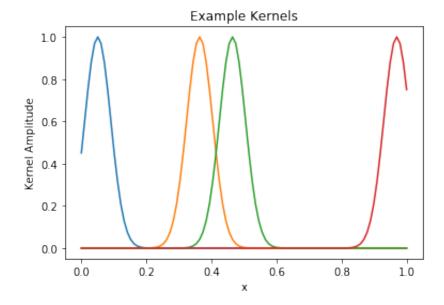
```
In [1]:
        import numpy as np
         import matplotlib.pyplot as plt
        np.random.seed(1024) # ensure same noise for each run
        # number of training points
        n = 50
        # sample n random points between 0 and 1
        x = np.random.rand(n,1)
        # set d = x^2 + .4 \sin(1.5 \text{ pi } x) + \text{noise}
        d = x*x + 0.4*np.sin(1.5*np.pi*x) + 0.04*np.random.randn(n,1)
        # plot result
        plt.plot(x,d,'bo')
        plt.xlabel('x')
         plt.ylabel('d')
        plt.title('Measured Data with Noise')
        plt.show()
```

<Figure size 640x480 with 1 Axes>

```
In [17]:
                                           sigma = 0.04 #defines Gaussian kernel width
                                            p = 100 #number of points on x-axis
                                           # Display examples of the kernels
                                           x_test = np.linspace(0,1.00,p) # uniformly sample interval [0,1]
                                           j list = [5, 36, 46, 96] #list of indices for example kernels
                                           Kdisplay = np.zeros((p,len(j_list)),dtype=float)
                                           for i in range(p):
                                                               for j in range(len(j_list)):
                                                                                 Kdisplay[i,j]= np.exp(-(x_test[i]-x_test[j_list[j]])**2/(2*sic_test[i]-x_test[j_list[j]])**2/(2*sic_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test[i]-x_test
                                            print('Sigma = ',sigma)
                                            plt.plot(x_test, Kdisplay)
                                           plt.title('Example Kernels')
                                            plt.xlabel('x')
                                            plt.ylabel('Kernel Amplitude')
                                            plt.show()
```

Sigma = 0.04



```
In [18]: # Kernel fitting to data

lam = 0.01 #ridge regression parameter

distsq=np.zeros((n,n),dtype=float)

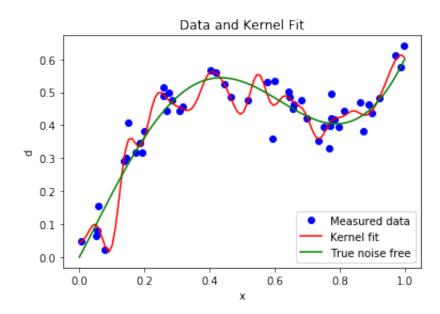
for i in range(0,n):
    for j in range(0,n):
        distsq[i,j]=(x[i]-x[j])**2

K = np.exp(-distsq/(2*sigma**2))

alpha = np.linalg.inv(K+lam*np.identity(n))@d
```

In [19]: # Generate smooth curve corresponding to data fit distsq_xtest = np.zeros((p,n),dtype=float) for i in range(0,p): for j in range(0,n): $distsq_xtest[i,j] = (x_test[i]-x[j])**2$ dtest = np.exp(-distsg xtest/(2*sigma**2))@alpha dtrue = x_test*x_test + 0.4*np.sin(1.5*np.pi*x_test) # noise free dat print('Sigma = ',sigma) print('Lambda = ',lam) plt.plot(x,d,'bo',label='Measured data') plt.plot(x_test,dtest,'r',label='Kernel fit') plt.plot(x_test,dtrue,'g',label='True noise free') plt.title('Data and Kernel Fit') plt.legend(loc='lower right') plt.xlabel('x') plt.ylabel('d') plt.show()

Sigma = 0.04Lambda = 0.01



1b)

xi is around 0.3

xi determines the actual position of a certain peak sigma determines the width between peaks

1d)

use cross validation to find the best sigma and lambda that generalizes well to new data.

In []:	
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