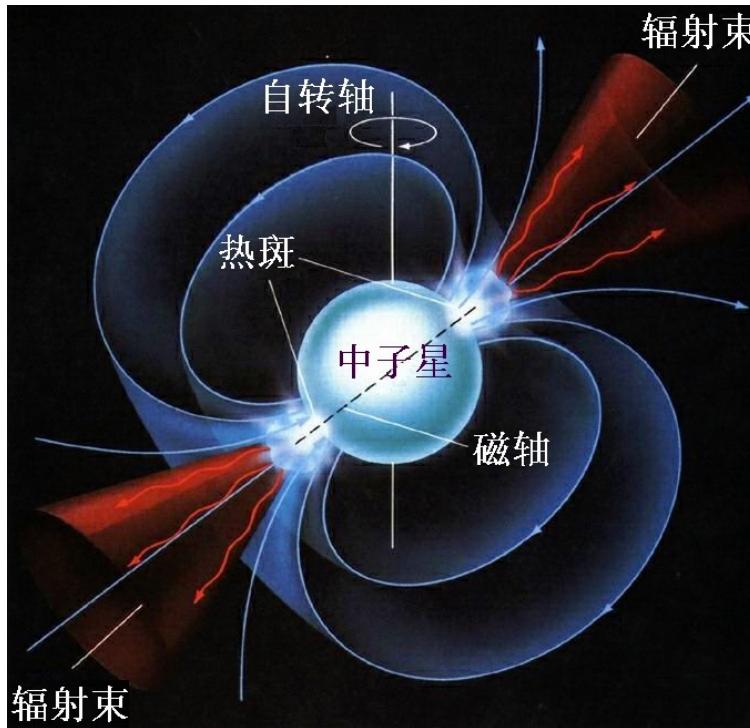


脉冲星分类方法

脉冲星简介



脉冲星是一种稀有的超级致密的中子星，每当脉冲星极冠转到地球视线方向，我们便看到其辐射信号，所以感觉收到了脉冲信号，脉冲星好比航海的灯塔，当辐射束扫过地球即可以观测一次脉冲。脉冲星半径约10千米、自旋很快，目前在射电波段观测到的旋转周期约在1.4毫秒~8.5秒之间。

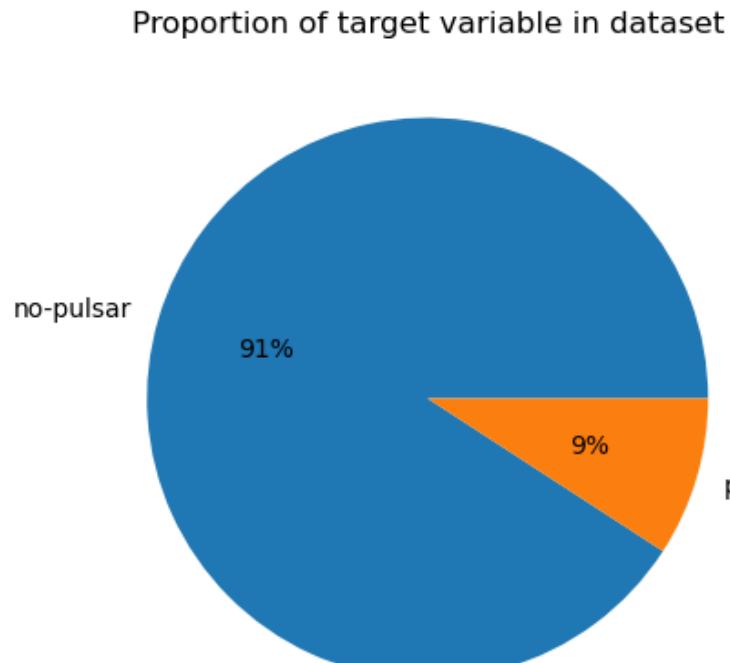
作为时空、星际介质和物质状态的探测器，它们具有相当大的科学意义：

- 1) 由于脉冲星的大质量和小半径，其表面引力场非常强，所以不能忽略广义相对论效应的存在，这使得脉冲星成为强引力场研究的天然实验室。
- 2) 由于脉冲星的超强磁场，这为我们研究磁层粒子加速机制、高能辐射、射电辐射过程提供了一个理想场所。
- 3) 脉冲星作为大质量恒星坍缩后超新星爆发的产物，它对于研究超新星爆发理论、理解脉冲星的形成机制相当重要。
- 4) 在应用研究方面，脉冲星因其自转周期的高度稳定性，在时间标准和航天器导航上有非常重要的应用前景。

天文学家已经观测到2700多颗脉冲星，至今已积累了一大批宝贵的资料，同时也存在不少现象和问题尚待解决。

自2017年10月10日首次对外宣布发现脉冲星以来，截至目前，被誉为“中国天眼”的500米口径球面射电望远镜已发现660余颗新脉冲星。

数据集介绍



数据集概况:

