

DSP assignment2 report

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Contents

1	Task1	2
1.1	2
1.2	2
1.3	3
2	Task2	5
2.1	5
2.2	8
3	Declaration of Originality and Submission Information	13
4	Appendix	14
4.1	hr-detect.py	14
4.2	ecg-filter.py	18
4.3	fir-filter.py	20

1 Task1

1.1

With the definition of FIR filter:

$$z(n) = \sum_{i=0}^{ntaps} h(i)x(n-i)$$

We implemented the FIR filter with buffer defined with:

```
1 #add a new value to the buffer
2 self._buffer[self._offset] = v
3
4 for indexH in range(self._ntaps):
5     # indexH means i and indexX means n-i
6     indexX = self._offset - indexH
7     if(indexX < 0):
8         indexX += self._ntaps
9     output += self._coefficients[indexH]*self._buffer[indexX]
10
11 self._offset+=1
12 if self._offset >= self._ntaps:
13     self._offset = self._offset - self._ntaps
```

By moving the offset(index) of current $x(n)$ rather than full array, we minimised the amount of data being shifted and limited the time complexity in $O(n)$

1.2

To test this FIR filter class, we defined a delay line, a coefficients for calculate. By implementing the equation mentioned above, we could manually calculate the expected output:

x	h	output
4	5	20
5	2	33
3		25

So, In code, we defined:

```
1 x = np.array([4,5,3])
2 h = np.array([5,2])
3
4 output_correct = np.array([20, 33, 25])
```

Once starting the test, one should get the output by feeding x values into fir-filter:

```

1 for value in x:
2     print("fir result:", fir_filter.dofilter(value))

```

So we could check test the filter by: python fir_filter and the correct result should be:

```

1 starting unittest
2 x value: [4 5 3]
3 h value [5 2]
4 correct output [20 33 25]
5 output from FIR_filter.dofilter: [20. 33. 25.]

```

1.3

To determined the cut-off frequency, we firstly observed the frequency spectrum of original signal (as shwon by 1):

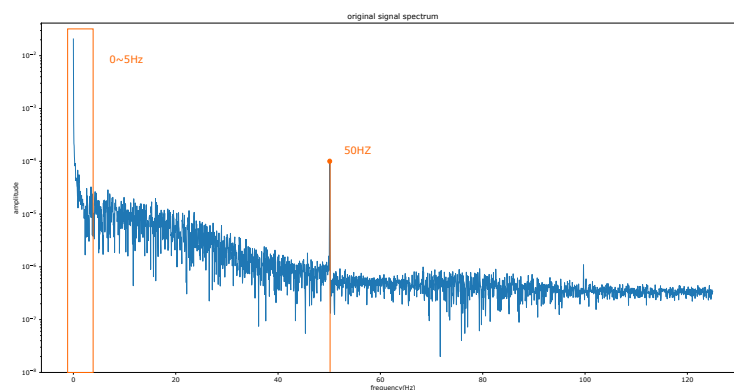


Figure 1: ECG data in frequency domain

As shwon by 1, the DC value is about 0-5HZ and the fundemental frequency is concentrated on around 50Hz. Thus, we created a filter template by:

```

1 H = np.ones(M)

```

Than, removing the 0-5Hz component and 45-55Hz component:

```

1 k0 = int(5/Fs * M)
2 k1 = int(45/Fs * M)
3 k2 = int(55/Fs * M)
4
5 H[0:k0+1] = 0
6 H[M-k0-1:M] = 0
7 H[k1:k2+1] = 0
8 H[M-k2-1:M-k1] = 0

```

Thus, we could get the ideal impulse response of this filter by IFFT:

```
1 htemp = np.fft.ifft(H)
2 htemp = np.real(htemp)
```

Finally, flipping the filter coefficients into a causal signal and implement a hamming window to fix the limited length problem:

```
1 h[0:int(M/2)] = htemp[int(M/2):M]
2 h[int(M/2):M] = htemp[0:int(M/2)]
3 h = h*np.hamming(M)
```

The frequency response as well as time response of this filter coefficients are shown in figure2:

