

①

a) $RHS = P(A) - P(A, B) + (1 - P(A) - 1)$

$$= P(A, B^c) - P(A) \neq P(A, B^c) = LHS$$

$\therefore (a)$ is false

b) $LHS = P(A) = 1 - P(A^c) = 1 - (P(A^c, B) + P(A^c, B^c)) = RHS$

$\therefore (b)$ is true

c) $LHS = P(A^c \cup B^c) = 1 - P(A \cap B) = 1 - [P(A) + P(B)] + P(A \cup B)$
 $\leq 2 \cdot 1 - (P(A) + P(B)) = RHS$

$\therefore (c)$ is true

② Given: positive = P , infective = I , negative = N .

$$P(P, I) = 0.95$$

$$P(N, I^c) = 0.99$$

$$P(I) = 0.001$$

a) $P(I) = 0.001$

should not be concerned.

b) risk = $P(P, I^c) \cdot P(I^c) + P(N, I) \cdot P(I)$

$$= 0.05 \times 0.998 + 0.01 \times 0.001$$

$$= 0.04996$$

c) risk = $P(N, I) \cdot P(I) = 0.0001$

d) Yes.