

①

$$a) RHS = (P(A) - P(A, B)) + (1 - P(A) - 1)$$

$$= P(A, B^c) - P(A) \neq P(A, B^c) = LHS$$

$\therefore$  (a) is false

$$b) LHS = P(A) = 1 - P(A^c) = 1 - (P(A^c, B) + P(A^c, B^c)) = RHS$$

$\therefore$  (b) is true

$$c) LHS = P(A^c \cup B^c) = 1 - P(A \cap B) = 1 - [P(A) + P(B)] + P(A \cup B)$$

$$\leq 2 - (P(A) + P(B)) = RHS$$

$\therefore$  (c) is true

② Given: positive = P, infective = I, negative = N.

$$P(P, I) = 0.95$$

$$P(N, I^c) = 0.99$$

$$P(I) = 0.001$$

$$a) P(I) = 0.001$$

should not be concerned.

$$b) risk = P(P, I^c) \cdot P(I^c) + P(N, I) \cdot P(I)$$

$$= .05 \times 0.999 + .01 \times 0.001$$

$$= 0.04996$$

$$c) risk = P(N, I) \cdot P(I) = 0.0001$$

d) Yes.