \text{allocmodule}(s, module, externaddr^*, val_{\sigma}^*, ref_{\tau}^*, (ref_{\sigma}^*)^*)
           \land f = \{ \text{module } module inst \} 
           \wedge \; instr_{\mathsf{e}}^* = \bigoplus \mathrm{runelem}_{i_{\mathsf{e}}} (\mathring{elem}^*[i_{\mathsf{e}}])^{i_{\mathsf{e}} < |\mathscr{elem}^*|}
           where:
evalglobal^*(z, globaltype^*, expr''^*)
    1. If globaltype^* = \epsilon and expr''^* = \epsilon, then:
          a. Return \epsilon.
   2. Assert: |expr''^*| > 1.
   3. Let expr \ expr'^* be expr''^*.
    4. Assert: |globaltype^*| \ge 1.
   5. Let gt \ gt'^* be globaltype^*.
   6. Let (s, f) be z.
   7. Let val be the result of evaluating expr with state z.
   8. Let a be allocated a be allocated as (s, gt, val).
   9. Append a to f.module.globals.
  10. Let val'^* be evalglobal*((s, f), gt'^*, expr'^*).
  11. Return val val'*.
evalglobal*(z, \epsilon, \epsilon)
                                               = (z, \epsilon)
evalglobal^*(z, gt gt'^*, expr expr'^*) = (z', val val'^*)
                                                          if z; expr \hookrightarrow^* z; val
                                                          \wedge z = s; f
                                                          \wedge (s', a) = \text{allocglobal}(s, gt, val)
                                                          \land (z', val'^*) = \text{evalglobal}^*((s'; f[.module.globals} = \oplus a]), gt'^*, expr'^*)
runelem<sub>x</sub>(elem rt e^n elemmode)
    1. If elemmode = passive, then:
           a. Return \epsilon.
   2. If elemmode = declare, then:
           a. Return (elem.drop x).
```

- 3. Assert: elemmode is active.
- 4. Let (active y  $instr^*$ ) be elemmode.
- 5. Return  $instr^*$  (i32.const 0) (i32.const n) (table.init y x) (elem.drop x).

rundata<sub>x</sub>(data  $b^n$  datamode)

- 1. If datamode = passive, then:
  - a. Return  $\epsilon$ .
- 2. Assert: datamode is active.
- 3. Let (active y  $instr^*$ ) be datamode.
- 4. Return  $instr^*$  (i32.const 0) (i32.const n) (memory.init y x) (data.drop x).

```
\begin{array}{lll} \operatorname{runelem}_x(\operatorname{elem}\ rt\ e^n\ (\operatorname{passive})) &=& \epsilon \\ \operatorname{runelem}_x(\operatorname{elem}\ rt\ e^n\ (\operatorname{declare})) &=& (\operatorname{elem.drop}\ x) \\ \operatorname{runelem}_x(\operatorname{elem}\ rt\ e^n\ (\operatorname{active}\ y\ instr^*)) &=& instr^*\ (\operatorname{i32.const}\ 0)\ (\operatorname{i32.const}\ n)\ (\operatorname{table.init}\ y\ x)\ (\operatorname{elem.drop}\ x) \\ \operatorname{rundata}_x(\operatorname{data}\ b^n\ (\operatorname{passive})) &=& \epsilon \\ \operatorname{rundata}_x(\operatorname{data}\ b^n\ (\operatorname{active}\ y\ instr^*)) &=& instr^*\ (\operatorname{i32.const}\ 0)\ (\operatorname{i32.const}\ n)\ (\operatorname{memory.init}\ y\ x)\ (\operatorname{data.drop}\ x) \end{array}
```

#### Note

Checking import types assumes that the module instance has already been allocated to compute the respective closed defined types. However, this forward reference merely is a way to simplify the specification. In practice, implementations will likely allocate or canonicalize types beforehand, when *compiling* a module, in a stage before instantiation and before imports are checked.

Similarly, module allocation and the evaluation of global and table initializers as well as element segments are mutually recursive because the global initialization values  $val_{\rm g}^*$ ,  $ref_{\rm t}$ , and element segment contents  $ref_{\rm e}^{**}$  are passed to the module allocator while depending on the module instance moduleinst and store s' returned by allocation. Again, this recursion is just a specification device. In practice, the initialization values can be determined beforehand by staging module allocation such that first, the module's own function instances are pre-allocated in the store, then the initializer expressions are evaluated in order, allocating globals on the way, then the rest of the module instance is allocated, and finally the new function instances' module fields are set to that module instance. This is possible because validation ensures that initialization expressions cannot actually call a function, only take their reference.

All failure conditions are checked before any observable mutation of the store takes place. Store mutation is not atomic; it happens in individual steps that may be interleaved with other threads.

Evaluation of constant expressions does not affect the store.

## 4.7.3 Invocation

 $invoke(s, funcaddr, val^*)$ 

- 1. Assert: the expansion of s-funcs[funcaddr].type is func.
- 2. Let (func  $functype_0$ ) be the expansion of s.funcs[funcaddr].type.
- 3. Let  $t_1^* \rightarrow t_2^*$  be  $functype_0$ .
- 4. Let *f* be {module {}}.
- 5. If  $|t_1^*| \neq |val^*|$ , then:
  - a. Fail.
- 6. For all  $t_1$ , and val in  $(t_1, val)^*$ :

- a. If val is not valid with type  $t_1$ , then:
  - 1) Fail.
- 7. Let k be the length of  $t_2^*$ .
- 8. Let F be the frame f whose arity is k.
- 9. Push the frame F.
- 10. Push the values  $val^*$  to the stack.
- 11. Push the value (ref.func funcaddr) to the stack.
- 12. Execute the instruction (call\_ref s.funcs[funcaddr].type).
- 13. Pop the values  $val'^k$  from the stack.
- 14. Pop the frame F from the stack.
- 15. Return  $val'^k$ .

Once a module has been instantiated, any exported function can be *invoked* externally via its function address funcaddr in the store s and an appropriate list  $val^*$  of argument values.

Invocation may *fail* with an error if the arguments do not fit the function type. Invocation can also result in an exception or trap. It is up to the embedder to define how such conditions are reported.

#### Note

If the embedder API performs type checks itself, either statically or dynamically, before performing an invocation, then no failure other than traps or exceptions can occur.

The following steps are performed:

- 1. Assert: S.funcs[funcaddr] exists.
- 2. Let funcinst be the function instance S.funcs[funcaddr].
- 3. Let func  $[t_1^n] \to [t_2^m]$  be the composite type expand(funcinst.type).
- 4. If the length  $|val^*|$  of the provided argument values is different from the number n of expected arguments, then:
  - a. Fail.
- 5. For each value type  $t_i$  in  $t_1^n$  and corresponding value  $val_i$  in  $val^*$ , do:
  - a. If  $val_i$  is not valid with value type  $t_i$ , then:
    - i. Fail.
- 6. Let F be the dummy frame {module {}}, locals  $\epsilon$ }.
- 7. Push the frame F to the stack.
- 8. Push the values  $val^*$  to the stack.
- 9. Invoke the function instance at address funcaddr.

Once the function has returned, the following steps are executed:

- 1. Assert: due to validation, m values are on the top of the stack.
- 2. Pop  $val_{res}^m$  from the stack.
- 3. Assert: due to validation, the frame F is now on the top of the stack.
- 4. Pop the frame F from the stack.

The values  $\mathit{val}_{\mathsf{res}}^m$  are returned as the results of the invocation.

```
\begin{array}{ll} \operatorname{invoke}(s, \operatorname{funcaddr}, \operatorname{val}^*) &=& s; f; \operatorname{val}^* \text{ (ref.func } \operatorname{funcaddr}) \text{ (call\_ref } s.\operatorname{funcs}[\operatorname{funcaddr}]. \text{type}) \\ & \text{ if } s.\operatorname{funcs}[\operatorname{funcaddr}]. \text{type} \approx \operatorname{func} \left(t_1^* \to t_2^*\right) \\ & \wedge \left(s \vdash \operatorname{val} : t_1\right)^* \\ & \wedge f = \left\{\operatorname{module}\left\{\right\}\right\} \end{array}
```

**Binary Format** 

## 5.1 Conventions

The binary format for WebAssembly modules is a dense linear *encoding* of their abstract syntax.<sup>28</sup>

The format is defined by an *attribute grammar* whose only terminal symbols are bytes. A byte sequence is a well-formed encoding of a module if and only if it is generated by the grammar.

Each production of this grammar has exactly one synthesized attribute: the abstract syntax that the respective byte sequence encodes. Thus, the attribute grammar implicitly defines a *decoding* function (i.e., a parsing function for the binary format).

Except for a few exceptions, the binary grammar closely mirrors the grammar of the abstract syntax.

#### Note

Some phrases of abstract syntax have multiple possible encodings in the binary format. For example, numbers may be encoded as if they had optional leading zeros. Implementations of decoders must support all possible alternatives; implementations of encoders can pick any allowed encoding.

The recommended extension for files containing WebAssembly modules in binary format is ".wasm" and the recommended Media Type<sup>27</sup> is "application/wasm".

## 5.1.1 Grammar

The following conventions are adopted in defining grammar rules for the binary format. They mirror the conventions used for abstract syntax. In order to distinguish symbols of the binary syntax from symbols of the abstract syntax, typewriter font is adopted for the former.

- Terminal symbols are bytes expressed in hexadecimal notation: 0x0F.
- Nonterminal symbols are written in typewriter font: valtype, instr.
- $B^n$  is a sequence of  $n \ge 0$  iterations of B.
- $B^*$  is a possibly empty sequence of iterations of B. (This is a shorthand for  $B^n$  used where n is not relevant.)

<sup>&</sup>lt;sup>28</sup> Additional encoding layers – for example, introducing compression – may be defined on top of the basic representation defined here. However, such layers are outside the scope of the current specification.

<sup>&</sup>lt;sup>27</sup> https://www.iana.org/assignments/media-types/media-types.xhtml

- $B^{?}$  is an optional occurrence of B. (This is a shorthand for  $B^{n}$  where  $n \leq 1$ .)
- x:B denotes the same language as the nonterminal B, but also binds the variable x to the attribute synthesized for B. A pattern may also be used instead of a variable, e.g., 7:B.
- Productions are written sym ::=  $B_1 \Rightarrow A_1 \mid \ldots \mid B_n \Rightarrow A_n$ , where each  $A_i$  is the attribute that is synthesized for sym in the given case, usually from attribute variables bound in  $B_i$ .
- Some productions are augmented by side conditions in parentheses, which restrict the applicability of the production. They provide a shorthand for a combinatorial expansion of the production into many separate cases.
- If the same meta variable or non-terminal symbol appears multiple times in a production (in the syntax or in an attribute), then all those occurrences must have the same instantiation. (This is a shorthand for a side condition requiring multiple different variables to be equal.)

#### Note

For example, the binary grammar for number types is given as follows:

```
numtype ::= 0x7C \Rightarrow f64

| 0x7D \Rightarrow f32

| 0x7E \Rightarrow i64

| 0x7F \Rightarrow i32
```

Consequently, the byte 0x7F encodes the type i32, 0x7E encodes the type i64, and so forth. No other byte value is allowed as the encoding of a number type.

The binary grammar for limits is defined as follows:

```
limits ::= 0x00 n:u64 \Rightarrow (i32, [n ... 2^{64} - 1]) 

| 0x01 n:u64 m:u64 \Rightarrow (i64, [n ... m]) 

| 0x04 n:u64 \Rightarrow (i32, [n ... 2^{64} - 1]) 

| 0x05 n:u64 m:u64 \Rightarrow (i64, [n ... m])
```

That is, a limits pair is encoded as either the byte 0x00 followed by the encoding of a u32 value, or the byte 0x01 followed by two such encodings. The variables n and m name the attributes of the respective u32 nonterminals, which in this case are the actual unsigned integers those decode into. The attribute of the complete production then is the abstract syntax for the limit, expressed in terms of the former values.

# 5.1.2 Auxiliary Notation

When dealing with binary encodings the following notation is also used:

- $\epsilon$  denotes the empty byte sequence.
- ||B|| is the length of the byte sequence generated from the production B in a derivation.

## 5.1.3 Lists

Lists are encoded with their u32 length followed by the encoding of their element sequence.

$$list(X) ::= n:u32 (el:X)^n \Rightarrow el^n$$

# 5.2 Values

#### **5.2.1 Bytes**

Bytes encode themselves.

byte ::= 
$$b:0x00 \mid \dots \mid b:0xFF \Rightarrow b$$

# 5.2.2 Integers

All integers are encoded using the LEB128<sup>29</sup> variable-length integer encoding, in either unsigned or signed variant.

Unsigned integers are encoded in unsigned LEB128<sup>30</sup> format. As an additional constraint, the total number of bytes encoding a uN value must not exceed ceil(N/7) bytes.

Signed integers are encoded in signed LEB128<sup>31</sup> format, which uses a two's complement representation. As an additional constraint, the total number of bytes encoding an sN value must not exceed ceil(N/7) bytes.

$$\begin{array}{lll} \mathrm{s} N & ::= & n \mathrm{:byte} & \Rightarrow & n & \text{if } n < 2^6 \wedge n < 2^{N-1} \\ & \mid & n \mathrm{:byte} & \Rightarrow & n - 2^7 & \text{if } 2^6 \leq n < 2^7 \wedge n \geq 2^7 - 2^{N-1} \\ & \mid & n \mathrm{:byte} \ i \mathrm{:u}(N-7) & \Rightarrow & 2^7 \cdot i + (n-2^7) & \text{if } n \geq 2^7 \wedge N > 7 \end{array}$$

Uninterpreted integers are encoded as signed integers.

$$iN ::= i:sN \Rightarrow signed_N^{-1}(i)$$

#### Note

The side conditions N>7 in the productions for non-terminal bytes of the uN and sN encodings restrict the encoding's length. However, "trailing zeros" are still allowed within these bounds. For example, 0x03 and 0x83 0x00 are both well-formed encodings for the value 3 as a us. Similarly, either of 0x7E and 0xFE 0x7F and 0xFE 0x7F are well-formed encodings of the value -2 as an s16.

The side conditions on the value n of terminal bytes further enforce that any unused bits in these bytes must be 0 for positive values and 1 for negative ones. For example, 0x83 0x10 is malformed as a us encoding. Similarly, both 0x83 0x3E and 0xFF 0x7B are malformed as ss encodings.

## 5.2.3 Floating-Point

Floating-point values are encoded directly by their IEEE 754<sup>32</sup> (Section 3.4) bit pattern in little endian<sup>33</sup> byte order:

$$fN ::= b^*: byte^{N/8} \Rightarrow bytes_{fN}^{-1}(b^*)$$

### **5.2.4 Names**

Names are encoded as a list of bytes containing the Unicode<sup>34</sup> (Section 3.9) UTF-8 encoding of the name's character sequence.

name ::= 
$$b^*$$
:list(byte)  $\Rightarrow$  name if utfs(name) =  $b^*$ 

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<sup>&</sup>lt;sup>29</sup> https://en.wikipedia.org/wiki/LEB128

 $<sup>^{30}\</sup> https://en.wikipedia.org/wiki/LEB128#Unsigned\_LEB128$ 

<sup>31</sup> https://en.wikipedia.org/wiki/LEB128#Signed\_LEB128

<sup>32</sup> https://ieeexplore.ieee.org/document/8766229

<sup>33</sup> https://en.wikipedia.org/wiki/Endianness#Little-endian

<sup>34</sup> https://www.unicode.org/versions/latest/

The auxiliary utf8 function expressing this encoding is defined as follows:

```
\begin{array}{lll} \mathrm{utfs}(ch^*) & = & \bigoplus \mathrm{utfs}(ch)^* \\ \mathrm{utfs}(ch) & = & b & \mathrm{if} \ ch < \mathrm{U} + 80 \\ & & \wedge ch = b \\ \mathrm{utfs}(ch) & = & b_1 \ b_2 & \mathrm{if} \ \mathrm{U} + 80 \leq ch < \mathrm{U} + 0800 \\ & & \wedge ch = 2^6 \cdot (b_1 - \mathrm{0xC0}) + \mathrm{cont}(b_2) \\ \mathrm{utfs}(ch) & = & b_1 \ b_2 \ b_3 & \mathrm{if} \ \mathrm{U} + 0800 \leq ch < \mathrm{U} + \mathrm{D}800 \vee \mathrm{U} + \mathrm{E}000 \leq ch < \mathrm{U} + 10000 \\ & & \wedge ch = 2^{12} \cdot (b_1 - \mathrm{0xE0}) + 2^6 \cdot \mathrm{cont}(b_2) + \mathrm{cont}(b_3) \\ \mathrm{utfs}(ch) & = & b_1 \ b_2 \ b_3 \ b_4 & \mathrm{if} \ \mathrm{U} + 10000 \leq ch < \mathrm{U} + 11000 \\ & & \wedge ch = 2^{18} \cdot (b_1 - \mathrm{0xF0}) + 2^{12} \cdot \mathrm{cont}(b_2) + 2^6 \cdot \mathrm{cont}(b_3) + \mathrm{cont}(b_4) \end{array}
```

where cont(b) = b - 0x80 if (0x80 < b < 0xC0)

#### Note

Unlike in some other formats, name strings are not 0-terminated.

# 5.3 Types

#### Note

In some places, possible types include both type constructors or types denoted by type indices. Thus, the binary format for type constructors corresponds to the encodings of small negative sN values, such that they can unambiguously occur in the same place as (positive) type indices.

# 5.3.1 Number Types

Number types are encoded by a single byte.

```
numtype ::= 0x7C \Rightarrow f64

| 0x7D \Rightarrow f32

| 0x7E \Rightarrow i64

| 0x7F \Rightarrow i32
```

## 5.3.2 Vector Types

Vector types are also encoded by a single byte.

```
vectype ::= 0x7B \Rightarrow v_{128}
```

# 5.3.3 Heap Types

Heap types are encoded as either a single byte, or as a type index encoded as a positive signed integer.

```
absheaptype ::=
                       0x69
                                                   exn
                        0x6A
                                             \Rightarrow
                                                   array
                       0x6B
                                             \Rightarrow
                                                   struct
                       0x6C
                                             \Rightarrow
                                                  i31
                       0x6D
                                             \Rightarrow
                                                   eq
                       0x6E
                                                  any
                       0x6F
                                             \Rightarrow extern
                       0x70
                                             \Rightarrow func
                       0x71
                                             \Rightarrow
                                                  none
                       0x72
                                                   noextern
                       0x73
                                                   nofunc
                                             \Rightarrow
                                             ⇒ noexn
                       0x74
                       ht:absheaptype \Rightarrow ht
   heaptype
                       x:s33
                                                               if x \ge 0
                                                   x
```

#### Note

The heap type bot cannot occur in a module.

# 5.3.4 Reference Types

Reference types are either encoded by a single byte followed by a heap type, or, as a short form, directly as an abstract heap type.

## 5.3.5 Value Types

Value types are encoded with their respective encoding as a number type, vector type, or reference type.

#### Note

The value type bot cannot occur in a module.

Value types can occur in contexts where type indices are also allowed, such as in the case of block types. Thus, the binary format for types corresponds to the signed LEB128 $^{35}$  encoding of small negative sN values, so that they can coexist with (positive) type indices in the future.

# 5.3.6 Result Types

Result types are encoded by the respective lists of value types.

```
resulttype ::= t^*:list(valtype) \Rightarrow t^*
```

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<sup>35</sup> https://en.wikipedia.org/wiki/LEB128#Signed\_LEB128

# 5.3.7 Composite Types

Composite types are encoded by a distinct byte followed by a type encoding of the respective form.

```
mut ::= 0x00
                 0x01
                                                             \Rightarrow mut
   \verb|comptype| ::= \verb|Ox5E| yt: \verb|fieldtype|
                                                             \Rightarrow array yt
                 | \text{ 0x5F } yt^*: \text{list(fieldtype)} |
                                                             \Rightarrow struct yt^*
                  0x60 t_1^*:resulttype t_2^*:resulttype \Rightarrow func (t_1^* 	o t_2^*)
  fieldtype := zt:storagetype mut?:mut
                                                             \Rightarrow mut? zt
storagetype ::= t:valtype
                                                                  t
                pt:packtype
                                                             \Rightarrow
                                                                  pt
   packtype ::= 0x77
                                                                 i16
               0x78
```

# 5.3.8 Recursive Types

Recursive types are encoded by the byte 0x4E followed by a list of sub types. Additional shorthands are recognized for unary recursions and sub types without super types.

### **5.3.9 Limits**

Limits are encoded with a preceding flag indicating whether a maximum is present, and a flag for the address type.

```
limits ::= 0x00 n:u64 \Rightarrow (i32, [n .. 2^{64} - 1])

| 0x01 n:u64 m:u64 \Rightarrow (i64, [n .. m])

| 0x04 n:u64 \Rightarrow (i32, [n .. 2^{64} - 1])

| 0x05 n:u64 m:u64 \Rightarrow (i64, [n .. m])
```

## 5.3.10 Memory Types

Memory types are encoded with their limits.

```
memtype ::= (at, lim):limits \Rightarrow at lim page
```

## 5.3.11 Table Types

Table types are encoded with their limits and the encoding of their element reference type.

```
tabletype ::= rt:reftype (at, lim):limits \Rightarrow at lim rt
```

## 5.3.12 Global Types

Global types are encoded by their value type and a flag for their mutability.

```
globaltype ::= t:valtype mut<sup>?</sup>:mut \Rightarrow mut<sup>?</sup> t
```

# 5.3.13 Tag Types

Tag types are encoded by a type index denoting a function type.

```
tagtype ::= 0x00 x:typeidx \Rightarrow x
```

#### Note

In future versions of WebAssembly, the preceding zero byte may encode additional flags.

# 5.3.14 External Types

External types are encoded by a distiguishing byte followed by an encoding of the respective form of type.

# 5.4 Instructions

Instructions are encoded by *opcodes*. Each opcode is represented by a single byte, and is followed by the instruction's immediate arguments, where present. The only exception are structured control instructions, which consist of several opcodes bracketing their nested instruction sequences.

### Note

Gaps in the byte code ranges for encoding instructions are reserved for future extensions.

## 5.4.1 Control Instructions

Control instructions have varying encodings. For structured instructions, the instruction sequences forming nested blocks are delimited with explicit opcodes for end and else.

Block types are encoded in special compressed form, by either the byte 0x40 indicating the empty type, as a single value type, or as a type index encoded as a positive signed integer.

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```
blocktype ::=
                     0x40
                                                                                             \epsilon
                                                                                             t
                     t:valtype
                                                                                        \Rightarrow
                                                                                                                          if i \geq 0
                     i:s33
                                                                                        \Rightarrow
                                                                                             i
     instr ::= 0x00
                                                                                             unreachable
                     0x01
                                                                                        \Rightarrow
                                                                                             nop
                     0x02 bt:blocktype (in:instr)^* 0x0B
                                                                                             block bt in*
                                                                                        \Rightarrow
                     0x03 bt:blocktype (in:instr)^* 0x0B
                                                                                        \Rightarrow
                                                                                             loop bt in^*
                     0x04 bt:blocktype (in:instr)^* 0x0B
                                                                                             if bt in^* else \epsilon
                    0x04 bt:blocktype (in_1:instr)^*
                                                                                              if bt in_1^* else in_2^*
                     0x05 (in_2:instr)^* 0x0B
                                                                                        \Rightarrow
                     0x08 x:tagidx
                                                                                             throw x
                     0x0A
                                                                                             throw ref
                                                                                        \Rightarrow
                                                                                             \mathsf{br}\ l
                     0x0C l:labelidx
                                                                                        \Rightarrow
                     0x0D l:labelidx
                                                                                             br_if l
                                                                                        \Rightarrow
                    0x0E l^*:list(labelidx) l_n:labelidx
                                                                                        \Rightarrow
                                                                                             br table l^* l_n
                     0x0F
                                                                                        \Rightarrow
                                                                                             return
                    0x10 x:funcidx
                                                                                             call x
                                                                                        \Rightarrow
                    0x11 y:typeidx x:tableidx
                                                                                        \Rightarrow call_indirect x y
                    0x12 x:funcidx
                                                                                        \Rightarrow return call x
                     0x13 y:typeidx x:tableidx
                                                                                        \Rightarrow
                                                                                             return_call_indirect x y
                     0x1F bt:blocktype c^*:list(catch) (in:instr)^* 0x0B \Rightarrow
                                                                                             try_table bt c^* in^*
     catch ::= 0x00 x:tagidx l:labelidx
                                                                                        \Rightarrow catch x l
                   0x01 x: tagidx l: labelidx
                                                                                        \Rightarrow catch_ref x l
                     0x02 l:labelidx
                                                                                             catch_all \it l
                     0x03 l:labelidx
                                                                                        \Rightarrow catch all ref l
```

## Note

The else opcode 0x05 in the encoding of an if instruction can be omitted if the following instruction sequence is empty.

Unlike any other occurrence, the type index in a block type is encoded as a positive signed integer, so that its signed LEB128 bit pattern cannot collide with the encoding of value types or the special code 0x40, which correspond to the LEB128 encoding of negative integers. To avoid any loss in the range of allowed indices, it is treated as a 33 bit signed integer.

#### 5.4.2 Reference Instructions

Generic reference instructions are represented by single byte codes, others use prefixes and type operands.

```
instr ::= ...
                  | 0xD0 ht:heaptype
                                                                                       \Rightarrow ref.null ht
                                                                                       ⇒ ref.is null
                     0xD1
                     0xD2 x:funcidx
                                                                                             \mathsf{ref}.\mathsf{func}\ x
                     0xD3
                                                                                       \Rightarrow ref.eq
                      0xD4
                                                                                       ⇒ ref.as_non_null
                     0xD5 l:labelidx
                                                                                      \Rightarrow br_on_null l
                      0xD6 l:labelidx
                                                                                      \Rightarrow br_on_non_null l
                    OXDOt.:labelitax\Rightarrow struct.new xOXFB0:u32x:typeidx\Rightarrow struct.new_default xOXFB2:u32x:typeidxi:u32\Rightarrow struct.get x iOXFB3:u32x:typeidxi:u32\Rightarrow struct.get_s x iOXFB4:u32x:typeidxi:u32\Rightarrow struct.set x iOXFB5:u32x:typeidx\Rightarrow array.new xOXFB6:u32x:typeidx\Rightarrow array.new_default xOXFB7:u32x:typeidx\Rightarrow array.new_fixed x nOXFB9:u32x:typeidx\Rightarrow array.new_data x yOXFB10:u32x:typeidx\Rightarrow array.new_elem x yOXFB11:u32x:typeidx\Rightarrow array.new_elem x y
                      OxFB 12:u32 x:typeidx
                                                                                      \Rightarrow array.get_s x
                      0xFB 13:u32 x:typeidx
                                                                                     \Rightarrow array.get_u x
                      0xFB 14:u32 x:typeidx
                                                                                     \Rightarrow array.set x
                      0xFB 15:u32
                                                                                     ⇒ array.len
                      0xFB 16:u32 x:typeidx
                                                                                      \Rightarrow array.fill x
                      OxFB 17:u32 x_1:typeidx x_2:typeidx
                                                                                      \Rightarrow array.copy x_1 x_2
                                                                                     \Rightarrow array.init_data x y
                      OxFB 18:u32 x:typeidx y:dataidx OxFB 19:u32 x:typeidx y:elemidx
                                                                                      \Rightarrow array.init_elem x y
                      OxFB 20:u32 ht:heaptype
                                                                                      \Rightarrow ref.test (ref ht)
                      OxFB 21:u32 ht:heaptype
                                                                                     \Rightarrow ref.test (ref null ht)
                     0xFB 22:u32 ht:heaptype

0xFB 23:u32 ht:heaptype

0xFB 24:u32 (null<sub>1</sub>, null<sub>2</sub>):castop
                                                                                    \Rightarrow ref.cast (ref ht)
                                                                                    \Rightarrow ref.cast (ref null ht)
                      l:labelidx ht_1:heaptype ht_2:heaptype \Rightarrow br_on_cast l (ref null\frac{?}{l} ht_1) (ref null\frac{?}{l} ht_2)
                      0xFB 25:u32 (null_1^2, null_2^2):castop
                      l:labelidx ht_1:heaptype ht_2:heaptype \Rightarrow br_on_cast_fail l (ref null ht_1) (ref null ht_2) ht_2)
                      0xFB 26:u32
                                                                                       \Rightarrow any.convert_extern
                      0xFB 27:u32
                                                                                       ⇒ extern.convert_any
                      0xFB 28:u32
                                                                                       ⇒ ref.i31
                      0xFB 29:u32
                                                                                       ⇒ i31.get_s
                      0xFB 30:u32
                                                                                       ⇒ i31.get_u
castop := 0x00
                                                                                       \Rightarrow (\epsilon, \epsilon)
                      0x01
                                                                                       \Rightarrow (null, \epsilon)
                      0x02
                                                                                               (\epsilon, \mathsf{null})
                      0x03
                                                                                               (null, null)
```

### 5.4.3 Parametric Instructions

Parametric instructions are represented by single byte codes, possibly followed by a type annotation.

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## 5.4.4 Variable Instructions

Variable instructions are represented by byte codes followed by the encoding of the respective index.

### 5.4.5 Table Instructions

Table instructions are represented either by a single byte or a one byte prefix followed by a variable-length unsigned integer.

```
instr ::= ...
                                                                    \Rightarrow table.get x
                0x25 x:tableidx
                0x26 x:tableidx
                                                                   \Rightarrow table.set x
                \texttt{OxFC} \ 12{:}\texttt{u32} \ y{:}\texttt{elemidx} \ x{:}\texttt{tableidx} \qquad \Rightarrow \quad \mathsf{table}.\mathsf{init} \ x \ y
               0xFC 13:u32 x:elemidx
                                                                 \Rightarrow elem.drop x
             0xFC 14:u32 x_1:tableidx x_2:tableidx \Rightarrow table.copy x_1 x_2
                \texttt{OxFC}\ 15: \texttt{u32}\ x: \texttt{tableidx}
                                                                          table.grow x
                                                                   \Rightarrow
                OxFC 16:u32 x:tableidx
                                                                 \Rightarrow
                                                                          table.size x
                0xFC 17:u32 x:tableidx
                                                                  \Rightarrow table.fill x
```

# 5.4.6 Memory Instructions

Each variant of memory instruction is encoded with a different byte code. Loads and stores are followed by the encoding of their *memarg* immediate, which includes the memory index if bit 6 of the flags field containing alignment is set; the memory index defaults to 0 otherwise.

```
(0, \{align n, offset m\})
                                                                                                if n < 2^6
memarg ::= n:u32 m:u32
                                                              (x, \{align (n-2^6), offset m\}) if 2^6 \le n < 2^7
           n:u32 x:memidx m:u32
 instr ::=
               0x28 (x, ao):memarg
                                                        \Rightarrow i32.load x ao
               0x29 (x, ao):memarg
                                                       \Rightarrow i64.load x ao
                                                       \Rightarrow f32.load x ao
                0x2A (x, ao):memarg
                0x2B(x,ao):memarg
                                                        \Rightarrow f64.load x ao
                0x2C(x, ao):memarg
                                                        \Rightarrow
                                                             i32.load8_s x ao
                0x2D(x,ao):memarg
                                                       \Rightarrow i32.load8_u x ao
                0x2E(x,ao):memarg
                                                      \Rightarrow i32.load16_s x ao
                0x2F(x,ao):memarg
                                                      \Rightarrow i32.load16_u x ao
                0x30 (x, ao):memarg
                                                      \Rightarrow i64.load8_s x ao
                0x31 (x, ao):memarg
                                                      \Rightarrow i64.load8_u x ao
                0x32 (x, ao):memarg
                                                      \Rightarrow i64.load16_s x ao
                0x33 (x, ao):memarg
                                                       \Rightarrow
                                                             i64.load16 ux ao
                0x34 (x, ao):memarg
                                                       \Rightarrow i64.load32 s x ao
                                                      \Rightarrow i64.load32_u x \ ao
                0x35 (x, ao):memarg
                0x36 (x, ao):memarg
                                                      \Rightarrow i32.store x ao
                0x37 (x, ao):memarg
                                                      \Rightarrow i64.store x ao
                0x38 (x, ao):memarg
                                                       \Rightarrow f32.store x ao
                0x39 (x, ao):memarg
                                                        \Rightarrow f64.store x ao
                Ox3A (x,ao):memarg
                                                             i32.store8 x ao
                0x3B(x,ao):memarg
                                                              i32.store16 x\ ao
                0x3C(x,ao):memarg
                                                        \Rightarrow i64.store8 x ao
                0x3D(x,ao):memarg
                                                       \Rightarrow i64.store16 x ao
                0x3E(x,ao):memarg
                                                      \Rightarrow i64.store32 x ao
                0x3F x:memidx
                                                      \Rightarrow memory.size x
                0x40 x:memidx
                                                       \Rightarrow memory.grow x
                \texttt{OxFC} \ 8: \texttt{u32} \ y: \texttt{dataidx} \ x: \texttt{memidx} \Rightarrow \texttt{memory.init} \ x \ y
                0xFC 9:u32 x:dataidx
                                                        \Rightarrow data.drop x
                0xFC \ 10:u32 \ x_1:memidx \ x_2:memidx \Rightarrow memory.copy \ x_1 \ x_2
                0xFC 11:u32 x:memidx
                                                      \Rightarrow memory.fill x
```

# 5.4.7 Numeric Instructions

All variants of numeric instructions are represented by separate byte codes.

The const instructions are followed by the respective literal.

All other numeric instructions are plain opcodes without any immediates.

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```
instr ::=
                 0x45 \Rightarrow
                                i32.eqz
                  0x46 \Rightarrow
                                i32.eq
                  0x47 \Rightarrow
                                i32.ne
                  0x48 \Rightarrow i32.lt_s
                  0x49 \Rightarrow i32.lt_u
                  0x4A \Rightarrow i32.gt_s
                  0x4B \Rightarrow i32.gt_u
                  0x4C \Rightarrow i32.le_s
                  0x4D \Rightarrow i32.le_u
                  0x4E \Rightarrow
                                i32.ge_s
                  0x4F \Rightarrow
                                 i32.ge_u
                  0x50 \Rightarrow
                                 i64.eqz
                  0x51 \Rightarrow
                                i64.eq
                  0x52 \Rightarrow
                                i64.ne
                  0x53 \Rightarrow
                                i64.lt_s
                  0x54 \Rightarrow
                                i64.lt_u
                  0x55 \Rightarrow i64.gt_s
                  0x56 \Rightarrow i64.gt_u
                  0x57 \Rightarrow
                                i64.le s
                 0x58 \Rightarrow
                                i64.le_u
                  0x59 \Rightarrow i64.ge_s
                  0x5A \Rightarrow i64.ge\_u
                  . . .
 instr ::=
                   0x5B \Rightarrow
                                   f32.eq
                   0x5C \Rightarrow
                                   f32.ne
                   0x5D \Rightarrow
                                   f32.lt
                   0x5E \Rightarrow
                                   f32.gt
                   0x5F \Rightarrow f_{32}.le
                   0x60 \Rightarrow f32.ge
                   0x61 \Rightarrow f_{64.eq}
                   0x62 \Rightarrow f_{64.ne}
                   0x63 \Rightarrow f64.lt
                                   f64.gt
                   0x64 \Rightarrow
                   0x65 \Rightarrow
                                   f64.le
                   0x66 \Rightarrow f64.ge
```

```
instr ::=
                                   i32.clz
                  0x67 \Rightarrow
                  0x68 \Rightarrow
                                   i32.ctz
                  0x69
                            \Rightarrow
                                   i32.popcnt
                  0x6A \Rightarrow
                                   i32.add
                  0x6B \Rightarrow
                                   i32.sub
                  0x6C \Rightarrow
                                   i32.mul
                  0x6D \Rightarrow
                                   i32.div_s
                  0x6E \Rightarrow
                                   i32.div_u
                  0x6F
                           \Rightarrow
                                   i32.rem_s
                                   i32.rem_u
                  0x70
                           \Rightarrow
                   0x71
                            \Rightarrow
                                    i32.and
                  0x72 \Rightarrow
                                    i32.or
                  0x73 \Rightarrow
                                   i32.xor
                  0x74 \Rightarrow
                                   i32.shl
                  0x75 \Rightarrow
                                   i32.shr_s
                  0x76 \Rightarrow
                                   i32.shr_u
                  0x77
                                   i32.rotl
                            \Rightarrow
                                   i32.rotr
                  0x78 \Rightarrow
                   0x79
                                   i64.clz
                  0x7A
                                   i64.ctz
                  0x7B \Rightarrow
                                   i64.popcnt
                  0x7C \Rightarrow
                                   i64.add
                  0x7D \Rightarrow
                                   i64.sub
                                   i64.mul
                  0x7E
                           \Rightarrow
                                   i64.div_s
                  0x7F
                            \Rightarrow
                                   i64.div_u
                   08x0
                            \Rightarrow
                   0x81
                            \Rightarrow
                                   i64.rem_s
                  0x82
                                   i64.rem_u
                           \Rightarrow
                  0x83
                                   i64.and
                   0x84
                                   i64.or
                   0x85
                                   i64.xor
                           \Rightarrow
                   0x86
                                   i64.shl
                           \Rightarrow
                   0x87
                                   i64.shr_s
                            \Rightarrow
                   88x0
                           \Rightarrow
                                    i64.shr_u
                   0x89
                           \Rightarrow
                                   i64.rotl
                   \Rightarrow A8x0
                                   i64.rotr
```

instr ::=

```
f32.abs
                      0x8B \Rightarrow
                      0x8C \Rightarrow
                                       f32.neg
                      0x8D
                                       f32.ceil
                              \Rightarrow
                      0x8E \Rightarrow
                                       f32.floor
                      0x8F
                               \Rightarrow
                                       f32.trunc
                      0x90 \Rightarrow
                                       f32.nearest
                      0x91 \Rightarrow
                                       f32.sqrt
                      0x92 \Rightarrow
                                       f32.add
                                      f32.sub
                      0x93 \Rightarrow
                      0x94 \Rightarrow
                                      f32.mul
                      0x95
                               \Rightarrow
                                      f<sub>32</sub>.div
                                       f32.min
                      0x96
                               \Rightarrow
                      0x97
                               \Rightarrow
                                       f32.max
                                       f32.copysign
                      0x98
                               \Rightarrow
                      0x99
                               \Rightarrow
                                       f64.abs
                      0x9A
                                       f64.neg
                      0x9B
                                       f64.ceil
                                      f64.floor
                      0x9C
                              \Rightarrow
                      0x9D
                                      f64.trunc
                              \Rightarrow
                      0x9E \Rightarrow
                                       f64.nearest
                      0x9F
                                       f64.sqrt
                      0xA0 \Rightarrow
                                       f64.add
                      0xA1 \Rightarrow
                                       f64.sub
                      0xA2 \Rightarrow
                                       f64.mul
                      0xA3 \Rightarrow
                                       f64.div
                      0xA4 \Rightarrow
                                       f64.min
                      0xA5 \Rightarrow
                                       f64.max
                      0xA6 \Rightarrow
                                       f64.copysign
                      . . .
instr ::=
                  0xA7 \Rightarrow
                                   i32.wrap_i64
                  0xA8 \Rightarrow
                                   i32.trunc_s_f32
                  0xA9 \Rightarrow
                                   i32.trunc_u_f32
                                   i32.trunc_s_f64
                  0xAA \Rightarrow
                  0xAB \Rightarrow
                                   i32.trunc u f64
                                   i64.extend_s_i32
                  0xAC \Rightarrow
                  0xAD \Rightarrow
                                   i64.extend_u_i32
                  0xAE \Rightarrow
                                   i64.trunc_s_f32
                  OxAF
                                   i64.trunc u f32
                          \Rightarrow
                  0xB0
                                   i64.trunc_s_f64
                          \Rightarrow
                  0xB1
                           \Rightarrow
                                   i64.trunc_u_f64
                  0xB2
                            \Rightarrow
                                   f32.convert_s_i32
                  0xB3
                                   f32.convert_u_i32
                  0xB4 \Rightarrow
                                   f32.convert_s_i64
                                   f32.convert_u_i64
                  0xB5 \Rightarrow
                  0xB6
                           \Rightarrow
                                   f32.demote_f64
                                   f64.convert_s_i32
                  0xB7
                            \Rightarrow
                                   f64.convert_u_i32
                  0xB8
                           \Rightarrow
                                   f_{64}.convert\_s\_i_{64}
                  0xB9
                            \Rightarrow
                  OxBA
                            \Rightarrow
                                   f64.convert_u_i64
                  0xBB
                            \Rightarrow
                                   f32.promote_f64
                  0xBC
                           \Rightarrow
                                   i32.reinterpret_f32
                  0xBD
                           \Rightarrow
                                   i64.reinterpret_f64
                  0xBE
                                   f32.reinterpret_i32
                  0xBF
                           \Rightarrow
                                   f64.reinterpret_i64
```

The saturating truncation instructions all have a one byte prefix, whereas the actual opcode is encoded by a variable-length unsigned integer.

#### 5.4.8 Vector Instructions

All variants of vector instructions are represented by separate byte codes. They all have a one byte prefix, whereas the actual opcode is encoded by a variable-length unsigned integer.

Vector loads and stores are followed by the encoding of their memarg immediate.