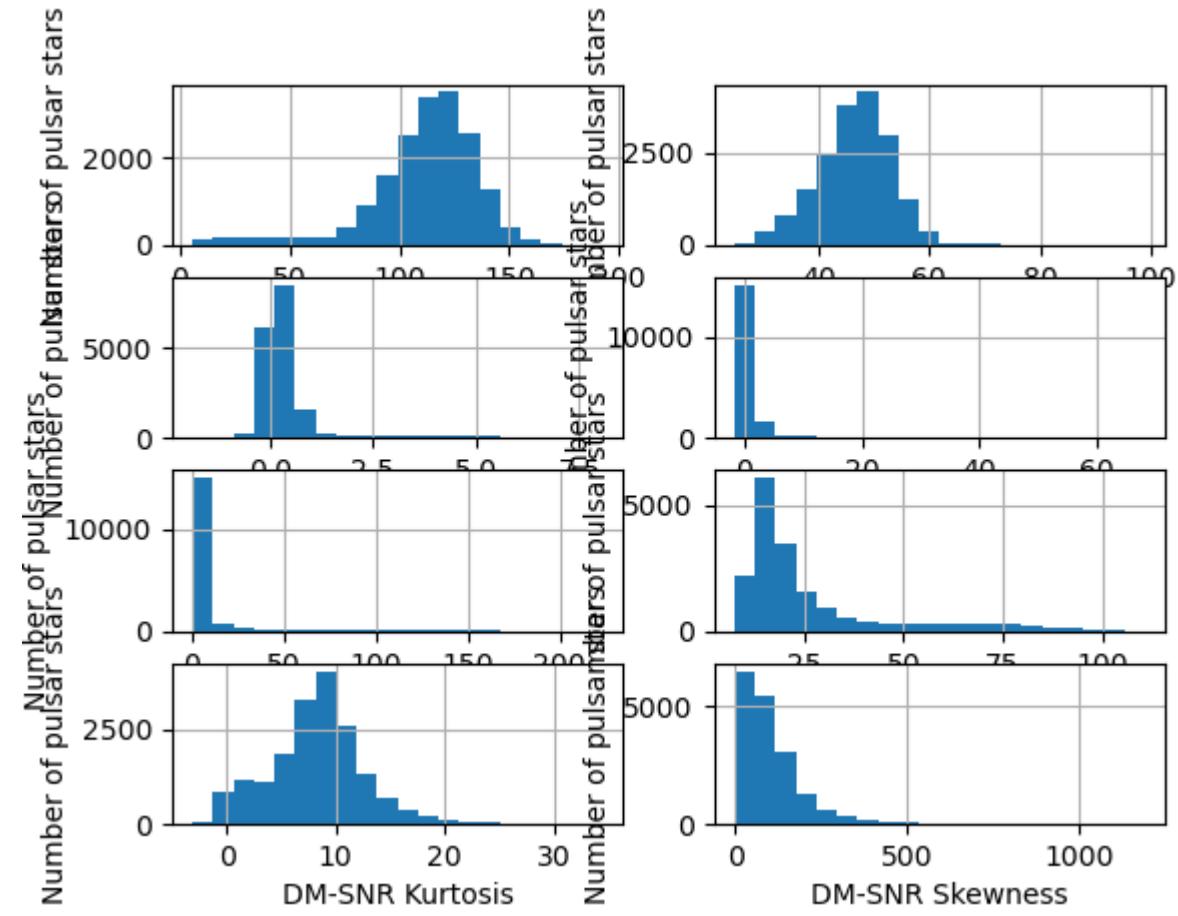
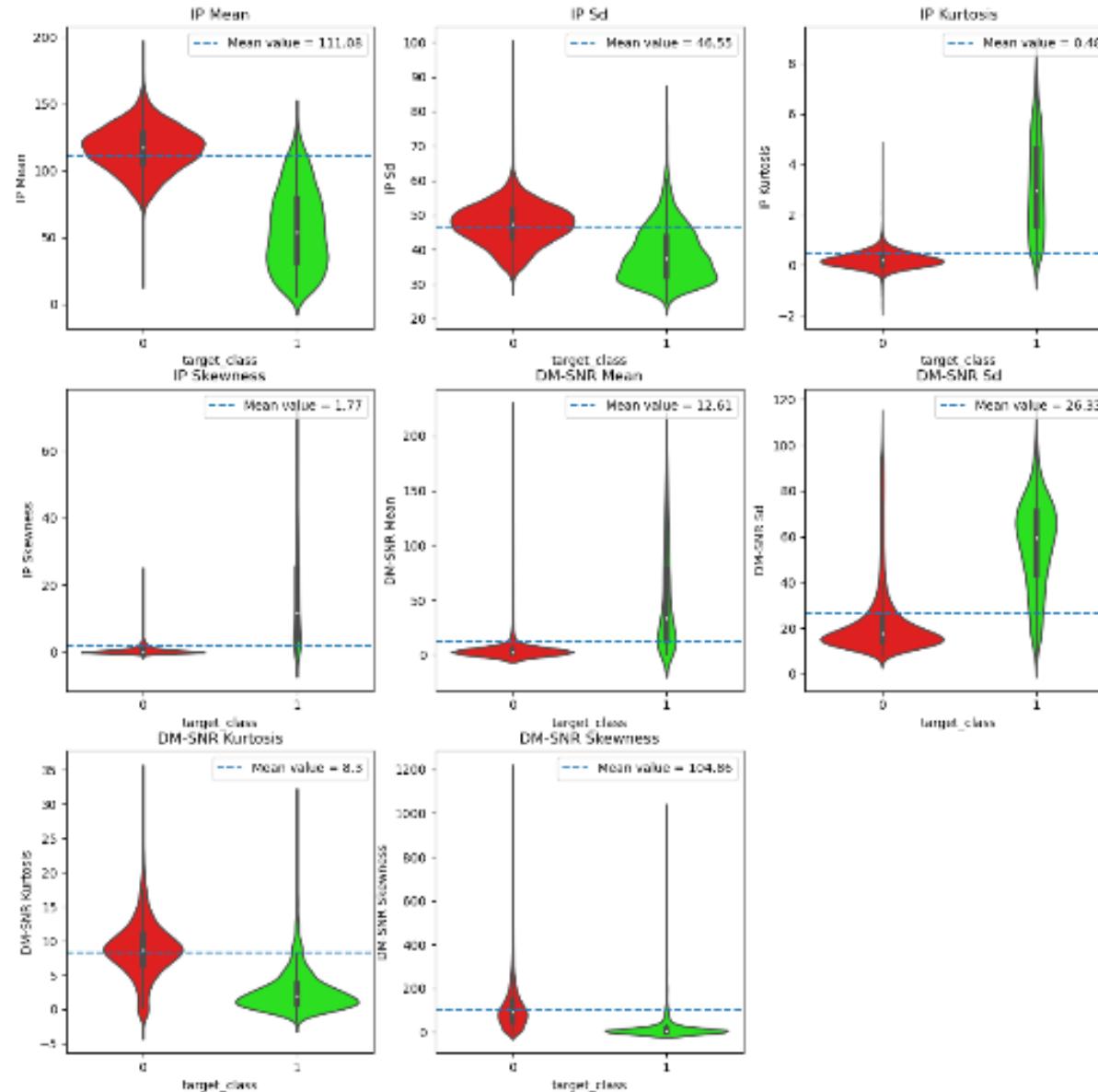
16259条因射频干扰而像脉冲星的记录,
1639条真真正的脉冲星记录

