

```
In [2]: import numpy as np
        from scipy.io import loadmat
        from sklearn.datasets import make_regression
        from sklearn.linear_model import LinearRegression

        in_data = loadmat('face_emotion_data.mat')
        print([key for key in in_data])

        X = in_data['X']
        y = in_data['y']

        ['__header__', '__version__', '__globals__', 'y', 'X']
```

## a

Use the training data X and y and a least squares problem to train your classifier weights.

```
In [3]: w = np.linalg.lstsq(X, y, rcond=None)[0]
        print("w = \n", w)

w =
[[ 0.94366942]
 [ 0.21373778]
 [ 0.26641775]
 [-0.39221373]
 [-0.00538552]
 [-0.01764687]
 [-0.16632809]
 [-0.0822838 ]
 [-0.16644364]]
```

## b

Suppose there is a new face with feature vectors  $x_i = [x_{i1} \ x_{i2} \ \dots \ x_{i9}]^T$ . Compute for label  $y_i = x_i^T @ w$ . If  $y_i > 0$ , then it will be classified as a happy face; if  $y_i < 0$ , then it will be classified as an angry face.

**c**

Feature related to the first column of X seems to be most important, since its corresponding weight,  $w_1$ , has the largest absolute value among all weights, meaning that the feature will have the largest effect on the value of its predicted label.

**d**

To design a classifier based on three of the nine features, choosing column 1, 4, and 3 can best represent the original matrix, since their respective weights have the highest 3 absolute values.

**e**

```
In [4]: # assessing performance using all 9 features.
y_head = X @ w
counter = 128;
for i in range(0, 128):
    if (y[i] > 0 and y_head[i] > 0) or (y[i] <= 0 and y_head[i] <= 0):
        counter-=1
print("error rate using 9 features: ", counter/128)

# assessing performance using only 3 features
X2 = np.hstack([X[:, 0:1], X[:, 2:3], X[:, 3:4]])
w2 = np.linalg.lstsq(X2, y, rcond=None)[0]
y2_head = X2 @ w2
counter = 128
for i in range(0, 128):
    if (y[i] > 0 and y2_head[i] > 0) or (y[i] <= 0 and y2_head[i] <= 0):
        counter-=1
print("error rate using 3 features: ", counter/128)

error rate using 9 features:  0.0234375
error rate using 3 features:  0.0625
```

```
In [5]: SETS = 8
SAMPLE_SIZE = 16
# [t*16 :(t+1)*16 - 1]
miss_rate = np.array(np.ones(SETS))
for t in range(0, SETS):
    X3 = np.delete(X, slice(t*16, (t+1)*16), 0)
    y3 = np.delete(y, slice(t*16, (t+1)*16), 0)
    w3 = np.linalg.lstsq(X3, y3, rcond=None)[0]
    y3_head = X3 @ w3
    counter = 0
    for i in range(0, 127-SAMPLE_SIZE):
        if (y3[i] > 0 and y3_head[i] <= 0) or (y3[i] <= 0 and y3_head[
i] > 0):
            counter+=1
    miss_rate[t] = counter / SAMPLE_SIZE
print("error rate = ", np.average(miss_rate))

error rate = 0.171875
```

In [ ]:

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