```
l
laneidx := l:byte
                                                                                    \Rightarrow
   instr ::=
                                                                     v128.load8x8_s x ao

v128.load8x8_s x ao

v128.load16x4_s x ao

v128.load16x4_s x ao

v128.load32x2_s x ao

v128.load32x2_u x ao

v128.load32x2_u x ao

v128.load8_splat x ao

v128.load8_splat x ao

v128.load16
                       0xFD 0:u32 (x, ao):memarg
                       OxFD 1:u32 (x, ao):memarg
                       OxFD 2:u32 (x, ao):memarg
                       OxFD 3:u32 (x, ao):memarg
                      0xFD 4:u32 (x, ao):memarg
0xFD 5:u32 (x, ao):memarg
0xFD 6:u32 (x, ao):memarg
0xFD 7:u32 (x, ao):memarg
                       0xFD 8:u32 (x, ao):memarg
                       OxFD 9:u32 (x, ao):memarg
                       \begin{array}{lll} \texttt{OxFD} & 10 \text{:u32} & (x,ao) \text{:memarg} & \Rightarrow & \texttt{v128.load64\_splat} \; x \; ao \\ \texttt{OxFD} & 11 \text{:u32} & (x,ao) \text{:memarg} & \Rightarrow & \texttt{v128.store} \; x \; ao \\ \end{array}
                       OxFD 84:u32 (x, ao):memarg l:laneidx \Rightarrow v128.load8_lane x \ ao \ l
                       OxFD 85:u32 (x, ao):memarg l:laneidx \Rightarrow v128.load16_lane x \ ao \ l
                       OxFD 86:u32 (x, ao):memarg l:laneidx \Rightarrow v128.load32_lane x \ ao \ l
                       OxFD 87:u32 (x,ao):memarg l:laneidx \Rightarrow v128.load64_lane x\ ao\ l
                       OxFD 88:u32 (x, ao):memarg l:laneidx \Rightarrow v128.store8_lane x \ ao \ l
                       OxFD 89:u32 (x, ao):memarg l:laneidx \Rightarrow v128.store16_lane x \ ao \ l
                       0xFD 90:u32 (x, ao):memarg l:laneidx \Rightarrow v128.store32_lane x ao l
                       \texttt{OxFD} 91:u32 (x, ao):memarg l:laneidx \Rightarrow v128.store64_lane x ao l
                       0xFD 92:u32 (x, ao):memarg \Rightarrow v128.load32_zero x ao
                       OxFD 93:u32 (x, ao):memarg
                                                                         \Rightarrow v<sub>128</sub>.load<sub>64</sub>_zero x ao
```

The const instruction for vectors is followed by 16 immediate bytes, which are converted into an u128 in

littleendian byte order:

The shuffle instruction is also followed by the encoding of 16 *laneidx* immediates.

Lane instructions are followed by the encoding of a *laneidx* immediate.

All other vector instructions are plain opcodes without any immediates.

```
instr ::=
               0xFD 35:u32
                                        i8x16.eq
                0xFD 36:u32
                                         i8x16.ne
               0xFD 37:u32
                                         i8x16.lt_s
                0xFD 38:u32
                                 \Rightarrow
                                         i8×16.lt u
                0xFD 39:u32
                                        i8x16.gt_s
                                \Rightarrow
                0xFD 40:u32 \Rightarrow
                                        i8x16.gt_u
                0xFD 41:u32 \Rightarrow
                                       i8x16.le_s
                0xFD 42:u32 \Rightarrow
                                       i8x16.le u
                0xFD 43:u32
                                  \Rightarrow
                                       i8X16.ge_s
                0xFD 44:u32
                                         i8x16.ge_u
                                  \Rightarrow
                0xFD 45:u32
                                   \Rightarrow
                                         i16x8.eq
                0xFD 46:u32
                                  \Rightarrow
                                         i16x8.ne
                0xFD 47:u32
                                  \Rightarrow
                                        i16x8.lt_s
               0xFD 48:u32
                                       i16x8.lt_u
                0xFD 49:u32
                                       i16x8.gt_s
                0xFD 50:u32
                                       i16x8.gt_u
                0xFD 51:u32
                                       i16x8.le_s
                                  \Rightarrow
                0xFD 52:u32
                                        i16x8.le u
                                  \Rightarrow
                0xFD 53:u32
                                        i16x8.ge s
               0xFD 54:u32 \Rightarrow
                                       i16x8.ge_u
               0xFD 55:u32 \Rightarrow
                                       i32x4.eq
               0xFD 56:u32 \Rightarrow
                                       i32x4.ne
                0xFD 57:u32 \Rightarrow
                                       i32x4.lt s
               0xFD 58:u32
                                       i32x4.lt_u
                                  \Rightarrow
                0xFD 59:u32
                                  \Rightarrow
                                        i32x4.gt_s
                0xFD 60:u32
                                  \Rightarrow
                                        i32x4.gt_u
                0xFD 61:u32
                                        i32x4.le_s
                                  \Rightarrow
                0xFD 62:u32
                                        i32x4.le_u
                                  \Rightarrow
                0xFD 63:u32
                                       i32x4.ge_s
                0xFD 64:u32
                                       i32x4.ge_u
                0xFD 214:u32 \Rightarrow
                                       i64x2.eq
                0xFD 215:u32 \Rightarrow
                                        i64x2.ne
                0xFD 216:u32
                                  \Rightarrow
                                         i64x2.lt_s
                0xFD 217:u32 \Rightarrow
                                         i64x2.gt_s
                0xFD 218:u32 \Rightarrow
                                         i64x2.le_s
                0xFD 219:u32 \Rightarrow
                                       i64x2.ge_s
  instr ::= ...
                  0xFD 65:u32 \Rightarrow
                                         f32x4.eq
                  0xFD 66:u32 \Rightarrow
                                         f32x4.ne
                  0xFD 67:u32 \Rightarrow f_{32\times4.lt}
                  0xFD 68:u32 \Rightarrow
                                         f32x4.gt
                  0xFD 69:u32 \Rightarrow
                                         f32x4.le
                  0xFD 70:u32 \Rightarrow
                                        f32x4.ge
                 0xFD 71:u32 \Rightarrow f64\times 2.eq
                 0xFD 72:u32 \Rightarrow f64x2.ne
                  0xFD 73:u32 \Rightarrow
                                       f64x2.lt
                  0xFD 74:u32 \Rightarrow
                                       f64x2.gt
                  0xFD 75:u32 \Rightarrow
                                         f64x2.le
                  0xFD 76:u32 \Rightarrow f_{64x2.ge}
```

```
instr ::= ...
                0xFD 77:u32 \Rightarrow v_{128.not}
                   0xFD 78:u32 \Rightarrow v_{128.and}
                   0xFD 79:u32 \Rightarrow v128.andnot
                   0xFD 80:u32 \Rightarrow v_{128.or}
                 0xFD 81:u32 \Rightarrow v128.xor
                 0xFD 82:u32 \Rightarrow v_{128}.bitselect
                   0xFD 83:u32 \Rightarrow v128.any\_true
instr ::= ...
               0xFD 96:u32 \Rightarrow
                                        i8x16.abs
               0xFD 97:u32 \Rightarrow
                                        i8x16.neg
               0xFD 98:u32 \Rightarrow
                                        i8x16.popcnt
               0xFD 99:u32 \Rightarrow
                                        i8x16.all_true
               0xFD 100:u32 \Rightarrow i8x16.bitmask
               0xFD 101:u32 \Rightarrow
                                        i8x16.narrow_i16x8_s
               0xFD 102:u32 \Rightarrow
                                        i8x16.narrow_i16x8_u
               0xFD 107:u32 \Rightarrow i8x16.shl
               0xFD 108:u32 \Rightarrow
                                        i8x16.shr_s
               0xFD 109:u32 \Rightarrow
                                        i8x16.shr_u
               0xFD 110:u32 \Rightarrow
                                        i8x16.add
               0xFD 111:u32 \Rightarrow
                                        i8x16.add_sat_s
               0xFD 112:u32 \Rightarrow i8x16.add_sat_u
               0xFD 113:u32 \Rightarrow
                                        i8x16.sub
               0xFD 114:u32 \Rightarrow
                                        i8x16.sub_sat_s
               0xFD 115:u32 \Rightarrow
                                        i8×16.sub_sat_u
               0xFD 118:u32 \Rightarrow
                                        i8x16.min_s
               0xFD 119:u32 \Rightarrow
                                        i8x16.min_u
               0xFD 120:u32 \Rightarrow
                                        i8x16.max s
               0xFD 121:u32 \Rightarrow i8x16.max_u
               \texttt{0xFD} \ 123: \texttt{u32} \ \Rightarrow \ \mathsf{i8x16.avgr\_u}
               . . .
```

```
instr ::=
               0xFD 124:u32 \Rightarrow
                                        i16x8.extadd_pairwise_s_i8x16
               0xFD 125:u32 \Rightarrow
                                        i16x8.extadd_pairwise_u_i8x16
               0xFD 128:u32 \Rightarrow
                                        i16x8.abs
               0xFD 129:u32 \Rightarrow
                                        i16x8.neg
               0xFD 131:u32 \Rightarrow
                                        i16x8.all_true
               0xFD 132:u32 \Rightarrow
                                        i16x8.bitmask
               0xFD 133:u32 \Rightarrow
                                        i16x8.narrow_i32x4_s
               0xFD 134:u32 \Rightarrow
                                        i16x8.narrow_i32x4_u
               0xFD 135:u32 \Rightarrow
                                        i16x8.(extend_s)_i8x16_low
               0xFD 136:u32 \Rightarrow
                                        i16x8.(extend_s)_i8x16_high
               0xFD 137:u32 \Rightarrow
                                        i16x8.(extend_u)_i8x16_low
               0xFD 138:u32 \Rightarrow
                                        i16x8.(extend_u)_i8x16_high
               0xFD 139:u32 \Rightarrow
                                        i16x8.shl
               0xFD 140:u32 \Rightarrow
                                        i16x8.shr_s
               0xFD 141:u32 \Rightarrow
                                        i16x8.shr_u
               0xFD 130:u32 \Rightarrow
                                        i16x8.q15mulr_sat_s
               0xFD 273:u32 \Rightarrow
                                        i16x8.relaxed_q15mulr_s
               0xFD 142:u32 \Rightarrow
                                        i16x8.add
               0xFD 143:u32 \Rightarrow
                                        i16x8.add_sat_s
               0xFD 144:u32 \Rightarrow
                                        i16x8.add sat u
               0xFD 145:u32 \Rightarrow
                                        i16x8.sub
               0xFD 146:u32 \Rightarrow
                                        i16x8.sub sat s
               0xFD 147:u32 \Rightarrow
                                        i16x8.sub_sat_u
               0xFD 149:u32 \Rightarrow
                                        i16x8.mul
               0xFD 150:u32 \Rightarrow
                                        i16x8.min s
               0xFD 151:u32 \Rightarrow
                                        i16x8.min_u
               0xFD 152:u32 \Rightarrow
                                        i16x8.max_s
               0xFD 153:u32 \Rightarrow
                                        i16x8.max_u
               0xFD 155:u32 \Rightarrow
                                        i16x8.avgr_u
               0xFD 156:u32 \Rightarrow
                                        i16x8.extmul_s_low_i8x16
               0xFD 157:u32 \Rightarrow
                                        i16x8.extmul_s_high_i8x16
               0xFD 158:u32 \Rightarrow
                                        i16x8.extmul_u_low_i8x16
               0xFD 159:u32 \Rightarrow
                                        i16x8.extmul_u_high_i8x16
               0xFD 274:u32 \Rightarrow i16x8.relaxed_dot_s_i8x16
```

```
instr ::= ...
                                         i32x4.extadd_pairwise_s_i16x8
               0xFD 126:u32 \Rightarrow
                0xFD 127:u32 \Rightarrow
                                         i32x4.extadd_pairwise_u_i16x8
                0xFD 160:u32 \Rightarrow
                                       i32x4.abs
                0xFD 161:u32 \Rightarrow
                                         i32x4.neg
                0xFD 163:u32 \Rightarrow
                                         i32x4.all_true
                0xFD 164:u32 \Rightarrow i32x4.bitmask
                0xFD 167:u32 \Rightarrow i32x4.(extend_s)_i16x8_low
                \texttt{0xFD} \ 168: \texttt{u32} \ \Rightarrow \ \mathsf{i32x4.} (\mathsf{extend\_s}) \_ \mathsf{i16x8\_high}
                0xFD 169:u32 \Rightarrow i32x4.(extend_u)_i16x8_low
                0xFD 170:u32 \Rightarrow i32x4.(extend_u)_i16x8_high
                0xFD 171:u32 \Rightarrow i32x4.shl
                0xFD 172:u32 \Rightarrow
                                         i32x4.shr_s
                0xFD 173:u32 \Rightarrow
                                         i32x4.shr_u
                0xFD 174:u32 \Rightarrow
                                         i32x4.add
                0xFD 177:u32 \Rightarrow i32x4.sub
                0xFD 181:u32 \Rightarrow i32x4.mul
                0xFD 182:u32 \Rightarrow i32x4.min_s
                0xFD 183:u32 \Rightarrow i32x4.min_u
                0xFD 184:u32 \Rightarrow i32x4.max_s
                0xFD 185:u32 \Rightarrow i32x4.max u
                0xFD 186:u32 \Rightarrow i32x4.dot_s_i16x8
                0xFD 188:u32 \Rightarrow i32x4.extmul_s_low_i16x8
                0xFD 189:u32 \Rightarrow i32x4.extmul_s_high_i16x8
                0xFD 190:u32 \Rightarrow i32x4.extmul_u_low_i16x8
                0xFD 191:u32 \Rightarrow i32x4.extmul u high i16x8
                0xFD 275:u32 \Rightarrow i32x4.relaxed_dot_add_s_i16x8
 instr ::=
                 0xFD 192:u32 \Rightarrow
                                          i64x2.abs
                 0xFD 193:u32 \Rightarrow
                                          i64x2.neg
                 0xFD 195:u32 \Rightarrow
                                          i64x2.all true
                 0xFD 196:u32 \Rightarrow
                                          i64x2.bitmask
                 0xFD 199:u32 \Rightarrow
                                          i64x2.(extend_s)_i32x4_low
                 0xFD 200:u32 \Rightarrow
                                          i64x2.(extend_s)_i32x4_high
                 \texttt{0xFD} \ 201{:}\texttt{u32} \ \Rightarrow
                                          i64x2.(extend_u)_i32x4_low
                 0xFD 202:u32 \Rightarrow
                                          i64x2.(extend_u)_i32x4_high
                 0xFD 203:u32 \Rightarrow
                                          i64x2.shl
                 0xFD 204:u32 \Rightarrow
                                          i64x2.shr_s
                 0xFD 205:u32 \Rightarrow
                                          i64x2.shr u
                 0xFD 206:u32 \Rightarrow
                                          i64x2.add
                 0xFD 209:u32 \Rightarrow
                                          i64x2.sub
                 0xFD 213:u32 \Rightarrow
                                          i64x2.mul
                 0xFD 220:u32 \Rightarrow
                                          i64x2.extmul_s_low_i32x4
                 0xFD 221:u32 \Rightarrow i64x2.extmul_s_high_i32x4
                 0xFD 222:u32 \Rightarrow
                                          i64x2.extmul u low i32x4
                 0xFD 223:u32 \Rightarrow
                                          i64x2.extmul u high i32x4
```

```
instr ::=
                 0xFD 103:u32 \Rightarrow
                                           f32x4.ceil
                                            f32x4.floor
                 0xFD 104:u32 \Rightarrow
                 0xFD 105:u32 \Rightarrow
                                            f32x4.trunc
                 0xFD 106:u32 \Rightarrow
                                            f32x4.nearest
                 0xFD 224:u32 \Rightarrow
                                            f32x4.abs
                 \texttt{0xFD} \ 225{:}\texttt{u32} \ \Rightarrow
                                            f32x4.neg
                 0xFD 227:u32 \Rightarrow
                                            f32x4.sqrt
                 0xFD 228:u32 \Rightarrow
                                            f32x4.add
                 0xFD 229:u32 \Rightarrow
                                            f32x4.sub
                 0xFD 230:u32 \Rightarrow
                                            f32x4.mul
                 0xFD 231:u32 \Rightarrow
                                            f32x4.div
                 0xFD 232:u32 \Rightarrow
                                            f32x4.min
                 0xFD 233:u32 \Rightarrow
                                            f32x4.max
                 0xFD 234:u32 \Rightarrow f_{32x4.pmin}
                 0xFD 235:u32 \Rightarrow f32x4.pmax
                 0xFD 269:u32 \Rightarrow
                                            f32x4.relaxed_min
                 0xFD 270:u32 \Rightarrow
                                            f32x4.relaxed_max
                 0xFD 261:u32 \Rightarrow
                                            f32x4.relaxed madd
                                            f32x4.relaxed nmadd
                 0xFD 262:u32 \Rightarrow
instr ::=
                 0xFD 116:u32 \Rightarrow
                                            f64x2.ceil
                 0xFD 117:u32 \Rightarrow
                                            f64x2.floor
                 0xFD 122:u32 \Rightarrow
                                            f64x2.trunc
                 0xFD 148:u32 \Rightarrow
                                            f64x2.nearest
                 0xFD 236:u32 \Rightarrow
                                            f64x2.abs
                 0xFD 237:u32 \Rightarrow
                                            f64x2.neg
                 0xFD 239:u32 \Rightarrow
                                            f64x2.sqrt
                 0xFD 240:u32 \Rightarrow
                                            f64x2.add
                 0xFD 241:u32 \Rightarrow
                                            f<sub>64</sub>x<sub>2</sub>.sub
                 0xFD 242:u32 \Rightarrow
                                          f64x2.mul
                 0xFD 243:u32 \Rightarrow
                                         f64x2.div
                 0xFD 244:u32 \Rightarrow f_{64\times 2.min}
                 0xFD 245:u32 \Rightarrow
                                            f64x2.max
                 0xFD 246:u32 \Rightarrow
                                            f<sub>64</sub>x<sub>2</sub>.pmin
                 0xFD 247:u32 \Rightarrow
                                          f<sub>64</sub>x<sub>2</sub>.pmax
                 0xFD 271:u32 \Rightarrow f64x2.relaxed_min
                 0xFD 272:u32 \Rightarrow f64x2.relaxed_max
                 0xFD 263:u32 \Rightarrow f_{64\times 2}.relaxed madd
                 0xFD 264:u32 \Rightarrow f_{64\times 2}.relaxed nmadd
```

```
instr ::=
                                       f32x4.demote f64x2 zero
              0xFD 94:u32 \Rightarrow
               0xFD 95:u32 \Rightarrow
                                     f64x2.promote f32x4 low
               0xFD 248:u32 \Rightarrow i32x4.(trunc_sat_s)_f32x4
                                       i32x4.(trunc_sat_u)_f32x4
               0xFD 249:u32 \Rightarrow
               0xFD 250:u32 \Rightarrow
                                       f32x4.(convert_s)_i32x4
               0xFD 251:u32 \Rightarrow
                                       f32x4.(convert u) i32x4
               0xFD 252:u32 \Rightarrow
                                       i32x4.(trunc_sat_s)_f64x2_zero
               0xFD 253:u32 \Rightarrow
                                       i32x4.(trunc_sat_u)_f64x2_zero
                                       f64x2.(convert_s)_i32x4_low
               0xFD 254:u32 \Rightarrow
               0xFD 255:u32 \Rightarrow
                                       f64x2.(convert_u)_i32x4_low
               0xFD 257:u32 \Rightarrow
                                       i32x4.(relaxed_trunc_s)_f32x4
               0xFD 258:u32 \Rightarrow
                                       i32x4.(relaxed_trunc_u)_f32x4
               0xFD 259:u32 \Rightarrow
                                       i32x4.(relaxed_trunc_s)_f64x2_zero
               0xFD 260:u32 \Rightarrow
                                       i32x4.(relaxed_trunc_u)_f64x2_zero
               0xFD 256:u32 \Rightarrow
                                       i16x8.relaxed_swizzle
               0xFD 257:u32 \Rightarrow
                                       i32x4.relaxed_trunc_f32x4_s
               0xFD 258:u32 \Rightarrow i32x4.relaxed\_trunc_f32x4_u
               0xFD 259:u32 \Rightarrow i32x4.relaxed\_trunc_f32x4\_s\_zero
               0xFD 260:u32 \Rightarrow i32x4.relaxed\_trunc_f32x4\_u\_zero
               0xFD 261:u32 \Rightarrow f32x4.relaxed_madd
               0xFD 262:u32 \Rightarrow f32x4.relaxed nmadd
               0xFD 263:u32 \Rightarrow f64x2.relaxed madd
               0xFD 264:u32 \Rightarrow f_{64x2.relaxed} nmadd
               0xFD 265:u32 \Rightarrow i8x16.relaxed laneselect
               0xFD 266:u32 \Rightarrow i16x8.relaxed laneselect
               0xFD 267:u32 \Rightarrow i32x4.relaxed laneselect
               0xFD 268:u32 \Rightarrow i64x2.relaxed laneselect
               0xFD 269:u32 \Rightarrow f32x4.relaxed min
               0xFD 270:u32 \Rightarrow f32x4.relaxed_max
               0xFD 271:u32 \Rightarrow f_{64x2.relaxed\_min}
               0xFD 272:u32 \Rightarrow f_{64x2.relaxed} max
               0xFD 273:u32 \Rightarrow i_{16x8.relaxed_q15mulr_s}
               0xFD 274:u32 \Rightarrow i_{16x8.relaxed\_dot_i8x16_i7x16\_s}
               0xFD 275:u32 \Rightarrow i16x8.relaxed_dot_i8x16_i7x16_add_s
```

# 5.4.9 Expressions

Expressions are encoded by their instruction sequence terminated with an explicit 0x0B opcode for end.

```
expr ::= (in:instr)^* OxOB \Rightarrow in^*
```

# 5.5 Modules

The binary encoding of modules is organized into *sections*. Most sections correspond to one component of a module record, except that function definitions are split into two sections, separating their type declarations in the function section from their bodies in the code section.

# Note

This separation enables *parallel* and *streaming* compilation of the functions in a module.

### 5.5.1 Indices

All basic indices are encoded with their respective value.

```
typeidx := x:u32
                                   x
  funcidx ::= x:u32 \Rightarrow
                                   x
 tableidx ::= x:u32 \Rightarrow
                                   x
   memidx ::= x:u32 \Rightarrow
                                   x
globalidx ::= x:u32 \Rightarrow
                                   x
   tagidx ::= x:u32 \Rightarrow
  elemidx ::= x:u32
  \texttt{dataidx} \ ::= \ x : \texttt{u32} \ \Rightarrow
                                   x
 localidx ::= x:u32 \Rightarrow
                                   x
labelidx ::= l:u32 \Rightarrow
                                   l
```

External indices are encoded by a distiguishing byte followed by an encoding of their respective value.

### 5.5.2 Sections

Each section consists of

- a one-byte section id,
- the use length of the contents, in bytes,
- the actual *contents*, whose structure is dependent on the section id.

Every section is optional; an omitted section is equivalent to the section being present with empty contents.

The following parameterized grammar rule defines the generic structure of a section with id N and contents described by the grammar X.

For most sections, the contents X encodes a list. In these cases, the empty result  $\epsilon$  is interpreted as the empty list.

### Note

Other than for unknown custom sections, the size is not required for decoding, but can be used to skip sections when navigating through a binary. The module is malformed if the size does not match the length of the binary contents X.

The following section ids are used:

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ld	Section
0	custom section
1	type section
2	import section
3	function section
4	table section
5	memory section
6	global section
7	export section
8	start section
9	element section
10	code section
11	data section
12	data count section
13	tag section

#### Note

Section ids do not always correspond to the order of sections in the encoding of a module.

### 5.5.3 Custom Section

Custom sections have the id 0. They are intended to be used for debugging information or third-party extensions, and are ignored by the WebAssembly semantics. Their contents consist of a name further identifying the custom section, followed by an uninterpreted sequence of bytes for custom use.

```
\begin{array}{rcl} \text{customsec} & ::= & \text{section}_0(\text{custom}) \\ & \text{custom} & ::= & \text{name byte}^* \end{array}
```

### Note

If an implementation interprets the data of a custom section, then errors in that data, or the placement of the section, must not invalidate the module.

# 5.5.4 Type Section

The *type section* has the id 1. It decodes into the list of recursive types of a module.

```
\begin{array}{rcl} \texttt{typesec} & ::= & ty^* : \texttt{section}_1(\texttt{list}(\texttt{type})) & \Rightarrow & ty^* \\ & \texttt{type} & ::= & qt : \texttt{rectype} & \Rightarrow & \texttt{type} \ qt \end{array}
```

# 5.5.5 Import Section

The *import section* has the id 2. It decodes into the list of imports of a module.

```
importsec ::= im^*:section<sub>2</sub>(list(import)) \Rightarrow im^*
import ::= nm_1:name nm_2:name xt:externtype \Rightarrow import nm_1 nm_2 xt
```

### 5.5.6 Function Section

The *function section* has the id 3. It decodes into a list of type indices that classify the functions defined by a module. The bodies of the respective functions are encoded separately in the code section.

```
funcsec ::= x^*:section<sub>3</sub>(list(typeidx)) \Rightarrow x^*
```

#### 5.5.7 Table Section

The table section has the id 4. It decodes into the list of tables defined by a module.

#### Note

The encoding of a table type cannot start with byte 0x40, hence decoding is unambiguous. The zero byte following it is reserved for future extensions.

# 5.5.8 Memory Section

The *memory section* has the id 5. It decodes into the list of memories defined by a module.

```
memsec ::= mem^*:section<sub>5</sub>(list(mem)) \Rightarrow mem^* mem ::= mt:memtype \Rightarrow memory mt
```

#### 5.5.9 Global Section

The *global section* has the id 6. It decodes into the list of globals defined by a module.

```
\begin{array}{lll} {\tt globalsec} & ::= & glob^* : {\tt section_6(list(global))} & \Rightarrow & glob^* \\ {\tt global} & ::= & gt : {\tt globaltype} & e : {\tt expr} & \Rightarrow & {\tt global} & gt & e \end{array}
```

### 5.5.10 Export Section

The *export section* has the id 7. It decodes into the list of exports of a module.

```
exportsec ::= ex^*:section<sub>7</sub>(list(export)) \Rightarrow ex^*
export ::= nm:name xx:externidx \Rightarrow export nm xx
```

### 5.5.11 Start Section

The start section has the id 8. It decodes into the optional start function of a module.

```
startsec ::= start^?:section_8(start) \Rightarrow start^?

start ::= x:funcidx \Rightarrow (start x)
```

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#### 5.5.12 Element Section

The *element section* has the id 9. It decodes into the list of element segments defined by a module.

```
elem^*
                 elem*:sectiong(list(elem))
 elemsec ::=
elemkind ::= 0x00
                                                                                       ref null func
                                                                                  \Rightarrow
     elem ::= 0:u32 e_o:expr y^*:list(funcidx)
                                                                                  \Rightarrow
                  elem (ref func) (ref.func y)* (active 0 e_o)
               1:u32 rt:elemkind y^*:list(funcidx)
                                                                                  \Rightarrow
                   elem rt (ref.func y)* passive
                 2:u32 x:tableidx e:expr rt:elemkind y^*:list(funcidx)
                   elem rt (ref.func y)* (active x e)
                 3:u32 rt:elemkind y^*:list(funcidx)
                   elem rt (ref.func y)* declare
                 4:u32 e_0:expr e^*:list(expr)
                                                                                  \Rightarrow
                   elem (ref null func) e^* (active 0 e_0)
                 5:u32 rt:reftype e^*:list(expr)
                   elem rt\ e^* passive
                 6:u32 x:tableidx e_0:expr e^*:list(expr)
                   elem (ref null func) e^* (active x e_0)
                 7:u32 rt:reftype e^*:list(expr)
                   elem rt e^* declare
```

#### Note

The initial integer can be interpreted as a bitfield. Bit 0 distinguishes a passive or declarative segment from an active segment, bit 1 indicates the presence of an explicit table index for an active segment and otherwise distinguishes passive from declarative segments, bit 2 indicates the use of element type and element expressions instead of element kind and element indices.

Additional element kinds may be added in future versions of WebAssembly.

### 5.5.13 Code Section

The *code section* has the id 10. It decodes into the list of *code* entries that are pairs of lists of locals and expressions. They represent the body of the functions defined by a module. The types of the respective functions are encoded separately in the function section.

The encoding of each code entry consists of

- the u32 length of the function code in bytes,
- the actual function code, which in turn consists of
  - the declaration of *locals*,
  - the function body as an expression.

Local declarations are compressed into a list whose entries consist of

- a *u32 count*,
- a value type,

denoting count locals of the same value type.

Here, code ranges over pairs ( $local^*$ , expr). Any code for which the length of the resulting sequence is out of bounds of the maximum size of a list is malformed.

#### Note

Like with sections, the code *size* is not needed for decoding, but can be used to skip functions when navigating through a binary. The module is malformed if a size does not match the length of the respective function code.

#### 5.5.14 Data Section

The data section has the id 11. It decodes into the list of data segments defined by a module.

#### Note

The initial integer can be interpreted as a bitfield. Bit 0 indicates a passive segment, bit 1 indicates the presence of an explicit memory index for an active segment.

### 5.5.15 Data Count Section

The data count section has the id 12. It decodes into an optional use count that represents the number of data segments in the data section. If this count does not match the length of the data segment list, the module is malformed.

```
datacntsec ::= n^?:section<sub>12</sub>(datacnt) \Rightarrow n^?
datacnt ::= n:u32 \Rightarrow n
```

#### Note

The data count section is used to simplify single-pass validation. Since the data section occurs after the code section, the memory init and data drop instructions would not be able to check whether the data segment index is valid until the data section is read. The data count section occurs before the code section, so a single-pass validator can use this count instead of deferring validation.

# 5.5.16 Tag Section

The *tag section* has the id 13. It decodes into the list of tags defined by a module.

```
tagsec ::= tag^*:section<sub>13</sub>(list(tag)) \Rightarrow tag^*
tag ::= x:typeidx \Rightarrow tag x
```

### **5.5.17 Modules**

The encoding of a module starts with a preamble containing a 4-byte magic number (the string '\Oasm') and a version field. The current version of the WebAssembly binary format is 1.

The preamble is followed by a sequence of sections. Custom sections may be inserted at any place in this sequence, while other sections must occur at most once and in the prescribed order. All sections can be empty.

The lengths of lists produced by the (possibly empty) function and code section must match up.

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Similarly, the optional data count must match the length of the data segment list. Furthermore, it must be present if any data index occurs in the code section.

```
magic ::= 0x00 0x61 0x73 0x6D
version ::= 0x01 0x00 0x00 0x00
 module ::= magic version
                customsec* type*:typesec
                customsec* import*:importsec
                 customsec^* typeidx^*:funcsec
                 customsec^* table^*:tablesec
                 \verb"customsec" mem": \verb"memsec"
                 {\tt customsec^*}\ tag^*{\tt :tagsec}
                 customsec^* global^*:globalsec
                 customsec^* export^*:exportsec
                 customsec* start?:startsec
                 customsec* elem*:elemsec
                 {\tt customsec^*}\ n^?{\tt :datacntsec}
                 customsec^* (local^*, expr)^*:codesec
                 customsec* data*:datasec
                 customsec*
                  module type* import* func* global* table* mem* tag* elem* data* start? export*
                       if (n = |data^*|)?
                       \wedge (n^? \neq \epsilon \vee \text{dataidx}(func^*) = \epsilon)
                       \land (func = func \ typeidx \ local^* \ expr)^*
```

#### Note

The version of the WebAssembly binary format may increase in the future if backward-incompatible changes have to be made to the format. However, such changes are expected to occur very infrequently, if ever. The binary format is intended to be forward-compatible, such that future extensions can be made without incrementing its version.

**Text Format** 

# 6.1 Conventions

The textual format for WebAssembly modules is a rendering of their abstract syntax into S-expressions<sup>36</sup>.

Like the binary format, the text format is defined by an *attribute grammar*. A text string is a well-formed description of a module if and only if it is generated by the grammar. Each production of this grammar has at most one synthesized attribute: the abstract syntax that the respective character sequence expresses. Thus, the attribute grammar implicitly defines a *parsing* function. Some productions also take a context as an inherited attribute that records bound identifiers.

Except for a few exceptions, the core of the text grammar closely mirrors the grammar of the abstract syntax. However, it also defines a number of *abbreviations* that are "syntactic sugar" over the core syntax.

The recommended extension for files containing WebAssembly modules in text format is ".wat". Files with this extension are assumed to be encoded in UTF-8, as per Unicode<sup>37</sup> (Section 2.5).

### 6.1.1 Grammar

The following conventions are adopted in defining grammar rules of the text format. They mirror the conventions used for abstract syntax and for the binary format. In order to distinguish symbols of the textual syntax from symbols of the abstract syntax, typewriter font is adopted for the former.

- Terminal symbols are either literal strings of characters enclosed in quotes or expressed as Unicode<sup>38</sup> scalar values: 'module', U+0A. (All characters written literally are unambiguously drawn from the 7-bit ASCII<sup>39</sup> subset of Unicode.)
- Nonterminal symbols are written in typewriter font: valtype, instr.
- $T^n$  is a sequence of n > 0 iterations of T.
- $T^*$  is a possibly empty sequence of iterations of T. (This is a shorthand for  $T^n$  used where n is not relevant.)
- $T^+$  is a sequence of one or more iterations of T. (This is a shorthand for  $T^n$  where  $n \ge 1$ .)
- $T^{?}$  is an optional occurrence of T. (This is a shorthand for  $T^{n}$  where  $n \leq 1$ .)

<sup>&</sup>lt;sup>36</sup> https://en.wikipedia.org/wiki/S-expression

<sup>37</sup> https://www.unicode.org/versions/latest/

<sup>38</sup> https://www.unicode.org/versions/latest/

<sup>&</sup>lt;sup>39</sup> https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

- x:T denotes the same language as the nonterminal T, but also binds the variable x to the attribute synthesized for T. A pattern may also be used instead of a variable, e.g., (x,y):T.
- Productions are written sym ::=  $T_1 \Rightarrow A_1 \mid \ldots \mid T_n \Rightarrow A_n$ , where each  $A_i$  is the attribute that is synthesized for sym in the given case, usually from attribute variables bound in  $T_i$ .
- Some productions are augmented by side conditions in parentheses, which restrict the applicability of the production. They provide a shorthand for a combinatorial expansion of the production into many separate cases.
- If the same meta variable or non-terminal symbol appears multiple times in a production (in the syntax or in an attribute), then all those occurrences must have the same instantiation.
- A distinction is made between *lexical* and *syntactic* productions. For the latter, arbitrary white space is allowed in any place where the grammar contains spaces. The productions defining lexical syntax and the syntax of values are considered lexical, all others are syntactic.

#### Note

For example, the textual grammar for number types is given as follows:

```
numtype ::= 'i32' \Rightarrow i32 | 'i64' \Rightarrow i64 | 'f32' \Rightarrow f32 | 'f64' \Rightarrow f64
```

The textual grammar for limits is defined as follows:

```
\begin{array}{cccc} \text{limits} & ::= & n: \text{u32} & \Rightarrow & \{\min n, \max \epsilon\} \\ & & | & n: \text{u32} & m: \text{u32} & \Rightarrow & \{\min n, \max m\} \end{array}
```

The variables n and m name the attributes of the respective u32 nonterminals, which in this case are the actual unsigned integers those parse into. The attribute of the complete production then is the abstract syntax for the limit, expressed in terms of the former values.

### 6.1.2 Abbreviations

In addition to the core grammar, which corresponds directly to the abstract syntax, the textual syntax also defines a number of *abbreviations* that can be used for convenience and readability.

Abbreviations are defined by rewrite rules specifying their expansion into the core syntax:

```
abbreviation\ syntax \equiv expanded\ syntax
```

These expansions are assumed to be applied, recursively and in order of appearance, before applying the core grammar rules to construct the abstract syntax.

### 6.1.3 Contexts

The text format allows the use of symbolic identifiers in place of indices. To resolve these identifiers into concrete indices, some grammar productions are indexed by an *identifier context* I as a synthesized attribute that records the declared identifiers in each index space. In addition, the context records the types defined in the module, so that parameter indices can be computed for functions.

It is convenient to define identifier contexts as records I with abstract syntax as follows:

```
(name?)*.
{ types
            (name?)*.
 funcs
            (name?)*,
 tables
            (name?)*
 mems
 globals
            (name?)*
            (name?)*
 tags
            (name?)*
 elem
 data
            (name^?)^*.
            (name^?)^*
 locals
            (name?)*
 labels
            ((name^?)^*)^*
 fields
 typedefs
           subtype* }
```

For each index space, such a context contains the list of names assigned to the defined indices, which were denoted by the corresponding identifiers. Unnamed indices are associated with empty  $(\epsilon)$  entries in these lists. Fields have *dependent* name spaces, and hence a separate list of field identifiers per type.

An identifier context is *well-formed* if no index space contains duplicate identifiers. For fields, names need only be unique within a single type.

#### **Conventions**

To avoid unnecessary clutter, empty components are omitted when writing out identifier contexts. For example, the record {} is shorthand for an identifier context whose components are all empty.

### 6.1.4 Lists

Lists are written as plain sequences, but with a restriction on the length of these sequence.

$$list(A) ::= (x:A)^n \Rightarrow x^n \qquad (if n < 2^{32})$$

# 6.2 Lexical Format

### 6.2.1 Characters

The text format assigns meaning to *source text*, which consists of a sequence of *characters*. Characters are assumed to be represented as valid Unicode<sup>40</sup> (Section 2.4) *scalar values*.

```
source ::= char* char ::= U+00 \mid ... \mid U+D7FF \mid U+E000 \mid ... \mid U+10FFFF
```

#### Note

While source text may contain any Unicode character in comments or string literals, the rest of the grammar is formed exclusively from the characters supported by the 7-bit ASCII<sup>41</sup> subset of Unicode.

### 6.2.2 Tokens

The character stream in the source text is divided, from left to right, into a sequence of *tokens*, as defined by the following grammar.

```
token ::= keyword |uN| sN |fN| string |id| '(' | ')' | reserved keyword ::= ('a' | ... | 'z') idchar* (if occurring as a literal terminal in the grammar) reserved ::= (idchar | string | ',' | ';' | '|' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | ',' | '
```

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<sup>40</sup> https://www.unicode.org/versions/latest/

<sup>41</sup> https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

Tokens are formed from the input character stream according to the *longest match* rule. That is, the next token always consists of the longest possible sequence of characters that is recognized by the above lexical grammar. Tokens can be separated by white space, but except for strings, they cannot themselves contain whitespace.

*Keyword* tokens are defined either implicitly by an occurrence of a terminal symbol in literal form, such as 'keyword', in a syntactic production of this chapter, or explicitly where they arise in this chapter.

Any token that does not fall into any of the other categories is considered reserved, and cannot occur in source text.

#### Note

The effect of defining the set of reserved tokens is that all tokens must be separated by either parentheses, white space, or comments. For example, '0\$x' is a single reserved token, as is "a""b"'. Consequently, they are not recognized as two separate tokens '0' and '\$x', or "a" and "b", respectively, but instead disallowed. This property of tokenization is not affected by the fact that the definition of reserved tokens overlaps with other token classes.

# 6.2.3 White Space

White space is any sequence of literal space characters, formatting characters, comments, or annotations. The allowed formatting characters correspond to a subset of the ASCII<sup>42</sup> format effectors, namely, horizontal tabulation (U+09), line feed (U+0A), and carriage return (U+0D).

```
\begin{array}{lll} \text{space} & ::= & (\text{`'|format|comment})^* \\ \text{format} & ::= & \text{newline} \mid U + 09 \\ \text{newline} & ::= & U + 0A \mid U + 0D \mid U + 0D \mid U + 0A \end{array}
```

The only relevance of white space is to separate tokens. It is otherwise ignored.

### 6.2.4 Comments

A *comment* can either be a *line comment*, started with a double semicolon ';;' and extending to the end of the line, or a *block comment*, enclosed in delimiters '(;' . . . ';)'. Block comments can be nested.

Here, the pseudo token eof indicates the end of the input. The *look-ahead* restrictions on the productions for blockchar disambiguate the grammar such that only well-bracketed uses of block comment delimiters are allowed.

#### Note

Any formatting and control characters are allowed inside comments.

#### 6.2.5 Annotations

An *annotation* is a bracketed token sequence headed by an *annotation id* of the form '@id' or '@"...". No space is allowed between the opening parenthesis and this id. Annotations are intended to be used for third-party extensions; they can appear anywhere in a program but are ignored by the WebAssembly semantics itself, which treats them as white space.

 $<sup>^{42}\</sup> https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986\%5bR2012\%5d$ 

Annotations can contain other parenthesized token sequences (including nested annotations), as long as they are well-nested. String literals and comments occurring in an annotation must also be properly nested and closed.

```
annot ::= '(@' annotid (space | token)* ')' annotid ::= idchar^+ | name
```

#### Note

The annotation id is meant to be an identifier categorising the extension, and plays a role similar to the name of a custom section. By convention, annotations corresponding to a custom section should use the custom section's name as an id.

Implementations are expected to ignore annotations with ids that they do not recognize. On the other hand, they may impose restrictions on annotations that they do recognize, e.g., requiring a specific structure by superimposing a more concrete grammar. It is up to an implementation how it deals with errors in such annotations.

### 6.3 Values

The grammar productions in this section define lexical syntax, hence no white space is allowed.

# 6.3.1 Integers

All integers can be written in either decimal or hexadecimal notation. In both cases, digits can optionally be separated by underscores.

The allowed syntax for integer literals depends on size and signedness. Moreover, their value must lie within the range of the respective type.

Uninterpreted integers can be written as either signed or unsigned, and are normalized to unsigned in the abstract syntax.

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# 6.3.2 Floating-Point

Floating-point values can be represented in either decimal or hexadecimal notation.