数据属性:

- | | |
|--|-----------------------|
| Mean of the integrated profile | : 脉冲轮廓宽度的平均值 |
| Standard deviation of the integrated profile | : 脉冲轮廓宽度的标准差 |
| Excess kurtosis of the integrated profile | : 脉冲轮廓宽度高于阈值的脉冲占比 |
| Skewness of the integrated profile | : 脉冲轮廓宽度偏度 |
| Mean of the DM-SNR curve | : DM-SNR(色散度-信噪比)曲线均值 |
| Standard deviation of the DM-SNR curve | : DM-SNR曲线标准差 |
| Excess kurtosis of the DM-SNR curve | : DM-SNR曲线的超额峰度 |
| Skewness of the DM-SNR curve | : DM-SNR曲线偏度 |
| Class | : 目标类型(label) |

数据集地址: <https://archive.ics.uci.edu/ml/datasets/HTRU2>

数据分布



数据集预处理

```
# 数据预处理
def date_preprocess(df: pd.DataFrame):
    # 区分特征向量和目标值
    y = df.get('target_class')

    # 分割训练集为训练集(80%)和测试集(20%)
    x_train, x_test, y_train, y_test = \
        train_test_split(df, y, test_size=0.2, random_state=3)

    # 下采样
    train_1 = x_train[x_train['target_class'] == 1]
    train_0 = x_train[x_train['target_class'] == 0]
    sample = train_0.sample(train_1.shape[0])
    train_all = train_1.append(sample)

    # 构造训练集 测试集
    svm.y_train = train_all.get('target_class')
    svm.x_train = train_all.drop(['target_class'], axis=1)
```

- 1) 按80%: 20% 的比例分割训练集和测试集
- 2) 下采样的方式解决数据不平衡问题
- 3) 特征缩放，将特征数据分布调整为标准正态分布，均值为0，方差为1

实验证明，进行数据下采样后再训练模型，测试结果都比较差，直接使用原始数据的效果反而不错。

SVM训练与测试

```
# C: 惩罚系数, 数值越高越容易过拟合
# gamma: 是选择径向基函数 (RBF) 作为kernel后, 该函数自带的一个参数
# gamma越大, 支持向量越少, gamma越小, 支持向量越多。数值越大越容易过拟合
def svm_train(kernel="rbf", C=1.0, gamma='auto'):

    svc = SVC(kernel=kernel, C=C, gamma=gamma)

    svc.fit(svm.x_train, svm.y_train)

    svm.y_pred_train = svc.predict(svm.x_train)
    train_score = accuracy_score(svm.y_train, svm.y_pred_train)

    # 预测
    svm.y_pred = svc.predict(svm.x_test)
    test_score = accuracy_score(svm.y_test, svm.y_pred)

    # print(score)

    print('Train Model accuracy score with kernel:{0}, C:{1}, gamma:{2} hyper parameters: {3:0.4f}'
          .format(kernel, C, gamma, train_score))
    print('Test Model accuracy score with kernel:{0}, C:{1}, gamma:{2} hyper parameters: {3:0.4f}'
          .format(kernel, C, gamma, test_score))
```

