

# Subtraction with Complements (1's and 2's)



## Lecture-4

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# Subtraction with Complements

- The **direct method** of subtraction taught in elementary schools uses the borrow concept.
- In this method, we borrow a 1 from a higher significant position when the minuend digit is smaller than the subtrahend digit.
- The method works well when people perform subtraction with paper and pencil.
- However, when subtraction is implemented with digital hardware, the method is **less efficient** than the method that uses complements.

# Subtraction of two *n*-digit unsigned numbers $M - N$ in base $r$

- The subtraction of two *n*-digit unsigned numbers  $M - N$  in base  $r$  can be done as follows:
  1. Add the minuend  $M$  to the  $r$ 's complement of the subtrahend  $N$ . Mathematically,  
$$M + (r^n - N) = M - N + r^n.$$
  2. If  $M \geq N$ , the sum will produce an end carry  $r^n$ , which can be discarded; what is left is the result  $M - N$ .

## ***Subtraction of two $n$ -digit unsigned numbers $M - N$ in base $r$***

3. If  $M < N$ , the sum does not produce an end carry and is equal to  $r^n - (N - M)$ , which is the  $r$ 's complement of  $(N - M)$ .

To obtain the answer in a familiar form, **take the  $r$ 's complement of the sum and place a negative sign in front.**

# Subtraction of two *n*-digit unsigned numbers $M - N$ in base $r$

- Both numbers must have the same number of digits

1. Calculate the  $r$ 's complement of the subtrahend  $N$ .  
Add the minuend  $M$  to the  $r$ 's complement of the subtrahend  $N$ .

Inspect the result obtained in step (1) for an end carry:

- (a) If an end carry occurs, discard it.
- (b) If an end carry does not occur, take the  $r$ 's complement of the number obtained in step (1) and place a negative sign in front.

# Subtraction Using 10's complement

Using 10's complement, subtract  $72532 - 3250$ .

$$\begin{array}{r} M = 72532 \\ 10\text{'s complement of } N = + \underline{96750} \\ \text{Sum} = 169282 \\ \text{Discard end carry } 10^5 = - \underline{100000} \\ \text{Answer} = 69282 \end{array}$$

# Subtraction Using 10's complement

Using 10's complement, subtract  $3250 - 72532$ .

$$M = 03250$$

$$10\text{'s complement of } N = + 27468$$

$$\text{Sum} = 30718$$

There is no end carry. Therefore, the answer is  $-(10\text{'s complement of } 30718) = -69282$ .

# Subtraction Using 2's complement

Given the two binary numbers  $X = 1010100$  and  $Y = 1000011$ , perform the subtraction (a)  $X - Y$  and (b)  $Y - X$  by using 2's complements.

$$\begin{array}{rcl} \text{(a)} & X = & 1010100 \\ & 2\text{'s complement of } Y = + & \underline{0111101} \\ & \text{Sum} = & 10010001 \\ & \text{Discard end carry } 2^7 = - & \underline{10000000} \\ & \text{Answer: } X - Y = & 0010001 \end{array}$$

$$\begin{array}{rcl} \text{(b)} & Y = & 1000011 \\ & 2\text{'s complement of } X = + & \underline{0101100} \\ & \text{Sum} = & 1101111 \end{array}$$

There is no end carry. Therefore, the answer is  $Y - X = -(2\text{'s complement of } 1101111) = -0010001$ .



# Subtraction with $r$ 's Complement

The subtraction of two positive numbers ( $M - N$ ), both of base  $r$ , may be done as follows:

- (1) Add the minuend  $M$  to the  $r$ 's complement of the subtrahend  $N$ .
- (2) Inspect the result obtained in step (1) for an end carry:
  - (a) If an end carry occurs, discard it.
  - (b) If an end carry does not occur, take the  $r$ 's complement of the number obtained in step (1) and place a negative sign in front.

# Subtraction with $(r-1)$ 's Complement

Both numbers must have the same number of digits

- (1) Add the minuend  $M$  to the  $(r - 1)$ 's complement of the subtrahend  $N$ .
- (2) Inspect the result obtained in step (1) for an end carry.
  - (a) If an end carry occurs, add 1 to the least significant digit (end around carry).
  - (b) If an end carry does not occur, take the  $(r - 1)$ 's complement of the number obtained in step (1) and place a negative sign in front.

# Subtraction Using 9's complement

(a)  $M = 72532$   
 $N = 03250$

end around carry

$$\begin{array}{r}
 + \quad 72532 \\
 + \quad 96749 \\
 \hline
 1 \quad 69281 \\
 \quad \quad 1 \\
 \hline
 69282
 \end{array}$$

9's complement of  $N = 96749$

ANSWER: 69282

(b)  $M = 03250$   
 $N = 72532$

no carry

$$\begin{array}{r}
 + \quad 03250 \\
 + \quad 27467 \\
 \hline
 30717
 \end{array}$$

9's complement of  $N = 27467$

ANSWER:  $-69282 = - (9's \text{ complement of } 30717)$

# Subtraction Using 1's complement

(a)  $X - Y = 1010100 - 1000011$

$$\begin{array}{r} X = 1010100 \\ 1\text{'s complement of } Y = + 0111100 \\ \text{Sum} = 10010000 \\ \text{End-around carry} = + \underline{\phantom{000}1} \\ \text{Answer: } X - Y = 0010001 \end{array}$$

(b)  $Y - X = 1000011 - 1010100$

$$\begin{array}{r} Y = 1000011 \\ 1\text{'s complement of } X = + \underline{0101011} \\ \text{Sum} = 1101110 \end{array}$$

There is no end carry. Therefore, the answer is  $Y - X = -(1\text{'s complement of } 1101110) = -0010001$ .

## Some additional problems:

- Perform subtraction on the given unsigned numbers using the **10's** and **9's** complement of the subtrahend. Where the result should be negative, find its **10's/9's** complement and affix a minus sign. Verify your answers.

(a)  $4,637 - 2,579$

(b)  $125 - 1,800$

(c)  $2,043 - 4,361$

(d)  $1,631 -$

745

# Additional Problems:

- Perform subtraction on the given unsigned binary numbers using the **2's and 1's** complement of the subtrahend. Where the result should be negative, find its **2's/1's** complement and affix a minus sign.

(a)  $10011 - 10010$

$100110$

(b)  $100010 -$

(c)  $1001 - 110101$

$10101$

(d)  $101000 -$