```
::= d:digit
                    d:digit '_', p:frac
               \Rightarrow (d+p/10)/10
              := h:hexdigit
                                                                                          h/16
              h:hexdigit '_,' p:hexfrac
                                                                                     \Rightarrow (h+p/16)/16
              ::= p:num '.'
float
                    p:num '.' q:frac
                                                                                     \Rightarrow p+q
                    p:num '.'?' ('E' | 'e') ±:sign e:num
p:num '.' q:frac ('E' | 'e') ±:sign e:num
                                                                                     \Rightarrow p \cdot 10^{\pm e}
                                                                                          (p+q) \cdot 10^{\pm e}
hexfloat ::= '0x' p:hexnum'.'
                                                                                     \Rightarrow p
               '0x' p:hexnum '.' q:hexfrac
                                                                                     \Rightarrow p+q
                     '0x' p:hexnum '.'? ('P' | 'p') \pm:sign e:num
                                                                                     \Rightarrow p \cdot 2^{\pm e}
                     '0x' p:hexnum '.' q:hexfrac ('P' | 'p') \pm:sign e:num \Rightarrow (p+q) \cdot 2^{\pm e}
```

The value of a literal must not lie outside the representable range of the corresponding IEEE  $754^{43}$  type (that is, a numeric value must not overflow to  $\pm$ infinity), but it may be rounded to the nearest representable value.

#### Note

Rounding can be prevented by using hexadecimal notation with no more significant bits than supported by the required type.

Floating-point values may also be written as constants for *infinity* or *canonical NaN* (*not a number*). Furthermore, arbitrary NaN values may be expressed by providing an explicit payload value.

### 6.3.3 Strings

Strings denote sequences of bytes that can represent both textual and binary data. They are enclosed in quotation marks and may contain any character other than  $ASCII^{44}$  control characters, quotation marks ('"'), or backslash ('\'), except when expressed with an *escape sequence*.

Each character in a string literal represents the byte sequence corresponding to its UTF-8 Unicode<sup>45</sup> (Section 2.5) encoding, except for hexadecimal escape sequences 'hh', which represent raw bytes of the respective value.

<sup>43</sup> https://ieeexplore.ieee.org/document/8766229

<sup>44</sup> https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

<sup>45</sup> https://www.unicode.org/versions/latest/

### **6.3.4 Names**

Names are strings denoting a literal character sequence. A name string must form a valid UTF-8 encoding as defined by Unicode<sup>46</sup> (Section 2.5) and is interpreted as a string of Unicode scalar values.

name ::= 
$$b^*$$
:string  $\Rightarrow c^*$  (if  $b^* = \text{utfs}(c^*)$ )

#### Note

Presuming the source text is itself encoded correctly, strings that do not contain any uses of hexadecimal byte escapes are always valid names.

### 6.3.5 Identifiers

Indices can be given in both numeric and symbolic form. Symbolic *identifiers* that stand in lieu of indices start with '\$', followed by eiter a sequence of printable ASCII<sup>47</sup> characters that does not contain a space, quotation mark, comma, semicolon, or bracket, or by a quoted name.

#### Note

The value of an identifier character is the Unicode codepoint denoting it.

#### **Conventions**

The expansion rules of some abbreviations require insertion of a *fresh* identifier. That may be any syntactically valid identifier that does not already occur in the given source text.

# 6.4 Types

### 6.4.1 Number Types

numtype
$$_{I}$$
 ::= 'i32'  $\Rightarrow$  i32 | 'i64'  $\Rightarrow$  i64 | 'f32'  $\Rightarrow$  f32 | 'f64'  $\Rightarrow$  f64

### 6.4.2 Vector Types

```
vectype_I ::= 'v128' \Rightarrow v_{128}
```

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<sup>46</sup> https://www.unicode.org/versions/latest/

<sup>&</sup>lt;sup>47</sup> https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

### 6.4.3 Heap Types

```
absheaptype ::= 'any'
                                         any
                 'eq'
                               \Rightarrow
                                          eq
                  'i31'
                                \Rightarrow
                                          i31
                 'struct'
'array'
                 \Rightarrow
                                         struct
                                         array
                                         none
                                         func
                                         nofunc
                                        extern
noexn
exn
noextern
heaptype_I ::= t:absheaptype \Rightarrow
             x: typeidx_I \Rightarrow
```

# **6.4.4 Reference Types**

#### **Abbreviations**

There are shorthands for references to abstract heap types.

```
'anyref' \( \equiv \text{ (' 'ref' 'null' 'eq' ')'} \)
'eqref' \( \equiv \text{ (' 'ref' 'null' 'i31' ')'} \)
'i31ref' \( \equiv \text{ (' 'ref' 'null' 'i31' ')'} \)
'structref' \( \equiv \text{ (' 'ref' 'null' 'struct' ')'} \)
'arrayref' \( \equiv \text{ (' 'ref' 'null' 'array' ')'} \)
'nullref' \( \equiv \text{ (' 'ref' 'null' 'none' ')'} \)
'funcref' \( \equiv \text{ (' 'ref' 'null' 'nofunc' ')'} \)
'exnref' \( \equiv \text{ (' 'ref' 'null' 'noexn' ')'} \)
'nullexnref' \( \equiv \text{ (' 'ref' 'null' 'noexn' ')'} \)
'externref' \( \equiv \text{ (' 'ref' 'null' 'extern' ')'} \)
'nullexternref' \( \equiv \text{ (' 'ref' 'null' 'noextern' ')'} \)
```

### 6.4.5 Value Types

### 6.4.6 Function Types

```
\begin{array}{llll} \texttt{functype}_I & ::= & \text{`(``func'} \ t_1^*: \texttt{list}(\texttt{param}_I) \ t_2^*: \texttt{list}(\texttt{result}_I) \ \text{`)'} & \Rightarrow & [t_1^*] \to [t_2^*] \\ \texttt{param}_I & ::= & \text{`(``param'} \ \text{id'} \ t: \texttt{valtype}_I \ \text{`)'} & \Rightarrow & t \\ \texttt{result}_I & ::= & \text{`(``result'} \ t: \texttt{valtype}_I \ \text{`)'} & \Rightarrow & t \\ \end{array}
```

#### Note

The optional identifier names for parameters in a function type only have documentation purpose. They cannot be referenced from anywhere.

#### **Abbreviations**

Multiple anonymous parameters or results may be combined into a single declaration:

```
'(' 'param' valtype* ')' \equiv ('(' 'param' valtype ')')* '(' 'result' valtype* ')' \equiv ('(' 'result' valtype ')')*
```

# 6.4.7 Aggregate Types

#### **Abbreviations**

Multiple anonymous structure fields may be combined into a single declaration:

```
'(' 'field' fieldtype* ')' \equiv ('(' 'field' fieldtype ')')*
```

# 6.4.8 Composite Types

### 6.4.9 Recursive Types

### **Abbreviations**

Singular recursive types can omit the 'rec' keyword:

```
typedef = '(' 'rec' typedef ')'
```

Similarly, final sub types with no super-types can omit the sub keyword and arguments:

```
comptype \equiv '(' 'sub' 'final' \epsilon comptype ')'
```

### 6.4.10 Address Types

```
addrtype ::= 'i32' \Rightarrow i32 | 'i64' \Rightarrow i64
```

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#### **Abbreviations**

The address type can be omited, in which case it defaults i32:

```
" \equiv i32"
```

### 6.4.11 Limits

```
limits ::= n:u32 \Rightarrow \{\min n, \max \epsilon\}
| n:u32 m:u32 \Rightarrow \{\min n, \max m\}
```

# 6.4.12 Memory Types

```
memtype_I ::= at:addrtype \ lim:limits \Rightarrow at \ lim
```

# 6.4.13 Table Types

```
tabletype_I ::= at:addrtype \ lim:limits \ et:reftype_I \Rightarrow at \ lim \ et
```

# 6.4.14 Global Types

# 6.5 Instructions

Instructions are syntactically distinguished into *plain* and *structured* instructions.

```
instr_I ::= in:plaininstr_I \Rightarrow in
in:blockinstr_I \Rightarrow in
```

In addition, as a syntactic abbreviation, instructions can be written as S-expressions in folded form, to group them visually.

#### **6.5.1 Labels**

Structured control instructions can be annotated with a symbolic label identifier. They are the only symbolic identifiers that can be bound locally in an instruction sequence. The following grammar handles the corresponding update to the identifier context by composing the context with an additional label entry.

#### Note

The new label entry is inserted at the *beginning* of the label list in the identifier context. This effectively shifts all existing labels up by one, mirroring the fact that control instructions are indexed relatively not absolutely.

If a label with the same name already exists, then it is shadowed and the earlier label becomes inaccessible.

#### 6.5.2 Control Instructions

Structured control instructions can bind an optional symbolic label identifier. The same label identifier may optionally be repeated after the corresponding end or else keywords, to indicate the matching delimiters.

Their block type is given as a type use, analogous to the type of functions. However, the special case of a type use that is syntactically empty or consists of only a single result is not regarded as an abbreviation for an inline function type, but is parsed directly into an optional value type.

```
\begin{aligned} &\text{blocktype}_I &::= & (t:\text{result}_I)^? &\Rightarrow & t^? \\ &\mid & x, I':\text{typeuse}_I &\Rightarrow & x & (\text{if } I' = \{\text{locals }(\epsilon)^*\}) \\ &\text{blockinstr}_I &::= & \text{'block'} & (v^?, I'): \text{label}_I & bt: \text{blocktype}_I & (in:\text{instr}_{I'})^* & \text{'end'} & v'^?: \text{id}^? \\ &&\Rightarrow & \text{block } bt & in^* \text{ end} & (\text{if } v'^? = \epsilon \lor v'^? = v^?) \\ &\mid & \text{'loop'} & (v^?, I'): \text{label}_I & bt: \text{blocktype}_I & (in:\text{instr}_{I'})^* & \text{'end'} & v'^?: \text{id}^? \\ &&\Rightarrow & \text{loop } bt & in^* \text{ end} & (\text{if } v'^? = \epsilon \lor v'^? = v^?) \\ &\mid & \text{'if'} & (v^?, I'): \text{label}_I & bt: \text{blocktype}_I & (in_1:\text{instr}_{I'})^* & \text{'else'} & v_1^?: \text{id}_1^2 & (in_2:\text{instr}_{I'})^* & \text{'end'} & v_2^?: \text{id}_2^2 \\ &&\Rightarrow & \text{if } bt & in_1^* \text{ else } in_2^* \text{ end} & (\text{if } v_1^? = \epsilon \lor v_1^? = v^?, v_2^? = \epsilon \lor v_2^? = v^?) \\ &\mid & \text{'try_table'} & I': \text{label}_I & bt: \text{blocktype} & (c:\text{catch}_I)^* & (in:\text{instr}_{I'})^* & \text{'end'} & \text{id}^? \\ &&\Rightarrow & \text{try_table } bt & c^* & in^* \text{ end} & (\text{if } \text{id}^? = \epsilon \lor \text{id}^? = \text{label}) \end{aligned} catch &::= & \text{'('' catch' } & x:\text{tagidx}_I & \text{l:labelidx}_I & \text{')'} & \Rightarrow & \text{catch} & x & l \\ &\mid & \text{'('' catch_all' } & l:\text{labelidx}_I & \text{')'} & \Rightarrow & \text{catch_all } l \\ &\mid & \text{'('' catch_all' } & l:\text{labelidx}_I & \text{')'} & \Rightarrow & \text{catch_all}_I & l \\ &\mid & \text{'('' catch_all_all_ref' } & l:\text{labelidx}_I & \text{')'} & \Rightarrow & \text{catch_all_ref} & l \end{aligned}
```

#### Note

The side condition stating that the identifier context I' must only contain unnamed entries in the rule for typeuse block types enforces that no identifier can be bound in any param declaration for a block type.

All other control instruction are represented verbatim.

```
plaininstr<sub>I</sub> ::= 'unreachable'
                                                                                              unreachable
                       'nop'
                                                                                               nop
                                                                                          \Rightarrow
                       'br' l:labelidx<sub>I</sub>
                                                                                          \Rightarrow br l
                       'br_if' l:labelidx_I
                                                                                          \Rightarrow br_if l
                       'br_table' l^*:list(labelidx_I) l_N:labelidx_I
                                                                                          \Rightarrow br_table l^* l_N
                       'br on null' l:labelidx_I
                                                                                          \Rightarrow br on null l
                       'br_on_non_null' l:labelidx_I
                                                                                          \Rightarrow br on non null l
                       'br_on_cast' l:labelidx_I t_1:reftype t_2:reftype
                                                                                          \Rightarrow br on cast l t_1 t_2
                       'br_on_cast_fail' l:labelidx_I t_1:reftype t_2:reftype
                                                                                          \Rightarrow br on cast fail l t_1 t_2
                       'return'
                                                                                          ⇒ return
                       'call' x: funcidx_I
                                                                                          \Rightarrow call x
                       'call_ref' x:typeidx
                                                                                          \Rightarrow call_ref x
                                                                                                                           (if I' = -
                       'call_indirect' x:tableidx y, I':typeuseI
                                                                                          \Rightarrow call_indirect x y
                       'return_call' x:funcidx_I
                                                                                          \Rightarrow return_call x
                       'return_call_ref' x:typeidx
                                                                                          \Rightarrow return_call_ref x
                       'return_call_indirect' x:tableidx y, I':typeuse_I
                                                                                          \Rightarrow return_call_indirect x y (if I' = -
                       'throw' x:tagidx_I
                                                                                               throw x
                       'throw ref'
                                                                                          \Rightarrow throw ref
```

### Note

The side condition stating that the identifier context I' must only contain unnamed entries in the rule for call\_indirect enforces that no identifier can be bound in any param declaration appearing in the type annotation.

#### **Abbreviations**

The 'else' keyword of an 'if' instruction can be omitted if the following instruction sequence is empty.

```
'if' label blocktype_I instr^* 'end' \equiv 'if' label blocktype_I instr^* 'else' 'end'
```

Also, for backwards compatibility, the table index to 'call\_indirect' and 'return\_call\_indirect' can be omitted, defaulting to 0.

#### 6.5.3 Reference Instructions

```
plaininstr_I ::= ...
                                   'ref.null' t:heaptype
                                                                                                                 \Rightarrow ref.null t
                                   'ref.func' x:funcidx
                                                                                                                 \Rightarrow ref.func x
                                                                                                                  ⇒ ref.is null
                                    'ref.is null'
                                    'ref.as_non_null'
                                                                                                                  \Rightarrow ref.as non null
                                    'ref.eq'
                                                                                                                 \Rightarrow ref.eq
                                   \texttt{`struct.get\_s'} \ x : \texttt{typeidx}_I \ y : \texttt{fieldidx}_{I,x} \quad \Rightarrow \quad \mathsf{struct.get\_s} \ x \ y
                                    \texttt{`struct.set'} \ x \texttt{:typeidx}_I \ y \texttt{:fieldidx}_{I,x} \qquad \Rightarrow \ \mathsf{struct.set} \ x \ y
                                   \begin{array}{lll} \text{`array.new'} & x: \text{typeid} x_I & \Rightarrow & \text{array.new} & x \\ \text{`array.new\_default'} & x: \text{typeid} x_I & \Rightarrow & \text{array.new\_default} & x \\ \text{`array.new\_fixed'} & x: \text{typeid} x_I & n: \text{u} \text{32} & \Rightarrow & \text{array.new\_fixed} & x & n \\ \end{array}
                                    'array.new_data' x:typeidx_I y:dataidx_I \Rightarrow array.new_data x y
                                    \verb"array.new_elem" \ x: \verb"typeidx"_I \ y: \verb"elemidx"_I \ \Rightarrow \ \verb"array.new_elem" \ x \ y
                                                                                 \Rightarrow array.get x
                                    'array.get' x:typeidx_I
                                   'array.get_u' x:typeidx_I
'array.get_s' x:typeidx_I
'array.set' x:typeidx_I
                                                                                                        \Rightarrow \quad \operatorname{array.get\_u} x
\Rightarrow \quad \operatorname{array.get\_s} x
\Rightarrow \quad \operatorname{array.set} x
                                   \begin{array}{lll} \text{`array.set'} & x: \mathsf{typeidx}_I & \Rightarrow & \mathsf{array.set} \ x \\ \text{`array.len'} & \Rightarrow & \mathsf{array.len} \\ \text{`array.fill'} & x: \mathsf{typeidx}_I & \Rightarrow & \mathsf{array.fill} \ x \\ \text{`array.copy'} & x: \mathsf{typeidx}_I & y: \mathsf{typeidx}_I & \Rightarrow & \mathsf{array.copy} \ x \ y \\ \end{array}
                                    'array.init_data' x:typeidx_I y:dataidx_I \Rightarrow array.init_data x y
                                    'array.init_elem' x:typeidx_I y:elemidx_I \Rightarrow array.init_elem x y
                                    'ref.i31'
                                                                                                                    ⇒ ref.i31
                                    'i31.get_u'
                                                                                                                   ⇒ i31.get_u
                                    'i31.get_s'
                                                                                                                  ⇒ i31.get_s
                                    'any.convert_extern'
                                                                                                                 ⇒ any.convert_extern
                                    'extern.convert_any'
                                                                                                                 ⇒ extern.convert_any
```

### 6.5.4 Parametric Instructions

### 6.5.5 Variable Instructions

### 6.5.6 Table Instructions

#### **Abbreviations**

For backwards compatibility, all table indices may be omitted from table instructions, defaulting to 0.

```
'table.get' \equiv 'table.get' '0'
'table.set' \equiv 'table.set' '0'
'table.size' \equiv 'table.size' '0'
'table.grow' \equiv 'table.grow' '0'
'table.fill' \equiv 'table.fill' '0'
'table.copy' \equiv 'table.copy' '0' '0'
'table.init' x:elemidx_I \equiv 'table.init' '0' x:elemidx_I
```

# 6.5.7 Memory Instructions

The offset and alignment immediates to memory instructions are optional. The offset defaults to 0, the alignment to the storage size of the respective memory access, which is its *natural alignment*. Lexically, an offset or align

 $memarg_N$ 

phrase is considered a single keyword token, so no white space is allowed around the '='.

```
o:offset a:align_N
                            offset
                                                              'offset='o:u32
                                                  ::=
                                                                                                                      \Rightarrow o
                                                   \Rightarrow 0
                                                              'align='a:u32
                            \operatorname{align}_N
                                                   ::=
                                                                                                                      \Rightarrow a
                                                                                                                      \Rightarrow N
                            plaininstr_I
                                                  ::=
                                                              'i32.load' x:memidx m:memarg_4

⇒ i32.loa
                                                              'i64.load' x:memidx m:memarg<sub>8</sub>
                                                                                                                     ⇒ i64.loa
                                                              'f32.load' x:memidx m:memarg<sub>4</sub>

⇒ f<sub>32</sub>.lo.

                                                              'f64.load' x:memidx m:memarg<sub>8</sub>
                                                                                                                     \Rightarrow f<sub>64</sub>.lo
                                                              'v128.load' x:memidx m:memarg_{16}

⇒ v128.le

                                                               'i32.load8_s' x:memidx m:memarg<sub>1</sub>

⇒ i32.loa
                                                              'i32.load8_u' x:memidx m:memarg<sub>1</sub>

⇒ i32.loa
                                                              'i32.load16_s' x:memidx m:memarg<sub>2</sub>

⇒ i32.loa
                                                              'i32.load16_u' x:memidx m:memarg<sub>2</sub>

⇒ i32.loa
                                                              "i64.load8_s" x:memidx m:memarg<sub>1</sub>
                                                                                                                    ⇒ i64.loa
                                                              'i64.load8_u' x:memidx m:memarg<sub>1</sub>
                                                                                                                    ⇒ i64.loa
                                                              'i64.load16_s' x:memidx m:memarg_2
                                                                                                                    ⇒ i64.loa
                                                               'i64.load16_u' x:memidx m:memarg_2
                                                                                                                    ⇒ i64.loa
                                                              'i64.load32_s' x:memidx m:memarg<sub>4</sub>
                                                                                                                    ⇒ i64.loa
                                                              'i64.load32_u' x:memidx m:memarg<sub>4</sub>

⇒ i64.loa

                                                              'v128.load8x8_s' x:memidx m:memarg<sub>8</sub>

⇒ v128.le

                                                              'v128.load8x8_u' x:memidx m:memarg<sub>8</sub>

⇒ v128.le

                                                              'v128.load16x4_s' x:memidx m:memarg<sub>8</sub>

⇒ v128.le

                                                              'v128.load16x4_u' x:memidx m:memarg<sub>8</sub>

⇒ v128.le

                                                              \verb"v128.load32x2_s" $x$:\texttt{memidx} $m$:\texttt{memarg}_8$

⇒ v128.le

                                                               'v128.load32x2_u' x:memidx m:memarg_8

⇒ v128.le

                                                              'v128.load8_splat' x:memidx m:memarg<sub>1</sub>

⇒ v128.le

                                                              'v128.load16_splat' x:memidx m:memarg2

⇒ v128.le

                                                              'v128.load32_splat' x:memidx m:memarg<sub>4</sub>

⇒ v128.le

                                                              'v128.load64_splat' x:memidx m:memarg<sub>8</sub>

⇒ v128.le

                                                              'v128.load32_zero' x:memidx m:memarg<sub>4</sub>

⇒ v128.le

                                                              'v128.load64_zero' x:memidx m:memarg<sub>8</sub>

⇒ v128.le

                                                              'v128.load8_lane' x:memidx m:memarg<sub>1</sub> y:u8

⇒ v128.le

                                                              'v128.load16_lane' x:memidx m:memarg<sub>2</sub> y:u8 \Rightarrow v128.lo
                                                              'v128.load32_lane' x:memidx m:memarg<sub>4</sub> y:u8 \Rightarrow v128.lo
                                                              'v128.load64_lane' x:memidx m:memarg<sub>8</sub> y:u8 \Rightarrow v128.lo
                                                              'i32.store' x:memidx m:memarg<sub>4</sub>
                                                                                                                      ⇒ i32.sto
                                                              'i64.store' x:memidx m:memarg_8
                                                                                                                     ⇒ i64.sto
                                                              'f32.store' x:memidx m:memarg_4

⇒ f32.st

                                                              'f64.store' x:memidx m:memarg<sub>8</sub>
                                                                                                                     \Rightarrow f<sub>64</sub>.st
                                                               'v128.store' x:memidx m:memarg<sub>16</sub>

→ V128.S
                                                               'i32.store8' x:memidx m:memarg_1

⇒ i32.sto

                                                              'i32.store16' x:memidx m:memarg<sub>2</sub>
                                                                                                                    ⇒ i32.sto
                                                              'i64.store8' x:memidx m:memarg<sub>1</sub>

⇒ i64.sto

                                                              'i64.store16' x:memidx m:memarg<sub>2</sub>

⇒ i64.sto

                                                              'i64.store32' x:memidx m:memarg<sub>4</sub>
                                                                                                                    ⇒ i64.sto
                                                              'v128.store8_lane' x:memidx m:memarg<sub>1</sub> y:u8 \Rightarrow v128.s
                                                               'v128.store16_lane' x:memidx m:memarg_2 y:u8 \Rightarrow v128.s
                                                               'v128.store32_lane' x:memidx m:memarg<sub>4</sub> y:u8 \Rightarrow v128.s
                                                              'v128.store64_lane' x:memidx m:memarg<sub>8</sub> y:u8 \Rightarrow v128.s
'memory.size' x:memidx \Rightarrow
                                             memory.size x
                                                              'memory.grow' x:memidx
                                                                                                                      \Rightarrow memo
                                                              'memory.fill' x:memidx
                                                                                                                      \Rightarrow memo
                                                              'memory.copy' x:memidx y:memidx
                                                                                                                      ⇒ memore
                                                              'memory.init' x:memidx y:dataidx_I
                                                                                                                      \Rightarrow memo
                                                                                                                      \Rightarrow data.
                                                              'data.drop' x:dataidx_I
```

{aligr

#### **Abbreviations**

As an abbreviation, the memory index can be omitted in all memory instructions, defaulting to 0.

```
numtype'.load' memarg
                      ≡ numtype'.load' '0' memarg
vectype'.load' memarg
                      numtype'.load'N'_'sx memarg \equiv numtype'.load'N'_'sx '0' memarg
numtype'.store' memarg
\equiv numtype'.store' '0' memarg
vectype'.store' memarg
                      ≡ vectype'.store' '0' memarg
vectype'.store'N'\_lane' memarg u8 \equiv vectype'.store'N'\_lane' '0' memarg u8
                      'memory.size'
                       'memory.grow'
                       'memory.fill'
                       ≡ 'memory.copy' '0' '0'
'memory.copy'
                    \equiv 'memory.init' '0' x:elemidx_I
'memory.init' x:elemidx_I
```

#### 6.5.8 Numeric Instructions

```
plaininstr_I ::=
                       'i32.const' n:i32 \Rightarrow i32.const n
                       'i64.const' n:i64 \Rightarrow i64.const n
                       'f32.const' z:f32 \Rightarrow f32.const z
                       'f64.const' z:f64 \Rightarrow f64.const z
                    'i32.clz' ⇒ i32.clz
                    'i32.ctz' ⇒ i32.ctz
                     'i32.popcnt' \Rightarrow i32.popcnt
                    'i32.add' ⇒ i32.add

'i32.sub' ⇒ i32.sub

'i32.mul' ⇒ i32.mul
                    "i32.div_s" \Rightarrow i32.div_s"
                    'i32.div_u' \Rightarrow i32.div_u
                    'i32.rem_s' \Rightarrow i32.rem_s
                    'i32.rem_u' \Rightarrow i32.rem_u
                    'i32.and' ⇒ i32.and
'i32.or' ⇒ i32.or
                    .52.xor ⇒ i32.xor

'i32.shl' ⇒ :--
                    'i32.shr s' \Rightarrow i32.shr s
                    'i32.shr u' \Rightarrow i32.shr u
                    'i32.rotl' ⇒ i32.rotl
                     'i32.rotr' ⇒ i32.rotr
```

```
'i64.clz'
                 ⇒ i64.clz
 'i64.ctz'
                  ⇒ i64.ctz
  'i64.popcnt' ⇒ i64.popcnt
 'i64.add'
              ⇒ i64.add
 'i64.sub'
               ⇒ i64.sub
 'i64.mul' ⇒ i64.mul
 'i64.div_s' ⇒ i64.div s
 i64.div_u' \Rightarrow i64.div_u
 'i64.rem_s'
                 ⇒ i64.rem s
  'i64.rem_u'
                 ⇒ i64.rem_u
 'i64.and' \Rightarrow i64.and
 'i64.or'
               ⇒ i64.or
 'i64.xor'
               ⇒ i64.xor
 'i64.shl' ⇒ i64.shl
 'i64.shr_s' \Rightarrow i64.shr_s
 'i64.shr_u' ⇒ i64.shr_u
 'i64.rotl'
                 ⇒ i64.rotl
 'i64.rotr'
                 ⇒ i64.rotr
15∠.abs' ⇒ f32.abs
'f32.neg' ⇒ f32.neg
'f32.ceil' ⇒ f32.neg
'f32.ceil' ⇒ f32.ceil

'f32.floor' ⇒ f32.floor

'f32.trunc' ⇒ f32.trunc
'f32.nearest' \Rightarrow f32.nearest
\texttt{`f32.sqrt'} \qquad \Rightarrow \quad \mathsf{f32.sqrt}
                 ⇒ f32.add
'f32.add'

    ⇒ f32.sub
    ⇒ f32.mul
    ⇒ f32.div

'f32.sub'
'f32.mul'
'f32.div'
'f32.min' ⇒ f32.min
'f32.max' ⇒ f32.max
'f32.copysign' \Rightarrow f32.copysign
'f64.abs'
                ⇒ f64.abs
'f64.neg'
                 ⇒ f64.neg
'f64.ceil'
                 ⇒ f<sub>64</sub>.ceil
'f64.floor'
                  ⇒ f64.floor
'f64.trunc'
                  ⇒ f64.trunc
'f64.nearest' \Rightarrow f64.nearest
'f64.sqrt' \Rightarrow f64.sqrt
                ⇒ f64.add
'f64.add'
'f64.sub'
                ⇒ f<sub>64</sub>.sub
'f64.mul'
                ⇒ f<sub>64</sub>.mul
'f64.div'
                 ⇒ f64.div
'f64.min' ⇒ f64.min
'f64.max' ⇒ f64.max
'f64.copysign' \Rightarrow f64.copysign
```

```
'i32.eqz'
                    ⇒ i32.eqz
ʻi32.eq'
                 ⇒ i32.eq
\begin{array}{lll} \mbox{`i32.ne'} & \Rightarrow & \mbox{i32.ne} \\ \mbox{`i32.lt\_s'} & \Rightarrow & \mbox{i32.lt\_s} \end{array}
"i32.lt_u" \Rightarrow i32.lt_u"
'i32.gt_s' ⇒ i32.gt_s
'i32.gt_u' ⇒ i32.gt_u
\begin{array}{ccc} \text{i32.gt\_u} & \Rightarrow & \text{i32.gt\_u} \\ \text{`i32.le\_s'} & \Rightarrow & \text{i32.le\_s} \\ \text{`i32.le\_u'} & \Rightarrow & \text{i32.le\_u} \end{array}
\begin{array}{ccc}
\text{`i32.ge\_s'} & \Rightarrow & \text{i32.ge\_s}
\end{array}
'i32.ge_u' ⇒ i32.ge_u
'i64.eqz'
                      ⇒ i64.eqz
\text{`i64.eq'} \Rightarrow \text{i64.eq}
\text{`i64.ne'} \Rightarrow \text{i64.ne}
'i64.ne' ⇒ i64.ne

'i64.lt_s' ⇒ i64.lt_s

'i64.lt_u' ⇒ i64.lt_u
i64.gt_s' \Rightarrow i64.gt_s
'i64.gt_u' ⇒ i64.gt_u
'i64.le_s'
                      ⇒ i64.le_s
'i64.le_u'
                      ⇒ i64.le_u
                   ⇒ i64.ge_s
'i64.ge_s'
'i64.ge_u'
                    ⇒ i64.ge_u
'f32.eq'
                    ⇒ f32.eq
                    ⇒ f<sub>32</sub>.ne
'f32.ne'
                    ⇒ f32.lt
'f32.1t'
'f32.gt'

⇒ f32.gt

                    ⇒ f32.le
'f32.le'
'f32.ge'
                      ⇒ f32.ge
 'f64.eq'
                     \Rightarrow f64.eq
                      ⇒ f<sub>64.ne</sub>
 'f64.ne'
                       \Rightarrow f64.lt
 'f64.lt'
 'f64.gt'
                    \Rightarrow f64.gt
                    \Rightarrow f<sub>64</sub>.le
 'f64.le'
 'f64.ge'
                    ⇒ f64.ge
```

```
      'i32.wrap_i64'
      ⇒
      i32.wrap_i64

      'i32.trunc_f32_s'
      ⇒
      i32.trunc_f32_s

      'i32.trunc_f32_u'
      ⇒
      i32.trunc_f32_u

      'i32.trunc_f64_s'
      ⇒
      i32.trunc_f64_s

      'i32.trunc_f64_u'
      ⇒
      i32.trunc_f64_u

 'i32.trunc_sat_f32_s' ⇒ i32.trunc_sat_f32_s
 'i32.trunc_sat_f32_u' ⇒ i32.trunc_sat_f32_u
 'i32.trunc_sat_f64_s' \Rightarrow i32.trunc_sat_f64_s
 'i32.trunc_sat_f64_u' \Rightarrow i32.trunc_sat_f64_u
\begin{array}{lll} \text{`i64.extend\_i32\_s'} & \Rightarrow & \text{i64.extend\_i32\_s'} \\ \text{`i64.extend\_i32\_u'} & \Rightarrow & \text{i64.extend\_i32\_u'} \\ \text{`i64.trunc\_f32\_s'} & \Rightarrow & \text{i64.trunc\_f32\_s'} \\ \end{array}
                                              ⇒ i64.extend_i32_u
\begin{array}{lll} \text{`i64.trunc\_f32\_u'} & \Rightarrow & \text{i64.trunc\_f32\_u} \\ \text{`i64.trunc\_f64\_s'} & \Rightarrow & \text{i64.trunc\_f64\_s} \\ \text{`i64.trunc\_f64\_u'} & \Rightarrow & \text{i64.trunc\_f64\_u} \\ \end{array}
 \texttt{`i64.trunc\_sat\_f32\_s'} \quad \Rightarrow \quad \texttt{i64.trunc\_sat\_f32\_s'}
 'i64.trunc_sat_f32_u' ⇒ i64.trunc_sat_f32_u
 i64.trunc_sat_f64_s' \Rightarrow i64.trunc_sat_f64_s
 'i64.trunc_sat_f64_u' ⇒ i64.trunc_sat_f64_u
 'f32.convert i32 s' \Rightarrow f32.convert i32 s
 'f32.convert_i32_u' ⇒ f32.convert_i32_u
'f32.convert_i64_s' ⇒ f32.convert_i64_s

'f32.convert_i64_u' ⇒ f32.convert_i64_u

'f32.demote_f64' ⇒ f32.demote_f64

'f64.convert_i32_s' ⇒ f64.convert_i32_s

'f64.convert_i64_s' ⇒ f64.convert_i64_s
\begin{tabular}{llll} `f64.convert\_i64\_u' &$\Rightarrow$ f64.convert\_i64\_u' \\ `f64.promote\_f32' &$\Rightarrow$ f64.promote\_f32 \\ \end{tabular}
 'i32.reinterpret_f32' ⇒ i32.reinterpret_f32
 'i64.reinterpret_f64' ⇒ i64.reinterpret_f64
 'f32.reinterpret_i32' ⇒ f32.reinterpret_i32
 'f64.reinterpret_i64' ⇒ f64.reinterpret_i64
      'i32.extend8 s' \Rightarrow i32.extend8 s
      'i32.extend16_s' \Rightarrow i32.extend16_s
'i64.extend8_s' \Rightarrow i64.extend8_s
      i64.extend16_s \Rightarrow i64.extend16_s
      i64.extend32_s' \Rightarrow i64.extend32_s
```

# 6.5.9 Vector Instructions

Vector constant instructions have a mandatory shape descriptor, which determines how the following values are parsed.

```
'i8x16.splat'
                                                 i8x16.splat
'i16x8.splat'
                                                i16x8.splat
'i32x4.splat'
                                            ⇒ i32x4.splat
'i64x2.splat'
                                            ⇒ i64x2.splat
'f32x4.splat'
                                            ⇒ f32x4.splat
'f64x2.splat'
                                            ⇒ f<sub>64</sub>x<sub>2</sub>.splat
'i8x16.extract_lane_s' laneidx:u8
                                                 i8x16.extract_lane_s laneidx
'i8x16.extract lane u' laneidx:u8
                                                 i8x16.extract lane u laneidx
'i8x16.replace lane' laneidx:u8
                                            \Rightarrow i8x16.replace lane laneidx
'i16x8.extract_lane_s' laneidx:u8
                                            \Rightarrow i16x8.extract lane s laneidx
'i16x8.extract_lane_u' laneidx:u8
                                                 i16x8.extract lane u laneidx
'i16x8.replace_lane' laneidx:u8
                                                i16x8.replace lane laneidx
                                            \Rightarrow i32x4.extract lane laneidx
'i32x4.extract_lane' laneidx:u8
                                            \Rightarrow i32x4.replace lane laneidx
'i32x4.replace_lane' laneidx:u8
'i64x2.extract_lane' laneidx:u8
                                            \Rightarrow i64x2.extract lane laneidx
'i64x2.replace_lane' laneidx:u8
                                            \Rightarrow i64x2.replace_lane laneidx
'f32x4.extract_lane' laneidx:u8
                                            \Rightarrow f<sub>32×4</sub>.extract lane laneidx
'f32x4.replace_lane' laneidx:u8
                                            \Rightarrow f32x4.replace_lane laneidx
'f64x2.extract_lane' laneidx:u8
                                            \Rightarrow f<sub>64×2</sub>.extract lane laneidx
'f64x2.replace_lane' laneidx:u8
                                                f<sub>64×2</sub>.replace lane laneidx
'i8x16.eq'
                                                 i8x16.eq
'i8x16.ne'
                                                 i8x16.ne
'i8x16.lt s'
                                                i8x16.lt s
                                            \Rightarrow
'i8x16.lt u'
                                            ⇒ i8x16.lt u
'i8x16.gt_s'
                                            \Rightarrow i8x16.gt_s
'i8x16.gt u'
                                            ⇒ i8x16.gt u
'i8x16.le s'
                                            \Rightarrow i8x16.le s
'i8x16.le_u'
                                            ⇒ i8x16.le_u
'i8x16.ge_s'
                                            \Rightarrow
                                                 i8X16.ge_s
'i8x16.ge u'
                                                 i8x16.ge u
'i16x8.eq'
                                                 i16x8.eq
                                            \Rightarrow
'i16x8.ne'
                                                i16x8.ne
                                            \Rightarrow
'i16x8.lt_s'
                                                i16x8.lt s
'i16x8.lt u'
                                            ⇒ i16x8.lt u
'i16x8.gt_s'
                                            \Rightarrow i16x8.gt_s
'i16x8.gt_u'
                                            ⇒ i16x8.gt_u
'i16x8.le_s'
                                            ⇒ i16x8.le_s
'i16x8.le u'
                                            ⇒ i16x8.le u
'i16x8.ge s'
                                            ⇒ i16x8.ge s
'i16x8.ge_u'
                                                 i16x8.ge_u
'i32x4.eq'
                                                i32x4.ea
                                            \Rightarrow
'i32x4.ne'
                                            ⇒ i32x4.ne
'i32x4.1t s'
                                                i32x4.lt s
'i32x4.1t u'
                                            ⇒ i32x4.lt u
'i32x4.gt_s'
                                            \Rightarrow i32x4.gt_s
'i32x4.gt_u'
                                            ⇒ i32x4.gt_u
'i32x4.le s'
                                            \Rightarrow i32x4.le s
'i32x4.le_u'
                                            ⇒ i32x4.le_u
'i32x4.ge_s'
                                            \Rightarrow i32x4.ge s
'i32x4.ge_u'
                                            ⇒ i32x4.ge_u
```

```
'i64x2.eq'
                                                 \Rightarrow i64x2.eq
'i64x2.ne'
                                                 \Rightarrow i64x2.ne
'i64x2.lt s'
                                                 \Rightarrow i64x2.lt s
'i64x2.gt_s'
                                                 \Rightarrow i64x2.gt_s
'i64x2.le_s'
                                                 \Rightarrow i64x2.le_s
'i64x2.ge_s'
                                                 \Rightarrow i64x2.ge_s
'f32x4.eq'
                                                 \Rightarrow f<sub>32</sub>x<sub>4</sub>.eq
'f32x4.ne'
                                                 \Rightarrow f<sub>32x4.ne</sub>
'f32x4.1t'
                                                 \Rightarrow f<sub>32x4.</sub>lt
'f32x4.gt'
                                                 \Rightarrow f32x4.gt
'f32x4.le'
                                                 \Rightarrow f<sub>32</sub>x<sub>4</sub>.le
'f32x4.ge'
                                                 \Rightarrow f32x4.ge
                                                 \Rightarrow f<sub>64</sub>x<sub>2</sub>.eq
'f64x2.eq'
'f64x2.ne'
                                                 \Rightarrow f<sub>64</sub>x<sub>2</sub>.ne
'f64x2.1t'
                                                 \Rightarrow f<sub>64</sub>x<sub>2</sub>.lt
'f64x2.gt'
                                                 \Rightarrow f64x2.gt
'f64x2.le'
                                                 \Rightarrow f<sub>64</sub>x<sub>2</sub>.le
'f64x2.ge'
                                                 \Rightarrow f64x2.ge
'v128.not'

⇒ v128.not

'v128.and'
                                                 ⇒ v128.and
'v128.andnot'
                                                 ⇒ v128.andnot
'v128.or'

⇒ v128.or

'v128.xor'
                                                 ⇒ v128.xor
'v128.bitselect'
                                                 ⇒ v128.bitselect
'v128.any_true'
                                                 ⇒ v128.any_true
'i8x16.abs'
                                                 ⇒ i8x16.abs
'i8x16.neg'
                                                 ⇒ i8x16.neg
'i8x16.all_true'
                                                 ⇒ i8x16.all_true
'i8x16.bitmask'
                                                 ⇒ i8x16.bitmask
'i8x16.narrow_i16x8_s'
                                                 \Rightarrow i8x16.narrow_i16x8_s
'i8x16.narrow_i16x8_u'
                                                 \Rightarrow i8x16.narrow_i16x8_u
'i8x16.shl'
                                                 \Rightarrow i8x16.shl
'i8x16.shr_s'
                                                 ⇒ i8x16.shr_s
'i8x16.shr u'
                                                 ⇒ i8x16.shr u
'i8x16.add'
                                                 ⇒ i8x16.add
'i8x16.add_sat_s'
                                                 ⇒ i8x16.add_sat_s
'i8x16.add sat u'
                                                 ⇒ i8x16.add sat u
'i8x16.sub'
                                                 ⇒ i8x16.sub
'i8x16.sub_sat_s'
                                                 ⇒ i8x16.sub_sat_s
'i8x16.sub_sat_u'
                                                 ⇒ i8x16.sub_sat_u
'i8x16.min_s'
                                                 ⇒ i8x16.min_s
'i8x16.min_u'
                                                 ⇒ i8x16.min_u
'i8x16.max_s'
                                                 \Rightarrow i8x16.max_s
\verb|`i8x16.max_u'|
                                                 ⇒ i8x16.max_u
'i8x16.avgr u'
                                                 ⇒ i8x16.avgr u
'i8x16.popcnt'
                                                 ⇒ i8x16.popcnt
```