分数评价指标

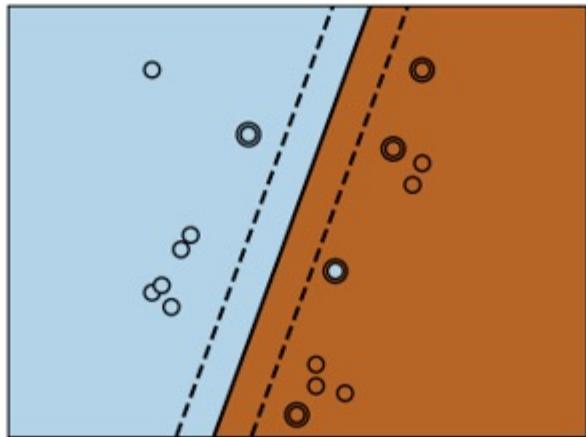
```
# 模型指标评价
def performance():
    # 混淆矩阵
    class_names = np.array(['0', '1'])
    with parallel_backend('threading', n_jobs=8):  
        8线程
            cm = confusion_matrix(svm.y_test, svm.y_pred)
            plot_confusion_matrix(cm, class_names)

    TP = cm[0, 0]
    TN = cm[1, 1]
    FP = cm[0, 1]
    FN = cm[1, 0]

    print('Co')
    # accuracy 精度 精度则是分类正确的样本数占样本总数的比例
    classification_accuracy = (TP + TN) / float(TP + TN + FP + FN)
    print('Tr')
    # error 错误率 错误率是分类错误的样本数占样本总数的比例
    classification_error = (FP + FN) / float(TP + TN + FP + FN)
    print('Tr')
    # precision 查准率 正确预测的正样本数占所有预测为正样本的数量的比值
    precision = TP / float(TP + FP)
    print('Fa')
    # recall(true positive rate) 查全率/召回率 正确预测的正样本数占真实正样本总数的比值
    recall = TP / float(TP + FN)
    print('Fa')
    false_positive_rate = FP / float(FP + TN)
    print('Cl')
    specificity = TN / (TN + FP)
    print('Cl')

# print(c
print('Cl')  
    )
```

线性核函数



```
# 线性
def svm_linear():
    print("##### linear kernel #####")

    kernel = 'linear'
    svm_train(kernel=kernel)

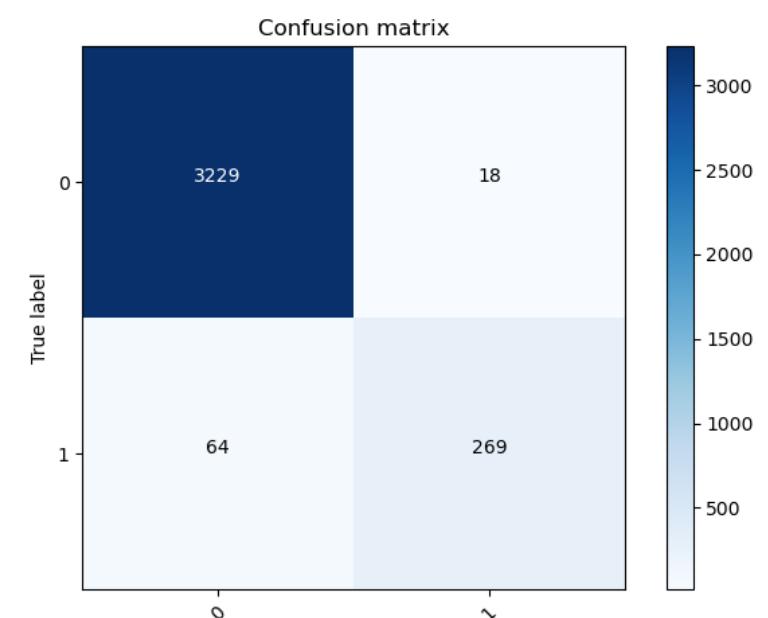
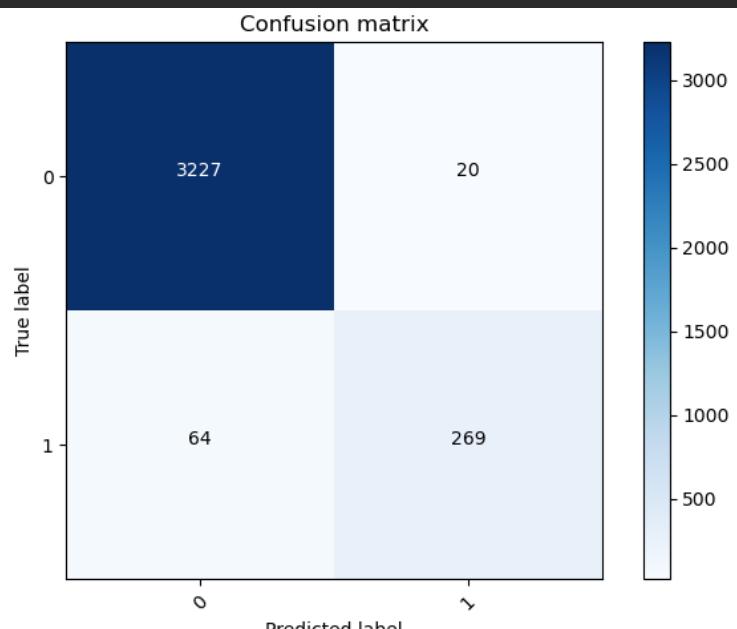
    svm_train(kernel=kernel, C=1.0)

    svm_train(kernel=kernel, C=100.0)

    svm_train(kernel=kernel, C=1000.0)
```