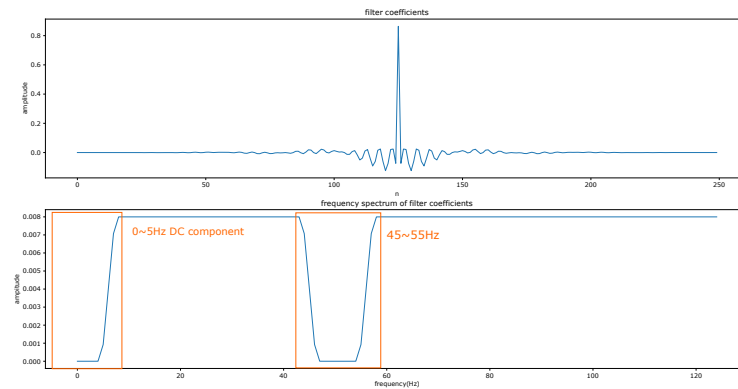


Figure 2: filter coefficients

After we create a fir-filter by these coefficients, for simulating the real time signal, we fed the ECG data into a for loop:

```
1 #feed values into filter in real time
2 fir_filter = fir.FIR_filter(h)
3 ecgDataFiltered = np.empty(0)
4 for value in ecgData:
5     ecgDataFiltered = np.append(ecgDataFiltered, fir_filter.dofilter
        (value))
```

The difference between the original signal and the filtered signal could be observed in time domain (as shown by 3):

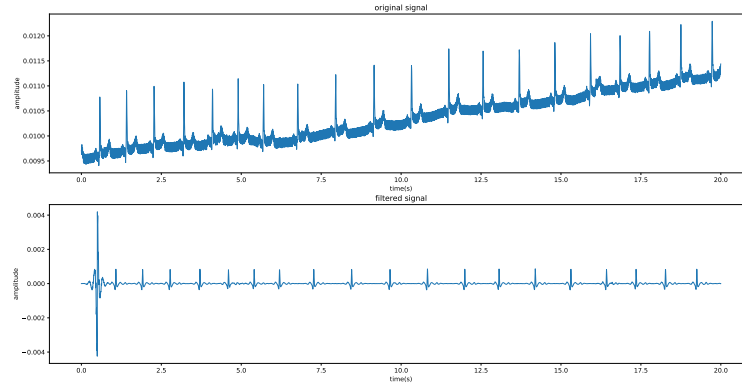


Figure 3: ECG data in time domain

The PQRST is intact and can be clearly found in figure :

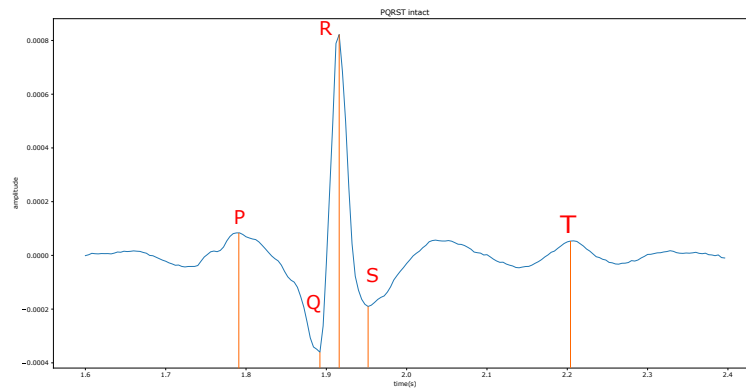


Figure 4: PQRST

2 Task2

2.1

To create a template of one single heart beat, we prefiltered the data by the method of Task1 (removing 0-5Hz and 45-55Hz component of the original signal). A template should contain QRST complex. Consequently, we could drive a template as shown by figure 5

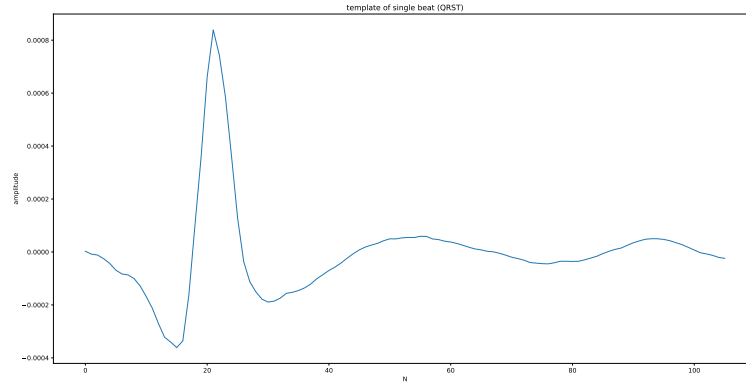


Figure 5: single beat of QRST complex

In order to find the R-peak in real-time processing, we defined a QRST intact when the result of match filter jump exceeds the threshold from low to high. In code:

```
1 #when the value exceed the threshold while the previous one didn
  't
2 if((matchedDataResult[N-1]>threshold) & (matchedDataResult[N-2]
  > threshold)):
3     peakPosition = np.append(peakPosition, index[0])
```