```
'i16x8.abs'
                                       ⇒ i16x8.abs
'i16x8.neg'
                                          i16x8.neg
'i16x8.all true'
                                      ⇒ i16x8.all true
                                      ⇒ i16x8.bitmask
'i16x8.bitmask'
'i16x8.narrow_i32x4_s'
                                      \Rightarrow i16x8.narrow_i32x4_s
'i16x8.narrow_i32x4_u'
                                      ⇒ i16x8.narrow_i32x4_u
'i16x8.extend_low_i8x16_s'
                                      \Rightarrow i16x8.extend low i8x16 s
'i16x8.extend_high_i8x16_s'
                                      ⇒ i16x8.extend_high_i8x16_s
'i16x8.extend_low_i8x16_u'
                                      ⇒ i16x8.extend low i8x16 u
'i16x8.extend_high_i8x16_u'
                                      ⇒ i16x8.extend_high_i8x16_u
'i16x8.shl'
                                      ⇒ i16x8.shl
'i16x8.shr s'
                                      ⇒ i16x8.shr s
                                      ⇒ i16x8.shr_u
'i16x8.shr_u'
'i16x8.add'
                                      ⇒ i16x8.add
'i16x8.add_sat_s'
                                      ⇒ i16x8.add_sat_s
                                      \Rightarrow i16x8.add_sat_u
'i16x8.add_sat_u'
'i16x8.sub'
                                      ⇒ i16x8.sub
'i16x8.sub sat s'
                                      ⇒ i16x8.sub sat s
'i16x8.sub_sat_u'
                                      ⇒ i16x8.sub sat u
'i16x8.mul'
                                      ⇒ i16x8.mul
'i16x8.min s'
                                      ⇒ i16x8.min s
'i16x8.min u'
                                      ⇒ i16x8.min u
                                      ⇒ i16x8.max_s
'i16x8.max s'
'i16x8.max_u'
                                      ⇒ i16x8.max_u
'i16x8.avgr_u'
                                      ⇒ i16x8.avgr_u
'i16x8.q15mulr_sat_s'
                                      ⇒ i16x8.q15mulr sat s
'i16x8.extmul_low_i8x16_s'
                                      \Rightarrow i16x8.extmul_low_i8x16_s
'i16x8.extmul high i8x16 s'
                                      ⇒ i16x8.extmul high i8x16 s
'i16x8.extmul_low_i8x16_u'
                                      ⇒ i16x8.extmul_low_i8x16_u
'i16x8.extmul_high_i8x16_u'
                                      \Rightarrow i16x8.extmul_high_i8x16_u
'i16x8.extadd_pairwise_i8x16_s'
                                      \Rightarrow i16x8.extadd_pairwise_i8x16_s
'i16x8.extadd_pairwise_i8x16_u'
                                      ⇒ i16x8.extadd_pairwise_i8x16_u
'i32x4.abs'
                                      ⇒ i32x4.abs
'i32x4.neg'

⇒ i32x4.neg

'i32x4.all_true'
                                       ⇒ i32x4.all_true
'i32x4.bitmask'
                                      ⇒ i32x4.bitmask
'i32x4.extadd_pairwise_i16x8_s'
                                      ⇒ i32x4.extadd_pairwise_i16x8_s
'i32x4.extadd_pairwise_i16x8_u'
                                      ⇒ i32x4.extadd_pairwise_i16x8_u
'i32x4.extend_low_i16x8_s'
                                      \Rightarrow i32x4.extend_low_i16x8_s
'i32x4.extend_high_i16x8_s'
                                      ⇒ i32x4.extend_high_i16x8_s
'i32x4.extend_low_i16x8_u'
                                      \Rightarrow i32x4.extend_low_i16x8_u
'i32x4.extend_high_i16x8_u'
                                      ⇒ i32x4.extend_high_i16x8_u
'i32x4.shl'
                                      ⇒ i32x4.shl
'i32x4.shr s'
                                      ⇒ i32x4.shr s
'i32x4.shr u'
                                      ⇒ i32x4.shr u
'i32x4.add'
                                      ⇒ i32x4.add
'i32x4.sub'
                                      ⇒ i32x4.sub
'i32x4.mul'
                                      ⇒ i32x4.mul
'i32x4.min_s'
                                      ⇒ i32x4.min_s
i32x4.min_u'
                                      ⇒ i32x4.min_u
                                      ⇒ i32x4.max s
'i32x4.max s'
'i32x4.max u'
                                      ⇒ i32x4.max u
'i32x4.dot_i16x8_s'
                                      \Rightarrow i32x4.dot_i16x8_s
'i32x4.extmul_low_i16x8_s'
                                      \Rightarrow i32x4.extmul_low_i16x8_s
'i32x4.extmul_high_i16x8_s'
                                      \Rightarrow i32x4.extmul_high_i16x8_s
                                      ⇒ i32x4.extmul_low_i16x8_u
'i32x4.extmul_low_i16x8_u'
                                      ⇒ i32x4.extmul_high_i16x8_u
'i32x4.extmul_high_i16x8_u'
```

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```
'i64x2.abs'
                                                   ⇒ i64x2.abs
'i64x2.neg'
                                                   ⇒ i64x2.neg
'i64x2.all_true'
                                                   ⇒ i64x2.all true
                                                   ⇒ i64x2.bitmask
'i64x2.bitmask'
'i64x2.extend_low_i32x4_s'
                                                   ⇒ i64x2.extend_low_i32x4_s
'i64x2.extend_high_i32x4_s'
                                                   ⇒ i64x2.extend_high_i32x4_s
'i64x2.extend low i32x4 u'
                                                   \Rightarrow i<sub>64</sub>x<sub>2</sub>.extend low i<sub>32</sub>x<sub>4</sub> u
'i64x2.extend_high_i32x4_u'
                                                   \Rightarrow i64x2.extend_high_i32x4_u
'i64x2.shl'
                                                   ⇒ i64x2.shl
                                                   ⇒ i64x2.shr_s
'i64x2.shr_s'
'i64x2.shr u'
                                                   ⇒ i64x2.shr u
                                                   \Rightarrow i64x2.add
'i64x2.add'
                                                   ⇒ i64x2.sub
'i64x2.sub'
'i64x2.mul'
                                                   ⇒ i64x2.mul
'i64x2.extmul_low_i32x4_s'
                                                   ⇒ i64x2.extmul_low_i32x4_s
'i64x2.extmul_high_i32x4_s'
                                                   \Rightarrow i64x2.extmul_high_i32x4_s
'i64x2.extmul_low_i32x4_u'
                                                   \Rightarrow i64x2.extmul_low_i32x4_u
'i64x2.extmul_high_i32x4_u'
                                                   ⇒ i64x2.extmul_high_i32x4_u
'f32x4.abs'
                                                   ⇒ f32x4.abs
'f32x4.neg'
                                                   ⇒ f32x4.neg
'f32x4.sqrt'
                                                   \Rightarrow f<sub>32</sub>x<sub>4</sub>.sart
'f32x4.ceil'
                                                   ⇒ f32x4.ceil
                                                   ⇒ f32x4.floor
'f32x4.floor'
'f32x4.trunc'
                                                   ⇒ f32x4.trunc
'f32x4.nearest'
                                                   ⇒ f<sub>32×4</sub>.nearest
                                                   ⇒ f32x4.add
'f32x4.add'
'f32x4.sub'
                                                   ⇒ f32x4.sub
'f32x4.mul'
                                                   ⇒ f<sub>32</sub>x<sub>4</sub>.mul
                                                   ⇒ f<sub>32</sub>x<sub>4</sub>.div
'f32x4.div'
                                                   ⇒ f<sub>32x4</sub>.min
'f32x4.min'
'f32x4.max'
                                                   ⇒ f32x4.max
'f32x4.pmin'
                                                   ⇒ f<sub>32</sub>x<sub>4</sub>.pmin
'f32x4.pmax'
                                                   ⇒ f32x4.pmax
'f64x2.abs'
                                                   \Rightarrow f<sub>64</sub>x<sub>2</sub>.abs
'f64x2.neg'
                                                   ⇒ f64x2.neg
'f64x2.sqrt'
                                                   \Rightarrow f<sub>64</sub>x<sub>2</sub>.sqrt
'f64x2.ceil'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>.ceil
                                                   \Rightarrow f<sub>64</sub>x<sub>2</sub>.floor
'f64x2.floor'
'f64x2.trunc'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>.trunc
'f64x2.nearest'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>.nearest
'f64x2.add'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>,add
'f64x2.sub'
                                                   \Rightarrow f<sub>64</sub>x<sub>2</sub>.sub
'f64x2.mul'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>.mul
                                                   ⇒ f<sub>64</sub>x2.div
'f64x2.div'
'f64x2.min'
                                                   \Rightarrow f<sub>64</sub>x<sub>2</sub>.min
'f64x2.max'
                                                   \Rightarrow f<sub>64</sub>x<sub>2</sub>.max
'f64x2.pmin'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>.pmin
'f64x2.pmax'
                                                   ⇒ f<sub>64</sub>x<sub>2</sub>.pmax
```

```
'i32x4.trunc_sat_f32x4_s'
                                        ⇒ i32x4.trunc_sat_f32x4_s
'i32x4.trunc_sat_f32x4_u'
                                         ⇒ i32x4.trunc_sat_f32x4_u
'i32x4.trunc_sat_f64x2_s_zero'
'i32x4.trunc_sat_f64x2_u_zero'
                                       ⇒ i32x4.trunc_sat_f64x2_s_zero
                                       ⇒ i32x4.trunc_sat_f64x2_u_zero
'f32x4.convert_i32x4_s'
                                        \Rightarrow f<sub>32x4</sub>.convert_i32x4_s
'f32x4.convert_i32x4_u'
                                        \Rightarrow f<sub>32×4</sub>.convert_i32×4_u
                                       \Rightarrow f<sub>64×2</sub>.convert low i32×4 s
'f64x2.convert low i32x4 s'
                                    ⇒ f<sub>64x2</sub>.convert_low_i32x4_u
'f64x2.convert_low_i32x4_u'
                                        \Rightarrow f<sub>32×4</sub>.demote f64×2 zero
'f32x4.demote f64x2 zero'
'f64x2.promote_low_f32x4'
                                        \Rightarrow f<sub>64x2</sub>.promote_low_f<sub>32x4</sub>
'i16x8.relaxed swizzle'
                                              ⇒ i16x8.relaxed swizzle
'i32x4.relaxed_trunc_f32x4_s'
'i32x4.relaxed_trunc_f32x4_u'
                                                  i32x4.relaxed trunc f32x4 s
                                             ⇒ i32x4.relaxed trunc f32x4 u
                                             ⇒ i32x4.relaxed_trunc_f32x4_s_zero
'i32x4.relaxed_trunc_f32x4_s_zero'
                                            ⇒ i32x4.relaxed_trunc_f32x4_u_zero
'i32x4.relaxed_trunc_f32x4_u_zero'
'f32x4.relaxed_madd'
                                             ⇒ f32x4.relaxed_madd
'f32x4.relaxed nmadd'
                                             ⇒ f32x4.relaxed nmadd
                                             ⇒ f64x2.relaxed_madd
'f64x2.relaxed_madd'
'f64x2.relaxed_nmadd'
                                             ⇒ f<sub>64</sub>×2.relaxed nmadd
'i8x16.relaxed laneselect'
                                             ⇒ i8x16.relaxed laneselect
'i16x8.relaxed laneselect'
                                             ⇒ i16x8.relaxed laneselect
                                             ⇒ i32x4.relaxed laneselect
'i32x4.relaxed_laneselect'
                                            ⇒ i64x2.relaxed laneselect
'i64x2.relaxed_laneselect'
'f32x4.relaxed min'
                                             ⇒ f32x4.relaxed min
'f32x4.relaxed max'
                                             ⇒ f32x4.relaxed max
'f64x2.relaxed_min'
                                             ⇒ f<sub>64</sub>x<sub>2</sub>.relaxed_min
'f64x2.relaxed_max'
                                             ⇒ f<sub>64</sub>x<sub>2</sub>.relaxed max
'i16x8.relaxed_q15mulr_s'
                                             ⇒ i16x8.relaxed q15mulr s
'i16x8.relaxed_dot i8x16 i7x16 s' \Rightarrow i16x8.relaxed_dot i8x16 i7x16 s
'i16x8.relaxed dot i8x16 i7x16 add s' \Rightarrow i16x8.relaxed dot i8x16 i7x16 add s
```

#### 6.5.10 Folded Instructions

Instructions can be written as S-expressions by grouping them into *folded* form. In that notation, an instruction is wrapped in parentheses and optionally includes nested folded instructions to indicate its operands.

In the case of block instructions, the folded form omits the 'end' delimiter. For if instructions, both branches have to be wrapped into nested S-expressions, headed by the keywords 'then' and 'else'.

The set of all phrases defined by the following abbreviations recursively forms the auxiliary syntactic class foldedinstr. Such a folded instruction can appear anywhere a regular instruction can.

```
'('plaininstr foldedinstr*')' \equiv foldedinstr* plaininstr \equiv 'block' label blocktype instr* '('block' label blocktype instr*')' \equiv 'block' label blocktype instr* 'end' \equiv 'loop' label blocktype instr* 'end' \equiv '('if' label blocktype foldedinstr* ('then' instr*')' ('('else' instr*')')' ')' \equiv foldedinstr* 'if' label blocktype catch* instr*')' \equiv 'try_table' label blocktype catch* instr* 'ond'
```

### Note

```
For example, the instruction sequence (\texttt{local.get} \ \$\texttt{x}) \ (\texttt{i32.const} \ 2) \ \texttt{i32.add} \ (\texttt{i32.const} \ 3) \ \texttt{i32.mul}
```

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```
can be folded into  ({\tt i32.mul}\;({\tt i32.add}\;({\tt local.get}\;\$x)\;({\tt i32.const}\;2))\;({\tt i32.const}\;3))  Folded instructions are solely syntactic sugar, no additional syntactic or type-based checking is implied.
```

# 6.5.11 Expressions

Expressions are written as instruction sequences. No explicit 'end' keyword is included, since they only occur in bracketed positions.

```
expr_I ::= (in:instr_I)^* \Rightarrow in^* end
```

# 6.6 Modules

### 6.6.1 Indices

Indices can be given either in raw numeric form or as symbolic identifiers when bound by a respective construct. Such identifiers are looked up in the suitable space of the identifier context I.

```
\mathsf{typeidx}_I
                 ::= x:u32 \Rightarrow
                       v\mathtt{:id}
                                      x (if I.types[x] = v)
                  \Rightarrow
funcidx,
                 ::= x:u32 \Rightarrow
                 v:id \Rightarrow x \text{ (if } I.funcs[x] = v)
               ::= x:u32 \Rightarrow x
tableidx_I
                 v:id \Rightarrow x \text{ (if } I.tables[x] = v)
memidx_I
                 ::= x:u32 \Rightarrow x
                        v:id \Rightarrow x \quad (if I.mems[x] = v)
                  globalidx_I ::= x:u32 \Rightarrow x
                        v{:}\mathtt{id}
                                 \Rightarrow x \text{ (if } I.\text{globals}[x] = v)
tagidx_I
                 ::=
                        x:u32 \Rightarrow x
                        v:id \Rightarrow x \text{ (if } I.tags[x] = v)
                  ::= x:u32 \Rightarrow x
elemidx_I
                        v:id \Rightarrow x \quad (if \ I.elem[x] = v)
                  \mathtt{dataidx}_I
                 ::= x:u32 \Rightarrow x
                  v:id \Rightarrow x \text{ (if } I.data[x] = v)
localidx_I
                 ::= x:u32 \Rightarrow x
                       v:id \Rightarrow x \quad (if I.locals[x] = v)
                  labelidx_I
                 ::= l:u32
                                 \Rightarrow l
                 v:id \Rightarrow l \text{ (if } I.labels[l] = v)
fieldidx_{I,x} ::= i:u32 \Rightarrow i
                        v:id
                                 \Rightarrow i (if I.fields[x][i] = v)
```

# 6.6.2 Type Uses

A *type use* is a reference to a function type definition. It may optionally be augmented by explicit inlined parameter and result declarations. That allows binding symbolic identifiers to name the local indices of parameters. If inline declarations are given, then their types must match the referenced function type.

#### Note

If inline declarations are given, their types must be *syntactically* equal to the types from the indexed definition; possible type substitutions from other definitions that might make them equal are not taken into account. This is to simplify syntactic pre-processing.

The synthesized attribute of a typeuse is a pair consisting of both the used type index and the local identifier context containing possible parameter identifiers. The following auxiliary function extracts optional identifiers from parameters:

$$id('(''param'id''...')') = id''$$

#### Note

Both productions overlap for the case that the function type is  $[] \rightarrow []$ . However, in that case, they also produce the same results, so that the choice is immaterial.

The well-formedness condition on I' ensures that the parameters do not contain duplicate identifiers.

#### **Abbreviations**

A typeuse may also be replaced entirely by inline parameter and result declarations. In that case, a type index is automatically inserted:

```
(t_1:param)^* (t_2:result)^* \equiv '(''type' x')' param* result*
```

where x is the smallest existing type index whose recursive type definition in the current module is of the form

```
'(' 'rec' '(' 'type' '(' 'sub' 'final' '(' 'func' param* result* ')' ')' ')'
```

If no such index exists, then a new recursive type of the same form is inserted at the end of the module.

Abbreviations are expanded in the order they appear, such that previously inserted type definitions are reused by consecutive expansions.

# 6.6.3 Imports

The descriptors in imports can bind a symbolic function, table, memory, tag, or global identifier.

```
\begin{array}{lll} \operatorname{import}_I & ::= & \text{`('`import' $mod$:name $nm$:name $d$:importdesc}_I \text{`)'} \\ & \Rightarrow & \{ \operatorname{module $mod$, name $nm$, desc $d$} \} \\ \operatorname{importdesc}_I & ::= & \text{`('`func' id}^? $x, I'$:typeuse}_I \text{`)'} & \Rightarrow & \operatorname{func $x$} \\ & & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ &
```

## **Abbreviations**

As an abbreviation, imports may also be specified inline with function, table, memory, global, or tag definitions; see the respective sections.

# 6.6.4 Functions

Function definitions can bind a symbolic function identifier, and local identifiers for its parameters and locals.

```
\begin{array}{lll} \text{func}_I & ::= & \text{`('`func' id}^? \ x, I': \text{typeuse}_I \ (loc: \text{local}_I)^* \ (in: \text{instr}_{I''})^* \ `)' \\ & \Rightarrow & \{ \text{type} \ x, \text{locals} \ loc^*, \text{body} \ in^* \ \text{end} \} \\ & & (\text{if} \ I'' = I \oplus I' \oplus \{ \text{locals} \ \text{id}(\text{local})^* \} \ \text{well-formed}) \\ & \text{local}_I \ ::= & \text{`('`local' id}^? \ t: \text{valtype}_I \ `)' \ \Rightarrow \ \{ \text{type} \ t \} \end{array}
```

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The definition of the local identifier context I'' uses the following auxiliary function to extract optional identifiers from locals:

$$id('('') cal' id'' ... ')') = id''$$

#### Note

The well-formedness condition on I'' ensures that parameters and locals do not contain duplicate identifiers.

#### **Abbreviations**

Multiple anonymous locals may be combined into a single declaration:

```
'(' 'local' valtype^* ')' \equiv ('(' 'local' valtype ')')^*
```

Functions can be defined as imports or exports inline:

```
'(' 'func' id' '(' 'import' name_1 name_2 ')' typeuse ')' \equiv '(' 'import' name_1 name_2 '(' 'func' id' typeuse ')' ')'
'(' 'func' id' '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'func' id' ')' '(' 'func' id' ... ')'
(if\ id' \neq \epsilon \wedge id' = id! \vee\ id! = \epsilon \wedge id' fresh)
```

#### Note

The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a function declaration can contain any number of exports, possibly followed by an import.

### **6.6.5 Tables**

Table definitions can bind a symbolic table identifier.

```
table_I ::= '(' 'table' id' tt:tabletype_I e:expr_I ')' \Rightarrow \{type tt, init e\}
```

#### **Abbreviations**

A table's initialization expression can be omitted, in which case it defaults to ref.null:

```
'(' 'table' id' tabletype ')' \equiv '(' 'table' id' tabletype '(' ref.null ht ')' ')' (if tabletype = limits '(' 'ref' 'null'' ht ')')
```

An element segment can be given inline with a table definition, in which case its offset is 0 and the limits of the table type are inferred from the length of the given segment:

```
'(''table' id' addrtype' reftype '(''elem' expr^n:list(elemexpr)')'')' \equiv '(''table' id' addrtype' n n reftype')' '(''elem' '(''table' id'')' '('addrtype'.const''0'')' reftype list(elemexpr)')' (if id^? \neq \epsilon \wedge id' = id^? \vee id^? = \epsilon \wedge id' fresh, if addrtype? \neq \epsilon \wedge addrtype' = addrtype? \vee addrtype? \neq \epsilon \wedge addrtype' = 'i32') '(''table' id' addrtype' reftype '(''elem' x^n:list(funcidx)')'')' \equiv '(''table' id' addrtype' n n reftype')' '(''elem' '(''table' id'')' '('addrtype''.const''0'')' reftype list('(''ref.func' funcidx')')'' (if id^? \neq \epsilon \wedge id' = id^? \vee id^? = \epsilon \wedge id' fresh, if addrtype? \neq \epsilon \wedge addrtype' = addrtype? \neq \epsilon \wedge addrtype' = 'i32')
```

Tables can be defined as imports or exports inline:

```
'(' 'table' id? '(' 'import' name<sub>1</sub> name<sub>2</sub> ')' tabletype ')' \equiv '(' 'import' name<sub>1</sub> name<sub>2</sub> '(' 'table' id? tabletype ')' ')' '(' 'table' id? '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'table' id' ')' ')' '(' 'table' id' ... ')' (if id? \neq \epsilon \land id' = id? \lor id? = \epsilon \land id' fresh)
```

#### Note

The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a table declaration can contain any number of exports, possibly followed by an import.

# 6.6.6 Memories

Memory definitions can bind a symbolic memory identifier.

```
mem_I ::= '('memory'id' mt:memtype_I')' \Rightarrow \{type mt\}
```

### **Abbreviations**

A data segment can be given inline with a memory definition, in which case its offset is 0 and the limits of the memory type are inferred from the length of the data, rounded up to page size:

Memories can be defined as imports or exports inline:

```
'(' 'memory' id? '(' 'import' name_1 name_2 ')' memtype ')' \equiv '(' 'import' name_1 name_2 '(' 'memory' id? memtype ')' ')' '(' 'memory' id? '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'memory' id' ')' ')' '(' 'memory' id' ... ')' (\text{if id}^? \neq \epsilon \wedge \text{id}' = \text{id}^? \vee \text{id}^? = \epsilon \wedge \text{id}' \text{ fresh})
```

### Note

The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a memory declaration can contain any number of exports, possibly followed by an import.

## 6.6.7 Globals

Global definitions can bind a symbolic global identifier.

```
global<sub>I</sub> ::= '(' 'global' id' qt:globaltype<sub>I</sub> e:expr<sub>I</sub> ')' \Rightarrow {type qt, init e}
```

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### **Abbreviations**

Globals can be defined as imports or exports inline:

```
'(' 'global' id' '(' 'import' name<sub>1</sub> name<sub>2</sub> ')' globaltype ')' \equiv '(' 'import' name<sub>1</sub> name<sub>2</sub> '(' 'global' id' globaltype ')' ')' '(' 'global' id' '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'global' id' ')' ')' '(' 'global' id' ... ')' (if id' \neq \epsilon \land id' = id' \lor id' = \epsilon \land id' fresh)
```

#### Note

The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a global declaration can contain any number of exports, possibly followed by an import.

# 6.6.8 Tags

An tag definition can bind a symbolic tag identifier.

```
\begin{array}{rcl} \mathsf{tag}_I & ::= & \text{`('`tag' id}^? \ x, I' : \mathsf{typeuse}_I \text{`)'} \\ & \Rightarrow & \{\mathsf{type} \ x\} \end{array}
```

#### **Abbreviations**

Tags can be defined as imports or exports inline:

```
'(' 'tag' id' '(' 'import' name_1 name_2 ')' typeuse ')' \equiv '(' 'import' name_1 name_2 '(' 'tag' id' typeuse ')' ')' 
'(' 'tag' id' '(' 'export' name ')' ... ')' \equiv '(' 'export' name '(' 'tag' id' ')' ')' '(' 'tag' id' ... ')' 
(if id' \neq \epsilon \land id' = id' \lor id' = \epsilon \land id' fresh)
```

#### Note

The latter abbreviation can be applied repeatedly, if "..." contains additional export clauses. Consequently, a memory declaration can contain any number of exports, possibly followed by an import.

# 6.6.9 Exports

The syntax for exports mirrors their abstract syntax directly.

# **Abbreviations**

As an abbreviation, exports may also be specified inline with function, table, memory, global, or tag definitions; see the respective sections.

### 6.6.10 Start Function

A start function is defined in terms of its index.

```
start_I ::= '('start' x:funcidx_I')' \Rightarrow \{func x\}
```

#### Note

At most one start function may occur in a module, which is ensured by a suitable side condition on the module grammar.

# 6.6.11 Element Segments

Element segments allow for an optional table index to identify the table to initialize.

```
\begin{array}{lll} \text{elem}_I & ::= & \text{`('`elem' id}^? \ (et,y^*) : elemlist_I \ ')'} \\ & \Rightarrow & \{ \text{type } et, \text{init } y^*, \text{mode passive} \} \\ & | & \text{`('`elem' id}^? \ x : \text{tableuse}_I \ `(' \text{`offset'} \ e : \text{expr}_I \ `)' \ (et,y^*) : elemlist_I \ `)'} \\ & \Rightarrow & \{ \text{type } et, \text{init } y^*, \text{mode active } \{ \text{table } x, \text{offset } e \} \} \\ & \text{`('`elem' id}^? \ `declare' \ (et,y^*) : elemlist_I \ `)'} \\ & \Rightarrow & \{ \text{type } et, \text{init } y^*, \text{mode declare} \} \\ & \text{elemlist}_I \ ::= \ t : \text{reftype}_I \ y^* : \text{list}(\text{elemexpr}_I) \ \Rightarrow \ (\text{type } t, \text{init } y^*) \\ & \text{elemexpr}_I \ ::= \ `(' \text{`item' } e : \text{expr}_I \ `)' \ \Rightarrow \ e \\ & \text{tableuse}_I \ ::= \ `(' \text{`table'} \ x : \text{tableidx}_I \ `)' \ \Rightarrow \ x \\ \end{array}
```

#### **Abbreviations**

As an abbreviation, a single instruction may occur in place of the offset of an active element segment or as an element expression:

```
'('instr')' \equiv '('offset'instr')'
'('instr')' \equiv '('item'instr')'
```

Also, the element list may be written as just a sequence of function indices:

```
'func' list(funcidx<sub>I</sub>) \equiv '(ref' 'func)' list('(' 'ref.func' funcidx<sub>I</sub> ')')
```

A table use can be omitted, defaulting to 0. Furthermore, for backwards compatibility with earlier versions of WebAssembly, if the table use is omitted, the 'func' keyword can be omitted as well.

```
 \epsilon \\ \text{`('`table' '0' ')'} \\ \text{`('`fable' '0' ')'} \\ \equiv \text{`('`table' '0' ')'} \\ \text{`('`table' '0' ')'}
```

As another abbreviation, element segments may also be specified inline with table definitions; see the respective section.

# 6.6.12 Data Segments

Data segments allow for an optional memory index to identify the memory to initialize. The data is written as a string, which may be split up into a possibly empty sequence of individual string literals.

```
\begin{array}{lll} \operatorname{data}_I & ::= & \text{`(``data' id}^? \ b^*: \operatorname{datastring')'} \\ & \Rightarrow & \{\operatorname{init} b^*, \operatorname{mode passive}\} \\ & | & \text{`(``data' id}^? \ x : \operatorname{memuse}_I \ `(``\operatorname{offset'} \ e : \operatorname{expr}_I \ `)` \ b^*: \operatorname{datastring'})' \\ & \Rightarrow & \{\operatorname{init} b^*, \operatorname{mode active} \{\operatorname{memory} \ x', \operatorname{offset} \ e\}\} \\ \operatorname{datastring} & ::= & (b^*: \operatorname{string})^* & \Rightarrow & \bigoplus ((b^*)^*) \\ \operatorname{memuse}_I & ::= & \text{`(``memory'} \ x : \operatorname{memidx}_I \ `)` & \Rightarrow \ x \\ \end{array}
```

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#### Note

In the current version of WebAssembly, the only valid memory index is 0 or a symbolic memory identifier resolving to the same value.

#### **Abbreviations**

As an abbreviation, a single instruction may occur in place of the offset of an active data segment:

```
'('instr')' \equiv '('offset' instr')'
```

Also, a memory use can be omitted, defaulting to 0.

```
\epsilon \equiv \text{`('`memory'`0'')'}
```

As another abbreviation, data segments may also be specified inline with memory definitions; see the respective section.

### **6.6.13 Modules**

A module consists of a sequence of fields that can occur in any order. All definitions and their respective bound identifiers scope over the entire module, including the text preceding them.

A module may optionally bind an identifier that names the module. The name serves a documentary role only.

#### Note

Tools may include the module name in the name section of the binary format.

```
::= '('module' id' (m:modulefield<sub>I</sub>)*')'
module
                                                                                         \bigoplus m^*
                                 (if I = \bigoplus idc(modulefield)^* well-formed)
modulefield_I ::= ty^*:rectype_I \Rightarrow \{types ty^*\}
                           im:import_I \Rightarrow \{imports im\}
                           fn: func_I \rightarrow {tables ta}
me: mem_I \Rightarrow {mems me}
                           fn: \mathtt{func}_I
                                             \Rightarrow {funcs fn}
                           gl: global_I \Rightarrow \{globals gl\}
                           tg: tag_I \Rightarrow \{tags \ tg\}
                           el:elem_I
                                             \Rightarrow {elems el}
                           da:data_I
                                             \Rightarrow \{ datas da \}
                           st:start_I
                                            \Rightarrow {start st}
                           ex:export_I \Rightarrow \{exports \ ex\}
```

The following restrictions are imposed on the composition of modules:  $m_1 \oplus m_2$  is defined if and only if

- $m_1.\mathsf{start} = \epsilon \lor m_2.\mathsf{start} = \epsilon$
- $m_1$ .funcs =  $m_1$ .tables =  $m_1$ .mems =  $m_1$ .globals =  $m_1$ .tags =  $\epsilon \vee m_2$ .imports =  $\epsilon$

#### Note

The first condition ensures that there is at most one start function. The second condition enforces that all imports must occur before any regular definition of a function, table, memory, global, or tag, thereby maintaining the ordering of the respective index spaces.

The well-formedness condition on I in the grammar for module ensures that no namespace contains duplicate identifiers.

The definition of the initial identifier context I uses the following auxiliary definition which maps each relevant definition to a singular context with one (possibly empty) identifier:

```
\begin{array}{l} \mathrm{idc}(\textrm{`('' 'rec' typedef* ')')} \\ \mathrm{idc}(\textrm{`('' 'type'} \ v^?:id^? \ \mathrm{subtype ')')} \\ \mathrm{idc}(\textrm{`('' 'func'} \ v^?:id^? \dots ')') \end{array}
                                                                                                              \bigoplus idc(typedef)^*
                                                                                                     = \{ \text{types } (v^2), \text{ fields idf(subtype)}, \text{ typedefs } st \}
                                                                                                     = \{funcs (v^?)\}
idc(`(``table' v^?:id^? ...`)')
                                                                                                     = {tables (v^?)}
idc('(' 'memory' v^?:id^? ... ')')
                                                                                                     = {mems (v^?)}
\begin{array}{l} \operatorname{idc}((\text{ `memory } v . \operatorname{id} \ldots )) \\ \operatorname{idc}((', \operatorname{`global'} v^? : \operatorname{id}^? \ldots ')') \\ \operatorname{idc}((', \operatorname{`tag'} v^? : \operatorname{id}^? \ldots ')') \\ \operatorname{idc}((', \operatorname{`global'} v^? : \operatorname{id}^? \ldots ')') \\ \operatorname{idc}((', \operatorname{`data'} v^? : \operatorname{id}^? \ldots ')') \end{array}
                                                                                                     = \{globals (v^?)\}
                                                                                                              \{tags(v^?)\}
                                                                                                              \{\text{elem }(v^?)\}
                                                                                                     = \{ data(v^?) \}
\operatorname{idc}('(', 'import', ..., '(', 'func', v^?:id^?, ..., ')', ')')) = \{funcs(v^?)\}
idc('(', 'import' ... '(', 'table' v':id' ... ')', ')') = \{tables(v', ')\}
idc('(', 'import', ..., '(', 'memory', v':id', ..., ')', ')') = \{mems(v', ')\}
idf('(' 'sub' ... comptype ')')
                                                                                                     = idf(comptype)
idf('(' 'struct' Tfield* ')')
idf('(' 'array' ... ')')
idf('(' 'func' ... ')')
                                                                                                     = \bigoplus idf(field)^*
                                                                                                      = \epsilon
idf('(''field'v'':id''...')')
                                                                                                     = v^{?}
```

### **Abbreviations**

In a source file, the toplevel (module ...) surrounding the module body may be omitted.

```
modulefield* \equiv '(''module' modulefield*')'
```

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**Appendix** 

# 7.1 Embedding

A WebAssembly implementation will typically be *embedded* into a *host* environment. An *embedder* implements the connection between such a host environment and the WebAssembly semantics as defined in the main body of this specification. An embedder is expected to interact with the semantics in well-defined ways.

This section defines a suitable interface to the WebAssembly semantics in the form of entry points through which an embedder can access it. The interface is intended to be complete, in the sense that an embedder does not need to reference other functional parts of the WebAssembly specification directly.

### Note

On the other hand, an embedder does not need to provide the host environment with access to all functionality defined in this interface. For example, an implementation may not support parsing of the text format.

# **7.1.1 Types**

In the description of the embedder interface, syntactic classes from the abstract syntax and the runtime's abstract machine are used as names for variables that range over the possible objects from that class. Hence, these syntactic classes can also be interpreted as types.

For numeric parameters, notation like i:u64 is used to specify a symbolic name in addition to the respective value range.

### 7.1.2 Booleans

Interface operation that are predicates return Boolean values:

```
bool ::= false \mid true
```

# 7.1.3 Exceptions and Errors

Invoking an exported function may throw or propagate exceptions, expressed by an auxiliary syntactic class:

```
exception ::= exception exnaddr
```

The exception address exnaddr identifies the exception thrown.

Failure of an interface operation is also indicated by an auxiliary syntactic class:

```
error ::= error
```

In addition to the error conditions specified explicitly in this section, such as invalid arguments or exceptions and traps resulting from execution, implementations may also return errors when specific implementation limitations are reached.

#### Note

Errors are abstract and unspecific with this definition. Implementations can refine it to carry suitable classifications and diagnostic messages.

# 7.1.4 Pre- and Post-Conditions

Some operations state *pre-conditions* about their arguments or *post-conditions* about their results. It is the embedder's responsibility to meet the pre-conditions. If it does, the post conditions are guaranteed by the semantics.

In addition to pre- and post-conditions explicitly stated with each operation, the specification adopts the following conventions for runtime objects (*store*, *moduleinst*, addresses):

- Every runtime object passed as a parameter must be valid per an implicit pre-condition.
- Every runtime object returned as a result is valid per an implicit post-condition.

#### Note

As long as an embedder treats runtime objects as abstract and only creates and manipulates them through the interface defined here, all implicit pre-conditions are automatically met.

# 7.1.5 Store

```
store_init(): store
```

1. Return the empty store.

```
store_init() = \{\}
```

# 7.1.6 Modules

 $module\_decode(byte^*) : module \mid error$ 

- 1. If there exists a derivation for the byte sequence  $byte^*$  as a module according to the binary grammar for modules, yielding a module m, then return m.
- 2. Else, return error.

```
\begin{array}{lll} \operatorname{module\_decode}(b^*) & = & m & \quad (\operatorname{if} \operatorname{module} \stackrel{*}{\Longrightarrow} m : b^*) \\ \operatorname{module\_decode}(b^*) & = & \operatorname{error} & \quad (\operatorname{otherwise}) \end{array}
```

 $module\_parse(char^*) : module \mid error$ 

- 1. If there exists a derivation for the source  $char^*$  as a module according to the text grammar for modules, yielding a module m, then return m.
- 2. Else, return error.

```
\begin{array}{lll} \operatorname{module\_parse}(c^*) & = & m & \quad (\text{if module} \overset{*}{\Longrightarrow} m {:} c^*) \\ \operatorname{module\_parse}(c^*) & = & \operatorname{error} & \quad (\text{otherwise}) \end{array}
```

 $module validate(module) : error^?$ 

- 1. If *module* is valid, then return nothing.
- 2. Else, return error.

```
module_validate(m) = \epsilon (if \vdash m : externtype^* \to externtype'^*) module_validate(m) = error (otherwise)
```

module instantiate(store, module,  $externaddr^*$ ): (store, moduleinst | exception | error)

- 1. Try instantiating module in store with external addresses  $externaddr^*$  as imports:
- a. If it succeeds with a module instance moduleinst, then let result be moduleinst.
- b. Else, let *result* be error.
- 2. Return the new store paired with result.

```
\begin{array}{lll} \text{module\_instantiate}(S,m,ev^*) & = & (S',F.\mathsf{module}) & \text{(if instantiate}(S,m,ev^*) \hookrightarrow {}^*S';F;\epsilon) \\ \text{module\_instantiate}(S,m,ev^*) & = & (S',\mathsf{error}) & \text{(otherwise, if instantiate}(S,m,ev^*) \hookrightarrow {}^*S';F;\mathit{result}) \end{array}
```

#### Note

The store may be modified even in case of an error.

 $module\_imports(module) : (name, name, externtype)^*$ 

- 1. Pre-condition: module is valid with the external import types externtype\* and external export types externtype'\*.
- 2. Let  $import^*$  be the imports module.imports.
- 3. Assert: the length of  $import^*$  equals the length of  $externtype^*$ .
- 4. For each  $import_i$  in  $import^*$  and corresponding  $externtype_i$  in  $externtype^*$ , do:
- a. Let  $result_i$  be the triple  $(import_i.module, import_i.name, externtype_i)$ .
- 5. Return the concatenation of all  $result_i$ , in index order.
- 6. Post-condition: each  $externtype_i$  is valid under the empty context.

```
module\_imports(m) = (im.module, im.name, externtype)^* 
(if im^* = m.imports \land \vdash m : externtype^* \rightarrow externtype'^*)
```

module exports(module): (name, externtype)\*

- 1. Pre-condition: *module* is valid with the external import types *externtype*\* and external export types *externtype*'\*.
- 2. Let  $export^*$  be the exports module.exports.
- 3. Assert: the length of export\* equals the length of externtype'\*.
- 4. For each export<sub>i</sub> in export<sup>\*</sup> and corresponding externtype'<sub>i</sub> in externtype'<sup>\*</sup>, do:
- a. Let  $result_i$  be the pair ( $export_i$ .name,  $externtype'_i$ ).
- 5. Return the concatenation of all  $result_i$ , in index order.
- 6. Post-condition: each externtype' is valid under the empty context.

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# 7.1.7 Module Instances

instance export(moduleinst, name):  $externaddr \mid error$ 

- 1. Assert: due to validity of the module instance *moduleinst*, all its export names are different.
- 2. If there exists an exportins  $t_i$  in module inst. exports such that name exportins  $t_i$  name equals name, then:
  - a. Return the external address  $exportinst_i$ .addr.
- 3. Else, return error.

```
instance\_export(m, name) = m.exports[i].addr (if m.exports[i].name = name) instance\_export(m, name) = error (otherwise)
```

### 7.1.8 Functions

 $func\_alloc(store, functype, hostfunc) : (store, funcaddr)$ 

- 1. Pre-condition: the *functype* is valid under the empty context.
  - 2. Let *funcaddr* be the result of allocating a host function in *store* with function type *functype*, host function code *hostfunc* and an empty module instance.
  - 3. Return the new store paired with *funcaddr*.

```
 \begin{aligned} \text{func\_alloc}(S, \textit{ft}, \textit{code}) &=& (S', a) \end{aligned} & ( \begin{aligned} & \text{if } \textit{dt} = (\text{rec } (\text{func } \textit{ft})).0 \\ & \land \text{alloc}(S, \textit{dt}, \textit{code}, \{\}) = S', a) \end{aligned}
```

### Note

This operation assumes that hostfunc satisfies the pre- and post-conditions required for a function instance with type functype.

Regular (non-host) function instances can only be created indirectly through module instantiation.

 $func\_type(store, funcaddr) : functype$ 

- 1. Let functype be the function type S.funcs[a].type.
- 2. Return functype.
- 3. Post-condition: the returned function type is valid.