结果分析

```
##### linear kernel #####
kernel:linear, C:1.0, gamma:auto hyper parameters
Train Model accuracy score: 0.9804
Train Model accuracy score: 0.9771
Train Model cross-validation scores:
[0.97835196 0.98219274 0.98218652 0.97589941 0.9804401 ]
Test Model cross-validation scores :
[0.98603352 0.97765363 0.97206704 0.97346369 0.97346369]
Train Model Average stratified cross-validation scores 0.9798
Test Model Average stratified cross-validation scores: 0.9765
True Positives(TP) = 3229
True Negatives(TN) = 269
False Positives(FP) = 18
```

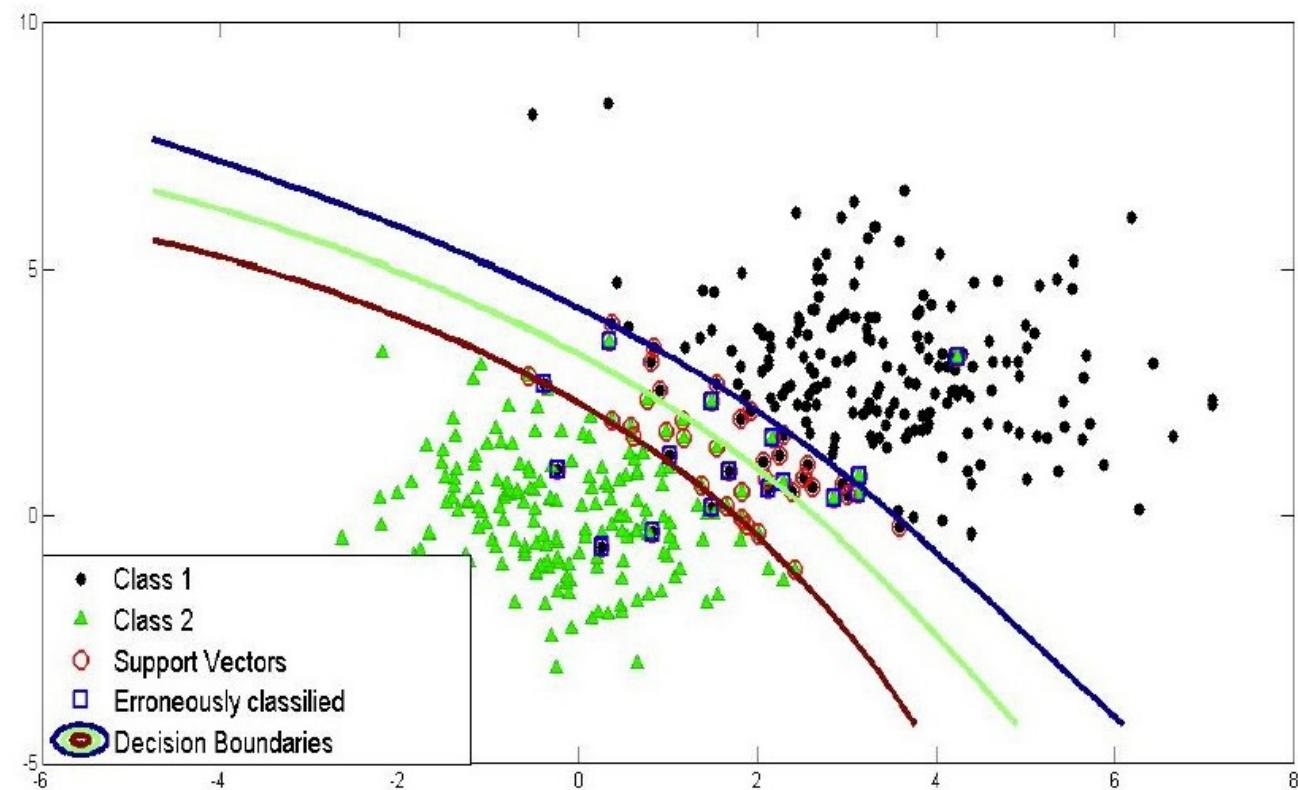


```
kernel:linear, C:100.0, gamma:auto hyper parameters
Train Model accuracy score: 0.9803
Train Model accuracy score: 0.9765
Train Model cross-validation scores:
[0.97835196 0.9825419 0.98218652 0.97694726 0.98113867]
Test Model cross-validation scores :
[0.98463687 0.97765363 0.97206704 0.97346369 0.97486034]
Train Model Average stratified cross-validation scores 0.9802
Test Model Average stratified cross-validation scores: 0.9765
True Positives(TP) = 3227
True Negatives(TN) = 269
False Positives(FP) = 20
False Negatives(FN) = 64
```