From previous trail and error results, we found one of best threshold:

```
1 threshold = 0.65e-11
```

Than, we fed the signal into our system, which is:

- prefilter ever input data
- match filter ever input data
- check if this data meet the QRST intact found conditions

In code:

```
1 for index, value in np.ndenumerate(ecgData):
2     prefilteredData = preFilter1.dofilter(value)
3     #record prefilter result
4     preFilterResult = np.append(preFilterResult, prefilteredData
  )
5     #record matchfilter result
6     matchedData = matchedFilter1.dofilter(prefilteredData)**2 #
  reduce S/N ratio
7     matchedDataResult = np.append(matchedDataResult, matchedData
  )
```

```

8
9     #define threshold
10    threshold = 0.65e-11
11    N = len(matchedDataResult)
12    #when the value exceeded the threshold while the previous
    one didn't
13    if((matchedDataResult[N-1]>threshold) & (matchedDataResult[N
-2] > threshold)):
14    peakPosition = np.append(peakPosition, index[0])

```

And the result of match filter is shown by figure6:

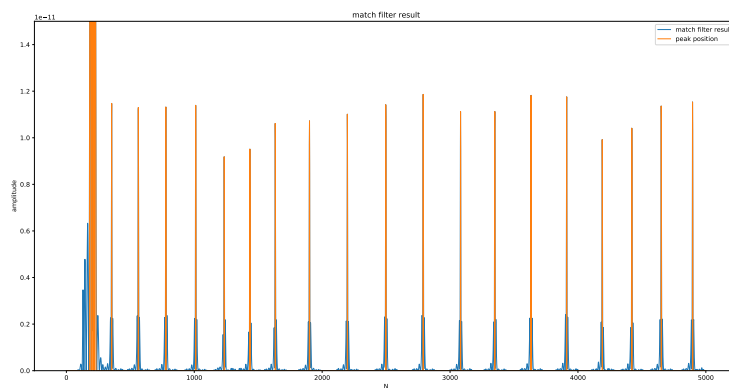


Figure 6: the match filter result and the found peaks

In command line:

```

1 peakFinding in 2.1: [ 181.  182.  183.  184.  185.  186.  187.
2   188.  189.  190.  191.  197.
3   198.  199.  200.  201.  202.  203.  204.  205.  206.  207.
4   210.  211.
5   212.  213.  214.  215.  216.  217.  222.  223.  224.  225.
6   226.  227.
7   228.  229.  230.  231.  353.  354.  355.  562.  563.  564.
8   777.  778.
   779. 1011. 1012. 1234. 1235. 1435. 1436. 1633. 1634. 1635.
   1900. 1901.
   1902. 2197. 2198. 2497. 2498. 2499. 2789. 2790. 2791. 3082.
   3083. 3349.
   3350. 3351. 3632. 3633. 3634. 3911. 3912. 3913. 4190. 4191.
   4421. 4422.
   4651. 4652. 4653. 4896. 4897. 4898.]

```

2.2

Heart rate can be calculated by the time gap between every heart beat (R-peak). Specifically:

```
1 heartRate = 60 // (N * (1 / Fs))
```

Where N is the number of sample points between each detected heart beat. Besides, for removing wrong detections, we limited the minimum interval to 100 sampling points. When coding, an IF statement has been implemented for this operator

```
1 if (N > Nlimited):
```

Consequently, when we implemented the heart rate detect function for each input data, it is similar to the R-peak detecting at the beginning:

```
1 #do prefilter
2 preFltValue = preFilter.dofilter(value)
3 #do match filter
4 matchedValue = matchedFilter.dofilter(preFltValue)
5 #increase S/N ratio
6 matchedValue *= matchedValue
```

Then we recorded each sampling point during the gap between each heart beat:

```
1 #recordding gap
2 template = np.append(template, matchedValue)
```

Once a heart beat had been detected, we calculate the new value of heartbeats rate and restart calculating the gap:

```
1 N = len(template)
2 if (N > Nlimited):
3     if ((template[N-1] > threshold) & (template[N-2] < threshold)):
4         #calculate the heartRate
5         heartRate = 60 // (N * (1 / Fs))
6         #calculate the time when beat occur
7         time = index[0] * (1 / Fs)
8         print("in", round(time, 2), "s:", heartRate, "Bpm")
9         heartRateResult = np.append(heartRateResult, heartRate)
10
11 #clear template
12 template = np.empty(0)
```