```
func\_type(S, a) = S.funcs[a].type
```

 $func_invoke(store, funcaddr, val^*) : (store, val^* \mid exception \mid error)$ 

- 1. Try invoking the function funcaddr in store with values  $val^*$  as arguments:
- a. If it succeeds with values  $val'^*$  as results, then let result be  $val'^*$ .
- b. Else if the outcome is an exception with a thrown exception ref.exn exnaddr as the result, then let result be exception exnaddr
- c. Else it has trapped, hence let result be error.

2. Return the new store paired with result.

```
\begin{array}{lll} \mathrm{func\_invoke}(S,a,v^*) &=& (S',v'^*) & \text{ (if invoke}(S,a,v^*) \hookrightarrow {}^*S';F;v'^*) \\ \mathrm{func\_invoke}(S,a,v^*) &=& (S',\operatorname{exception}\,a') & \text{ (if invoke}(S,a,v^*) \hookrightarrow {}^*S';F;(\operatorname{ref.exn}\,a')\operatorname{throw\_ref} \\ \mathrm{func\_invoke}(S,a,v^*) &=& (S',\operatorname{error}) & \text{ (if invoke}(S,a,v^*) \hookrightarrow {}^*S';F;\operatorname{trap}) \end{array}
```

#### Note

The store may be modified even in case of an error.

# **7.1.9 Tables**

 $table\_alloc(store, tabletype, ref) : (store, tableaddr)$ 

- 1. Pre-condition: the *tabletype* is valid under the empty context.
- 2. Let tableaddr be the result of allocating a table in store with table type tabletype and initialization value ref.
- 3. Return the new store paired with tableaddr.

```
table_alloc(S, tt, r) = (S', a) (if alloctable(S, tt, r) = S', a)
```

 $table\_type(store, tableaddr) : tabletype$ 

- 1. Return S.tables[a].type.
- 2. Post-condition: the returned table type is valid under the empty context.

$$table\_type(S, a) = S.tables[a].type$$

 $table\_read(store, tableaddr, i : u64) : ref \mid error$ 

- 1. Let ti be the table instance store.tables[tableaddr].
- 2. If i is larger than or equal to the length of ti.elem, then return error.
- 3. Else, return the reference value ti.elem[i].

```
 \begin{array}{lll} {\rm table\_read}(S,a,i) & = & r & \quad & ({\rm if} \; S. {\rm tables}[a]. {\rm elem}[i] = r) \\ {\rm table\_read}(S,a,i) & = & {\rm error} & \quad & ({\rm otherwise}) \\ \end{array}
```

 $table\_write(store, tableaddr, i : u64, ref) : store \mid error$ 

- 1. Let ti be the table instance store.tables[tableaddr].
- 2. If i is larger than or equal to the length of ti.elem, then return error.
- 3. Replace ti.elem[i] with the reference value ref.
- 4. Return the updated store.

```
\begin{array}{lll} {\rm table\_write}(S,a,i,r) &=& S' & \quad & ({\rm if}\ S'=S\ {\rm with}\ {\rm tables}[a].{\rm elem}[i]=r) \\ {\rm table\_write}(S,a,i,r) &=& {\rm error} & \quad & ({\rm otherwise}) \end{array}
```

 $table\_size(store, tableaddr) : u64$ 

1. Return the length of *store*.tables[tableaddr].elem.

```
table\_size(S, a) = n (if |S.tables[a].elem| = n)
```

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 $table\_grow(store, tableaddr, n : u64, ref) : store \mid error$ 

- 1. Try growing the table instance store.tables[tableaddr] by n elements with initialization value ref:
  - a. If it succeeds, return the updated store.
  - b. Else, return error.

```
\begin{array}{lll} {\rm table\_grow}(S,a,n,r) &=& S' & \text{ (if } S'=S \text{ with } {\rm tables}[a] = {\rm growtable}(S.{\rm tables}[a],n,r)) \\ {\rm table\_grow}(S,a,n,r) &=& {\rm error} & \text{ (otherwise)} \end{array}
```

# 7.1.10 Memories

 $mem\_alloc(store, memtype) : (store, memaddr)$ 

- 1. Pre-condition: the *memtype* is valid under the empty context.
- 2. Let memaddr be the result of allocating a memory in store with memory type memtype.
- 3. Return the new store paired with *memaddr*.

$$\operatorname{mem\_alloc}(S, mt) = (S', a)$$
 (if  $\operatorname{allocmem}(S, mt) = S', a$ )

 $mem\_type(store, memaddr) : memtype$ 

- 1. Return S.mems[a].type.
- 2. Post-condition: the returned memory type is valid under the empty context.

$$mem\_type(S, a) = S.mems[a].type$$

 $mem\_read(store, memaddr, i : u64) : byte \mid error$ 

- 1. Let mi be the memory instance store.mems[memaddr].
- 2. If i is larger than or equal to the length of mi bytes, then return error.
- 3. Else, return the byte mi.bytes[i].

```
\begin{array}{lll} \operatorname{mem\_read}(S,a,i) & = & b & \quad \text{(if $S$.mems}[a].bytes[i] = b) \\ \operatorname{mem\_read}(S,a,i) & = & \operatorname{error} & \quad \text{(otherwise)} \end{array}
```

 $mem\_write(store, memaddr, i : u64, byte) : store | error$ 

- 1. Let mi be the memory instance store.mems[memaddr].
- 2. If i is larger than or equal to the length of mi. bytes, then return error.
- 3. Replace mi.bytes[i] with byte.
- 4. Return the updated store.

```
\begin{array}{lll} \operatorname{mem\_write}(S,a,i,b) & = & S' & \quad \text{(if } S' = S \text{ with } \operatorname{mems}[a].\operatorname{bytes}[i] = b) \\ \operatorname{mem\_write}(S,a,i,b) & = & \operatorname{error} & \quad \text{(otherwise)} \end{array}
```

 $mem\_size(store, memaddr) : u64$ 

1. Return the length of *store*.mems[memaddr].bytes divided by the page size.

```
mem\_size(S, a) = n (if |S.mems[a].bytes| = n \cdot 64 \text{ Ki})
```

 $mem\_grow(store, memaddr, n : u64) : store \mid error$ 

- 1. Try growing the memory instance store.mems[memaddr] by n pages:
  - a. If it succeeds, return the updated store.
  - b. Else, return error.

```
\begin{array}{lll} \operatorname{mem\_grow}(S,a,n) & = & S' & \quad \text{(if } S' = S \text{ with } \operatorname{mems}[a] = \operatorname{growmem}(S.\operatorname{mems}[a],n)) \\ \operatorname{mem\_grow}(S,a,n) & = & \operatorname{error} & \quad \text{(otherwise)} \end{array}
```

# 7.1.11 Tags

 $tag\_alloc(store, tagtype) : (store, tagaddr)$ 

- 1. Pre-condition: tagtype is valid.
- 2. Let tagaddr be the result of allocating a tag in store with tag type tagtype.
- 3. Return the new store paired with *tagaddr*.

$$tag\_alloc(S, tt) = (S', a)$$
 (if  $alloctag(S, tt) = S', a$ )

 $tag\_type(store, tagaddr) : tagtype$ 

- 1. Return S.tags[a].type.
- 2. Post-condition: the returned tag type is valid.

$$tag\_type(S, a) = S.tags[a].type$$

# 7.1.12 Exceptions

 $\exp_{\text{alloc}}(store, tagaddr, val^*) : (store, exnaddr)$ 

- 1. Pre-condition: tagaddr is an allocated tag address.
- 2. Let exnaddr be the result of allocating an exception instance in store with tag address tagaddr and initialization values  $val^*$ .
- 3. Return the new store paired with *exnaddr*.

```
\operatorname{exn\_alloc}(S, tagaddr, val^*) = (S \oplus \{\operatorname{exns} exninst\}, |S.\operatorname{exns}|) (if exninst = \{\operatorname{tag} tagaddr, \operatorname{fields} val^*\}
```

 $\verb|exn_tag|(store, exnaddr): tagaddr|$ 

- 1. Let exninst be the exception instance store.exns[exnaddr].
- 2. Return the tag address exninst.tag.

```
\exp_{\text{tag}}(S, a) = exninst. \text{tag} \quad (\text{if } exninst = S. \exp[a])
```

 $\exp_{\text{read}}(store, exnaddr) : val^*$ 

- 1. Let exninst be the exception instance store.exns[exnaddr].
- 2. Return the values exninst.fields.

```
exn_read(S, a) = exninst.fields (if exninst = S.exns[a])
```

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# **7.1.13 Globals**

 $global\_alloc(store, globaltype, val) : (store, globaladdr)$ 

- 1. Pre-condition: the *globaltype* is valid under the empty context.
- 2. Let *globaladdr* be the result of allocating a global in *store* with global type *globaltype* and initialization value *val*.
- 3. Return the new store paired with *globaladdr*.

$$global\_alloc(S, gt, v) = (S', a)$$
 (if  $allocglobal(S, gt, v) = S', a$ )

 $global\_type(store, globaladdr) : globaltype$ 

- 1. Return S.globals[a].type.
- 2. Post-condition: the returned global type is valid under the empty context.

$$global\_type(S, a) = S.globals[a].type$$

global read(store, globaladdr): val

- 1. Let gi be the global instance store.globals[globaladdr].
- 2. Return the value gi.value.

$$global_read(S, a) = v$$
 (if  $S.globals[a].value = v$ )

global\_write(store, globaladdr, val): store | error

- 1. Let gi be the global instance store.globals[globaladdr].
- 2. Let  $mut\ t$  be the structure of the global type gi.type.
- 3. If *mut* is not var, then return error.
- 4. Replace gi.value with the value val.
- 5. Return the updated store.

```
 \begin{split} & \text{global\_write}(S, a, v) &= S' & \text{ (if $S$.globals}[a]. \\ & \text{type} = \text{var } t \land S' = S \text{ with globals}[a]. \\ & \text{value} = v) \\ & \text{global\_write}(S, a, v) &= \text{error} \\ & \text{ (otherwise)} \\ \end{aligned}
```

# **7.1.14 Values**

 $ref_type(store, ref) : reftype$ 

- 1. Pre-condition: the reference  $\mathit{ref}$  is valid under store S.
- 2. Return the reference type t with which ref is valid.
- 3. Post-condition: the returned reference type is valid under the empty context.

$$\operatorname{ref\_type}(S,r) \ = \ t \qquad (\operatorname{if} S \vdash r:t)$$

# Note

In future versions of WebAssembly, not all references may carry precise type information at run time. In such cases, this function may return a less precise supertype.

val default(valtype) : val

- 1. If  $default_{valtupe}$  is not defined, then return error.
- 1. Else, return the value default<sub>valtupe</sub>.

```
val\_default(t) = v (if default_t = v)

val\_default(t) = error (if default_t = \epsilon)
```

# 7.1.15 Matching

 $match\_valtype(valtype_1, valtype_2) : bool$ 

- 1. Pre-condition: the value types  $valtype_1$  and  $valtype_2$  are valid under the empty context.
- 2. If  $valtype_1$  matches  $valtype_2$ , then return true.
- 3. Else, return false.

```
\begin{array}{lll} \text{match\_reftype}(t_1,t_2) & = & \textit{true} & & (\text{if } \vdash t_1 \leq t_2) \\ \text{match\_reftype}(t_1,t_2) & = & \textit{false} & & (\text{otherwise}) \\ \end{array}
```

 $match_externtype(externtype_1, externtype_2): bool$ 

- 1. Pre-condition: the extern types externtype<sub>1</sub> and externtype<sub>2</sub> are valid under the empty context.
- 2. If  $externtype_1$  matches  $externtype_2$ , then return true.
- 3. Else, return false.

```
\begin{array}{lll} \text{match\_externtype}(\mathit{et}_1, \mathit{et}_2) & = & \mathit{true} & \quad (\text{if } \vdash \mathit{et}_1 \leq \mathit{et}_2) \\ \text{match\_externtype}(\mathit{et}_1, \mathit{et}_2) & = & \mathit{false} & \quad (\text{otherwise}) \\ \end{array}
```

# 7.2 Profiles

To enable the use of WebAssembly in as many environments as possible, *profiles* specify coherent language subsets that fit constraints imposed by common classes of host environments. A host platform can thereby decide to support the language only under a restricted profile, or even the intersection of multiple profiles.

# 7.2.1 Conventions

A profile modification is specified by decorating selected rules in the main body of this specification with a *profile annotation* that defines them as conditional on the choice of profile.

For that purpose, every profile defines a *profile marker*, an alphanumeric short-hand like ABC. A profile annotation of the form  $^{[!ABC\ XYZ]}$  on a rule indicates that this rule is *excluded* for either of the profiles whose marker is ABC or XYZ.

There are two ways of subsetting the language in a profile:

- Syntactic, by omitting a feature, in which case certain constructs are removed from the syntax altogether.
- Semantic, by restricting a feature, in which case certain constructs are still present but some behaviours are ruled out.

## **Syntax Annotations**

To omit a construct from a profile syntactically, respective productions in the grammar of the abstract syntax are annotated with an associated profile marker. This is defined to have the following implications:

- 1. Any production in the binary or textual syntax that produces abstract syntax with a marked construct is omitted by extension.
- 2. Any validation or execution rule that handles a marked construct is omitted by extension.

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The overall effect is that the respective construct is no longer part of the language under a respective profile.

#### Note

For example, a "busy" profile marked BUSY could rule out the nop instruction by marking the production for it in the abstract syntax as follows:

```
\begin{array}{ccc} instr & ::= & \dots \\ [!BUSY] & | & \mathsf{nop} \\ & | & \mathsf{unreachable} \end{array}
```

A rule may be annotated by multiple markers, which could be the case if a construct is in the intersection of multiple features.

#### **Semantics Annotations**

To restrict certain behaviours in a profile, individual validation or reduction rules or auxiliary definitions are annotated with an associated marker.

This has the consequence that the respective rule is no longer applicable under the given profile.

#### Note

For example, an "infinite" profile marked INF could define that growing memory never fails:

```
S; F; (\mathsf{i32.const}\ n)\ \mathsf{memory.grow}\ x \quad \hookrightarrow \quad S'; F; (\mathsf{i32.const}\ sz) \\ (\mathsf{if}\ F.\mathsf{module.mems}[x] = a \\ \land sz = |S.\mathsf{mems}[a].\mathsf{datas}|/64\,\mathsf{Ki} \\ \land S' = S\ \mathsf{with}\ \mathsf{mems}[a] = \mathsf{growmem}(S.\mathsf{mems}[a], n)) \\ [!INF] \quad S; F; (\mathsf{i32.const}\ n)\ \mathsf{memory.grow}\ x \quad \hookrightarrow \quad S; F; (\mathsf{i32.const}\ \mathsf{signed}_{32}^{-1}(-1))
```

### **Properties**

All profiles are defined such that the following properties are preserved:

- All profiles represent syntactic and semantic subsets of the full profile, i.e., they do not add syntax or alter behaviour.
- All profiles are mutually compatible, i.e., no two profiles subset semantic behaviour in inconsistent or ambiguous ways, and any intersection of profiles preserves the properties described here.
- Profiles do not violate soundness, i.e., all configurations valid under that profile still have well-defined execution behaviour.

### Note

Tools are generally expected to handle and produce code for the full profile by default. In particular, producers should not generate code that *depends* on specific profiles. Instead, all code should preserve correctness when executed under the full profile.

Moreover, profiles should be considered static and fixed for a given platform or ecosystem. Runtime conditioning on the "current" profile is not intended and should be avoided.

# 7.2.2 Defined Profiles

#### Note

The number of defined profiles is expected to remain small in the future. Profiles are intended for broad and permanent use cases only. In particular, profiles are not intended for language versioning.

### Full Profile (FUL)

The *full* profile contains the complete language and all possible behaviours. It imposes no restrictions, i.e., all rules and definitions are active. All other profiles define sub-languages of this profile.

## **Deterministic Profile (DET)**

The *deterministic* profile excludes all rules marked <sup>[!DET]</sup>. It defines a sub-language that does not exhibit any incidental non-deterministic behaviour:

- All NaN values generated by floating-point instructions are canonical and positive.
- · All relaxed vector instructions have a fixed behaviour that does not depend on the implementation.

Even under this profile, the memory.grow and table.grow instructions technically remain non-deterministic, in order to be able to indicate resource exhaustion.

#### Note

In future versions of WebAssembly, new non-deterministic behaviour may be added to the language, such that the deterministic profile will induce additional restrictions.

# 7.3 Implementation Limitations

Implementations typically impose additional restrictions on a number of aspects of a WebAssembly module or execution. These may stem from:

- physical resource limits,
- constraints imposed by the embedder or its environment,
- limitations of selected implementation strategies.

This section lists allowed limitations. Where restrictions take the form of numeric limits, no minimum requirements are given, nor are the limits assumed to be concrete, fixed numbers. However, it is expected that all implementations have "reasonably" large limits to enable common applications.

### Note

A conforming implementation is not allowed to leave out individual *features*. However, designated subsets of WebAssembly may be specified in the future.

# 7.3.1 Syntactic Limits

#### **Structure**

An implementation may impose restrictions on the following dimensions of a module:

- the number of types in a module
- the number of functions in a module, including imports
- the number of tables in a module, including imports
- the number of memories in a module, including imports

- the number of globals in a module, including imports
- the number of tags in a module, including imports
- the number of element segments in a module
- the number of data segments in a module
- the number of imports to a module
- the number of exports from a module
- the number of sub types in a recursive type
- the subtyping depth of a sub type
- the number of fields in a structure type
- the number of parameters in a function type
- the number of results in a function type
- the number of parameters in a block type
- the number of results in a block type
- the number of locals in a function
- the number of instructions in a function body
- the number of instructions in a structured control instruction
- the number of structured control instructions in a function
- the nesting depth of structured control instructions
- the number of label indices in a br table instruction
- the number of instructions in a constant expression
- the length of the array in a array.new\_fixed instruction
- the length of an element segment
- the length of a data segment
- the length of a name
- the range of characters in a name

If the limits of an implementation are exceeded for a given module, then the implementation may reject the validation, compilation, or instantiation of that module with an embedder-specific error.

#### Note

The last item allows embedders that operate in limited environments without support for Unicode<sup>48</sup> to limit the names of imports and exports to common subsets like ASCII<sup>49</sup>.

## **Binary Format**

For a module given in binary format, additional limitations may be imposed on the following dimensions:

- the size of a module
- the size of any section
- the size of an individual function's code
- the size of a structured control instruction

<sup>48</sup> https://www.unicode.org/versions/latest/

<sup>&</sup>lt;sup>49</sup> https://webstore.ansi.org/RecordDetail.aspx?sku=INCITS+4-1986%5bR2012%5d

- the size of an individual constant expression's instruction sequence
- the number of sections

#### **Text Format**

For a module given in text format, additional limitations may be imposed on the following dimensions:

- the size of the source text
- the size of any syntactic element
- the size of an individual token
- the nesting depth of folded instructions
- the length of symbolic identifiers
- the range of literal characters allowed in the source text

#### 7.3.2 Validation

An implementation may defer validation of individual functions until they are first invoked.

If a function turns out to be invalid, then the invocation, and every consecutive call to the same function, results in a trap.

### Note

This is to allow implementations to use interpretation or just-in-time compilation for functions. The function must still be fully validated before execution of its body begins.

### 7.3.3 Execution

Restrictions on the following dimensions may be imposed during execution of a WebAssembly program:

- the number of allocated module instances
- the number of allocated function instances
- the number of allocated table instances
- the number of allocated memory instances
- the number of allocated global instances
- the number of allocated tag instances
- the number of allocated structure instances
- the number of allocated array instances
- the number of allocated exception instances
- the size of a table instance
- the size of a memory instance
- the size of an array instance
- the number of frames on the stack
- the number of labels on the stack
- the number of values on the stack

If the runtime limits of an implementation are exceeded during execution of a computation, then it may terminate that computation and report an embedder-specific error to the invoking code.

Some of the above limits may already be verified during instantiation, in which case an implementation may report exceedance in the same manner as for syntactic limits.

#### Note

Concrete limits are usually not fixed but may be dependent on specifics, interdependent, vary over time, or depend on other implementation- or embedder-specific situations or events.

# 7.4 Type Soundness

The type system of WebAssembly is *sound*, implying both *type safety* and *memory safety* with respect to the WebAssembly semantics. For example:

- All types declared and derived during validation are respected at run time; e.g., every local or global variable will only contain type-correct values, every instruction will only be applied to operands of the expected type, and every function invocation always evaluates to a result of the right type (if it does not diverge, throw an exception, or trap).
- No memory location will be read or written except those explicitly defined by the program, i.e., as a local, a global, an element in a table, or a location within a linear memory.
- There is no undefined behavior, i.e., the execution rules cover all possible cases that can occur in a valid program, and the rules are mutually consistent.

Soundness also is instrumental in ensuring additional properties, most notably, *encapsulation* of function and module scopes: no locals can be accessed outside their own function and no module components can be accessed outside their own module unless they are explicitly exported or imported.

The typing rules defining WebAssembly validation only cover the *static* components of a WebAssembly program. In order to state and prove soundness precisely, the typing rules must be extended to the *dynamic* components of the abstract runtime, that is, the store, configurations, and administrative instructions.<sup>50</sup>

# 7.4.1 Contexts

In order to check rolled up recursive types, the context is locally extended with an additional component that records the sub type corresponding to each recursive type index within the current recursive type:

$$C ::= \{ \dots, \mathsf{recs} \ \mathit{subtype}^* \}$$

# **7.4.2 Types**

Well-formedness for extended type forms is defined as follows.

# Heap Type bot

• The heap type is valid.

 $\overline{C \vdash \mathsf{bot} : \mathsf{ok}}$ 

<sup>&</sup>lt;sup>50</sup> The formalization and theorems are derived from the following article: Andreas Haas, Andreas Rossberg, Derek Schuff, Ben Titzer, Dan Gohman, Luke Wagner, Alon Zakai, JF Bastien, Michael Holman. Bringing the Web up to Speed with WebAssembly<sup>51</sup>. Proceedings of the 38th ACM SIGPLAN Conference on Programming Language Design and Implementation (PLDI 2017). ACM 2017.

<sup>&</sup>lt;sup>51</sup> https://dl.acm.org/citation.cfm?doid=3062341.3062363

# Heap Type rec i

- The recursive type index i must exist in C.recs.
- Then the heap type is valid.

$$\frac{C.\mathsf{recs}[i] = subtype}{C \vdash \mathsf{rec}\ i : \mathsf{ok}}$$

# Value Type bot

• The value type is valid.

$$\overline{C \vdash \mathsf{bot} : \mathsf{ok}}$$

# Recursive Types rec subtype\*

- Let C' be the current context C, but where recs is  $subtype^*$ .
- There must be a type index x, such that for each sub type  $subtype_i$  in  $subtype^*$ :
  - Under the context C', the sub type  $subtype_i$  must be valid for type index x + i and recursive type index i.
- Then the recursive type is valid for the type index x.

$$\frac{C, \mathsf{recs}\; subtype^* \vdash \mathsf{rec}\; subtype^* : \mathsf{ok}(x,0)}{C \vdash \mathsf{rec}\; subtype^* : \mathsf{ok}(x)}$$
 
$$\frac{C \vdash subtype : \mathsf{ok}(x,i) \qquad C \vdash \mathsf{rec}\; subtype'^* : \mathsf{ok}(x+1,i+1)}{C \vdash \mathsf{rec}\; subtype\; subtype'^* : \mathsf{ok}(x,i)}$$

#### Note

These rules are a generalisation of the ones previously given.

# **Sub types** sub final? $ht^*$ comptype

- The composite type *comptype* must be valid.
- The sequence  $ht^*$  may be no longer than 1.
- For every heap type  $ht_k$  in  $ht^*$ :
  - The heap type  $ht_k$  must be ordered before a type index x and recursive type index a i, meaning:
    - \* Either  $ht_k$  is a defined type.
    - \* Or  $ht_k$  is a type index  $y_k$  that is smaller than x.
    - \* Or  $ht_k$  is a recursive type index rec  $j_k$  where  $j_k$  is smaller than i.
  - Let sub type  $subtype_k$  be the unrolling of the heap type  $ht_k$ , meaning:
    - \* Either  $ht_k$  is a defined type  $deftype_k$ , then  $subtype_k$  must be the unrolling of  $deftype_k$ .
    - \* Or  $ht_k$  is a type index  $y_k$ , then  $subtype_k$  must be the unrolling of the defined type C.types $[y_k]$ .
    - \* Or  $ht_k$  is a recursive type index rec  $j_k$ , then  $subtype_k$  must be  $C.recs[j_k]$ .
  - The sub type  $subtype_k$  must not contain final.
  - Let  $comptype'_k$  be the composite type in  $subtype_k$ .
  - The composite type comptype must match comptype'<sub>k</sub>.
- Then the sub type is valid for the type index x and recursive type index i.

$$\frac{|ht^*| \leq 1 \quad (ht \prec x, i)^* \quad (\operatorname{unroll}_C(ht) = \operatorname{sub} \ ht'^* \ comptype')^*}{C \vdash \operatorname{sub} \ final^? \ ht^* \ comptype : \operatorname{ok}(x, i)}$$

where:

$$\begin{array}{lll} (deftype \prec x,i) & = & \text{true} \\ (y \prec x,i) & = & y < x \\ (\text{rec } j \prec x,i) & = & j < i \\ \\ \text{unroll}_C(deftype) & = & \text{unroll}(deftype) \\ \text{unroll}_C(y) & = & \text{unroll}(C.\text{types}[y]) \\ \text{unroll}_C(\text{rec } j) & = & C.\text{recs}[j] \\ \end{array}$$

### Note

This rule is a generalisation of the ones previously given, which only allowed type indices as supertypes.

# 7.4.3 Subtyping

In a rolled-up recursive type, a recursive type indices rec i matches another heap type ht if:

- Let sub final?  $ht'^*$  comptype be the sub type C.recs[i].
- The heap type ht is contained in  $ht'^*$ .

$$\frac{C.\mathsf{recs}[i] = \mathsf{sub\ final}^?\ (ht_1^*\ ht\ ht_2^*)\ comptype}{C \vdash \mathsf{rec}\ i \le ht}$$

#### Note

This rule is only invoked when checking validity of rolled-up recursive types.

# 7.4.4 Results

Results can be classified by result types as follows.

### Results val\*

- For each value  $val_i$  in  $val^*$ :
  - The value  $val_i$  is valid with some value type  $t_i$ .
- Let  $t^*$  be the concatenation of all  $t_i$ .
- Then the result is valid with result type  $[t^*]$ .

$$\frac{(S \vdash val:t)^*}{S \vdash val^*:[t^*]}$$

# **Results** (ref.exn a) throw\_ref

- The value ref.exn a must be valid.
- Then the result is valid with result type  $[t^*]$ , for any valid closed result types.

$$\frac{S \vdash REFEXNADDR\ a : REF\ EXN \qquad \vdash [t^*] : \mathsf{ok}}{S \vdash (\mathsf{ref.exn}\ a)\ \mathsf{throw\_ref} : [t'^*]}$$

### Results trap

• The result is valid with result type  $[t^*]$ , for any valid closed result types.

$$\frac{\vdash [t^*] : \mathsf{ok}}{S \vdash \mathsf{trap} : [t^*]}$$

# 7.4.5 Store Validity

The following typing rules specify when a runtime store S is *valid*. A valid store must consist of function, table, memory, global, tag, element, data, structure, array, exception, and module instances that are themselves valid, relative to S.

To that end, each kind of instance is classified by a respective function, table, memory, global, tag, element, or data type, or just ok in the case of structures, arrays, or exceptions. Module instances are classified by *module contexts*, which are regular contexts repurposed as module types describing the index spaces defined by a module.

#### Store S

- Each function instance funcinst<sub>i</sub> in S.funcs must be valid with some function type functype<sub>i</sub>.
- Each table instance tableinst<sub>i</sub> in S.tables must be valid with some table type tabletype<sub>i</sub>.
- Each memory instance meminst<sub>i</sub> in S.mems must be valid with some memory type memtype<sub>i</sub>.
- Each global instance qlobalinst<sub>i</sub> in S.globals must be valid with some global type qlobaltype<sub>i</sub>.
- Each tag instance  $taginst_i$  in S.tags must be valid with some tag type  $tagtype_i$ .
- Each element instance *eleminst*<sub>i</sub> in S.elems must be valid with some reference type reftype<sub>i</sub>.
- Each data instance  $datainst_i$  in S.datas must be valid.
- Each structure instance structinst<sub>i</sub> in S.structs must be valid.
- Each array instance  $arrayinst_i$  in S. arrays must be valid.
- Each exception instance  $exninst_i$  in S.exns must be valid.
- No reference to a bound structure address must be reachable from itself through a path consisting only of indirections through immutable structure, or array fields or fields of exception instances.
- No reference to a bound array address must be reachable from itself through a path consisting only of indirections through immutable structure or array fields or fields of exception instances.
- No reference to a bound exception address must be reachable from itself through a path consisting only of indirections through immutable structure or array fields or fields of exception instances.
- Then the store is valid.

```
(S \vdash funcinst : deftype)^*
                                                                   (S \vdash tableinst : tabletype)^*
                     (S \vdash meminst : memtype)^*
                                                                  (S \vdash globalinst : globaltype)^*
                                                (S \vdash taginst : tagtype)^*
                              (S \vdash eleminst : reftype)^*
                                                                         (S \vdash datainst : ok)^*
              (S \vdash structinst : ok)^*
                                                 (S \vdash arrayinst : ok)^*
                                                                                        (S \vdash exninst : ok)^*
S = \{\text{funcs } funcinst^*, \text{globals } globalinst^*, \text{tables } tableinst^*, \text{mems } meminst^*, \text{tags } taginst^*, \}
        elems eleminst^*, datas datainst^*, structs structinst^*, arrays arrayinst^*, exns exninst^*}
                                                           ((\text{ref.struct } a_s) \gg_S^+ (\text{ref.struct } a_s))^* 
((\text{ref.array } a_a) \gg_S^+ (\text{ref.array } a_a))^*
                (S.\mathsf{structs}[a_s] = structinst)^*
                  (S.arrays[a_a] = arrayinst)^*
                                                             ((\text{ref.exn } a_e) \gg_S^+ (\text{ref.exn } a_e))^*
                       (S.\mathsf{exns}[a_e] = exninst)^*
                                                            \vdash S : \mathsf{ok}
```

where  $val_1 \gg_S^+ val_2$  denotes the transitive closure of the following immutable reachability relation on values:

#### Note

The constraint on reachability through immutable fields prevents the presence of cyclic data structures that can not be constructed in the language. Cycles can only be formed using mutation.

# **Function Instances** {type *functype*, module *moduleinst*, code *func*}

- The function type functype must be valid under an empty context.
- The module instance module inst must be valid with some context C.
- Under context C:
  - The function func must be valid with some function type functype'.
  - The function type functype' must match functype.
- Then the function instance is valid with function type functype.

```
\begin{tabular}{ll} & \vdash functype: {\sf ok} & S \vdash module inst: C \\ & C \vdash func: functype' & C \vdash functype' \leq functype \\ \hline & S \vdash \{ {\sf type} \ functype, {\sf module} \ module inst, {\sf code} \ func \}: functype \\ \hline \end{tabular}
```

# **Host Function Instances** {type *functype*, hostfunc *hf* }

- The function type functype must be valid under an empty context.
- Let  $[t_1^*] \rightarrow [t_2^*]$  be the function type functype.
- For every valid store  $S_1$  extending S and every sequence  $val^*$  of values whose types coincide with  $t_1^*$ :
  - Executing hf in store  $S_1$  with arguments  $val^*$  has a non-empty set of possible outcomes.
  - For every element R of this set:
    - \* Either R must be  $\perp$  (i.e., divergence).
    - \* Or R consists of a valid store  $S_2$  extending  $S_1$  and a result result whose type coincides with  $[t_2^*]$ .
- Then the function instance is valid with function type functype.

```
\forall S_1, val^*, \vdash S_1 : \mathsf{ok} \land \vdash S \preceq S_1 \land S_1 \vdash val^* : [t_1^*] \Longrightarrow \\ hf(S_1; val^*) \supset \emptyset \land \\ \forall R \in hf(S_1; val^*), \ R = \bot \lor \\ \vdash [t_1^*] \rightarrow [t_2^*] : \mathsf{ok} \qquad \exists S_2, result, \vdash S_2 : \mathsf{ok} \land \vdash S_1 \preceq S_2 \land S_2 \vdash result : [t_2^*] \land R = (S_2; result) \\ S \vdash \{\mathsf{type} [t_1^*] \rightarrow [t_2^*], \mathsf{hostfunc} \ hf\} : [t_1^*] \rightarrow [t_2^*]
```

## Note

This rule states that, if appropriate pre-conditions about store and arguments are satisfied, then executing the host function must satisfy appropriate post-conditions about store and results. The post-conditions match the ones in the execution rule for invoking host functions.

Any store under which the function is invoked is assumed to be an extension of the current store. That way, the function itself is able to make sufficient assumptions about future stores.

### **Table Instances** {type ( $addrtype \ limits \ t$ ), elem $ref^*$ }

- The table type addrtype limits t must be valid under the empty context.
- The length of ref\* must equal limits.min.
- For each reference  $ref_i$  in the table's elements  $ref^n$ :

- The reference  $ref_i$  must be valid with some reference type  $t'_i$ .
- The reference type  $t'_i$  must match the reference type t.
- Then the table instance is valid with table type  $addrtype\ limits\ t$ .

$$\frac{\vdash addrtype \ limits \ t : \mathsf{ok} \qquad n = limits.\mathsf{min} \qquad (S \vdash ref : t')^n \qquad (\vdash t' \leq t)^n}{S \vdash \{\mathsf{type} \ (addrtype \ limits \ t), \mathsf{elem} \ ref^n\} : addrtype \ limits \ t}$$

# **Memory Instances** {type ( $addrtype \ limits$ ), bytes $b^*$ }

- The memory type addrtype limits must be valid under the empty context.
- The length of  $b^*$  must equal limits.min multiplied by the page size 64 Ki.
- Then the memory instance is valid with memory type addrtype limits.

$$\frac{\vdash addrtype \ limits : \mathsf{ok} \qquad n = limits.\mathsf{min} \cdot 64 \, \mathsf{Ki}}{S \vdash \{\mathsf{type} \ (addrtype \ limits), \mathsf{bytes} \ b^n\} : addrtype \ limits}$$

# Global Instances {type $mut\ t$ , value val}

- The global type  $mut\ t$  must be valid under the empty context.
- The value val must be valid with some value type t'.
- The value type t' must match the value type t.
- Then the global instance is valid with global type  $mut\ t$ .

$$\frac{\vdash \textit{mut } t : \mathsf{ok} \qquad S \vdash \textit{val} : t' \qquad \vdash t' \leq t}{S \vdash \{\mathsf{type} \; \textit{mut } t, \mathsf{value} \; \textit{val}\} : \textit{mut } t}$$

# **Tag Instances** {type tagtype}

- The tag type tagtype must be valid under the empty context.
- Then the tag instance is valid with tag type tagtype.

$$\frac{\vdash \textit{tagtype} : \mathsf{ok}}{S \vdash \{\mathsf{type} \; \textit{tagtype}\} : \textit{tagtype}}$$

# **Element Instances** {type t, elem $ref^*$ }

- The reference type t must be valid under the empty context.
- For each reference  $ref_i$  in the elements  $ref^n$ :
  - The reference  $ref_i$  must be valid with some reference type  $t'_i$ .
  - The reference type  $t'_i$  must match the reference type t.
- Then the element instance is valid with reference type t.

$$\frac{\vdash t : \mathsf{ok} \qquad (S \vdash \mathit{ref} : t')^* \qquad (\vdash t' \leq t)^*}{S \vdash \{\mathsf{type}\ t, \mathsf{elem}\ \mathit{ref}^*\} : t}$$

# **Data Instances** {bytes $b^*$ }

• The data instance is valid.

$$\overline{S \vdash \{\text{bytes } b^*\} : \text{ok}}$$

# **Structure Instances** {type deftype, fields fieldval\*}

- The defined type deftype must be valid under the empty context.
- The expansion of deftype must be a structure type struct fieldtype\*.
- The length of the sequence of field values *fieldval\** must be the same as the length of the sequence of field types *fieldtype\**.
- For each field value fieldval<sub>i</sub> in fieldval<sup>\*</sup> and corresponding field type fieldtype<sub>i</sub> in fieldtype<sup>\*</sup>:
  - Let  $fieldtype_i$  be  $mut\ storagetype_i$ .
  - The field value  $fieldval_i$  must be valid with storage type  $storagetype_i$ .
- Then the structure instance is valid.

$$\frac{\vdash dt : \mathsf{ok} \qquad \mathrm{expand}(dt) = \mathsf{struct} \; (mut \; st)^* \qquad (S \vdash fv : st)^*}{S \vdash \{\mathsf{type} \; dt, \mathsf{fields} \; fv^*\} : \mathsf{ok}}$$

# **Array Instances** {type deftype, fields fieldval\*}

- The defined type deftype must be valid under the empty context.
- The expansion of deftype must be an array type array fieldtype.
- Let fieldtype be mut storagetype.
- For each field value fieldval<sub>i</sub> in fieldval\*:
  - The field value  $fieldval_i$  must be valid with storage type storagetype.
- Then the array instance is valid.

$$\frac{\vdash dt : \mathsf{ok} \qquad \mathrm{expand}(dt) = \mathsf{array}\; (\mathit{mut}\; \mathit{st}) \qquad (S \vdash \mathit{fv} : \mathit{st})^*}{S \vdash \{\mathsf{type}\; \mathit{dt}, \mathsf{fields}\; \mathit{fv}^*\} : \mathsf{ok}}$$

# Field Values fieldval

- If fieldval is a value val, then:
  - The value val must be valid with value type t.
  - Then the field value is valid with value type t.
- Else, fieldval is a packed value packval:
  - Let packtype.pack i be the field value fieldval.
  - Then the field value is valid with packed type packtype.

$$\overline{S \vdash pt.\mathsf{pack}\ i:pt}$$

# **Exception Instances** $\{tag \ a, fields \ val^*\}$

- The store entry S.tags[a] must exist.
- Let  $[t^*] \to [{t'}^*]$  be the tag type S.tags[a].type.
- The result type  $[t'^*]$  must be empty.
- The sequence  $val^a st$  of values must have the same length as the sequence  $t^*$  of value types.
- For each value  $val_i$  in  $val^ast$  and corresponding value type  $t_i$  in  $t^*$ , the value  $val_i$  must be valid with type  $t_i$ .
- Then the exception instance is valid.

$$\frac{S.\mathsf{tags}[a] = \{\mathsf{type} = [t^*] \to []\} \qquad (S \vdash val:t)^*}{S \vdash \{\mathsf{tag}\; a, \mathsf{fields}\; val^*\} : \mathsf{ok}}$$

# **Export Instances** {name name, addr externaddr}

- The external address externaldr must be valid with some external type externtype.
- Then the export instance is valid.

$$\frac{S \vdash externaddr : externtype}{S \vdash \{ name \ name, addr \ externaddr \} : ok}$$

#### Module Instances moduleinst

- Each defined type deftype; in moduleinst.types must be valid under the empty context.
- For each function address  $funcaddr_i$  in module inst. funcs, the external address func  $funcaddr_i$  must be valid with some external type func  $functype_i$ .
- For each table address  $tableaddr_i$  in module inst.tables, the external address table  $tableaddr_i$  must be valid with some external type table  $table type_i$ .
- For each memory address  $memaddr_i$  in module inst mems, the external address mem  $memaddr_i$  must be valid with some external type mem  $memtype_i$ .
- For each global address  $globaladdr_i$  in module inst. globals, the external address global  $globaladdr_i$  must be valid with some external type global  $global type_i$ .
- For each tag address  $tagaddr_i$  in module inst.tags, the external address tag  $tagaddr_i$  must be valid with some external type tag  $tagtype_i$ .
- For each element address  $elemaddr_i$  in module inst. elems, the element instance S. elems  $[elemaddr_i]$  must be valid with some reference type  $reftype_i$ .
- For each data address  $dataaddr_i$  in module inst.datas, the data instance S.datas  $[dataaddr_i]$  must be valid with  $ok_i$ .
- Each export instance  $exportinst_i$  in module inst. exports must be valid.
- For each export instance *exportinst<sub>i</sub>* in *moduleinst*.exports, the name *exportinst<sub>i</sub>*.name must be different from any other name occurring in *moduleinst*.exports.
- Let  $deftype^*$  be the concatenation of all  $deftype_i$  in order.
- Let  $functype^*$  be the concatenation of all  $functype_i$  in order.
- Let  $table type^*$  be the concatenation of all  $table type_i$  in order.
- Let  $memtype^*$  be the concatenation of all  $memtype_i$  in order.
- Let  $globaltype^*$  be the concatenation of all  $globaltype_i$  in order.
- Let  $tagtype^*$  be the concatenation of all  $tagtype_i$  in order.
- Let  $reftype^*$  be the concatenation of all  $reftype_i$  in order.
- Let  $ok^*$  be the concatenation of all  $ok_i$  in order.
- Let m be the length of moduleinst.funcs.
- Let  $x^*$  be the sequence of function indices from 0 to m-1.
- Then the module instance is valid with context {types  $deftype^*$ , funcs  $functype^*$ , tables  $tabletype^*$ , mems  $memtype^*$ , globals  $globaltype^*$ , CTAGS~tagtype^ast, elems  $reftype^*$ , datas  $ok^*$ , refs  $x^*$ }.

