

Q1

b) $p(y|x) = \frac{p(x|y) \cdot p(y)}{p(x)}$

c) $\hat{y} = \operatorname{argmax}_y p(y|x) = \operatorname{argmax}_y \frac{p(x|y) \cdot p(y)}{p(x)}$

For continuous variable x , this is $\operatorname{argmax}_y \frac{f(x|y) \cdot p(y)}{p(x)}$

Since $f(x)$ does not change the value of argmax

$$\hat{y} = \operatorname{argmax}_y f(x|y) \cdot p(y) \text{ holds } \square$$

Since we are taking the max argument, applying log still
yield the same argument

$$\therefore \hat{y} = \operatorname{argmax}_y \log(f(x|y) \cdot p(y)) \text{ holds } \square$$

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