The final output of heartbeat in real-time system is shown by figure7

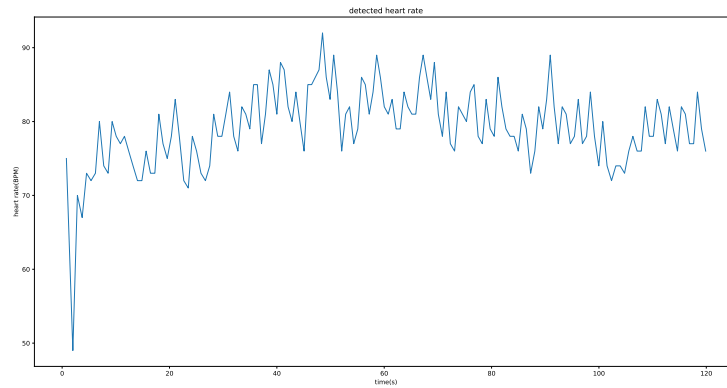


Figure 7: the match filter result and the found peaks

In command line:

```

1 in 0.79 s: 75.0 Bpm
2 in 2.0 s: 49.0 Bpm
3 in 2.84 s: 70.0 Bpm
4 in 3.73 s: 67.0 Bpm
5 in 4.55 s: 73.0 Bpm
6 in 5.38 s: 72.0 Bpm
7 in 6.2 s: 73.0 Bpm
8 in 6.94 s: 80.0 Bpm
9 in 7.75 s: 74.0 Bpm
10 in 8.56 s: 73.0 Bpm
11 in 9.31 s: 80.0 Bpm
12 in 10.08 s: 78.0 Bpm
13 in 10.85 s: 77.0 Bpm
14 in 11.61 s: 78.0 Bpm
15 in 12.4 s: 76.0 Bpm
16 in 13.21 s: 74.0 Bpm
17 in 14.04 s: 72.0 Bpm
18 in 14.86 s: 72.0 Bpm
19 in 15.64 s: 76.0 Bpm
20 in 16.46 s: 73.0 Bpm
21 in 17.27 s: 73.0 Bpm
22 in 18.01 s: 81.0 Bpm
23 in 18.79 s: 77.0 Bpm
24 in 19.58 s: 75.0 Bpm
25 in 20.35 s: 78.0 Bpm
26 in 21.07 s: 83.0 Bpm
27 in 21.83 s: 78.0 Bpm
28 in 22.66 s: 72.0 Bpm
29 in 23.5 s: 71.0 Bpm
30 in 24.26 s: 78.0 Bpm
31 in 25.04 s: 76.0 Bpm

```

32 in 25.86 s: 73.0 Bpm
33 in 26.69 s: 72.0 Bpm
34 in 27.5 s: 74.0 Bpm
35 in 28.23 s: 81.0 Bpm
36 in 28.99 s: 78.0 Bpm
37 in 29.76 s: 78.0 Bpm
38 in 30.49 s: 81.0 Bpm
39 in 31.2 s: 84.0 Bpm
40 in 31.96 s: 78.0 Bpm
41 in 32.74 s: 76.0 Bpm
42 in 33.47 s: 82.0 Bpm
43 in 34.21 s: 81.0 Bpm
44 in 34.96 s: 79.0 Bpm
45 in 35.67 s: 85.0 Bpm
46 in 36.37 s: 85.0 Bpm
47 in 37.14 s: 77.0 Bpm
48 in 37.88 s: 81.0 Bpm
49 in 38.57 s: 87.0 Bpm
50 in 39.27 s: 85.0 Bpm
51 in 40.0 s: 81.0 Bpm
52 in 40.68 s: 88.0 Bpm
53 in 41.36 s: 87.0 Bpm
54 in 42.09 s: 82.0 Bpm
55 in 42.83 s: 80.0 Bpm
56 in 43.54 s: 84.0 Bpm
57 in 44.29 s: 80.0 Bpm
58 in 45.07 s: 76.0 Bpm
59 in 45.77 s: 85.0 Bpm
60 in 46.48 s: 85.0 Bpm
61 in 47.17 s: 86.0 Bpm
62 in 47.86 s: 87.0 Bpm
63 in 48.51 s: 92.0 Bpm
64 in 49.2 s: 86.0 Bpm
65 in 49.92 s: 83.0 Bpm
66 in 50.59 s: 89.0 Bpm
67 in 51.3 s: 84.0 Bpm
68 in 52.08 s: 76.0 Bpm
69 in 52.82 s: 81.0 Bpm
70 in 53.54 s: 82.0 Bpm
71 in 54.32 s: 77.0 Bpm
72 in 55.08 s: 79.0 Bpm
73 in 55.77 s: 86.0 Bpm
74 in 56.48 s: 85.0 Bpm
75 in 57.21 s: 81.0 Bpm
76 in 57.92 s: 84.0 Bpm
77 in 58.59 s: 89.0 Bpm
78 in 59.28 s: 86.0 Bpm
79 in 60.01 s: 82.0 Bpm
80 in 60.75 s: 81.0 Bpm