```
(\vdash deftype : ok)^*
    (S \vdash \mathsf{func}\, funcaddr : \mathsf{func}\, functype)^*
                                                         (S \vdash \mathsf{table}\ table \ table \ table \ table \ table \ table \ type)^*
(S \vdash \mathsf{mem}\ memaddr : \mathsf{mem}\ memtype)^*
                                                         (S \vdash \mathsf{global}\ globaladdr : \mathsf{global}\ globaltype)^*
                                   (S \vdash \mathsf{tag}\ tagaddr : \mathsf{tag}\ tagtype)^*
           (S \vdash S.\mathsf{elems}[elemaddr] : reftype)^* \qquad (S \vdash S.\mathsf{datas}[dataaddr] : ok)^*
                     (S \vdash exportinst : ok)^*
                                                       (exportinst.name)* disjoint
                S \vdash \{\text{types} \quad deftype^*,
                       funcs funcaddr^*
                        tables tableaddr^*
                        mems memaddr^*
                        globals globaladdr^*
                        tags tagaddr^*,
                        elems elemaddr^*
                        datas dataaddr^*.
                        exports exportinst^* } : {types deftype^*,
                                                       funcs functype^*
                                                       tables tabletype*
                                                       mems memtupe*
                                                       globals globaltype*.
                                                       tags tagtype^*,
                                                       elems reftype^*,
                                                       datas ok^*,
                                                       refs 0 \dots (|funcaddr^*| - 1)
```

# 7.4.6 Configuration Validity

To relate the WebAssembly type system to its execution semantics, the typing rules for instructions must be extended to configurations S; T, which relates the store to execution threads.

Configurations and threads are classified by their result type. In addition to the store S, threads are typed under a return type resulttype?, which controls whether and with which type a return instruction is allowed. This type is absent  $(\epsilon)$  except for instruction sequences inside an administrative frame instruction.

Finally, frames are classified with *frame contexts*, which extend the module contexts of a frame's associated module instance with the locals that the frame contains.

### Configurations S; T

- The store S must be valid.
- Under no allowed return type, the thread T must be valid with some result type  $[t^*]$ .
- Then the configuration is valid with the result type  $[t^*]$ .

$$\frac{\vdash S : \mathsf{ok} \qquad S; \epsilon \vdash T : [t^*]}{\vdash S; T : [t^*]}$$

## Threads F; $instr^*$

- Let resulttype? be the current allowed return type.
- The frame F must be valid with a context C.
- Let C' be the same context as C, but with return set to resulttype?
- Under context C', the instruction sequence  $instr^*$  must be valid with some type  $[] \to [t^*]$ .
- Then the thread is valid with the result type  $[t^*]$ .

$$\frac{S \vdash F : C \qquad S; C, \text{return } resulttype^? \vdash instr^* : [] \rightarrow [t^*]}{S; resulttype^? \vdash F; instr^* : [t^*]}$$

# Frames {locals $val^*$ , module module inst}

- The module instance module inst must be valid with some module context C.
- Each value  $val_i$  in  $val^*$  must be valid with some value type  $t_i$ .
- Let  $t^*$  be the concatenation of all  $t_i$  in order.
- Let C' be the same context as C, but with the value types  $t^*$  prepended to the locals list.
- Then the frame is valid with frame context C'.

$$\frac{S \vdash moduleinst : C \qquad (S \vdash val : t)^*}{S \vdash \{\text{locals } val^*, \text{module } moduleinst}\} : (C, \text{locals } t^*)}$$

### 7.4.7 Administrative Instructions

Typing rules for administrative instructions are specified as follows. In addition to the context C, typing of these instructions is defined under a given store S.

To that end, all previous typing judgements  $C \vdash prop$  are generalized to include the store, as in  $S; C \vdash prop$ , by implicitly adding S to all rules -S is never modified by the pre-existing rules, but it is accessed in the extra rules for administrative instructions given below.

#### trap

• The instruction is valid with any valid instruction type of the form  $[t_1^*] o [t_2^*]$ .

$$\frac{C \vdash [t_1^*] \rightarrow [t_2^*] : \mathsf{ok}}{S; C \vdash \mathsf{trap} : [t_1^*] \rightarrow [t_2^*]}$$

val

- The value val must be valid with value type t.
- Then it is valid as an instruction with type [] 
  ightarrow [t].

$$\frac{S \vdash val: t}{S; C \vdash val: [] \rightarrow [t]}$$

# invoke funcaddr

- The external function address func funcaddr must be valid with external function type func functype'.
- Let  $[t_1^*] \rightarrow [t_2^*]$  be the function type functype.
- Then the instruction is valid with type  $[t_1^*] \rightarrow [t_2^*]$

$$\frac{S \vdash \mathsf{func}\,\mathit{funcaddr} : \mathsf{func}\,[t_1^*] \to [t_2^*]}{S; C \vdash \mathsf{invoke}\,\mathit{funcaddr} : [t_1^*] \to [t_2^*]}$$

# $label_n\{instr_0^*\}\ instr^*$ end

- The instruction sequence  $instr_0^*$  must be valid with some type  $[t_1^n] \to_{x^*} [t_2^*]$ .
- Let C' be the same context as C, but with the result type  $[t_1^n]$  prepended to the labels list.
- Under context C', the instruction sequence  $instr^*$  must be valid with type  $[] \to_{x'^*} [t_2^*]$ .
- Then the compound instruction is valid with type  $[] \rightarrow [t_2^*]$ .

$$\frac{S; C \vdash instr_0^* : [t_1^n] \to_{x^*} [t_2^*] \qquad S; C, \mathsf{labels} \, [t_1^n] \vdash instr^* : [] \to_{x'^*} [t_2^*]}{S; C \vdash \mathsf{label}_n \{instr_0^*\} \ instr^* \ \mathsf{end} : [] \to [t_2^*]}$$

 $frame_n\{F\}\ instr^*\ end$ 

- Under the valid return type  $[t^n]$ , the thread F;  $instr^*$  must be valid with result type  $[t^n]$ .
- Then the compound instruction is valid with type  $[] \rightarrow [t^n]$ .

$$\frac{C \vdash [t^n] : \mathsf{ok} \qquad S; [t^n] \vdash F; instr^* : [t^n]}{S; C \vdash \mathsf{frame}_n\{F\} \ instr^* \ \mathsf{end} : [] \to [t^n]}$$

 $handler_n\{catch^*\}\ instr^*\ end$ 

- For every catch clause  $catch_i$  in  $catch^*$ ,  $catch_i$  must be valid.
- The instruction sequence  $instr^*$  must be valid with some type  $[t_1^*] \to [t_2^*]$ .
- Then the compound instruction is valid with type  $[t_1^*] \rightarrow [t_2^*]$ .

$$\frac{(C \vdash catch : \mathsf{ok})^* \qquad S; C \vdash instr^* : [t_1^*] \to [t_2^*]}{S; C \vdash \mathsf{handler}_n\{catch^*\} \ instr^* \ \mathsf{end} : [t_1^*] \to [t_2^*]}$$

# 7.4.8 Store Extension

Programs can mutate the store and its contained instances. Any such modification must respect certain invariants, such as not removing allocated instances or changing immutable definitions. While these invariants are inherent to the execution semantics of WebAssembly instructions and modules, host functions do not automatically adhere to them. Consequently, the required invariants must be stated as explicit constraints on the invocation of host functions. Soundness only holds when the embedder ensures these constraints.

The necessary constraints are codified by the notion of store *extension*: a store state S' extends state S, written  $S \leq S'$ , when the following rules hold.

#### Note

Extension does not imply that the new store is valid, which is defined separately above.

### Store S

- The length of S.funcs must not shrink.
- The length of S.tables must not shrink.
- ullet The length of S.mems must not shrink.
- The length of S.globals must not shrink.
- ullet The length of S.tags must not shrink.
- The length of S.elems must not shrink.
- ullet The length of  $S.\mathsf{datas}$  must not shrink.
- The length of S.structs must not shrink.
- ullet The length of S.arrays must not shrink.
- The length of S.exns must not shrink.
- For each function instance  $funcinst_i$  in the original S.funcs, the new function instance must be an extension of the old.
- For each table instance  $tableinst_i$  in the original S.tables, the new table instance must be an extension of the old.
- For each memory instance meminst<sub>i</sub> in the original S.mems, the new memory instance must be an extension
  of the old.

- For each global instance  $globalinst_i$  in the original S.globals, the new global instance must be an extension of the old.
- For each tag instance  $taginst_i$  in the original S.tags, the new tag instance must be an extension of the old.
- For each element instance  $eleminst_i$  in the original S.elems, the new element instance must be an extension of the old.
- For each data instance datainst<sub>i</sub> in the original S.datas, the new data instance must be an extension of the old.
- For each structure instance  $structinst_i$  in the original S.structs, the new structure instance must be an extension of the old.
- For each array instance  $arrayinst_i$  in the original S.arrays, the new array instance must be an extension of the old.
- For each exception instance exninst<sub>i</sub> in the original S.exns, the new exception instance must be an extension of the old.

```
S_1. \mathsf{funcs} = \mathit{funcinst}_1^* \qquad S_2. \mathsf{funcs} = \mathit{funcinst}_1'^* \mathit{funcinst}_2^* \qquad (\vdash \mathit{funcinst}_1 \preceq \mathit{funcinst}_1')^* \\ S_1. \mathsf{tables} = \mathit{tableinst}_1^* \qquad S_2. \mathsf{tables} = \mathit{tableinst}_1'^* \mathit{tableinst}_2^* \qquad (\vdash \mathit{tableinst}_1 \preceq \mathit{tableinst}_1')^* \\ S_1. \mathsf{mems} = \mathit{meminst}_1^* \qquad S_2. \mathsf{mems} = \mathit{meminst}_1'^* \mathit{meminst}_2^* \qquad (\vdash \mathit{tableinst}_1 \preceq \mathit{tableinst}_1')^* \\ S_1. \mathsf{globals} = \mathit{globalinst}_1^* \qquad S_2. \mathsf{globals} = \mathit{globalinst}_1'^* \mathit{globalinst}_2^* \qquad (\vdash \mathit{globalinst}_1 \preceq \mathit{meminst}_1')^* \\ S_1. \mathsf{atags} = \mathit{taginst}_1^* \qquad S_2. \mathsf{taggs} = \mathit{taginst}_1'^* \mathit{taginst}_2^* \qquad (\vdash \mathit{taginst}_1 \preceq \mathit{taginst}_1')^* \\ S_1. \mathsf{datas} = \mathit{datainst}_1^* \qquad S_2. \mathsf{datas} = \mathit{datainst}_1'^* \mathit{datainst}_2^* \qquad (\vdash \mathit{datainst}_1 \preceq \mathit{datainst}_1')^* \\ S_1. \mathsf{atrays} = \mathit{arrayinst}_1^* \qquad S_2. \mathsf{structs} = \mathit{structinst}_1'^* \mathit{arrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{arrayinst}_1')^* \\ S_1. \mathsf{atrays} = \mathit{arrayinst}_1^* \qquad S_2. \mathsf{atrays} = \mathit{arrayinst}_1'^* \mathit{arrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{arrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{arrayinst}_1'^* \mathit{arrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{arrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{atrayinst}_1'^* \mathit{atrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{atrayinst}_1'^* \mathit{atrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{atrayinst}_1'^* \mathit{atrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{atrayinst}_1'^* \mathit{atrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{atrayinst}_1'^* \mathit{atrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \\ S_2. \mathsf{atrays} = \mathit{atrayinst}_1'^* \mathit{atrayinst}_2^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \\ \mathsf{atrayinst}_1 \preceq \mathit{atrayinst}_1'^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^* \qquad (\vdash \mathit{atrayinst}_1 \preceq \mathit{atrayinst}_1')^
```

# $\vdash S_1 \preceq S_2$

# **Function Instance** *funcinst*

• A function instance must remain unchanged.

$$\vdash funcinst \prec funcinst$$

#### **Table Instance** *tableinst*

- The table type tableinst.type must remain unchanged.
- The length of *tableinst*.elem must not shrink.

$$\frac{n_1 \leq n_2}{\vdash \{\mathsf{type}\ tt, \mathsf{elem}\ (fa_1^?)^{n_1}\} \leq \{\mathsf{type}\ tt, \mathsf{elem}\ (fa_2^?)^{n_2}\}}$$

## **Memory Instance** *meminst*

- The memory type *meminst*.type must remain unchanged.
- The length of *meminst*.bytes must not shrink.

$$\frac{n_1 \leq n_2}{\vdash \{\mathsf{type}\ mt, \mathsf{bytes}\ b_1^{n_1}\} \leq \{\mathsf{type}\ mt, \mathsf{bytes}\ b_2^{n_2}\}}$$

#### Global Instance globalinst

- The global type *globalinst*.type must remain unchanged.
- Let *mut t* be the structure of *globalinst*.type.
- If mut is const, then the value globalinst.value must remain unchanged.

$$\frac{mut = \mathsf{var} \vee val_1 = val_2}{\vdash \{\mathsf{type}\,(mut\,\,t), \mathsf{value}\,\,val_1\} \leq \{\mathsf{type}\,(mut\,\,t), \mathsf{value}\,\,val_2\}}$$

## Tag Instance taginst

• A tag instance must remain unchanged.

$$\vdash taginst \prec taginst$$

#### **Element Instance** *eleminst*

- The reference type *eleminst*.type must remain unchanged.
- The list *eleminst*.elem must:
  - either remain unchanged,
  - or shrink to length 0.

# Data Instance datainst

- The list *datainst*.bytes must:
  - either remain unchanged,
  - or shrink to length 0.

## Structure Instance structinst

- The defined type *structinst*.type must remain unchanged.
- Assert: due to store well-formedness, the expansion of *structinst*.type is a structure type.
- Let struct *fieldtype*\* be the expansion of *structinst*.type.
- The length of the list *structinst*.fields must remain unchanged.
- Assert: due to store well-formedness, the length of structinst.fields is the same as the length of fieldtype\*.
- For each field value fieldval<sub>i</sub> in structinst.fields and corresponding field type fieldtype<sub>i</sub> in fieldtype\*:
  - Let  $mut_i$   $st_i$  be the structure of  $fieldtype_i$ .
  - If  $mut_i$  is const, then the field value  $fieldval_i$  must remain unchanged.

$$\frac{(mut = \mathsf{var} \lor fieldval_1 = fieldval_2)^*}{\vdash \{\mathsf{type}\,(mut\;st)^*, \mathsf{fields}\;fieldval_1^*\} \preceq \{\mathsf{type}\,(mut\;st)^*, \mathsf{fields}\;fieldval_2^*\}}$$

## **Array Instance** arrayinst

- The defined type arrayinst.type must remain unchanged.
- Assert: due to store well-formedness, the expansion of arrayinst.type is an array type.
- Let array *fieldtype* be the expansion of *arrayinst*.type.
- The length of the list *arrayinst*.fields must remain unchanged.
- Let *mut st* be the structure of *fieldtype*.
- If mut is const, then the sequence of field values arrayinst. fields must remain unchanged.

```
\frac{mut = \mathsf{var} \lor fieldval_1^* = fieldval_2^*}{\vdash \{\mathsf{type} \ (mut \ st), \mathsf{fields} \ fieldval_1^*\} \le \{\mathsf{type} \ (mut \ st), \mathsf{fields} \ fieldval_2^*\}}
```

## **Exception Instance** *exninst*

• An exception instance must remain unchanged.

 $\vdash exninst \prec exninst$ 

## 7.4.9 Theorems

Given the definition of valid configurations, the standard soundness theorems hold. 5254

**Theorem (Preservation).** If a configuration S;T is valid with result type  $[t^*]$  (i.e.,  $\vdash S;T:[t^*]$ ), and steps to S';T' (i.e.,  $S;T\hookrightarrow S';T'$ ), then S';T' is a valid configuration with the same result type (i.e.,  $\vdash S';T':[t^*]$ ). Furthermore, S' is an extension of S (i.e.,  $\vdash S \prec S'$ ).

A *terminal* thread is one whose sequence of instructions is a result. A terminal configuration is a configuration whose thread is terminal.

**Theorem (Progress).** If a configuration S; T is valid (i.e.,  $\vdash S; T : [t^*]$  for some result type  $[t^*]$ ), then either it is terminal, or it can step to some configuration S'; T' (i.e.,  $S; T \hookrightarrow S'; T'$ ).

From Preservation and Progress the soundness of the WebAssembly type system follows directly.

**Corollary** (Soundness). If a configuration S;T is valid (i.e.,  $\vdash S;T:[t^*]$  for some result type  $[t^*]$ ), then it either diverges or takes a finite number of steps to reach a terminal configuration S';T' (i.e.,  $S;T\hookrightarrow *S';T'$ ) that is valid with the same result type (i.e.,  $\vdash S';T':[t^*]$ ) and where S' is an extension of S (i.e.,  $\vdash S \preceq S'$ ).

In other words, every thread in a valid configuration either runs forever, traps, throws an exception, or terminates with a result that has the expected type. Consequently, given a valid store, no computation defined by instantiation or invocation of a valid module can "crash" or otherwise (mis)behave in ways not covered by the execution semantics given in this specification.

# 7.5 Type System Properties

# 7.5.1 Principal Types

The type system of WebAssembly features both subtyping and simple forms of polymorphism for instruction types. That has the effect that every instruction or instruction sequence can be classified with multiple different instruction types.

<sup>&</sup>lt;sup>52</sup> A machine-verified version of the formalization and soundness proof of the PLDI 2017 paper is described in the following article: Conrad Watt. Mechanising and Verifying the WebAssembly Specification<sup>53</sup>. Proceedings of the 7th ACM SIGPLAN Conference on Certified Programs and Proofs (CPP 2018). ACM 2018.

<sup>53</sup> https://dl.acm.org/citation.cfm?id=3167082

<sup>&</sup>lt;sup>54</sup> Machine-verified formalizations and soundness proofs of the semantics from the official specification are described in the following article: Conrad Watt, Xiaojia Rao, Jean Pichon-Pharabod, Martin Bodin, Philippa Gardner. Two Mechanisations of WebAssembly 1.0<sup>55</sup>. Proceedings of the 24th International Symposium on Formal Methods (FM 2021). Springer 2021.

 $<sup>^{55}\</sup> https://link.springer.com/chapter/10.1007/978-3-030-90870-6\_4$ 

However, the typing rules still allow deriving *principal types* for instruction sequences. That is, every valid instruction sequence has one particular type scheme, possibly containing some unconstrained place holder *type variables*, that is a subtype of all its valid instruction types, after substituting its type variables with suitable specific types.

Moreover, when deriving an instruction type in a "forward" manner, i.e., the *input* of the instruction sequence is already fixed to specific types, then it has a principal *output* type expressible without type variables, up to a possibly polymorphic stack bottom representable with one single variable. In other words, "forward" principal types are effectively *closed*.

#### Note

For example, in isolation, the instruction ref.as\_non\_null has the type  $[(\text{ref null }ht)] \rightarrow [(\text{ref }ht)]$  for any choice of valid heap type ht. Moreover, if the input type [(ref null ht)] is already determined, i.e., a specific ht is given, then the output type [(ref ht)] is fully determined as well.

The implication of the latter property is that a validator for *complete* instruction sequences (as they occur in valid modules) can be implemented with a simple left-to-right algorithm that does not require the introduction of type variables.

A typing algorithm capable of handling *partial* instruction sequences (as might be considered for program analysis or program manipulation) needs to introduce type variables and perform substitutions, but it does not need to perform backtracking or record any non-syntactic constraints on these type variables.

Technically, the syntax of heap, value, and result types can be enriched with type variables as follows:

```
\begin{array}{lll} \textit{null} & ::= & \text{null}^? \mid \alpha_{\textit{null}} \\ \textit{heaptype} & ::= & \dots \mid \alpha_{\textit{heaptype}} \\ \textit{reftype} & ::= & \text{ref } \textit{null } \textit{heaptype} \\ \textit{valtype} & ::= & \dots \mid \alpha_{\textit{valtype}} \mid \alpha_{\textit{numvectype}} \\ \textit{resulttype} & ::= & \left[\alpha_{\textit{valtype}^*}^? \textit{valtype}^*\right] \end{array}
```

where each  $\alpha_{xyz}$  ranges over a set of type variables for syntactic class xyz, respectively. The special class numvectype is defined as  $numtype \mid vectype \mid$  bot, and is only needed to handle unannotated select instructions.

A type is *closed* when it does not contain any type variables, and *open* otherwise. A *type substitution*  $\sigma$  is a finite mapping from type variables to closed types of the respective syntactic class. When applied to an open type, it replaces the type variables  $\alpha$  from its domain with the respective  $\sigma(\alpha)$ .

**Theorem (Principal Types).** If an instruction sequence  $instr^*$  is valid with some closed instruction type instrtype (i.e.,  $C \vdash instr^* : instrtype$ ), then it is also valid with a possibly open instruction type  $instrtype_{\min}$  (i.e.,  $C \vdash instr^* : instrtype_{\min}$ ), such that for every closed type instrtype' with which  $instr^*$  is valid (i.e., for all  $C \vdash instr^* : instrtype'$ ), there exists a substitution  $\sigma$ , such that  $\sigma(instrtype_{\min})$  is a subtype of instrtype' (i.e.,  $C \vdash \sigma(instrtype_{\min}) \le instrtype'$ ). Furthermore,  $instrtype_{\min}$  is unique up to the choice of type variables.

Theorem (Closed Principal Forward Types). If closed input type  $[t_1^*]$  is given and the instruction sequence  $instr^*$  is valid with instruction type  $[t_1^*] \to_{x^*} [t_2^*]$  (i.e.,  $C \vdash instr^* : [t_1^*] \to_{x^*} [t_2^*]$ ), then it is also valid with instruction type  $[t_1^*] \to_{x^*} [\alpha_{valtype^*} t^*]$  (i.e.,  $C \vdash instr^* : [t_1^*] \to_{x^*} [\alpha_{valtype^*} t^*]$ ), where all  $t^*$  are closed, such that for every closed result type  $[t_2'^*]$  with which  $instr^*$  is valid (i.e., for all  $C \vdash instr^* : [t_1^*] \to_{x^*} [t_2'^*]$ ), there exists a substitution  $\sigma$ , such that  $[t_2'^*] = [\sigma(\alpha_{valtype^*}) t^*]$ .

# 7.5.2 Type Lattice

The Principal Types property depends on the existence of a *greatest lower bound* for any pair of types.

**Theorem (Greatest Lower Bounds for Value Types).** For any two value types  $t_1$  and  $t_2$  that are valid (i.e.,  $C \vdash t_1$ : ok and  $C \vdash t_2$ : ok), there exists a valid value type t that is a subtype of both  $t_1$  and  $t_2$  (i.e.,  $C \vdash t$ : ok and  $C \vdash t \leq t_1$  and  $C \vdash t \leq t_2$ ), such that *every* valid value type t' that also is a subtype of both  $t_1$  and  $t_2$  (i.e., for all  $C \vdash t'$ : ok and  $C \vdash t' \leq t_1$  and  $C \vdash t' \leq t_2$ ), is a subtype of t (i.e.,  $C \vdash t' \leq t_2$ ).

#### Note

The greatest lower bound of two types may be bot.

**Theorem (Conditional Least Upper Bounds for Value Types).** Any two value types  $t_1$  and  $t_2$  that are valid (i.e.,  $C \vdash t_1 :$  ok and  $C \vdash t_2 :$  ok) either have no common supertype, or there exists a valid value type t that is a supertype of both  $t_1$  and  $t_2$  (i.e.,  $C \vdash t :$  ok and  $C \vdash t_1 \le t$  and  $C \vdash t_2 \le t$ ), such that *every* valid value type t' that also is a supertype of both  $t_1$  and  $t_2$  (i.e., for all  $C \vdash t' :$  ok and  $C \vdash t_1 \le t'$  and  $C \vdash t_2 \le t'$ ), is a supertype of t (i.e.,  $C \vdash t \le t'$ ).

#### Note

If a top type was added to the type system, a least upper bound would exist for any two types.

**Corollary** (**Type Lattice**). Assuming the addition of a provisional top type, value types form a lattice with respect to their subtype relation.

Finally, value types can be partitioned into multiple disjoint hierarchies that are not related by subtyping, except through bot.

**Theorem (Disjoint Subtype Hierarchies).** The greatest lower bound of two value types is bot or ref bot if and only if they do not have a least upper bound.

In other words, types that do not have common supertypes, do not have common subtypes either (other than bot or ref bot), and vice versa.

#### Note

Types from disjoint hierarchies can safely be represented in mutually incompatible ways in an implementation, because their values can never flow to the same place.

# 7.5.3 Compositionality

Valid instruction sequences can be freely *composed*, as long as their types match up.

**Theorem (Composition).** If two instruction sequences  $instr_1^*$  and  $instr_2^*$  are valid with types  $[t_1^*] \rightarrow_{x_1^*} [t^*]$  and  $[t^*] \rightarrow_{x_2^*} [t_2^*]$ , respectively (i.e.,  $C \vdash instr_1^* : [t_1^*] \rightarrow_{x_1^*} [t^*]$  and  $C \vdash instr_1^* : [t^*] \rightarrow_{x_2^*} [t_2^*]$ ), then the concatenated instruction sequence  $(instr_1^* \ instr_2^*)$  is valid with type  $[t_1^*] \rightarrow_{x_1^* \ x_2^*} [t_2^*]$  (i.e.,  $C \vdash instr_1^* \ instr_2^* : [t_1^*] \rightarrow_{x_1^* \ x_2^*} [t_2^*]$ ).

### Note

More generally, instead of a shared type  $[t^*]$ , it suffices if the output type of  $instr_1^*$  is a subtype of the input type of  $instr_1^*$ , since the subtype can always be weakened to its supertype by subsumption.

Inversely, valid instruction sequences can also freely be *decomposed*, that is, splitting them anywhere produces two instruction sequences that are both valid.

**Theorem (Decomposition).** If an instruction sequence  $instr^*$  that is valid with type  $[t_1^*] \to_{x^*} [t_2^*]$  (i.e.,  $C \vdash instr^* : [t_1^*] \to_{x^*} [t_2^*]$ ) is split into two instruction sequences  $instr_1^*$  and  $instr_2^*$  at any point (i.e.,  $instr^* = instr_1^* \ instr_2^*$ ), then these are separately valid with some types  $[t_1^*] \to_{x_1^*} [t^*]$  and  $[t^*] \to_{x_2^*} [t_2^*]$ , respectively (i.e.,  $C \vdash instr_1^* : [t_1^*] \to_{x_1^*} [t^*]$  and  $C \vdash instr_1^* : [t^*] \to_{x_2^*} [t_2^*]$ ), where  $x^* = x_1^* \ x_2^*$ .

## Note

This property holds because validation is required even for unreachable code. Without that,  $instr_2^*$  might not be valid in isolation.

# 7.6 Validation Algorithm

The specification of WebAssembly validation is purely *declarative*. It describes the constraints that must be met by a module or instruction sequence to be valid.

This section sketches the skeleton of a sound and complete *algorithm* for effectively validating code, i.e., sequences of instructions. (Other aspects of validation are straightforward to implement.)

In fact, the algorithm is expressed over the flat sequence of opcodes as occurring in the binary format, and performs only a single pass over it. Consequently, it can be integrated directly into a decoder.

The algorithm is expressed in typed pseudo code whose semantics is intended to be self-explanatory.

# 7.6.1 Data Structures

#### **Types**

Value types are representable as sets of enumerations:

```
type num_type = I32 | I64 | F32 | F64
type vec_type = V128
type heap_type =
  Any | Eq | I31 | Struct | Array | None |
  Func | Nofunc | Exn | Noexn | Extern | Noextern | Bot |
  Def(def : def_type)
type ref_type = Ref(heap : heap_type, null : bool)
type val_type = num_type | vec_type | ref_type | Bot

func is_num(t : val_type) : bool =
  return t = I32 || t = I64 || t = F32 || t = F64 || t = Bot

func is_vec(t : val_type) : bool =
  return t = V128 || t = Bot

func is_ref(t : val_type) : bool =
  return not (is_num t || is_vec t) || t = Bot
```

Similarly, defined types def\_type can be represented:

```
type pack_type = I8 | I16
type field_type = Field(val : val_type | pack_type, mut : bool)

type struct_type = Struct(fields : list(field_type))
type array_type = Array(fields : field_type)
type func_type = Func(params : list(val_type), results : list(val_type))
type comp_type = struct_type | array_type | func_type

type sub_type = Sub(super : list(def_type), body : comp_type, final : bool)
type rec_type = Rec(types : list(sub_type))

type def_type = Def(rec : rec_type, proj : int32)

func unpack_field(t : field_type) : val_type =
    if (it = I8 || t = I16) return I32
    return t
```

```
func expand_def(t : def_type) : comp_type =
  return t.rec.types[t.proj].body
```

These representations assume that all types have been closed by substituting all type indices (in concrete heap types and in sub types) with their respective defined types. This includes *recursive* references to enclosing defined types, such that type representations form graphs and may be *cyclic* for recursive types.

We assume that all types have been *canonicalized*, such that equality on two type representations holds if and only if their closures are syntactically equivalent, making it a constant-time check.

#### Note

For the purpose of type canonicalization, recursive references from a heap type to an enclosing recursive type (i.e., forward edges in the graph that form a cycle) need to be distinguished from references to previously defined types. However, this distinction does not otherwise affect validation, so is ignored here. In the graph representation, all recursive types are effectively infinitely unrolled.

We further assume that validation and subtyping checks are defined on value types, as well as a few auxiliary functions on composite types:

```
func validate_val_type(t : val_type)
func validate_ref_type(t : ref_type)

func matches_val(t1 : val_type, t2 : val_type) : bool
func matches_ref(t1 : val_type, t2 : val_type) : bool

func is_func(t : comp_type) : bool
func is_struct(t : comp_type) : bool
func is_array(t : comp_type) : bool
```

Finally, the following function computes the least precise supertype of a given heap type (its corresponding top type):

```
func top_heap_type(t : heap_type) : heap_type =
 switch (t)
   case (Any | Eq | I31 | Struct | Array | None)
      return Any
   case (Func | Nofunc)
     return Func
   case (Extern | Noextern)
     return Extern
   case (Def(dt))
      switch (dt.rec.types[dt.proj].body)
        case (Struct(_) | Array(_))
          return Any
        case (Func(_))
          return Func
   case (Bot)
      raise CannotOccurInSource
```

#### **Context**

Validation requires a context for checking uses of indices. For the purpose of presenting the algorithm, it is maintained in a set of global variables:

```
var return_type : list(val_type)
var types : array(def_type)
var locals : array(val_type)
var locals_init : array(bool)
var globals : array(global_type)
var funcs : array(func_type)
var tables : array(table_type)
var mems : array(mem_type)
```

This assumes suitable representations for the various types besides val\_type, which are omitted here.

For locals, there is an additional array recording the initialization status of each local.

#### **Stacks**

The algorithm uses three separate stacks: the *value stack*, the *control stack*, and the *initialization stack*. The value stack tracks the types of operand values on the stack. The control stack tracks surrounding structured control instructions and their associated blocks. The initialization stack records all locals that have been initialized since the beginning of the function.

```
type val_stack = stack(val_type)
type init_stack = stack(u32)

type ctrl_stack = stack(ctrl_frame)
type ctrl_frame = {
  opcode : opcode
    start_types : list(val_type)
    end_types : list(val_type)
    val_height : nat
    init_height : nat
    unreachable : bool
}
```

For each entered block, the control stack records a *control frame* with the originating opcode, the types on the top of the operand stack at the start and end of the block (used to check its result as well as branches), the height of the operand stack at the start of the block (used to check that operands do not underflow the current block), the height of the initialization stack at the start of the block (used to reset initialization status at the end of the block), and a flag recording whether the remainder of the block is unreachable (used to handle stack-polymorphic typing after branches).

For the purpose of presenting the algorithm, these stacks are simply maintained as global variables:

```
var vals : val_stack
var inits : init_stack
var ctrls : ctrl_stack
```

However, these variables are not manipulated directly by the main checking function, but through a set of auxiliary functions:

```
func push_val(type : val_type) =
  vals.push(type)

func pop_val() : val_type =
  if (vals.size() = ctrls[0].height && ctrls[0].unreachable) return Bot
  error_if(vals.size() = ctrls[0].height)
  return vals.pop()

func pop_val(expect : val_type) : val_type =
  let actual = pop_val()
```

```
error_if(not matches_val(actual, expect))
 return actual
func pop_num() : num_type | Bot =
 let actual = pop_val()
  error_if(not is_num(actual))
 return actual
func pop_ref() : ref_type =
 let actual = pop_val()
 error_if(not is_ref(actual))
 if (actual = Bot) return Ref(Bot, false)
 return actual
func push_vals(types : list(val_type)) = foreach (t in types) push_val(t)
func pop_vals(types : list(val_type)) : list(val_type) =
 var popped := []
 foreach (t in reverse(types)) popped.prepend(pop_val(t))
 return popped
```

Pushing an operand value simply pushes the respective type to the value stack.

Popping an operand value checks that the value stack does not underflow the current block and then removes one type. But first, a special case is handled where the block contains no known values, but has been marked as unreachable. That can occur after an unconditional branch, when the stack is typed polymorphically. In that case, the Bot type is returned, because that is a *principal* choice trivially satisfying all use constraints.

A second function for popping an operand value takes an expected type, which the actual operand type is checked against. The types may differ by subtyping, including the case where the actual type is Bot, and thereby matches unconditionally. The function returns the actual type popped from the stack.

Finally, there are accumulative functions for pushing or popping multiple operand types.

### Note

The notation stack[i] is meant to index the stack from the top, so that, e.g., ctrls[0] accesses the element pushed last.

The initialization stack and the initialization status of locals is manipulated through the following functions:

```
func get_local(idx : u32) =
  error_if(not locals_init[idx])

func set_local(idx : u32) =
  if (not locals_init[idx])
   inits.push(idx)
   locals_init[idx] := true

func reset_locals(height : nat) =
  while (inits.size() > height)
  locals_init[inits.pop()] := false
```

Getting a local verifies that it is known to be initialized. When a local is set that was not set already, then its initialization status is updated and the change is recorded in the initialization stack. Thus, the initialization status of all locals can be reset to a previous state by denoting a specific height in the initialization stack.

The size of the initialization stack is bounded by the number of (non-defaultable) locals in a function, so can be preallocated by an algorithm.

The control stack is likewise manipulated through auxiliary functions:

```
func push_ctrl(opcode : opcode, in : list(val_type), out : list(val_type)) =
 let frame = ctrl_frame(opcode, in, out, vals.size(), inits.size(), false)
 ctrls.push(frame)
 push_vals(in)
func pop_ctrl() : ctrl_frame =
 error_if(ctrls.is_empty())
 let frame = ctrls[0]
 pop_vals(frame.end_types)
 error_if(vals.size() =/= frame.val_height)
 reset_locals(frame.init_height)
 ctrls.pop()
 return frame
func label_types(frame : ctrl_frame) : list(val_types) =
 return (if (frame.opcode = loop) frame.start_types else frame.end_types)
func unreachable() =
 vals.resize(ctrls[0].height)
 ctrls[0].unreachable := true
```

Pushing a control frame takes the types of the label and result values. It allocates a new frame record recording them along with the current height of the operand stack and marks the block as reachable.

Popping a frame first checks that the control stack is not empty. It then verifies that the operand stack contains the right types of values expected at the end of the exited block and pops them off the operand stack. Afterwards, it checks that the stack has shrunk back to its initial height. Finally, it undoes all changes to the initialization status of locals that happend inside the block.

The type of the label associated with a control frame is either that of the stack at the start or the end of the frame, determined by the opcode that it originates from.

Finally, the current frame can be marked as unreachable. In that case, all existing operand types are purged from the value stack, in order to allow for the stack-polymorphism logic in pop\_val to take effect. Because every function has an implicit outermost label that corresponds to an implicit block frame, it is an invariant of the validation algorithm that there always is at least one frame on the control stack when validating an instruction, and hence, ctrls[0] is always defined.

#### Note

Even with the unreachable flag set, consecutive operands are still pushed to and popped from the operand stack. That is necessary to detect invalid examples like (unreachable (i32.const) i64.add). However, a polymorphic stack cannot underflow, but instead generates Bot types as needed.

## 7.6.2 Validation of Opcode Sequences

The following function shows the validation of a number of representative instructions that manipulate the stack. Other instructions are checked in a similar manner.

```
func validate(opcode) =
   switch (opcode)
   case (i32.add)
    pop_val(I32)
    pop_val(I32)
    push_val(I32)
```

```
case (drop)
  pop_val()
case (select)
  pop_val(I32)
  let t1 = pop_val()
 let t2 = pop_val()
  error_if(not (is_num(t1) && is_num(t2) || is_vec(t1) && is_vec(t2)))
  error_if(t1 =/= t2 && t1 =/= Bot && t2 =/= Bot)
 push_val(if (t1 = Bot) t2 else t1)
case (select t)
  pop_val(I32)
  pop_val(t)
 pop_val(t)
 push_val(t)
case (ref.is_null)
  pop_ref()
  push_val(I32)
case (ref.as_non_null)
  let rt = pop_ref()
  push_val(Ref(rt.heap, false))
case (ref.test rt)
  validate_ref_type(rt)
  pop_val(Ref(top_heap_type(rt), true))
 push_val(I32)
case (local.get x)
  get_local(x)
  push_val(locals[x])
case (local.set x)
  pop_val(locals[x])
  set_local(x)
case (unreachable)
  unreachable()
case (block t1*->t2*)
  pop_vals([t1*])
  push_ctrl(block, [t1*], [t2*])
case (loop t1*->t2*)
 pop_vals([t1*])
  push_ctrl(loop, [t1*], [t2*])
case (if t1*->t2*)
  pop_val(I32)
  pop_vals([t1*])
 push_ctrl(if, [t1*], [t2*])
case (end)
  let frame = pop_ctrl()
```

```
push_vals(frame.end_types)
case (else)
  let frame = pop_ctrl()
  error_if(frame.opcode =/= if)
  push_ctrl(else, frame.start_types, frame.end_types)
case (br n)
  error_if(ctrls.size() < n)
  pop_vals(label_types(ctrls[n]))
  unreachable()
case (br_if n)
  error_if(ctrls.size() < n)</pre>
  pop_val(I32)
  pop_vals(label_types(ctrls[n]))
  push_vals(label_types(ctrls[n]))
case (br_table n* m)
  pop_val(I32)
  error_if(ctrls.size() < m)</pre>
  let arity = label_types(ctrls[m]).size()
  foreach (n in n*)
    error_if(ctrls.size() < n)</pre>
    error_if(label_types(ctrls[n]).size() =/= arity)
    push_vals(pop_vals(label_types(ctrls[n])))
  pop_vals(label_types(ctrls[m]))
  unreachable()
case (br_on_null n)
  error_if(ctrls.size() < n)</pre>
  let rt = pop_ref()
  pop_vals(label_types(ctrls[n]))
  push_vals(label_types(ctrls[n]))
  push_val(Ref(rt.heap, false))
case (br_on_cast n rt1 rt2)
  validate_ref_type(rt1)
  validate_ref_type(rt2)
  pop_val(rt1)
  push_val(rt2)
  pop_vals(label_types(ctrls[n]))
  push_vals(label_types(ctrls[n]))
  pop_val(rt2)
  push_val(diff_ref_type(rt2, rt1))
case (return)
  pop_vals(return_types)
  unreachable()
case (call_ref x)
  let t = expand_def(types[x])
  error_if(not is_func(t))
  pop_vals(t.params)
  pop_val(Ref(Def(types[x])))
  push_vals(t.results)
```

```
case (return_call_ref x)
  let t = expand_def(types[x])
  error_if(not is_func(t))
  pop_vals(t.params)
  pop_val(Ref(Def(types[x])))
  error_if(t.results.len() =/= return_types.len())
  push_vals(t.results)
  pop_vals(return_types)
  unreachable()
case (struct.new x)
  let t = expand_def(types[x])
  error_if(not is_struct(t))
  for (ti in reverse(t.fields))
    pop_val(unpack_field(ti))
  push_val(Ref(Def(types[x])))
case (struct.set x n)
  let t = expand_def(types[x])
  error_if(not is_struct(t) || n >= t.fields.len())
  pop_val(Ref(Def(types[x])))
  pop_val(unpack_field(st.fields[n]))
case (throw x)
   pop_vals(tags[x].type.params)
   unreachable()
case (try_table t1*->t2* handler*)
  pop_vals([t1*])
  foreach (handler in handler*)
    error_if(ctrls.size() < handler.label)</pre>
    push_ctrl(catch, [], label_types(ctrls[handler.label]))
    switch (handler.clause)
      case (catch x)
        push_vals(tags[x].type.params)
      case (catch_ref x)
        push_vals(tags[x].type.params)
        push_val(Exnref)
      case (catch_all)
        skip
      case (catch_all_ref)
        push_val(Exnref)
    pop_ctrl()
  push_ctrl(try_table, [t1*], [t2*])
```

### Note

It is an invariant under the current WebAssembly instruction set that an operand of Bot type is never duplicated on the stack. This would change if the language were extended with stack instructions like dup. Under such an extension, the above algorithm would need to be refined by replacing the Bot type with proper *type variables* to ensure that all uses are consistent.

# 7.7 Custom Sections and Annotations

This appendix defines dedicated custom sections for WebAssembly's binary format and annotations for the text format. Such sections or annotations do not contribute to, or otherwise affect, the WebAssembly semantics, and may be ignored by an implementation. However, they provide useful meta data that implementations can make use of to improve user experience or take compilation hints.

## 7.7.1 Name Section

The *name section* is a custom section whose name string is itself 'name'. The name section should appear only once in a module, and only after the data section.

The purpose of this section is to attach printable names to definitions in a module, which e.g. can be used by a debugger or when parts of the module are to be rendered in text form.

#### Note

All names are represented in Unicode<sup>56</sup> encoded in UTF-8. Names need not be unique.

#### **Subsections**

The data of a name section consists of a sequence of subsections. Each subsection consists of a

- a one-byte subsection id,
- the use size of the contents, in bytes,
- the actual contents, whose structure is dependent on the subsection id.

The following subsection ids are used:

ld	Subsection
0	module name
1	function names
2	local names
4	type names
10	field names
11	tag names

Each subsection may occur at most once, and in order of increasing id.

#### **Name Maps**

A *name map* assigns names to indices in a given index space. It consists of a list of index/name pairs in order of increasing index value. Each index must be unique, but the assigned names need not be.