RBF 径向基函数

Radial Basis Function kernel

$$k(x, y) = \exp\left(-\frac{\|x - y\|^2}{2\sigma^2}\right)$$



```
# 径向核函数
def svm_rbf():
    print("##### rbf kernel #####")
    kernel = 'rbf'
    svm_train(kernel=kernel)

    svm_train(kernel=kernel, gamma=0.1)

    svm_train(kernel=kernel, gamma=0.5)

    svm_train(kernel=kernel, gamma=0.9)

    svm_train(kernel=kernel, gamma=1)

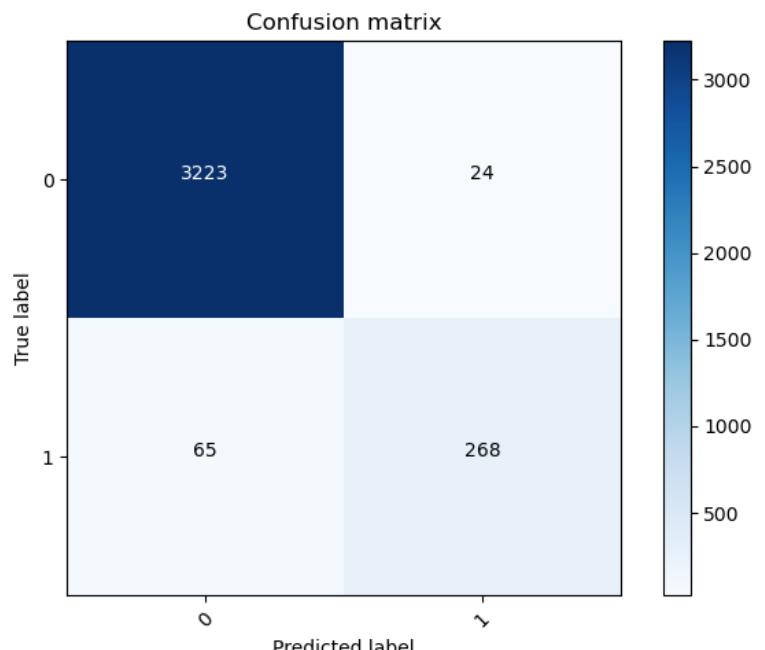
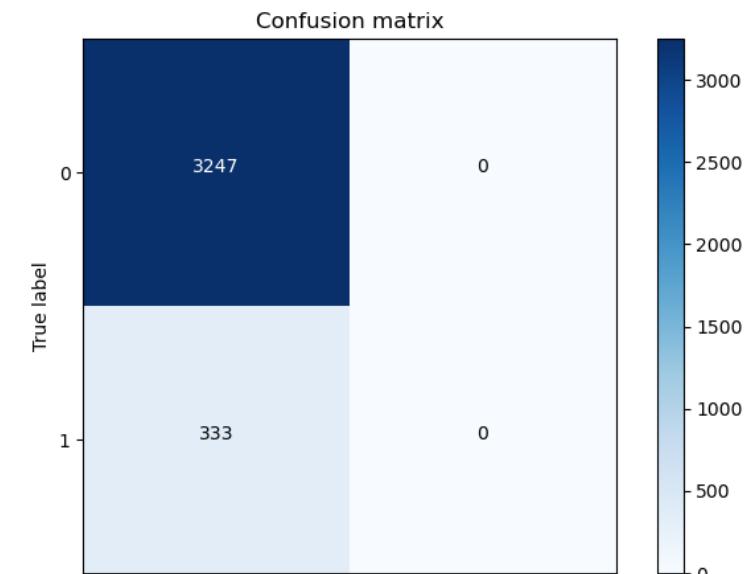
    svm_train(kernel=kernel, gamma=100)

    svm_train(kernel=kernel, gamma=1000)
```

RBF可以作为一个通用的核函数使用，经常在我们对数据了解不多的时候使用，也是svm的默认核函数。

结果分析

```
##### rbf kernel #####
kernel:rbf, C:1.0, gamma:auto hyper parameters
Train Model accuracy score: 0.9802
Train Model accuracy score: 0.9751
Train Model cross-validation scores:
[0.97590782 0.98114525 0.98218652 0.97555012 0.98078938]
Test Model cross-validation scores :
[0.98044693 0.97625698 0.97067039 0.97346369 0.97206704]
Train Model Average stratified cross-validation scores 0.9791
Test Model Average stratified cross-validation scores: 0.9746
```

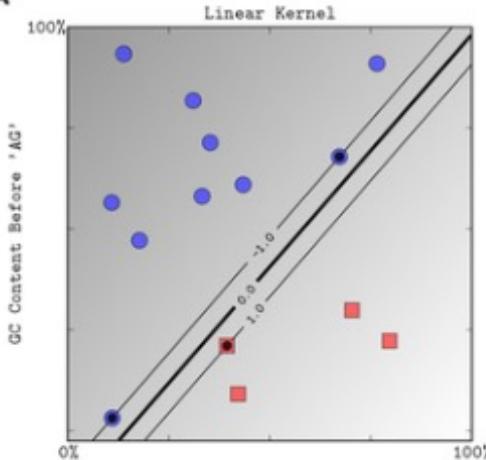


```
kernel:rbf, C:1.0, gamma:1000 hyper parameters
Train Model accuracy score: 1.0000
Train Model accuracy score: 0.9070
Train Model cross-validation scores:
[0.9127095 0.90572626 0.91372686 0.89451624 0.9172197 ]
Test Model cross-validation scores :
[0.89804469 0.92178771 0.91201117 0.89944134 0.90363128]
Train Model Average stratified cross-validation scores 0.9088
Test Model Average stratified cross-validation scores: 0.9070
True Positives(TP) = 3247
True Negatives(TN) = 0
False Positives(FP) = 0
False Negatives(FN) = 333
```