81 in 61.47 s: 83.0 Bpm
82 in 62.22 s: 79.0 Bpm
83 in 62.98 s: 79.0 Bpm
84 in 63.69 s: 84.0 Bpm
85 in 64.41 s: 82.0 Bpm
86 in 65.15 s: 81.0 Bpm
87 in 65.88 s: 81.0 Bpm
88 in 66.58 s: 86.0 Bpm
89 in 67.25 s: 89.0 Bpm
90 in 67.94 s: 86.0 Bpm
91 in 68.66 s: 83.0 Bpm
92 in 69.34 s: 88.0 Bpm
93 in 70.08 s: 81.0 Bpm
94 in 70.84 s: 78.0 Bpm
95 in 71.55 s: 84.0 Bpm
96 in 72.32 s: 77.0 Bpm
97 in 73.11 s: 76.0 Bpm
98 in 73.84 s: 82.0 Bpm
99 in 74.57 s: 81.0 Bpm
100 in 75.32 s: 80.0 Bpm
101 in 76.03 s: 84.0 Bpm
102 in 76.73 s: 85.0 Bpm
103 in 77.5 s: 78.0 Bpm
104 in 78.27 s: 77.0 Bpm
105 in 78.99 s: 83.0 Bpm
106 in 79.74 s: 79.0 Bpm
107 in 80.5 s: 78.0 Bpm
108 in 81.2 s: 86.0 Bpm
109 in 81.92 s: 82.0 Bpm
110 in 82.68 s: 79.0 Bpm
111 in 83.44 s: 78.0 Bpm
112 in 84.2 s: 78.0 Bpm
113 in 84.98 s: 76.0 Bpm
114 in 85.72 s: 81.0 Bpm
115 in 86.47 s: 79.0 Bpm
116 in 87.28 s: 73.0 Bpm
117 in 88.06 s: 76.0 Bpm
118 in 88.78 s: 82.0 Bpm
119 in 89.54 s: 79.0 Bpm
120 in 90.26 s: 83.0 Bpm
121 in 90.93 s: 89.0 Bpm
122 in 91.66 s: 82.0 Bpm
123 in 92.43 s: 77.0 Bpm
124 in 93.16 s: 82.0 Bpm
125 in 93.9 s: 81.0 Bpm
126 in 94.67 s: 77.0 Bpm
127 in 95.44 s: 78.0 Bpm
128 in 96.16 s: 83.0 Bpm
129 in 96.93 s: 77.0 Bpm

```

130 in 97.7 s: 78.0 Bpm
131 in 98.41 s: 84.0 Bpm
132 in 99.17 s: 78.0 Bpm
133 in 99.97 s: 74.0 Bpm
134 in 100.72 s: 80.0 Bpm
135 in 101.52 s: 74.0 Bpm
136 in 102.35 s: 72.0 Bpm
137 in 103.15 s: 74.0 Bpm
138 in 103.96 s: 74.0 Bpm
139 in 104.78 s: 73.0 Bpm
140 in 105.56 s: 76.0 Bpm
141 in 106.33 s: 78.0 Bpm
142 in 107.11 s: 76.0 Bpm
143 in 107.9 s: 76.0 Bpm
144 in 108.62 s: 82.0 Bpm
145 in 109.38 s: 78.0 Bpm
146 in 110.14 s: 78.0 Bpm
147 in 110.86 s: 83.0 Bpm
148 in 111.6 s: 81.0 Bpm
149 in 112.37 s: 77.0 Bpm
150 in 113.1 s: 82.0 Bpm
151 in 113.85 s: 79.0 Bpm
152 in 114.63 s: 76.0 Bpm
153 in 115.36 s: 82.0 Bpm
154 in 116.1 s: 81.0 Bpm
155 in 116.87 s: 77.0 Bpm
156 in 117.64 s: 77.0 Bpm
157 in 118.36 s: 84.0 Bpm
158 in 119.11 s: 79.0 Bpm
159 in 119.89 s: 76.0 Bpm

```

Besides, adding the capability of processing Python command line arguments provides a user-friendly interface. Thus we add an "-c" or "--clear" argument to make the output less verbose. After passing the argument by:

```

1 python hr_detect.py -c/--clear

```

the output would only be a graph of heart rate and time.