```
namemap ::= list(nameassoc)
nameassoc ::= idx name
```

<sup>&</sup>lt;sup>56</sup> https://www.unicode.org/versions/latest/

An *indirect name map* assigns names to a two-dimensional index space, where secondary indices are *grouped* by primary indices. It consists of a list of primary index/name map pairs in order of increasing index value, where each name map in turn maps secondary indices to names. Each primary index must be unique, and likewise each secondary index per individual name map.

```
indirectnamemap ::= list(indirectnameassoc)
indirectnameassoc ::= idx namemap
```

#### **Module Names**

The module name subsection has the id 0. It simply consists of a single name that is assigned to the module itself.

```
modulenamesubsec ::= namesubsection_0(name)
```

#### **Function Names**

The function name subsection has the id 1. It consists of a name map assigning function names to function indices.

```
functionamesubsec ::= namesubsection<sub>1</sub>(namemap)
```

#### **Local Names**

The *local name subsection* has the id 2. It consists of an indirect name map assigning local names to local indices grouped by function indices.

```
localnamesubsec ::= namesubsection_2(indirectnamemap)
```

## **Type Names**

The type name subsection has the id 4. It consists of a name map assigning type names to type indices.

```
typenamesubsec := namesubsection<sub>4</sub>(namemap)
```

#### **Field Names**

The *field name subsection* has the id 10. It consists of an indirect name map assigning field names to field indices grouped by the type indices of their respective structure types.

```
fieldnamesubsec ::= namesubsection<sub>1</sub>0(indirectnamemap)
```

#### **Tag Names**

The tag name subsection has the id 11. It consists of a name map assigning tag names to tag indices.

```
tagnamesubsec ::= namesubsection<sub>1</sub>(namemap)
```

### 7.7.2 Name Annotations

*Name annotations* are the textual analogue to the name section and provide a textual representation for it. Consequently, their id is @name.

Analogous to the name section, name annotations are allowed on modules, functions, and locals (including parameters). They can be placed where the text format allows binding occurrences of respective identifiers. If both an identifier and a name annotation are given, the annotation is expected *after* the identifier. In that case, the annotation takes precedence over the identifier as a textual representation of the binding's name. At most one name annotation may be given per binding.

All name annotations have the following format:

```
nameannot ::= '(@name' string')'
```

#### Note

All name annotations can be arbitrary UTF-8 strings. Names need not be unique.

#### **Module Names**

A module name annotation must be placed on a module definition, directly after the 'module' keyword, or if present, after the following module identifier.

```
modulenameannot ::= nameannot
```

#### **Function Names**

A function name annotation must be placed on a function definition or function import, directly after the 'func' keyword, or if present, after the following function identifier or.

```
funcnameannot ::= nameannot
```

#### **Parameter Names**

A parameter name annotation must be placed on a parameter declaration, directly after the 'param' keyword, or if present, after the following parameter identifier. It may only be placed on a declaration that declares exactly one parameter.

```
paramnameannot ::= nameannot
```

## **Local Names**

A *local name annotation* must be placed on a local declaration, directly after the 'local' keyword, or if present, after the following local identifier. It may only be placed on a declaration that declares exactly one local.

```
localnameannot ::= nameannot
```

# **Type Names**

A type name annotation must be placed on a type declaration, directly after the 'type' keyword, or if present, after the following type identifier.

```
\mathtt{typenameannot} \ ::= \ \mathtt{nameannot}
```

#### **Field Names**

A *field name annotation* must be placed on the field of a structure type, directly after the 'field' keyword, or if present, after the following field identifier. It may only be placed on a declaration that declares exactly one field.

```
fieldnameannot ::= nameannot
```

#### **Tag Names**

A tag name annotation must be placed on a tag declaration or tag import, directly after the 'tag' keyword, or if present, after the following tag identifier.

```
tagnameannot ::= nameannot
```

## 7.7.3 Custom Annotations

*Custom annotations* are a generic textual representation for any custom section. Their id is @custom. By generating custom annotations, tools converting between binary format and text format can maintain and round-trip the content of custom sections even when they do not recognize them.

Custom annotations must be placed inside a module definition. They must occur anywhere after the 'module' keyword, or if present, after the following module identifier. They must not be nested into other constructs.

```
'(@custom' string customplace? datastring ')'
customannot ::=
                    `(``before'``first'``)'
customplace
                       'before' sec')'
                       'after' sec')'
                       'after' 'last' ')'
sec
                    'type'
                    'import'
                    'func'
                    'table'
                    'memory'
                    'global'
                    'export'
                    'start'
                    'elem'
                    'code'
                    'data'
                    'datacount'
```

The first string in a custom annotation denotes the name of the custom section it represents. The remaining strings collectively represent the section's payload data, written as a data string, which can be split up into a possibly empty sequence of individual string literals (similar to data segments).

An arbitrary number of custom annotations (even of the same name) may occur in a module, each defining a separate custom section when converting to binary format. Placement of the sections in the binary can be customized via explicit *placement* directives, that position them either directly before or directly after a known section. That section must exist and be non-empty in the binary encoding of the annotated module. The placements (before first) and (after last) denote virtual sections before the first and after the last known section, respectively. When the placement directive is omitted, it defaults to (after last).

If multiple placement directives appear for the same position, then the sections are all placed there, in order of their appearance in the text. For this purpose, the position after a section is considered different from the position before the consecutive section, and the former occurs before the latter.

#### Note

Future versions of WebAssembly may introduce additional sections between others or at the beginning or end of a module. Using first and last guarantees that placement will still go before or after any future section, respectively.

If a custom section with a specific section id is given as well as annotations representing the same custom section (e.g., @name annotations as well as a @custom annotation for a name section), then two sections are assumed to be created. Their relative placement will depend on the placement directive given for the @custom annotation as well as the implicit placement requirements of the custom section, which are applied to the other annotation.

#### Note

For example, the following module,

```
(module
  (@custom "A" "aaa")
  (type $t (func))
  (@custom "B" (after func) "bbb")
  (@custom "C" (before func) "ccc")
  (@custom "D" (after last) "ddd")
  (table 10 funcref)
  (func (type $t))
  (@custom "E" (after import) "eee")
  (@custom "F" (before type) "fff")
  (@custom "G" (after data) "ggg")
  (@custom "H" (after code) "hhh")
  (@custom "I" (after func) "iii")
  (@custom "J" (before func) "jjj")
  (@custom "K" (before first) "kkk")
)
```

will result in the following section ordering:

```
custom section "K"

custom section "F"

type section

custom section "E"

custom section "C"

custom section "J"

function section

custom section "B"

custom section "I"

table section

code section

custom section "H"

custom section "G"

custom section "G"

custom section "A"