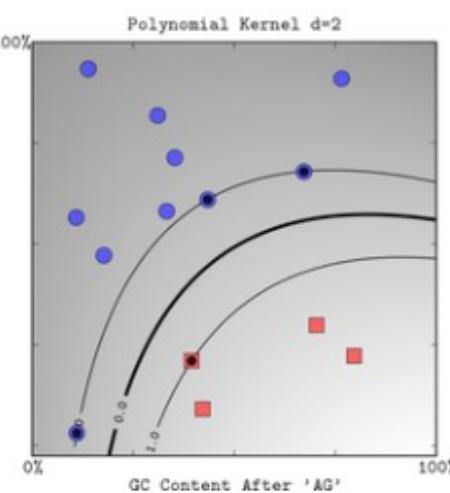
多项式核函数

Polynomial Kernel

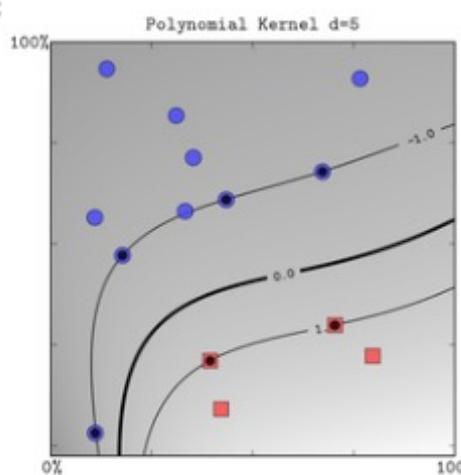
A



B

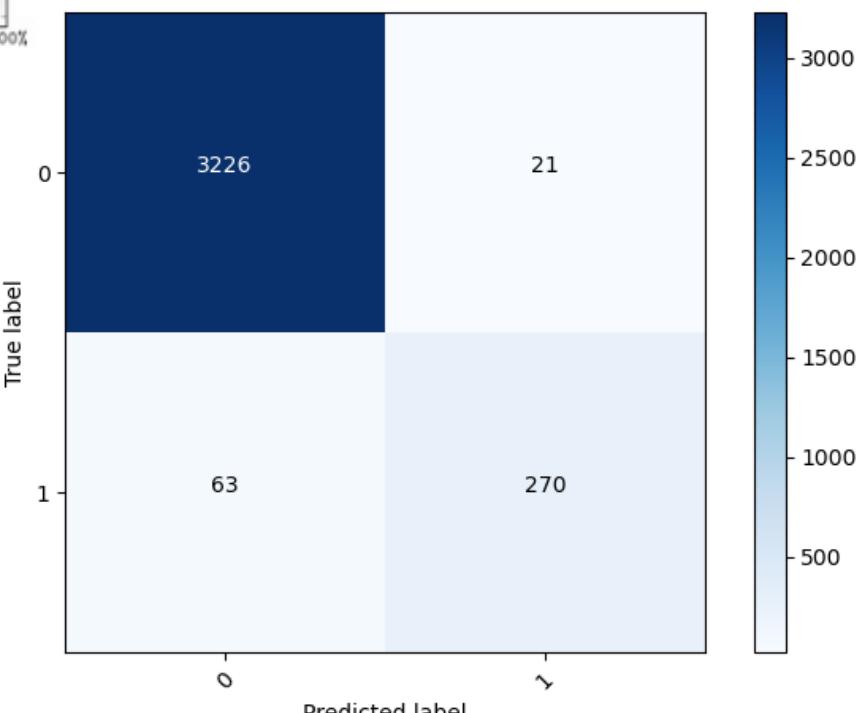


C



$$K(x_i, x_j) = (\gamma x_i^T x_j + r)^d, \gamma > 0$$

Confusion matrix



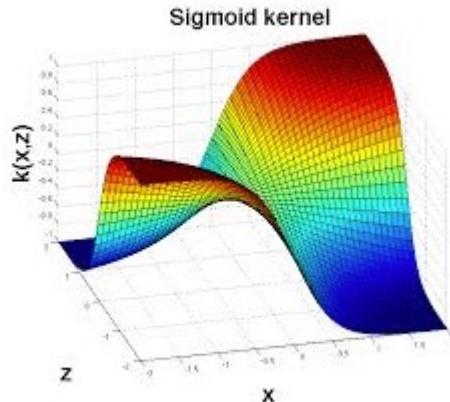
```
def svm_polynomial():
    print("##### polynomial kernel #####")
    kernel = 'poly'
    svm_train(kernel, C=1.0)

    svm_train(kernel, C=100.0)

    svm_train(kernel, C=1000.0)
```