3 Declaration of Originality and Submission Information

I affirm that this submission is my own / the groups original work in accordance with the University of Glasgow Regulations and the School of Engineering Requirements.

- Student Number: 2533494w Student Name: Jingyan Wang
- Student Number: 2595993w Student Name: Qianqian Wang

4 Appendix

4.1 hr-detect.py

```
1 #!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
3 """
4 Created on Wed Nov 4 18:23:05 2020
5
6 @author: wayenvan
7 """
8
9 import numpy as np
10 import matplotlib.pyplot as plt
11 import fir_filter as fir
12 import sys
13 import getopt
14
15 from ecg_gudb_database import GUDb
16
17
18 def heartRateCalculate(peaks, FS):
19     """this function calculate the heart rate when we get peak
20     sequencies, just for verifying"""
21     ret = np.empty(0)
22     for index, value in np.ndenumerate(peaks):
23         if(index[0]==0):
24             continue
25         N = value-peaks[index[0]-1]
26         ret=np.append(ret, 60//(N*(1/FS)))
27     return ret
28
29 def heartRateDetect(data, preFilter: fir.FIR_filter,
30 matchedFilter: fir.FIR_filter):
31     """detect heart rate in by filters
32
33     """
34     global verbose
35     Fs = 250
36     threshold = 2e-11
37     Nlimited = 100
38
39     template = np.empty(0)
40
41     #reference variable to recorld some information
42     preFilterResult = np.empty(0)
43     matchedResult = np.empty(0)
44     heartRateResult = np.empty(0)
```

```

43 R_peakPoint = np.empty(0)
44
45 for index, value in np.ndenumerate(data):
46
47     #do prefilter
48     preFltValue = preFilter.dofilter(value)
49     #do match filter
50     matchedValue = matchedFilter.dofilter(preFltValue)
51     #increase S/N ratio
52     matchedValue *= matchedValue
53
54     #recordding gap
55     template = np.append(template, matchedValue)
56
57     #record other data for verifying
58     preFilterResult = np.append(preFilterResult, preFltValue
59 )
60     matchedResult = np.append(matchedResult, matchedValue)
61
62     N = len(template)
63     if(N>Nlimited):
64         if((template[N-1]>threshold)&(template[N-2]<
threshold)):
65             #calculate the heartRate
66             heartRate =60//(N*(1/Fs))
67             #calculate the time when beat occur
68             time = index[0]*(1/Fs)
69
70             if(verbose):
71                 print("in",round(time, 2),"s:", heartRate, "
Bpm")
72
73             heartRateResult = np.append(heartRateResult,
heartRate)
74             R_peakPoint = np.append(R_peakPoint, index[0])
75
76             #clear template
77             template = np.empty(0)
78
79     return (preFilterResult,
80             matchedResult,
81             heartRateResult,
82             R_peakPoint)
83
84 """2.1 create a matched filter"""
85
86 #check command line argues
87 verbose = True

```

```

88 if __name__ == '__main__':
89     try:
90         options, args = getopt.getopt(sys.argv[1:], "c", ["clear
91         "])
92     except getopt.GetoptError:
93         sys.exit()
94
95     for name, value in options:
96         if name in ('-c', "--clear"):
97             verbose = False
98
99 #pre filtering
100 ecgData = np.genfromtxt('ECG_msc_matric_4.dat',
101                          dtype=None)
102 N = len(ecgData)
103 Fs = 250
104 M = 250
105
106 k0 = int(5/Fs * M)
107 k1 = int(45/Fs * M)
108 k2 = int(55/Fs * M)
109
110 H = np.ones(M)
111 H[0:k0+1] = 0
112 H[M-k0-1:M] = 0
113 H[k1:k2+1] = 0
114 H[M-k2-1:M-k1] = 0
115
116 htemp = np.fft.ifft(H)
117 htemp = np.real(htemp)
118
119 h = np.zeros(M)
120
121 h[0:int(M/2)] = htemp[int(M/2):M]
122 h[int(M/2):M] = htemp[0:int(M/2)]
123 h = h*np.hamming(M)
124
125 fir_filter = fir.FIR_filter(h)
126 ecgDataFiltered = np.empty(0)
127 for value in ecgData:
128     ecgDataFiltered = np.append(ecgDataFiltered, fir_filter.
129     dofilter(value))
130
131 #create a matched filter coefficients
132 matchedCore = ecgDataFiltered[906:1012]
133 matchedCore = matchedCore[::-1]
134 templateRPosition = 21