custom section "D"
```

# 7.8 Change History

Since the original release 1.0 of the WebAssembly specification, a number of proposals for extensions have been integrated. The following sections provide an overview of what has changed.

# 7.8.1 Release 2.0

# **Sign Extension Instructions**

Added new numeric instructions for performing sign extension within integer representations.<sup>57</sup>

- New numeric instructions:
  - $inn.extendN_s$

## **Non-trapping Float-to-Int Conversions**

Added new conversion instructions that avoid trapping when converting a floating-point number to an integer.<sup>58</sup>

- New numeric instructions:
  - inn.trunc\_sat\_fmm\_sx

## **Multiple Values**

Generalized the result type of blocks and functions to allow for multiple values; in addition, introduced the ability to have block parameters.<sup>59</sup>

- Function types allow more than one result
- Block types can be arbitrary function types

# **Reference Types**

Added funcref and externref as new value types and respective instructions.<sup>60</sup>

- New reference value types:
  - funcref
  - externref
- New reference instructions:
  - ref.null
  - ref.func
  - ref.is\_null
- Extended parametric instruction:
  - select with optional type immediate
- New declarative form of element segment

# **Table Instructions**

Added instructions to directly access and modify tables.<sup>60</sup>

- Table types allow any reference type as element type
- New table instructions:
  - table.get
  - table.set
  - table.size
  - table.grow

 $<sup>^{57}\</sup> https://github.com/WebAssembly/spec/tree/main/proposals/sign-extension-ops/$ 

 $<sup>^{58}\</sup> https://github.com/WebAssembly/spec/tree/main/proposals/nontrapping-float-to-int-conversion/$ 

<sup>59</sup> https://github.com/WebAssembly/spec/tree/main/proposals/multi-value/

<sup>60</sup> https://github.com/WebAssembly/spec/tree/main/proposals/reference-types/

## **Multiple Tables**

Added the ability to use multiple tables per module. Page 303, 60

- · Modules may
  - define multiple tables
  - import multiple tables
  - export multiple tables
- Table instructions take a table index immediate:
  - table.get
  - table.set
  - table.size
  - table.grow
  - call\_indirect
- Element segments take a table index

# **Bulk Memory and Table Instructions**

Added instructions that modify ranges of memory or table entries.  $^{\text{Page }303,\,6061}$ 

- New memory instructions:
  - memory.fill
  - memory.init
  - memory.copy
  - data.drop
- New table instructions:
  - table.fill
  - table.init
  - table.copy
  - elem.drop
- New passive form of data segment
- New passive form of element segment
- New data count section in binary format
- · Active data and element segments boundaries are no longer checked at compile time but may trap instead

## **Vector Instructions**

Added vector type and instructions that manipulate multiple numeric values in parallel (also known as SIMD, single instruction multiple data)<sup>62</sup>

- New value type:
  - V128
- New memory instructions:
  - v128.load
  - v128.load $NxM\_sx$

 $<sup>^{61}\</sup> https://github.com/WebAssembly/spec/tree/main/proposals/bulk-memory-operations/$ 

<sup>62</sup> https://github.com/WebAssembly/spec/tree/main/proposals/simd/

- v128.loadN\_zero
- $v128.loadN_splat$
- v128.load $N_{\rm lane}$
- v128.store
- $v128.storeN_lane$
- New constant vector instruction:
  - v128.const
- New unary vector instructions:
  - v128.not
  - i $N \times M$ .abs
  - -iNxM.neg
  - i8x16.popcnt
  - fNxM.abs
  - fNxM.neg
  - fNxM.sqrt
  - fNxM.ceil
  - fNxM.floor
  - fNxM.trunc
  - fNxM.nearest
- New binary vector instructions:
  - v128.and
  - v128.andnot
  - v128.or
  - v128.xor
  - i $N \times M$ .add
  - -iNxM.sub
  - $iN \times M$ .mul
  - $iN\!x\!M.\mathsf{add\_sat\_}sx$
  - i $NxM.sub\_sat\_sx$
  - i $NxM.min\_sx$
  - $iNxM.max\_sx$
  - iNxM.shl
  - $\ \mathrm{i} N\!\mathrm{x} M.\mathrm{shr} \_sx$
  - fNxM.add
  - fNxM.sub
  - fNxM.mul
  - fNxM.div
  - i16x8.extadd\_pairwise\_i8x16\_sx
  - i32x4.extadd\_pairwise\_i16x8\_sx

- i $N \times M$ .extmul $\_half\_iN' \times M'\_sx$
- i16x8.q15mulr\_sat\_s
- $-i32x4.dot_i16x8_s$
- i8x16.avgr\_u
- i16x8.avgr\_u
- fNxM.min
- fNxM.max
- fNxM.pmin
- fNxM.pmax
- New ternary vector instruction:
  - v128.bitselect
- New test vector instructions:
  - v128.any\_true
  - iNxM.all\_true
- New relational vector instructions:
  - -iNxM.eq
  - i $N \times M$ .ne
  - i $N \times M.lt_s x$
  - i $NxM.gt_sx$
  - $iNxM.le\_sx$
  - i $N \times M$ .ge $\_sx$
  - fNxM.eq
  - fNxM.ne
  - fNxM.lt
  - fNxM.gt
  - fNxM.le
  - fNxM.ge
- New conversion vector instructions:
  - $i32x4.trunc_sat_f32x4_sx$
  - i32x4.trunc\_sat\_f64x2\_sx\_zero
  - $f32x4.convert_i32x4_sx$
  - f32x4.demote\_f64x2\_zero
  - f64x2.convert\_low\_i32x4\_sx
  - f64x2.promote\_low\_f32x4
- New lane access vector instructions:
  - $iNxM.extract_lane_sx^?$
  - iNxM.replace\_lane
  - fNxM.extract\_lane
  - fNxM.replace\_lane

- New lane splitting/combining vector instructions:
  - iNxM.extend\_half\_iN'xM'\_sx
  - $i8x16.narrow_i16x8_sx$
  - i16x8.narrow\_i32x4\_sx
- New byte reordering vector instructions:
  - i8x16.shuffle
  - i8x16.swizzle
- New injection/projection vector instructions:
  - i $N \times M$ .splat
  - fNxM.splat
  - iNxM.bitmask

# 7.8.2 Release 3.0

# **Extended Constant Expressions**

Allowed basic numeric computations in constant expressions.<sup>63</sup>

- Extended set of constant instructions with:
  - -inn.add
  - -inn.sub
  - inn.mul
  - global.get for any previously declared immutable global

#### Note

The garbage collection extension added further constant instructions.

## **Tail Calls**

Added instructions to perform tail calls.<sup>64</sup>

- New control instructions:
  - return\_call
  - return\_call\_indirect

## **Exception Handling**

Added tag definitions, imports, and exports, and instructions to throw and catch exceptions<sup>65</sup>

- · Modules may
  - define tags
  - import tags
  - export tags
- New heap types:
  - exn

 $<sup>^{63}\</sup> https://github.com/WebAssembly/spec/tree/main/proposals/extended-const/$ 

<sup>64</sup> https://github.com/WebAssembly/spec/tree/main/proposals/tail-call/

<sup>65</sup> https://github.com/WebAssembly/spec/tree/main/proposals/exception-handling/

- noexn
- New reference type short-hands:
  - exnref
  - nullexnref
- New control instructions:
  - throw
  - throw\_ref
  - try\_table
- New tag section in binary format.

# **Multiple Memories**

Added the ability to use multiple memories per module.<sup>66</sup>

- · Modules may
  - define multiple memories
  - import multiple memories
  - export multiple memories
- Memory instructions take a memory index immediate:
  - memory.size
  - memory.grow
  - memory.fill
  - memory.copy
  - memory.init
  - -t.load
  - t.store
  - -t.loadN sx
  - t.storeN
  - v128.load/\(\frac{1}{2}\)\(\frac{1}\)\(\frac{1}\)\(\frac{1}\)\(\frac{1}\)\(\frac{1}\)\(\frac{1}\}\
  - v128.loadN\_zero
  - v128.loadN\_splat
  - v128.loadN\_lane
  - $v128.storeN_lane$
- Data segments take a memory index

# **64-bit Address Space**

Added the ability to declare an i64 address type for tables and memories. 67

- Address types denote a subset of the integral number types
- Table types include an address type
- Memory types include an address type

<sup>66</sup> https://github.com/WebAssembly/spec/tree/main/proposals/multi-memory/

<sup>67</sup> https://github.com/WebAssembly/spec/tree/main/proposals/memory64/

• Operand types of table and memory instructions now depend on the subject's declared address type: - table.get - table.set - table.size - table.grow - table.fill table.copy - table.init - memory.size - memory.grow - memory.fill - memory.copy - memory.init -t.load-t.store- t.loadN sx- t.storeN- v128.load $NxM\_sx$ - v128.loadN\_zero - v128.load $N_{\rm splat}$ - v128.loadN\_lane v128.storeN\_lane **Typeful References** Added more precise types for references.<sup>68</sup> • New generalised form of reference types: - (ref null? heaptype) • New class of heap types: - func extern - typeidx • Basic subtyping on reference and value types • New reference instructions: - ref.as\_non\_null - br\_on\_null

br\_on\_non\_nullNew control instruction:

<sup>68</sup> https://github.com/WebAssembly/spec/tree/main/proposals/function-references/

- Refined typing of reference instruction:
  - ref.func with more precise result type
- Refined typing of local instructions and instruction sequences to track the initialization status of locals with non-defaultable type
- Refined decoding of active element segments with implicit element type and plain function indices (opcode 0) to produce non-nullable reference type.
- Extended table definitions with optional initializer expression

# **Garbage Collection**

Added managed reference types.<sup>69</sup>

•	New	forms	of	heap	types:

- any
- eq
- **–** i31
- struct
- array
- none
- nofunc
- noextern
- New reference type short-hands:
  - anyref
  - eqref
  - i31ref
  - structref
  - arrayref
  - nullref
  - nullfuncref
  - nullexternref
- New forms of type definitions:
  - structure
  - array types
  - sub types
  - recursive types
- Enriched subtyping based on explicitly declared sub types and the new heap types
- New generic reference instructions:
  - ref.ea
  - ref.test
  - ref.cast
  - br\_on\_cast

 $<sup>^{69}\</sup> https://github.com/WebAssembly/spec/tree/main/proposals/gc/$ 

- br\_on\_cast\_fail
- New reference instructions for unboxed scalars:
  - ref.i31
  - i31.get\_sx
- New reference instructions for structure types:
  - struct.new
  - struct.new\_default
  - struct.get\_sx?
  - struct.set
- New reference instructions for array types:
  - array.new
  - array.new\_default
  - array.new\_fixed
  - array.new\_data
  - array.new\_elem
  - array.get\_sx?
  - array.set
  - array.len
  - array.fill
  - array.copy
  - array.init\_data
  - array.init\_elem
- New reference instructions for converting external types:
  - any.convert\_extern
  - extern.convert\_any
- Extended set of constant instructions with:
  - ref.i31
  - struct.new
  - struct.new\_default
  - array.new
  - array.new\_default
  - array.new\_fixed
  - any.convert\_extern
  - extern.convert\_any

## **Relaxed Vector Instructions**

Added new *relaxed* vector instructions, whose behaviour is non-deterministic and implementation-dependent.<sup>70</sup>

• New binary vector instruction:

<sup>70</sup> https://github.com/WebAssembly/spec/tree/main/proposals/relaxed-simd/

- fNxM.relaxed\_min
- fNxM.relaxed\_max
- i16x8.relaxed\_q15mulr\_s
- i16x8.relaxed\_dot\_i8x16\_i7x16\_s
- New ternary vector instruction:
  - fNxM.relaxed\_madd
  - fNxM.relaxed\_nmadd
  - iNxM.relaxed laneselect
  - i32x4.relaxed\_dot\_i8x16\_i7x16\_add\_s
- New conversion vector instructions:
  - i32x4.relaxed\_trunc\_f32x4\_sx
  - i32x4.relaxed\_trunc\_f64x2\_sx\_zero
- New byte reordering vector instruction:
  - i8x16.relaxed\_swizzle

### **Profiles**

Introduced the concept of profile for specifying language subsets.

• A new profile defining a deterministic mode of execution.

## **Custom Annotations**

Added generic syntax for custom annotations in the text format, mirroring the role of custom sections in the binary format.<sup>71</sup>

- Annotations of the form '(@id ...)' are allowed anywhere in the text format
- Identifiers can be escaped as '@" . . . "' with arbitrary names
- Defined name annotations '(@name "...")' for:
  - module names
  - type names
  - function names
  - local names
  - field names
- ullet Defined custom annotation '(@custom"...")' to represent arbitrary custom sections in the text format

# 7.9 Index of Types

Category	Constructor	Binary Opcode
Type index	x	(positive number as s32 or u32)
Number type	i32	0x7F (-1 as s7)
Number type	i64	0x7E (-2 as s7)
Number type	f32	0x7D (-3 as s7)
Number type	f64	0x7C (-4 as s7)
Vector type	V128	0x7B (-5 as s7)

<sup>71</sup> https://github.com/WebAssembly/spec/tree/main/proposals/annotations/

Table 1 – continued from previous page

Category	Constructor	Binary Opcode
(reserved)		0x7A 0x79
Packed type	i8	0x78 (-8 as s7)
Packed type	i16	0x77 (-9 as s7)
(reserved)		0x78 0x75
Heap type	noexn	0x74 (-14 as s7)
Heap type	nofunc	0x73 (-13 as s7)
Heap type	noextern	0x72 (-14 as s7)
Heap type	none	0x71 (-15 as s7)
Heap type	func	0x70 (-16 as s7)
Heap type	extern	0x6F (-17 as s7)
Heap type	any	0x6E (-18 as s7)
Heap type	eq	0x6D (-19 as s7)
Heap type	i31	0x6C (-20 as s7)
Heap type	struct	0x6B (-21 as s7)
Heap type	array	0x6A (-22 as s7)
Heap type	exn	0x69 (-23 as s7)
(reserved)		0x68 0x65
Reference type	ref	0x64 (-28 as s7)
Reference type	ref null	0x63 (-29 as s7)
(reserved)		0x62 0x61
Composite type	func $[valtype^*] \rightarrow [valtype^*]$	0x60 (-32 as s7)
Composite type	struct fieldtype*	0x5F (-33 as s7)
Composite type	array $fieldtype$	0x5E (-34 as s7)
(reserved)		0x5D 0x51
Sub type	sub typeidx* comptype	0x50 (-48 as s7)
Sub type	sub final typeidx* comptype	0x4F (-49 as s7)
Recursive type	rec $subtype^*$	0x4E (-50 as s7)
(reserved)		0x4D 0x41
Result type	$[\epsilon]$	0x40 (-64 as s7)
Table type	limits reftype	(none)
Memory type	limits	(none)
Global type	$mut\ valtype$	(none)
Tag type	functype	(none)

# 7.10 Index of Instructions

Instruction	Binary Opcode	Туре	Validation	Executio
unreachable	0x00	$[t_1^*]  o [t_2^*]$	validation	execution
nop	0x01	[]  ightarrow []	validation	execution
block $bt$	0x02	$[t_1^*]  o [t_2^*]$	validation	execution
$loop\ bt$	0x03	$[t_1^*]  ightarrow [t_2^*]$	validation	execution
if $bt$	0x04	$[t_1^*$ із2 $] o[t_2^*]$	validation	execution
else	0x05			
(reserved)	0x06			
(reserved)	0x07			
throw $x$	80x0	$[t_1^*~t_x^*]  ightarrow [t_2^*]$	validation	execution
(reserved)	0x09			
throw_ref	OxOA	$[t_1^*  ext{ exnref}]  o [t_2^*]$	validation	execution
end	0x0B			
br <i>l</i>	0x0C	$[t_1^*~t^*]  ightarrow [t_2^*]$	validation	execution
br_if $\mathit{l}$	OxOD	$[t^*$ i32 $] o [t^*]$	validation	execution
br_table $l^*$ $l$	0x0E	$[t_1^*~t^*$ is2 $] ightarrow [t_2^*]$	validation	execution

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
return	0x0F	$[t_1^*~t^*]  ightarrow [t_2^*]$	validation	execution
$\operatorname{call} x$	0x10	$[t_1^*]  o [t_2^*]$	validation	execution
call_indirect $x y$	0x11	$[t_1^*$ i32 $]  o [t_2^*]$	validation	execution
return_call $x$	0x12	$[t_1^*]  ightarrow [t_2^*]$	validation	execution
return_call_indirect $x y$	0x13	$[t_1^*$ i32 $] o [t_2^*]$	validation	execution
call_ref x	0x14	$[t_1^* \ (ref \ null \ x)]  o [t_2^*]$	validation	execution
return_call_ref $x$	0x15	$[t_1^* \text{ (ref null } x)]  o [t_2^*]$	validation	execution
(reserved)	0x16	,, ,, ,,		
(reserved)	0x17			
(reserved)	0x18			
(reserved)	0x19			
drop	0x1A	[t]  ightarrow []	validation	execution
select	0x1B	$[t \ t \ i32]  ightarrow [t]$	validation	execution
select t	0x1C	$\begin{bmatrix} t \ t \ i32 \end{bmatrix} \to \begin{bmatrix} t \end{bmatrix}$	validation	execution
(reserved)	0x1D	[0 0 132] / [0]	variation	Checation
(reserved)	0x1E			
try_table bt	0x1E 0x1F	$[t_1^*]  o [t_2^*]$	validation	execution
local.get x	0x20	$[l_1]  o [l_2] \ [l]  o [t]$	validation	execution
local.set x	0x21	[t]  o []	validation	execution
local.tee x	0x21	$[t]  ightarrow [t] \ [t]  ightarrow [t]$	validation	execution
global.get $x$	0x23	[l]  ightarrow [l]  ightarrow [t]	validation	execution
global.set $x$	0x24	[t]  o [t]	validation	execution
table.get x	0x25	$egin{array}{c} [t]  ightarrow [] \ [i32]  ightarrow [t] \end{array}$	validation	execution
table.set $x$	0x26		validation	execution
		$[i32\ t] \to []$	vandation	execution
(reserved)	0x27	[ical v [ical	validation	arra austi a
is load x memarg	0x28	$[i32] \rightarrow [i32]$	validation	execution
i64.load <i>x memarg</i>	0x29	$[i32] \rightarrow [i64]$	validation	execution
facilized memory	0x2A	$[i32] \rightarrow [f32]$	validation	execution
f64.load x memarg	0x2B	$[i32] \rightarrow [f64]$	validation	execution
i32.load8_s x memarg	0x2C	$[i32] \rightarrow [i32]$	validation	execution
i32.load8_u x memarg	0x2D	$[i32] \rightarrow [i32]$	validation	execution
i32.load16_s x memarg	0x2E	$[i32] \rightarrow [i32]$	validation	execution
i32.load16_u x memarg	0x2F	[i32] → [i32]	validation	execution
i64.load8_s x memarg	0x30	[i32]  ightarrow [i64]	validation	execution
i64.load8_u x memarg	0x31	$[i32] \rightarrow [i64]$	validation	execution
i64.load16_s x memarg	0x32	[i32]  ightarrow [i64]	validation	execution
i64.load $16$ _u $x\ memarg$	0x33	[i32]  ightarrow [i64]	validation	execution
i64.load32_s x memarg	0x34	$[i32] \rightarrow [i64]$	validation	execution
i64.load32_u $x\ memarg$	0x35	$[i32] \rightarrow [i64]$	validation	execution
i32.store $x \ memarg$	0x36	[i32 i32] → []	validation	execution
i64.store $x\ memarg$	0x37	[i32 i64] → []	validation	execution
f32.store $x\ memarg$	0x38	$[i32\ f32] \to []$	validation	execution
f64.store $x\ memarg$	0x39	$[i32\;f64]\to[]$	validation	execution
i32.store8 $x\ memarg$	0x3A	$[i32\;i32]\to[]$	validation	execution
i32.store16 $x\ memarg$	0x3B	[i32 i32] → []	validation	execution
i64.store8 $x\ memarg$	0x3C	$[i32\;i64] \to []$	validation	execution
i64.store16 x memarg	0x3D	$[i32\ i64] ightarrow []$	validation	execution
i64.store32 x memarg	0x3E	$[i32\;i64]\to []$	validation	executio
memory.size $x$	0x3F	[]  ightarrow [i32]	validation	executio
memory.grow $x$	0x40	$[i32] \rightarrow [i32]$	validation	executio
i32.const <i>i32</i>	0x41	$[] \rightarrow [i32]$	validation	executio
i64.const <i>i</i> 64	0x42	$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$	validation	executio
f32.const <i>f</i> 32	0x42		validation	executio
f64.const $f64$	0x43 0x44	$[] \rightarrow [f_{64}]$	validation	execution
i32.eqz	0x45	$[i32] \rightarrow [i32]$	validation	executio

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
i32.eq	0x46	$[i32\;i32]\to[i32]$	validation	execution
i32.ne	0x47	$[i32\;i32]\to[i32]$	validation	execution
i32.lt_ <b>s</b>	0x48	[i32 i32] → [i32]	validation	execution
i32.lt_u	0x49	$[i32\;i32]\to[i32]$	validation	execution
i32.gt_s	Ox4A	[i32 i32] → [i32]	validation	execution
i32.gt_u	0x4B	[i32 i32] → [i32]	validation	execution
i32.le_ <b>s</b>	0x4C	[i32 i32] → [i32]	validation	execution
i32.le_u	0x4D	[i32 i32] → [i32]	validation	execution
i32.ge_s	0x4E	[i32 i32] → [i32]	validation	execution
i32.ge_u	0x4F	[i32 i32] → [i32]	validation	execution
i64.eqz	0x50	[i64] → [i32]	validation	execution
i64.eq	0x51	$[i64 i64] \rightarrow [i32]$	validation	execution
i64.ne	0x52	$[i64\;i64]\to[i32]$	validation	execution
i64.lt_s	0x53	$[i64\;i64]\to[i32]$	validation	execution
i64.lt_u	0x54	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.gt_s	0x55	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.gt_u	0x56	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.le_s	0x57	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.le_u	0x58	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.ge_s	0x59	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.ge_u	0x5A	$\begin{bmatrix} i64 \ i64 \end{bmatrix} \to \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
f32.eq	0x5B	$[f_{32} f_{32}] \rightarrow [i_{32}]$	validation	execution
f32.ne	0x5C	$[f_{32} f_{32}] \rightarrow [i_{32}]$ $[f_{32} f_{32}] \rightarrow [i_{32}]$	validation	
f32.lt				execution
	0x5D	$[f_{32} f_{32}] \rightarrow [i_{32}]$	validation	execution
f32.gt	0x5E	$[f_{32} f_{32}] \rightarrow [i_{32}]$	validation	execution
f32.le	0x5F	$[f_{32} f_{32}] \rightarrow [i_{32}]$	validation	execution
f32.ge	0x60	$[f_{32} f_{32}] \rightarrow [i_{32}]$	validation	execution
f64.eq	0x61	$[f64f64] \to [i32]$	validation	execution
f64.ne	0x62	$[f64\;f64] \to [i32]$	validation	execution
f64.lt	0x63	$[f64\;f64]\to[i32]$	validation	execution
f64.gt	0x64	$[f64\;f64]\to[i32]$	validation	execution
f64.le	0x65	$[f64\;f64]\to[i32]$	validation	execution
f64.ge	0x66	$[f64\ f64] \to [i32]$	validation	execution
i32.clz	0x67	$[i32] \rightarrow [i32]$	validation	execution
i32.ctz	0x68	$[i32] \rightarrow [i32]$	validation	execution
i32.popcnt	0x69	$[i32] \rightarrow [i32]$	validation	execution
i32.add	0x6A	[i32 i32] → [i32]	validation	execution
i32.sub	0x6B	[i32 i32] → [i32]	validation	execution
i32.mul	0x6C	[i32 i32] → [i32]	validation	execution
i32.div_s	0x6D	[i32 i32] → [i32]	validation	execution
i32.div_u	0x6E	[i32 i32] → [i32]	validation	execution
i32.rem_s	0x6F	$[i32\;i32]\to[i32]$	validation	execution
i32.rem_u	0x70	[i32 i32] → [i32]	validation	execution
i32.and	0x71	[i32 i32] → [i32]	validation	execution
i32.or	0x72	[i32 i32] → [i32]	validation	execution
i32.xor	0x73	[i32 i32] → [i32]	validation	execution
i32.shl	0x74	[i32 i32] → [i32]	validation	execution
i32.shr_s	0x75	[i32 i32] → [i32]	validation	execution
i32.shr_u	0x76	$[i32 i32] \rightarrow [i32]$	validation	execution
i32.rotl	0x77	$[i32\;i32]\to[i32]$	validation	execution
i32.rotr	0x78	$\begin{bmatrix} i32 \ i32 \end{bmatrix} \rightarrow \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.clz	0x79	$[i64] \rightarrow [i64]$	validation	execution
i64.ctz	Ox7A	$[i64] \rightarrow [i64]$	validation	execution
1011-062	0x7B	$[i64] \rightarrow [i64]$	validation	
i64.popcnt	OV/R	$11641 \rightarrow 11641$	Vandanon	execution

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
i64.sub	0x7D	$[i64\ i64]  ightarrow [i64]$	validation	execution
i64.mul	0x7E	$[i64\ i64]  o [i64]$	validation	execution
i64.div_s	0x7F	[i64 i64] → [i64]	validation	execution
i64.div_u	0x80	$[i64\ i64]  o [i64]$	validation	execution
i64.rem_s	0x81	$[i64\;i64] o[i64]$	validation	execution
i64.rem_u	0x82	$[i64\ i64]  o [i64]$	validation	execution
i64.and	0x83	[i64 i64] → [i64]	validation	execution
i64.or	0x84	$[i64\;i64] o[i64]$	validation	execution
i64.xor	0x85	[i64 i64] → [i64]	validation	execution
i64.shl	0x86	$[i64 i64] \rightarrow [i64]$	validation	execution
i64.shr_s	0x87	[i64 i64] → [i64]	validation	execution
i64.shr_u	0x88	[i64 i64] → [i64]	validation	execution
i64.rotl	0x89	[i64 i64] → [i64]	validation	execution
i64.rotr	A8x0	[i64 i64] → [i64]	validation	execution
f32.abs	0x8B	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.neg	0x8C	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.ceil	0x8D	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.floor	0x8E	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.trunc	0x8F	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.nearest	0x90	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.sqrt	0x91	$[f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.add	0x92	$[f_{32} f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.sub	0x93	$[f_{32} f_{32}] \rightarrow [f_{32}]$ $[f_{32} f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.mul	0x94	$[f_{32} f_{32}] \rightarrow [f_{32}]$ $[f_{32} f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.div	0x95	$[f_{32} f_{32}] \rightarrow [f_{32}]$ $[f_{32} f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.min	0x96	$[f_{32} f_{32}] \rightarrow [f_{32}]$ $[f_{32} f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.max	0x90 0x97	$\begin{bmatrix} 132 & 132 \end{bmatrix} \rightarrow \begin{bmatrix} 132 \end{bmatrix}$ $\begin{bmatrix} f_{32} & f_{32} \end{bmatrix} \rightarrow \begin{bmatrix} f_{32} \end{bmatrix}$	validation	execution
	0x98	$[f_{32} f_{32}] \rightarrow [f_{32}]$ $[f_{32} f_{32}] \rightarrow [f_{32}]$	validation	execution
f32.copysign f64.abs	0x99	$[f_{64}] \rightarrow [f_{64}]$	validation	execution
	0x9A		validation	
f64.neg f64.ceil		$[f_{64}] \rightarrow [f_{64}]$	validation	execution execution
	0x9B	$[f64] \rightarrow [f64]$		
f64.floor	0x9C	$[f64] \rightarrow [f64]$	validation	execution
f64.trunc	0x9D	$[f64] \rightarrow [f64]$	validation	execution
f64.nearest	0x9E	[f64]  o [f64]	validation	execution
f64.sqrt	0x9F	$[f64] \rightarrow [f64]$	validation	execution
f64.add	OxA0	$[f64\;f64]\to[f64]$	validation	execution
f64.sub	OxA1	$[f64\;f64]\to[f64]$	validation	execution
f64.mul	0xA2	$[f64\ f64] \to [f64]$	validation	execution
f64.div	0xA3	$[f64\;f64]\to[f64]$	validation	execution
f64.min	OxA4	$[f64\;f64]\to[f64]$	validation	execution
f64.max	0xA5	$[f64\ f64] \to [f64]$	validation	execution
f64.copysign	0xA6	$[f64\;f64]\to[f64]$	validation	execution
i32.wrap_i64	OxA7	[i64]  o [i32]	validation	execution
i32.trunc_f32_s	0xA8	$[f_{32}] \rightarrow [i_{32}]$	validation	execution
i32.trunc_f32_u	0xA9	$[f_{32}] \rightarrow [i_{32}]$	validation	execution
i32.trunc_f64_s	OxAA	[f64]  o [i32]	validation	execution
i32.trunc_f64_ <b>u</b>	OxAB	[f64]  o [i32]	validation	execution
i64.extend_i32_s	OxAC	[i32] → [i64]	validation	execution
i64.extend_i32_u	OxAD	[i32]  ightarrow [i64]	validation	execution
i64.trunc_f32_s	OxAE	$[f_{32}]  o [i_{64}]$	validation	execution
i64.trunc_f32_u	OxAF	$[f_{32}] \rightarrow [i_{64}]$	validation	execution
i64.trunc_f64_s	0xB0	[f64]  o [i64]	validation	execution
i64.trunc_f64_u	0xB1	$[f64] \rightarrow [i64]$	validation	execution
f32.convert_i32_s	0xB2	$[i32] \rightarrow [f32]$	validation	execution
f32.convert_i32_u	0xB3	$[i32] \rightarrow [f32]$	validation	execution

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
f32.convert_i64_s	0xB4	[i64] → [f32]	validation	execution
f32.convert_i64_u	0xB5	$[i64] \rightarrow [f32]$	validation	execution
f32.demote_f64	0xB6	$[f_{64}] \rightarrow [f_{32}]$	validation	execution
f64.convert_i32_s	0xB7	$[i32] \rightarrow [f64]$	validation	execution
f64.convert_i32_u	0xB8	$[i32] \rightarrow [f64]$	validation	execution
f64.convert_i64_s	0xB9	$[i64] \rightarrow [f64]$	validation	execution
f64.convert_i64_u	OxBA	$[i64] \rightarrow [f64]$	validation	execution
f64.promote_f32	0xBB	$[f_{32}] \rightarrow [f_{64}]$	validation	execution
i32.reinterpret_f32	0xBC	$[f_{32}] \rightarrow [i_{32}]$	validation	execution
i64.reinterpret_f64	0xBD	$[f64] \rightarrow [i64]$	validation	execution
f32.reinterpret_i32	0xBE	$[i32] \rightarrow [f32]$	validation	execution
f64.reinterpret_i64	0xBF	$[i64] \rightarrow [f64]$	validation	execution
i32.extend8_s	0xC0	$[i32] \rightarrow [i32]$	validation	execution
i32.extend16_s	0xC1	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} i32 \end{bmatrix}$ $\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} i32 \end{bmatrix}$	validation	execution
i64.extend8_s	0xC2		validation	execution
	0xC3	$[i64] \to [i64]$	validation	execution
i64.extend16_s i64.extend32_s	0xC3 0xC4	$\begin{bmatrix} i64 \end{bmatrix} \to \begin{bmatrix} i64 \end{bmatrix}$	validation	execution
(reserved)	0xC4 0xC5	[i64]  o [i64]	vanuauon	execution
(reserved)	0xC6			
(reserved)	0xC7			
(reserved)	0xC8			
(reserved)	0xC9			
(reserved)	OxCA			
(reserved)	OxCB			
(reserved)	0xCC			
(reserved)	OxCD			
(reserved)	OxCE			
(reserved)	OxCF			
ref.null $ht$	0xD0	$[]  ightarrow [(ref \; null \; ht)]$	validation	execution
ref.is_null	0xD1	$[(ref\;null\;ht)]  o [i32]$	validation	execution
$\operatorname{ref} olimits.func olimits x$	0xD2	$[]  ightarrow [ref\ ht]$	validation	execution
ref.eq	0xD3	$[eqref\;eqref]  o [i32]$	validation	execution
ref.as_non_null	0xD4	$[(ref\;null\;ht)] \to [(ref\;ht)]$	validation	execution
br_on_null $\it l$	0xD5	$[t^* \ (ref \ null \ ht)]  o [t^* \ (ref$	[ht] validation	execution
br_on_non_null $\it l$	0xD6	$[t^* \ (ref \ null \ ht)]  o [t^*]$	validation	execution
(reserved)	0xD7			
(reserved)	0xD8			
(reserved)	0xD9			
(reserved)	OxDA			
(reserved)	OxDB			
(reserved)	0xDC			
(reserved)	OxDD			
(reserved)	0xDE			
(reserved)	OxDF			
(reserved)	0xE0			
(reserved)	0xE1			
(reserved)	0xE2			
(reserved)	0xE3			
(reserved)	0xE4			
(reserved)	0xE4 0xE5			
(reserved)	0xE6			
(reserved)	0xE7			
(reserved)	0xE8			
(reserved)	0xE9			
(reserved)	OxEA			

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
(reserved)	0xEB			
(reserved)	OxEC			
(reserved)	OxED			
(reserved)	0xEE			
(reserved)	OxEF			
(reserved)	0xF0			
(reserved)	0xF1			
(reserved)	0xF2			
(reserved)	0xF3			
(reserved)	0xF4			
(reserved)	0xF5			
(reserved)	0xF6			
(reserved)	0xF7			
(reserved)	0xF8			
(reserved)	0xF9			
(reserved)	OxFA			
struct.new $x$	0xFB 0x00	$[t^*]  o [(ref\ x)]$	validation	execution
struct.new_default $x$	0xFB 0x01	$[] \rightarrow [(ref\ x)]$	validation	execution
struct.get $x$ $y$	0xFB 0x02	$[(ref null\ x)] \to [t]$	validation	execution
struct.get_s x y	0xFB 0x03	$[(ref \ null \ x)] \to [i32]$	validation	execution
struct.get_u x y	0xFB 0x04	$[(ref null \ x)] \to [i32]$	validation	execution
struct.set $x$ $y$	0xFB 0x05	$[(ref \; null \; x)] \to []$	validation	execution
array.new $x$	0xFB 0x06	[t  i32]  ightharpoonup [(ref  x)]	validation	execution
array.new_default $x$	0xFB 0x07	$[i32] \rightarrow [(ref x)]$	validation	execution
array.new_fixed $x$ $n$	0xFB 0x08	$[t^n]  o [(\operatorname{ref}\ x)]$	validation	execution
array.new_data $x$ $y$	0xFB 0x09	$[i32 i32] \rightarrow [(ref x)]$	validation	execution
array.new_elem $x y$	OxFB OxOA	$[i32 i32] \rightarrow [(ref x)]$	validation	execution
array.get $x$	0xFB 0x0B	$[(ref \; null \; x) \; i32] \to [t]$	validation	execution
array.get_s x	0xFB 0x0C	$[(ref \; null \; x) \; i32] \rightarrow [i32]$	validation	execution
array.get_u x	0xFB 0x0D	$[(ref \; null \; x) \; i32] \rightarrow [i32]$	validation	execution
array.set $x$	0xFB 0x0E	$[(ref \; null \; x) \; is2]  \neq [is2]$ $[(ref \; null \; x) \; is2 \; t] \rightarrow []$	validation	execution
array.len	0xFB 0x0F	$[(\text{ref null array})] \rightarrow [\text{i32}]$	validation	execution
array.fill $x$	0xFB 0x0F	[(ref null  x)  is  2  t  is  2]	validation	execution
array.copy $x$ $y$	0xFB 0x10	[(ref null $x$ ) is $z$ (ref null $y$ ) is $z$ is $z$ ] $\rightarrow$ []	validation	execution
array.copy $x$ $y$ array.init_data $x$ $y$	0xFB 0x11	[(ref null $x$ ) is 2 (ref null $y$ ) is 2 is	validation	execution
array.init_elem $x y$	0xFB 0x12	$[(ref \; null \; x) \; i32 \; i32 \; i32] \to []$ $[(ref \; null \; x) \; i32 \; i32 \; i32] \to []$	validation	execution
ref.test (ref $t$ )	0xFB 0x13	$[(ref\ t')] \to [i32]$	validation	execution
ref.test (ref null t)	0xFB 0x14 0xFB 0x15	$  [(ref\ t\ )] \to [i32]                                    $	validation	execution
ref.cast (ref $t$ )	0xFB 0x15 0xFB 0x16	$ [(\operatorname{ref} t')] \to [\operatorname{ref} t) ] $	validation	execution
ref.cast (ref null $t$ )	0xFB 0x16 0xFB 0x17		validation	
br_on_cast $(rer null t)$	0xFB 0x17 0xFB 0x18	$egin{aligned} & [(ref \; null \; t')]  ightarrow [(ref \; null \; t)] \ & [t_1]  ightarrow [t_1 \setminus t_2] \end{aligned}$	validation	execution
			validation	execution
br_on_cast_fail $t_1 t_2$	0xFB 0x19	$[t_1]  ightarrow [t_2]$		executio
any.convert_extern	0xFB 0x1A	$[(\text{ref null extern})] \rightarrow [(\text{ref null extern})]$	validation	executio
extern.convert_any	0xFB 0x1B	$[(\text{ref null any})] \rightarrow [(\text{ref null extern})]$	validation	executio
ref.i31	0xFB 0x1C	$[i32] \rightarrow [(ref i31)]$	validation	executio
i31.get_s	0xFB 0x1D	$[i31ref] \rightarrow [i32]$	validation	executio
i31.get_u	0xFB 0x1E	$[i31ref] \to [i32]$	validation	executio
(reserved)	0xFB 0x1E	[0-1] . [1-1]	.1:1	
i32.trunc_sat_f32_s	0xFC 0x00	$[f32] \rightarrow [i32]$	validation	executio
i32.trunc_sat_f32_u	0xFC 0x01	$[f32] \rightarrow [i32]$	validation	executio
i32.trunc_sat_f64_s	0xFC 0x02	$[f64] \to [i32]$	validation	executio
i32.trunc_sat_f64_u	0xFC 0x03	$[f_{64}]  o [i_{32}]$	validation	executio
i64.trunc_sat_f32_s	0xFC 0x04	$[f_{32}]  o [i_{64}]$	validation	executio
i64.trunc_sat_f32_u	0xFC 0x05	$[f_{32}]  ightarrow [i_{64}]$	validation	executio
i64.trunc_sat_f64_s	0xFC 0x06	[f64]  o [i64]	validation	executio

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
i64.trunc_sat_f64_u	0xFC 0x07	$[f_{64}]  ightarrow [i_{64}]$	validation	execution
memory.init $x y$	0xFC 0x08	[i32 i32 i32] → []	validation	execution
data.drop $x$	0xFC 0x09	$] \rightarrow []$	validation	execution
memory.copy $x\ y$	OxFC OxOA	[i32 i32 i32] → []	validation	execution
memory.fill $y$	0xFC 0x0B	[i32 i32 i32] → []	validation	execution
table.init $x y$	0xFC 0x0C	[i32 i32 i32] → []	validation	execution
elem.drop $x$	OxFC OxOD		validation	execution
table.copy $x y$	0xFC 0x0E	[i32 i32 i32] → []	validation	execution
table.grow $x$	0xFC 0x0F	$[t  ext{ i32}]  ightarrow [ ext{i32}]$	validation	execution
table.size $x$	0xFC 0x10	$]$ $\rightarrow$ [i32]	validation	execution
table.fill $x$	0xFC 0x11	$[i32\ t\ i32] \to []$	validation	execution
(reserved)	0xFC 0x1E	[ ] - []		
v128.load x memarg	0xFD 0x00	[i32] → [v128]	validation	execution
v128.load8x8_s x memarg	0xFD 0x01	$[i32] \rightarrow [V128]$	validation	execution
v128.load8x8_u x memarg	0xFD 0x02	$[i32] \rightarrow [v128]$	validation	execution
v128.load16x4_s <i>x memarg</i>	0xFD 0x03	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.load16x4_u <i>x memarg</i>	0xFD 0x04	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.load32x2_s x memarg	0xFD 0x05	$[i32] \rightarrow [v128]$	validation	execution
v128.load32x2_u x memarg	0xFD 0x06	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.load8_splat x memarg	0xFD 0x07	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.load16_splat $x$ memary	0xFD 0x08	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.load32_splat <i>x memarg</i>	0xFD 0x09	$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.load64_splat x memarg	OxFD OxOA		validation	
		$\begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.store x memarg	0xFD 0x0B	$\begin{bmatrix} i32\ v128 \end{bmatrix} \to \begin{bmatrix} l \\ l \end{bmatrix}$	validation	execution
v128.const $i$ 128 i8x16.shuffle $laneidx$ $^{16}$	0xFD 0x0C	$[] \rightarrow [v_{128}]$		execution
	0xFD 0x0D	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i8x16.swizzle	0xFD 0x0E	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i8x16.splat	0xFD 0x0F	$[i32] \rightarrow [v128]$	validation	execution
i16x8.splat	0xFD 0x10	$[i32] \rightarrow [v128]$	validation	execution
i32x4.splat	0xFD 0x11	$\begin{bmatrix} i32 \end{bmatrix} \to \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
i64x2.splat	0xFD 0x12	$\begin{bmatrix} i64 \end{bmatrix} \to \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
f32x4.splat	0xFD 0x13	$[f_{32}] \rightarrow [v_{128}]$	validation	execution
f64x2.splat	0xFD 0x14	$[f64] \to [v128]$	validation	execution
i8x16.extract_lane_s laneidx	0xFD 0x15	$[v_{128}] \rightarrow [i_{32}]$	validation	execution
i8x16.extract_lane_u laneidx	0xFD 0x16	[v128] → [i32]	validation	execution
i8x16.replace_lane laneidx	0xFD 0x17	[V128 i32] → [V128]	validation	execution
i16x8.extract_lane_s laneidx	0xFD 0x18	$[v_{128}] \rightarrow [i_{32}]$	validation	execution
i16x8.extract_lane_u laneidx	0xFD 0x19	[V128] → [i32]	validation	execution
i16x8.replace_lane $laneidx$	0xFD 0x1A	$[v_{128} i_{32}] \rightarrow [v_{128}]$	validation	execution
i32x4.extract_lane $laneidx$	0xFD 0x1B	[v128] → [i32]	validation	execution
i32x4.replace_lane $laneidx$	0xFD 0x1C	[V128 i32] → [V128]	validation	execution
i64x2.extract_lane $laneidx$	0xFD 0x1D	[V128] → [i64]	validation	execution
i64x2.replace_lane $laneidx$	0xFD 0x1E	[V128 i64] → [V128]	validation	execution
f32x4.extract_lane $laneidx$	0xFD 0x1F	$[v_{128}]  o [f_{32}]$	validation	execution
f32x4.replace_lane laneidx	0xFD 0x20	[v128 f32] → [v128]	validation	execution
f64x2.extract_lane $laneidx$	0xFD 0x21	$[v_{128}]  ightarrow [f_{64}]$	validation	execution
f64x2.replace_lane laneidx	0xFD 0x22	[v128 f64] → [v128]	validation	execution
i8x16.eq	0xFD 0x23	$[v_{128}v_{128}] \to [v_{128}]$	validation	execution
i8x16.ne	0xFD 0x24	$\left[v_{128}v_{128}\right] \to \left[v_{128}\right]$	validation	execution
i8x16.lt_ <b>s</b>	0xFD 0x25	$[v_{128}v_{128}]  o [v_{128}]$	validation	execution
i8x16.lt_u	0xFD 0x26	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
i8x16.gt_s	0xFD 0x27	[V128 V128] → [V128]	validation	execution
i8x16.gt_u	0xFD 0x28	[V128 V128] → [V128]	validation	execution
i8x16.le_s	0xFD 0x29	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution

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Instruction	Binary Opcode	Туре	Validation	Executio
i8x16.ge_ <b>s</b>	0xFD 0x2B	$[v128\;v128] \to [v128]$	validation	execution
i8x16.ge_u	0xFD 0x2C	$\left[V128\;V128\right]\rightarrow\left[V128\right]$	validation	execution
i16x8.eq	0xFD 0x2D	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.ne	0xFD 0x2E	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.lt_s	0xFD 0x2F	$[ extsf{V}128  extsf{V}128]  ightarrow [ extsf{V}128]$	validation	execution
i16x8.lt_u	0xFD 0x30	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.gt_s	0xFD 0x31	$[v_{128} \ v_{128}]  ightarrow [v_{128}]$	validation	execution
i16x8.gt_u	0xFD 0x32	$[v_{128} \ v_{128}]  ightarrow [v_{128}]$	validation	execution
i16x8.le_s	0xFD 0x33	$[v_{128} v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.le_u	0xFD 0x34	$[v_{128} v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.ge_s	0xFD 0x35	$[v_{128} v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.ge_u	0xFD 0x36	$[v_{128} v_{128}] \rightarrow [v_{128}]$	validation	execution
i32x4.eq	0xFD 0x37	[V128 V128] → [V128]	validation	execution
i32x4.ne	0xFD 0x38	[V128 V128] → [V128]	validation	execution
i32x4.lt_ <b>s</b>	0xFD 0x39	[V128 V128] → [V128]	validation	execution
i32x4.lt_u	OxFD Ox3A	[V128 V128] → [V128]	validation	execution
i32x4.gt_s	0xFD 0x3B	[V128 V128] → [V128]	validation	execution
i32X4.gt_u	0xFD 0x3C	$\begin{bmatrix} v_{128} \ v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i32x4.le_ <b>s</b>	0xFD 0x3D	[V128 V128] → [V128]	validation	execution
i32x4.le_u	0xFD 0x3E	$\begin{bmatrix} V_{128} & V_{128} \end{bmatrix} \rightarrow \begin{bmatrix} V_{128} \end{bmatrix}$	validation	execution
i32X4.ge_ <b>S</b>	0xFD 0x3F	$\begin{bmatrix} V_{128} & V_{128} \end{bmatrix} \rightarrow \begin{bmatrix} V_{128} \end{bmatrix}$	validation	execution
i32x4.ge_u	0xFD 0x40	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f32x4.eq	0xFD 0x41	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
f32x4.ne	0xFD 0x42	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f32x4.lt	0xFD 0x43	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
f32x4.gt	0xFD 0x44	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
f32x4.le	0xFD 0x45	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
f32x4.ge	0xFD 0x46	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.eq	0xFD 0x47	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.ne	0xFD 0x48	$[V128 \ V128] \rightarrow [V128]$	validation	execution
f64x2.lt	0xFD 0x49	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.gt	OxFD Ox4A	$\begin{bmatrix} v_{128} \ v_{128} \end{bmatrix} \to \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.le	0xFD 0x4B	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.ge	0xFD 0x4C	$[V128 \ V128] \rightarrow [V128]$	validation	execution
V128.not	OxFD Ox4D	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
v128.and	0xFD 0x4E	$\begin{bmatrix} v128 & v & v128 \end{bmatrix} \to \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
v128.andnot	0xFD 0x4F	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
V128.or	0xFD 0x50	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
V128.XOT	0xFD 0x51	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
v128.bitselect	0xFD 0x51	$[V128 \ V128] \rightarrow [V128]$	validation	execution
v128.any_true	0xFD 0x53	$\begin{bmatrix} v_{128} & v_{126} & v_{126} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
v128.load8_lane memarg laneidx	0xFD 0x54	$\begin{bmatrix} 132 & 128 \end{bmatrix} \rightarrow \begin{bmatrix} 132 \end{bmatrix}$	validation	execution
v128.load16_lane memarg laneidx	0xFD 0x55	$\begin{bmatrix} i32 \ V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
v128.load32_lane memarg laneidx	0xFD 0x56	$\begin{bmatrix} i32 \ V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
v128.load64_lane memarg laneidx	0xFD 0x50 0xFD 0x57	$\begin{bmatrix} i32 \ V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
v128.store8_lane memarg laneidx	0xFD 0x57	$\begin{bmatrix} i32V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
v128.store16_lane memarg laneidx	0xFD 0x50	$\begin{bmatrix} 132 & V120 \end{bmatrix} \rightarrow \begin{bmatrix} \\ \end{bmatrix}$	validation	execution
v128.store32_lane memarg laneidx	0xFD 0x5A	$ \begin{bmatrix} i32 \ V128 \end{bmatrix} \rightarrow \begin{bmatrix} \\ \end{aligned} $	validation	execution
v128.store64_lane memarg laneidx	0xFD 0x5A 0xFD 0x5B	$\begin{bmatrix} 132 \text{ V}128 \end{bmatrix} \rightarrow \begin{bmatrix} \\ \end{bmatrix}$ $\begin{bmatrix} 132 \text{ V}128 \end{bmatrix} \rightarrow \begin{bmatrix} \\ \end{bmatrix}$	validation	execution
v128.load32_zero memarg	0xFD 0x5C	$ \begin{bmatrix} i32 & \sqrt{128} & \rightarrow \\ i32 & \rightarrow & \sqrt{128} \end{bmatrix} $	validation	execution
v128.load64_zero memarg	0xFD 0x5C 0xFD 0x5D	$ \begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix} $ $ \begin{bmatrix} i32 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix} $	validation	execution
f32x4.demote_f64x2_zero	0xFD 0x5E	$ \begin{bmatrix} 132 \\  \hline  \hline $	validation	execution
f64x2.promote_low_f32x4	0xFD 0x5E 0xFD 0x5F	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i8x16.abs	0xFD 0x60	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
	0xFD 0x60 0xFD 0x61		validation	execution
i8x16.neg	OYLD OXOI	$[v_{128}]  ightarrow [v_{128}]$	vanuation	execution

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Instruction	Binary Opcode	Туре	Validation	Execution
i8x16.popcnt	0xFD 0x62	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i8x16.all_true	0xFD 0x63	$[v_{128}]  o [i_{32}]$	validation	execution
i8x16.bitmask	0xFD 0x64	$[v_{128}]  ightarrow [i_{32}]$	validation	execution
i8x16.narrow_i16x8_s	0xFD 0x65	$[V128\;V128]\to[V128]$	validation	execution
i8x16.narrow_i16x8_u	0xFD 0x66	$[v_{128}v_{128}] \to [v_{128}]$	validation	execution
f <sub>32</sub> x <sub>4</sub> .ceil	0xFD 0x67	$[v_{128}]  o [v_{128}]$	validation	execution
f32x4.floor	0xFD 0x68	$[v_{128}]  o [v_{128}]$	validation	execution
f32x4.trunc	0xFD 0x69	$[v_{128}]  o [v_{128}]$	validation	execution
f32x4.nearest	0xFD 0x6A	$[v_{128}]  ightarrow [v_{128}]$	validation	execution
i8x16.shl	0xFD 0x6B	[v128 i32] → [v128]	validation	execution
i8x16.shr_s	0xFD 0x6C	[v128 i32] → [v128]	validation	execution
i8x16.shr_u	0xFD 0x6D	[v128 i32] → [v128]	validation	execution
i8x16.add	0xFD 0x6E	[V128 V128] → [V128]	validation	execution
i8x16.add_sat_s	0xFD 0x6F	[V128 V128] → [V128]	validation	execution
i8x16.add_sat_u	0xFD 0x70	[V128 V128] → [V128]	validation	execution
i8x16.sub	0xFD 0x71	[V128 V128] → [V128]	validation	execution
i8x16.sub_sat_s	0xFD 0x72	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i8x16.sub_sat_u	0xFD 0x73	$\begin{bmatrix} V128\ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
f <sub>64x2</sub> .ceil	0xFD 0x74	$\begin{bmatrix} v_{128} \end{bmatrix} \to \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.floor	0xFD 0x75	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i8x16.min_s	0xFD 0x76	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i8x16.min_u	OxFD Ox77	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i8x16.max_s	0xFD 0x78	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i8x16.max_u	0xFD 0x79	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
f64x2.trunc	0xFD 0x7A	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i8x16.avgr_u	0xFD 0x7R 0xFD 0x7B	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i16x8.extadd_pairwise_i8x16_s	0xFD 0x7B	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i16x8.extadd_pairwise_i8x16_u	0xFD 0x7C 0xFD 0x7D	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i32x4.extadd_pairwise_i16x8_s	0xFD 0x7D 0xFD 0x7E	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
•	0xFD 0x7E 0xFD 0x7F		validation	execution
i32x4.extadd_pairwise_i16x8_u	0xFD 0x7F 0xFD 0x80 0x01	$[V128] \rightarrow [V128]$	validation	execution
i16x8.abs	0xFD 0x80 0x01 0xFD 0x81 0x01	$[V128] \rightarrow [V128]$	validation	
i16x8.neg	0xFD 0x81 0x01 0xFD 0x82 0x01	$[V128] \rightarrow [V128]$		execution
i16x8.q15mulr_sat_s		$\begin{bmatrix} V128 \ V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i16x8.all_true	0xFD 0x83 0x01	$\begin{bmatrix} v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} i_{32} \end{bmatrix}$	validation	execution
i16x8.bitmask	0xFD 0x84 0x01	$[v_{128}] \rightarrow [i_{32}]$	validation	execution
i16x8.narrow_i32x4_s	0xFD 0x85 0x01	[V128 V128] → [V128]	validation	execution
i16x8.narrow_i32x4_u	0xFD 0x86 0x01	$\begin{bmatrix} v_{128}v_{128} \end{bmatrix} \to \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i16x8.extend_low_i8x16_s	0xFD 0x87 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.extend_high_i8x16_s	0xFD 0x88 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.extend_low_i8x16_u	0xFD 0x89 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.extend_high_i8x16_u	0xFD 0x8A 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i16x8.shl	0xFD 0x8B 0x01	[v128 i32] → [v128]	validation	execution
i16x8.shr_s	0xFD 0x8C 0x01	[v128 i32] → [v128]	validation	execution
i16x8.shr_u	0xFD 0x8D 0x01	[v128 i32] → [v128]	validation	execution
i16x8.add	0xFD 0x8E 0x01	$\begin{bmatrix} V128\ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i16x8.add_sat_s	0xFD 0x8F 0x01	$[V128\;V128]\to[V128]$	validation	execution
i16x8.add_sat_u	0xFD 0x90 0x01	$[V128\;V128]\to[V128]$	validation	execution
i16x8.sub	0xFD 0x91 0x01	$[V128\ V128] \to [V128]$	validation	execution
i16x8.sub_sat_s	0xFD 0x92 0x01	$[v_{128}v_{128}] \to [v_{128}]$	validation	execution
i16x8.sub_sat_u	0xFD 0x93 0x01	[v128 v128] → [v128]	validation	executio
f64x2.nearest	0xFD 0x94 0x01	[v128] → [v128]	validation	executio
i16x8.mul	0xFD 0x95 0x01	[V128 V128] → [V128]	validation	executio
i16x8.min_s	0xFD 0x96 0x01	$[V128 V128] \rightarrow [V128]$	validation	executio
i16x8.min_u	0xFD 0x97 0x01	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	executio
i16x8.max_s	0xFD 0x98 0x01	$\begin{bmatrix} V128\ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	executio

continues on

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Executio
i16x8.max_u	0xFD 0x99 0x01	[V128 V128] → [V128]	validation	execution
(reserved)	0xFD 0x9A 0x01	, , ,		
i16x8.avgr_u	0xFD 0x9B 0x01	[V128 V128] → [V128]	validation	execution
i16x8.extmul_low_i8x16_s	0xFD 0x9C 0x01	$[V128 V128] \rightarrow [V128]$	validation	execution
i16x8.extmul_high_i8x16_s	0xFD 0x9D 0x01	$[V128\ V128] \rightarrow [V128]$	validation	execution
i16x8.extmul_low_i8x16_u	0xFD 0x9E 0x01	$[V128 V128] \rightarrow [V128]$	validation	execution
i16x8.extmul_high_i8x16_u	0xFD 0x9F 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
i32x4.abs	0xFD 0xA0 0x01	[V128] → [V128]	validation	execution
i32x4.neg	0xFD 0xA1 0x01	[V128] → [V128]	validation	execution
(reserved)	0xFD 0xA2 0x01	[1-1-1]		
i32x4.all_true	0xFD 0xA3 0x01	[v128] → [i32]	validation	execution
i32x4.bitmask	0xFD 0xA4 0x01	$\begin{bmatrix} v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} i_{32} \end{bmatrix}$	validation	execution
(reserved)	0xFD 0xA5 0x01	[*125] / [152]	validation	CACCACION
(reserved)	0xFD 0xA6 0x01			
i32x4.extend_low_i16x8_s	OxFD OxA7 OxO1	[V128] → [V128]	validation	execution
i32x4.extend_high_i16x8_s	0xFD 0xA8 0x01	$\begin{bmatrix} v128 \end{bmatrix} \to \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
i32x4.extend_low_i16x8_u	0xFD 0xA9 0x01	$\begin{bmatrix} v_{128} \end{bmatrix} \to \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i32x4.extend_high_i16x8_u	OxFD OxAA OxO1	$\begin{bmatrix} v128 \end{bmatrix} \to \begin{bmatrix} v128 \end{bmatrix}$	validation	execution
i32x4.shl	OxFD OxAB OxO1	$\begin{bmatrix} v_{128} & i_{32} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i32x4.shr_s	OxFD OxAC OxO1	$[v_{128} \ i_{32}] \rightarrow [v_{128}]$	validation	execution
i32x4.shr_u	OxFD OxAD OxO1	$[v_{128} \ i_{32}] \rightarrow [v_{128}]$	validation	execution
i32x4.add	0xFD 0xAE 0x01	$\begin{bmatrix} v_{128} \ v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
(reserved)	0xFD 0xAF 0x01	[V120 V120] / [V120]	vandation	CACCULION
(reserved)	0xFD 0xB0 0x01			
i32×4.sub	0xFD 0xB0 0x01	[V128 V128] → [V128]	validation	execution
(reserved)	0xFD 0xB1 0x01	[V126 V126] -7 [V126]	vanuation	CACCULION
(reserved)	0xFD 0xB3 0x01			
(reserved)	0xFD 0xB4 0x01			
i32x4.mul	0xFD 0xB5 0x01	[V128 V128] → [V128]	validation	execution
i32x4.min_s	0xFD 0xB6 0x01	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i32x4.min_u	0xFD 0xB0 0x01	$[V128 \ V128] \rightarrow [V128]$	validation	execution
i32x4.max_s	0xFD 0xB8 0x01	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i32x4.max_u	0xFD 0xB9 0x01	$[V128 \ V128] \rightarrow [V128]$	validation	execution
i32x4.dot_i16x8_s	0xFD 0xBA 0x01	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i32x4.extmul_low_i16x8_s	0xFD 0xBC 0x01	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i32x4.extmul_high_i16x8_s	0xFD 0xBD 0x01	$\begin{bmatrix} V128 \ V128 \end{bmatrix} \to \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i32x4.extmul_low_i16x8_u	0xFD 0xBE 0x01	$[V128 \ V128] \rightarrow [V128]$	validation	execution
i32x4.extmul_high_i16x8_u	0xFD 0xBF 0x01	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$ $\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i64x2.abs	0xFD 0xC0 0x01	$\begin{bmatrix} V128 & V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i64x2.neg	0xFD 0xC0 0x01	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$ $\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
(reserved)	0xFD 0xC1 0x01 0xFD 0xC2 0x01	[V120] -7 [V128]	vailuatioil	CACCULION
i64x2.all_true	0xFD 0xC2 0x01 0xFD 0xC3 0x01	[v128] → [i32]	validation	execution
i64x2.bitmask	0xFD 0xC3 0x01		validation	
	0xFD 0xC4 0x01 0xFD 0xC5 0x01	[V128] → [i32]	vanuation	execution
(reserved)	0xFD 0xC5 0x01 0xFD 0xC6 0x01			
(reserved)		[V128] → [V128]	validation	avacution
i64x2.extend_low_i32x4_s	0xFD 0xC7 0x01			execution
i64x2.extend_high_i32x4_s	0xFD 0xC8 0x01	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i64x2.extend_low_i32x4_u	0xFD 0xC9 0x01	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i64x2.extend_high_i32x4_u	0xFD 0xCA 0x01	$\begin{bmatrix} V128 \end{bmatrix} \rightarrow \begin{bmatrix} V128 \end{bmatrix}$	validation	execution
i64x2.shl	0xFD 0xCB 0x01	$[V128 i32] \rightarrow [V128]$	validation	execution
i64x2.shr_s	0xFD 0xCC 0x01	$[v128 i32] \rightarrow [v128]$	validation	execution
i64x2.shr_u	0xFD 0xCD 0x01	$[v_{128} i_{32}] \rightarrow [v_{128}]$	validation	execution
i64x2.add	0xFD 0xCE 0x01	[V128 V128] → [V128]	validation	execution
(reserved)	0xFD 0xCF 0x01			
(reserved)	0xFD 0xD0 0x01			

continues on

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Execution
i64x2.sub	0xFD 0xD1 0x01	$[V128\;V128]\to[V128]$	validation	execution
(reserved)	0xFD 0xD2 0x01			
(reserved)	0xFD 0xD3 0x01			
(reserved)	0xFD 0xD4 0x01			
i64x2.mul	0xFD 0xD5 0x01	$[V128\;V128]\to[V128]$	validation	execution
i64x2.eq	0xFD 0xD6 0x01	$[V128\;V128]\to[V128]$	validation	execution
i64x2.ne	0xFD 0xD7 0x01	$[V128\;V128]\to[V128]$	validation	execution
i64x2.lt_s	0xFD 0xD8 0x01	$[\texttt{V128 V128}] \rightarrow [\texttt{V128}]$	validation	execution
i64X2.gt_ <b>s</b>	0xFD 0xD9 0x01	$\left[ V128\;V128\right] \to \left[ V128\right]$	validation	execution
i64x2.le_ <b>s</b>	OxFD OxDA OxO1	$\left[ V128\;V128\right] \rightarrow \left[ V128\right]$	validation	execution
i64x2.ge_s	0xFD 0xDB 0x01	$[ extsf{V}128 \  extsf{V}128]  ightarrow [ extsf{V}128]$	validation	execution
i64x2.extmul_low_i32x4_s	0xFD 0xDC 0x01	$[V128\;V128]\to[V128]$	validation	execution
i64x2.extmul_high_i32x4_s	0xFD 0xDD 0x01	$[v_{128} \ v_{128}]  ightarrow [v_{128}]$	validation	execution
i64x2.extmul_low_i32x4_u	0xFD 0xDE 0x01	$[v_{128} \ v_{128}]  ightarrow [v_{128}]$	validation	execution
i64x2.extmul_high_i32x4_u	0xFD 0xDF 0x01	$[v_{128} \ v_{128}]  ightarrow [v_{128}]$	validation	execution
f32x4.abs	0xFD 0xE0 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
f32x4.neg	0xFD 0xE1 0x01	$[v_{128}]  ightarrow [v_{128}]$	validation	execution
(reserved)	0xFD 0xE2 0x01			
f32x4.sqrt	0xFD 0xE3 0x01	$[v_{128}]  ightarrow [v_{128}]$	validation	execution
f32x4.add	0xFD 0xE4 0x01	[V128 V128] → [V128]	validation	execution
f32x4.sub	0xFD 0xE5 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f32x4.mul	0xFD 0xE6 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f32x4.div	0xFD 0xE7 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f32x4.min	0xFD 0xE8 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f32x4.max	0xFD 0xE9 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f32x4.pmin	OxFD OxEA OxO1	[V128 V128] → [V128]	validation	execution
f32x4.pmax	0xFD 0xEB 0x01	$\begin{bmatrix} v_{128} \ v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f <sub>64</sub> x2.abs	0xFD 0xEC 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
f64x2.neg	0xFD 0xED 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
f64x2.sqrt	0xFD 0xEF 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
f <sub>64</sub> x2.add	0xFD 0xF0 0x01	$\begin{bmatrix} v_{128} \ v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f64x2.sub	0xFD 0xF1 0x01	[V128 V128] → [V128]	validation	execution
f64x2.mul	0xFD 0xF2 0x01	[V128 V128] → [V128]	validation	execution
f64x2.div	0xFD 0xF3 0x01	[V128 V128] → [V128]	validation	execution
f64x2.min	0xFD 0xF4 0x01	[V128 V128] → [V128]	validation	execution
f64x2.max	0xFD 0xF5 0x01	[V128 V128] → [V128]	validation	execution
f64x2.pmin	0xFD 0xF6 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f64x2.pmax	0xFD 0xF7 0x01	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
i32x4.trunc_sat_f32x4_s	0xFD 0xF8 0x01	[V128] → [V128]	validation	execution
i32x4.trunc_sat_f32x4_u	0xFD 0xF9 0x01	[V128] → [V128]	validation	execution
f <sub>32×4</sub> .convert_i32×4_s	OxFD OxFA OxO1	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
f <sub>32</sub> x <sub>4</sub> .convert_i32x <sub>4</sub> _u	0xFD 0xFB 0x01	[V128] → [V128]	validation	execution
i32x4.trunc_sat_f64x2_s_zero	0xFD 0xFC 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i32x4.trunc_sat_f64x2_u_zero	0xFD 0xFD 0x01	[V128] → [V128]	validation	execution
f64x2.convert_low_i32x4_s	0xFD 0xFE 0x01	$[V128] \rightarrow [V128]$	validation	execution
f64x2.convert_low_i32x4_u	0xFD 0xFF 0x01	$[v_{128}] \rightarrow [v_{128}]$	validation	execution
i8x16.relaxed_swizzle	0xFD 0x80 0x02	$\begin{bmatrix} v_{128} & v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
i32x4.relaxed_trunc_f32x4_s	0xFD 0x81 0x02	[v128] → [v128]	validation	execution
i32x4.relaxed_trunc_f32x4_u	0xFD 0x82 0x02	$[V128] \rightarrow [V128]$	validation	execution
i32x4.relaxed_trunc_f64x2_s	0xFD 0x83 0x02	$[V128] \rightarrow [V128]$	validation	execution
i32x4.relaxed_trunc_f64x2_u	0xFD 0x84 0x02	$\begin{bmatrix} v_{128} \end{bmatrix} \rightarrow \begin{bmatrix} v_{128} \end{bmatrix}$	validation	execution
f32x4.relaxed_madd	0xFD 0x85 0x02	[V128]   V128]   V128]   V128]	validation	execution
f32x4.relaxed_madd	0xFD 0x86 0x02	$[V128 \ V128 \ V128] \rightarrow [V128]$	validation	execution
f64x2.relaxed_madd	0xFD 0x80 0x02 0xFD 0x87 0x02		validation	execution
f64x2.relaxed_nmadd	0xFD 0x87 0x02 0xFD 0x88 0x02	$[V128 \ V128 \ V128] \rightarrow [V128]$ $[V128 \ V128 \ V128] \rightarrow [V128]$	validation	execution

continues on

Table 2 – continued from previous page

Instruction	Binary Opcode	Туре	Validation	Executio
i8x16.relaxed_laneselect	0xFD 0x89 0x02	[V128 V128 V128] → [V128]	validation	execution
i16x8.relaxed_laneselect	0xFD 0x8A 0x02	$[v_{128} \ v_{128} \ v_{128}]  o [v_{128}]$	validation	execution
i32x4.relaxed_laneselect	0xFD 0x8B 0x02	$[v_{128} \ v_{128} \ v_{128}]  o [v_{128}]$	validation	execution
i64x2.relaxed_laneselect	0xFD 0x8C 0x02	$[v_{128}\ v_{128}\ v_{128}]  o [v_{128}]$	validation	execution
f32x4.relaxed_min	0xFD 0x8D 0x02	$[v128\;v128] \to [v128]$	validation	execution
f32x4.relaxed_max	0xFD 0x8E 0x02	$[v_{128} \ v_{128}] \rightarrow [v_{128}]$	validation	execution
f64x2.relaxed_min	0xFD 0x8F 0x02	$\left[ V128\;V128\right] \rightarrow \left[ V128\right]$	validation	execution
f64x2.relaxed_max	0xFD 0x90 0x02	$\left[ V128\;V128\right] \rightarrow \left[ V128\right]$	validation	execution
i16x8.relaxed_q15mulr_s	0xFD 0x91 0x02	$\left[ V128\;V128\right] \rightarrow \left[ V128\right]$	validation	execution
i16x8.relaxed_dot_i8x16_i7x16_s	0xFD 0x92 0x02	$\left[ V128\;V128\right] \rightarrow \left[ V128\right]$	validation	execution
i32x4.relaxed_dot_i8x16_i7x16_add_s	0xFD 0x93 0x02	$[v_{128} \ v_{128} \ v_{128}]  o [v_{128}]$	validation	execution
(reserved)	0xFD 0x94 0x02			
(reserved)	OxFE			
(reserved)	0xFF			

#### Note

Multi-byte opcodes are given with the shortest possible encoding in the table. However, what is following the first byte is actually a u32 with variable-length encoding and consequently has multiple possible representations.

## 7.11 Index of Semantic Rules

## 7.11.1 Well-formedness of Types

Construct	Judgement
Numeric type	$C \vdash numtype : ok$
Vector type	$C \vdash vectype : ok$
Heap type	$C \vdash heaptype : ok$
Reference type	$C \vdash reftype : ok$
Value type	$C \vdash valtype : ok$
Packed type	$C \vdash packtype$ : ok
Storage type	$C \vdash storagetype : ok$
Field type	$C \vdash fieldtype : ok$
Result type	$C \vdash result type : ok$
Instruction type	$C \vdash instrtype : ok$
Function type	$C \vdash functype : ok$
Structure type	$C \vdash structtype : ok$
Array type	$C \vdash array type : ok$
Composite type	$C \vdash comptype : ok$
Sub type	$C \vdash subtype : ok$
Recursive type	$C \vdash rectype : ok$
Defined type	$C \vdash \mathit{deftype} : ok$
Block type	$C \vdash blocktype : instrtype$
Table type	$C \vdash table type : ok$
Memory type	$C \vdash memtype : ok$
Global type	$C \vdash globaltype : ok$
Tag type	$C \vdash tagtype$ : ok
External type	$C \vdash externtype : ok$
Type definitions	$C \vdash type^* : ok$

## **7.11.2 Typing of Static Constructs**

Construct	Judgement
Instruction	$S; C \vdash instr: instrtype$
Instruction sequence	$S; C \vdash instr^* : instrtype$
Catch clause	$C \vdash catch : ok$
Expression	$C \vdash expr : result type$
Function	$C \vdash func: functype$
Local	$C \vdash local : local type$
Table	$C \vdash table: table type$
Memory	$C \vdash mem : memtype$
Limits	$C \vdash limits: k$
Global	$C \vdash global: globaltype$
Tag	$C \vdash tag: tagtype$
Element segment	$C \vdash elem : reftype$
Element mode	$C \vdash elemmode : reftype$
Data segment	$C \vdash data : ok$
Data mode	$C \vdash datamode : ok$
Start function	$C \vdash start : ok$
Export	$C \vdash export : externtype$
Export description	$C \vdash export desc : externtype$
Import	$C \vdash import : externtype$
Import description	$C \vdash importdesc : externtype$
Module	$\vdash module : externtype^* \rightarrow externtype^*$

# **7.11.3 Typing of Runtime Constructs**

Construct	Judgement
Value	$S \vdash val : valtype$
Result	$S \vdash result : result type$
Packed value	$S \vdash packval : packtype$
Field value	$S \vdash fieldval : storage type$
External address	$S \vdash externaddr : externtype$
Function instance	$S \vdash funcinst : functype$
Table instance	$S \vdash tableinst: table type$
Memory instance	$S \vdash meminst : memtype$
Global instance	$S \vdash globalinst: globaltype$
Tag instance	$S \vdash taginst: tagtype$
Element instance	$S \vdash eleminst: t$
Data instance	$S \vdash \mathit{datainst} : ok$
Structure instance	$S \vdash structinst: ok$
Array instance	$S \vdash arrayinst: ok$
Export instance	$S \vdash exportinst$ : ok
Module instance	$S \vdash module inst: C$
Store	⊢ store : ok
Configuration	$\vdash config : [t^*]$
Thread	$S; result type^? \vdash thread : result type$
Frame	$S \vdash frame : C$

### 7.11.4 Constantness

Construct	Judgement
Constant expression	$C \vdash expr$ const
Constant instruction	$C \vdash instr const$

## 7.11.5 Matching

Construct	Judgement
Number type	$C \vdash numtype_1 \leq numtype_2$
Vector type	$C \vdash vectype_1 \leq vectype_2$
Heap type	$C \vdash heaptype_1 \leq heaptype_2$
Reference type	$C \vdash reftype_1 \leq reftype_2$
Value type	$C \vdash valtype_1 \leq valtype_2$
Packed type	$C \vdash packtype_1 \leq packtype_2$
Storage type	$C \vdash storagetype_1 \leq storagetype_2$
Field type	$C \vdash fieldtype_1 \leq fieldtype_2$
Result type	$C \vdash result type_1 \leq result type_2$
Instruction type	$C \vdash instrtype_1 \leq instrtype_2$
Function type	$C \vdash functype_1 \leq functype_2$
Structure type	$C \vdash structtype_1 \leq structtype_2$
Array type	$C \vdash array type_1 \leq array type_2$
Composite type	$C \vdash comptype_1 \leq comptype_2$
Defined type	$C \vdash deftype_1 \leq deftype_2$
Table type	$C \vdash tabletype_1 \leq tabletype_2$
Memory type	$C \vdash memtype_1 \leq memtype_2$
Global type	$C \vdash globaltype_1 \leq globaltype_2$
Tag type	$C \vdash tagtype_1 \leq tagtype_2$
External type	$C \vdash externtype_1 \leq externtype_2$
Limits	$C \vdash limits_1 \leq limits_2$

### 7.11.6 Store Extension

Construct	Judgement
Function instance	$\vdash funcinst_1 \leq funcinst_2$
Table instance	$\vdash tableinst_1 \leq tableinst_2$
Memory instance	$\vdash meminst_1 \leq meminst_2$
Global instance	$\vdash globalinst_1 \leq globalinst_2$
Tag instance	$\vdash taginst_1 \leq taginst_2$
Element instance	$\vdash eleminst_1 \leq eleminst_2$
Data instance	$\vdash datainst_1 \leq datainst_2$
Structure instance	$\vdash structinst_1 \leq structinst_2$
Array instance	$\vdash arrayinst_1 \preceq arrayinst_2$
Store	$\vdash store_1 \leq store_2$

## 7.11.7 Execution

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Expression	$S; F; expr \hookrightarrow S'; F'; expr'$

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