```



```

135 #begin create matchedFilter and find peaks
136 matchedDataResult = np.empty(0)
137 preFilterResult = np.empty(0)
138 peakPosition = np.empty(0)
139 matchedFilter1 = fir.FIR_filter(matchedCore)
140 preFilter1 = fir.FIR_filter(h) #clear fir_filter
141
142 #find peaks
143 for index, value in np.ndenumerate(ecgData):
144     prefilteredData = preFilter1.dofilter(value)
145     #record prefilter result
146     preFilterResult = np.append(preFilterResult, prefilteredData
    )
147     #record matchfilter result
148     matchedData = matchedFilter1.dofilter(prefilteredData)**2 #
    reduce S/N ratio
149     matchedDataResult = np.append(matchedDataResult, matchedData
    )
150
151     #define threshold
152     threshold = 0.65e-11
153     N = len(matchedDataResult)
154     #when the value exceed the threshold while the previous one
    didn't
155     if((matchedDataResult[N-1]>threshold) & (matchedDataResult[N
    -2] > threshold)):
156         peakPosition = np.append(peakPosition, index[0])
157
158 print("peakFinding in 2.1:", peakPosition)
159
160 """2.2 detect heart rate"""
161 #create corresponding filters
162 ecg_class = GUDb(14, "walking")
163 matchedFilter = fir.FIR_filter(matchedCore)
164 preFilter = fir.FIR_filter(h)
165
166 result = heartRateDetect(ecg_class.einthoven_III, preFilter,
    matchedFilter)
167
168 #compare with the original signal
169 tresult = heartRateCalculate(ecg_class.anno_cs, 250)
170
171
172 """plot figures"""
173
174 #2.1
175 # plt.figure(figsize=(20,10))
176 # plt.title("template of single beat (QRST)")
177 # plt.plot(matchedCore[::-1])

```

```

178 # plt.xlabel("N")
179 # plt.ylabel("amplitude")
180 # plt.savefig("./Figures/matchCore.pdf")
181
182 # a = np.zeros(len(ecgData))
183 # a[peakPosition.astype('int')] = 1
184 # plt.figure(figsize=(20,10))
185 # plt.title("match filter result")
186 # plt.plot(matchedDataResult, label="match filter result")
187 # plt.plot(a*matchedDataResult, label="peak position")
188 # plt.legend()
189 # plt.xlabel("N")
190 # plt.ylabel("amplitude")
191 # plt.ylim(0.0e-10, 1.5e-11)
192 # plt.savefig("./Figures/matchResult.pdf")
193
194 if(verbose==False):
195     plt.figure(figsize=(20,10))
196     plt.plot(result[3]*1/250, result[2])
197     plt.title("detected heart rate")
198     plt.ylabel("heart rate(BPM)")
199     plt.xlabel("time(s)")
200     #plt.savefig("./Figures/heartRate.pdf")
201     plt.show()

```

4.2 ecg-filter.py

```

1 #!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
3 """
4 Created on Sun Nov 1 22:39:50 2020
5
6 @author: wayenvan
7 """
8
9 import numpy as np
10 import fir_filter as fir
11 import matplotlib.pyplot as plt
12
13 """define functions"""
14 def generateXf(sampleRate, N):
15     """generateXf for frequency domain"""
16     return np.linspace(0.0, (N-1)*sampleRate/N, N)
17
18 def generateXt(sampleRate, N):
19     """generateXt for time domain"""
20     return np.linspace(0.0, (N-1)*1/sampleRate, N)
21
22 """main function"""

```

```

23 ecgData = np.genfromtxt('ECG_msc_matric_4.dat',
24                          dtype=None)
25 N = len(ecgData)
26 Fs = 250
27 M = 250
28
29 k0 = int(5/Fs * M)
30 k1 = int(45/Fs * M)
31 k2 = int(55/Fs * M)
32
33 #generate filter coefficients
34 H = np.ones(M)
35
36 H[0:k0+1] = 0
37 H[M-k0-1:M] = 0
38 H[k1:k2+1] = 0
39 H[M-k2-1:M-k1] = 0
40
41 htemp = np.fft.ifft(H)
42 htemp = np.real(htemp)
43
44 h = np.zeros(M)
45
46 h[0:int(M/2)] = htemp[int(M/2):M]
47 h[int(M/2):M] = htemp[0:int(M/2)]
48 h = h*np.hamming(M)
49
50 #feed values into filter in real time
51 fir_filter = fir.FIR_filter(h)
52 ecgDataFiltered = np.empty(0)
53 for value in ecgData:
54     ecgDataFiltered = np.append(ecgDataFiltered, fir_filter.
55                                 dofilter(value))
56
57 """plot figures"""
58 frequencySeriesH = generateXf(Fs, M)
59 plt.figure(figsize=(20,10))
60 plt.subplot(2,1,1)
61 plt.title("filter coefficients")
62 plt.plot(h)
63 plt.xlabel("n")
64 plt.ylabel("amplitude")
65
66 H2 = 2/M*np.abs(np.fft.fft(h))
67 plt.subplot(2,1,2)
68 plt.title("frequency spectrum of filter coefficients")
69 plt.plot(frequencySeriesH[0:M//2], H2[0:M//2])
70
71 #draw points

```

```

71 plt.xlabel("frequency(Hz)")
72 plt.ylabel("amplitude")
73 #plt.savefig("./Figures/filterCoefficients.pdf")
74
75 frequencySeries=generateXf(Fs, N)
76
77 plt.figure(figsize=(20,10))
78 plt.plot(frequencySeries[0:N//2], 2/N*np.abs(np.fft.fft(ecgData)
79         [0:N//2]))
80 plt.xlabel("frequency(Hz)")
81 plt.ylabel("amplitude")
82 plt.title("original signal spectrum")
83 plt.yscale("log")
84 #plt.savefig("./Figures/ecgDataFrequency.pdf")
85
86 timeSeries=generateXt(Fs, N)
87
88 plt.figure(figsize=(20,10))
89 plt.subplot(2, 1, 1)
90 plt.plot(timeSeries, ecgData)
91 plt.title("original signal")
92 plt.xlabel("time(s)")
93 plt.ylabel("amplitude")
94
95 plt.subplot(2, 1, 2)
96 plt.plot(timeSeries, ecgDataFiltered)
97 plt.title("filtered signal")
98 plt.xlabel("time(s)")
99 plt.ylabel("amplitude")
100 #plt.savefig("./Figures/ecgDataTime.pdf")
101
102 plt.figure(figsize=(20,10))
103 plt.plot(timeSeries[400:600], ecgDataFiltered[400:600])
104 plt.title("PQRST intact")
105 plt.xlabel("time(s)")
106 plt.ylabel("amplitude")
107 #plt.savefig("./Figures/PQRST.pdf")
108
109 #plot filter coefficients
110
111
112 plt.show()

```

4.3 fir-filter.py

```

1 #!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
3 """

```

```

4 Created on Sun Nov 1 14:17:26 2020
5
6 @author: wayenvan
7 """
8 import numpy as np
9
10 class FIR_filter:
11
12     def __init__(self, _coefficcients):
13         """create a filter"""
14         self._ntaps = len(_coefficcients)
15         self._coefficcients = _coefficcients
16         self._buffer = np.zeros(self._ntaps)
17         self._offset = 0 #the current place of x(n)
18
19     def dofilter(self, v):
20         """dofilter for this """
21         output = 0
22         self._buffer[self._offset] = v
23
24         # loop to calculate the ring buffer
25         for indexH in range(self._ntaps):
26             indexX = self._offset - indexH
27             if(indexX < 0):
28                 indexX += self._ntaps
29             output +=self._coefficcients[indexH]*self._buffer[
indexX]
30
31         #when reach the end, turn the offset into the first
position
32         self._offset+=1
33         if self._offset >= self._ntaps:
34             self._offset =self._offset - self._ntaps
35
36         return output
37
38 def unittest():
39     x = np.array([4,5,3])
40     h = np.array([5,2])
41     output_correct = np.array([20, 33, 25])
42
43     output = np.empty(0)
44
45     fir_filter = FIR_filter(h)
46
47     print("starting unittest")
48     print("x value:", x)
49     print("h value", h)
50     print("correct output", output_correct)

```

```
51     for value in x:
52         output=np.append(output, fir_filter.dofilter(value))
53
54     print("output from FIR_filter.dofilter:", output)
55
56 if __name__=="__main__":
57     unittest()
```