Sigmoid核函数

sigmoid kernel : $k(x, y) = \tanh(\alpha x^T y + c)$

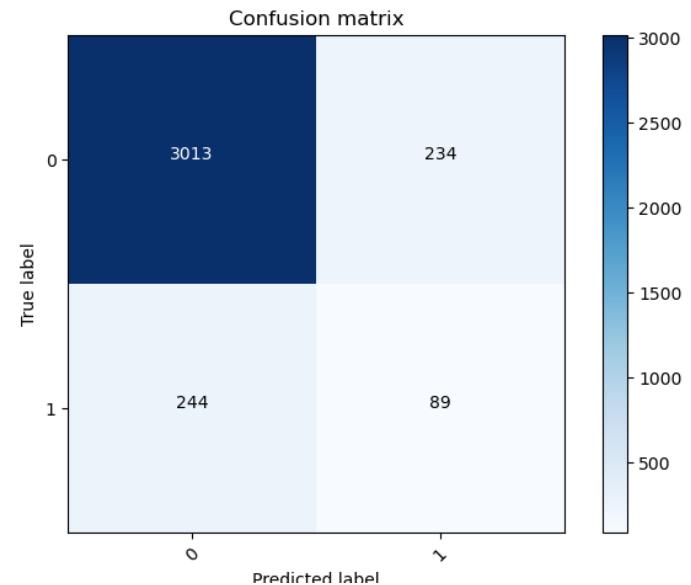


```
def svm_sigmoid():
    print("##### polynomial kernel #####")
    kernel = 'sigmoid'
    svm_train(kernel, C=1.0)

     svm_train(kernel, C=100.0)

    svm_train(kernel, C=1000.0)
```

```
kernel:sigmoid, C:10000.0, gamma:auto hyper parameters
Train Model accuracy score: 0.8744
Train Model accuracy score: 0.8668
Train Model cross-validation scores:
[0.87604749 0.86941341 0.88438701 0.86866923 0.87041565]
Test Model cross-validation scores :
[0.85614525 0.85893855 0.87011173 0.86731844 0.87011173]
Train Model Average stratified cross-validation scores 0.8738
Test Model Average stratified cross-validation scores: 0.8645
True Positives(TP) = 3013
True Negatives(TN) = 90
False Positives(FP) = 234
False Negatives(FN) = 243
```



Grid Search查找最优算法

```
def grid_search():
    svc = SVC()
    # declare parameters for hyperparameter tuning
    parameters = [{ 'C': [1, 10, 100, 1000], 'kernel': ['linear']},
                   {'C': [1, 10, 100, 1000], 'kernel': ['rbf'], 'gamma':
                     [0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9]},
                   {'C': [1, 10, 100, 1000], 'kernel': ['poly'], 'degree': [2, 3, 4],
                     'gamma': [0.01, 0.02, 0.03, 0.04, 0.05]}
                  ]
    with parallel_backend('threading', n_jobs=8): 8线程
        grid_search = GridSearchCV(estimator=svc,
                                   param_grid=parameters,
```

GridSearch CV best score : 0.9804

Parameters that give the best results : {'C': 10, 'kernel': 'linear'}

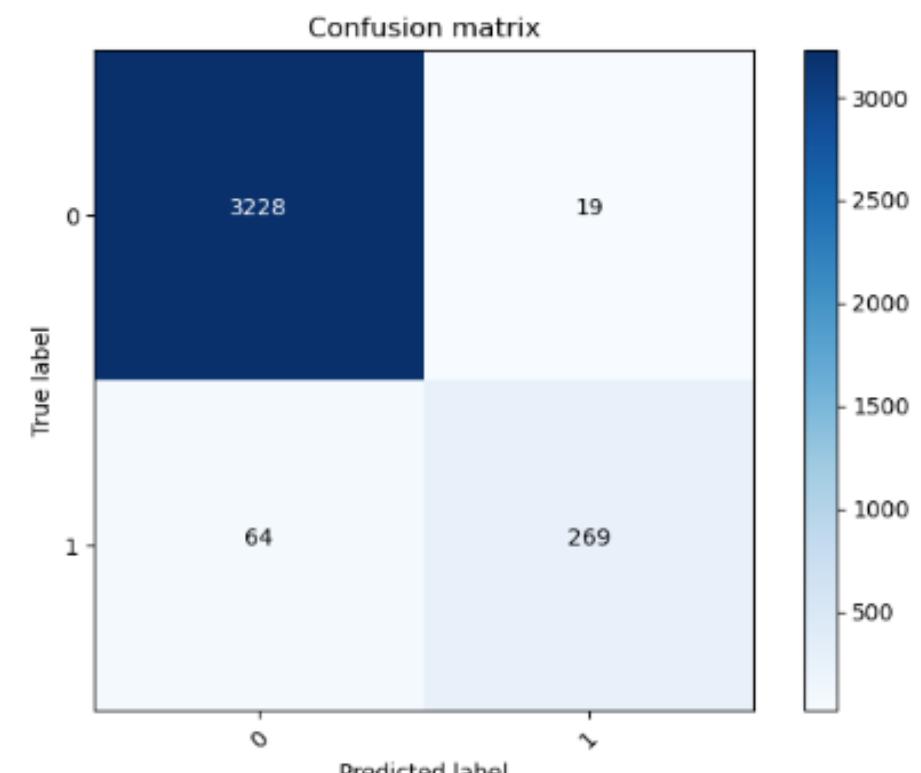
Estimator that was chosen by the search : SVC(C=10, kernel='linear')

GridSearch CV score on test set: 0.9768

```
    print('Parameters that give the best results :', (grid_search.best_params_))
    # print estimator that was chosen by the GridSearch
    print('Estimator that was chosen by the search :', (grid_search.best_estimator_))
    print('GridSearch CV score on test set: {0:0.4f}'.format(grid_search.score(svm.x_test, svm.y_test)))
```

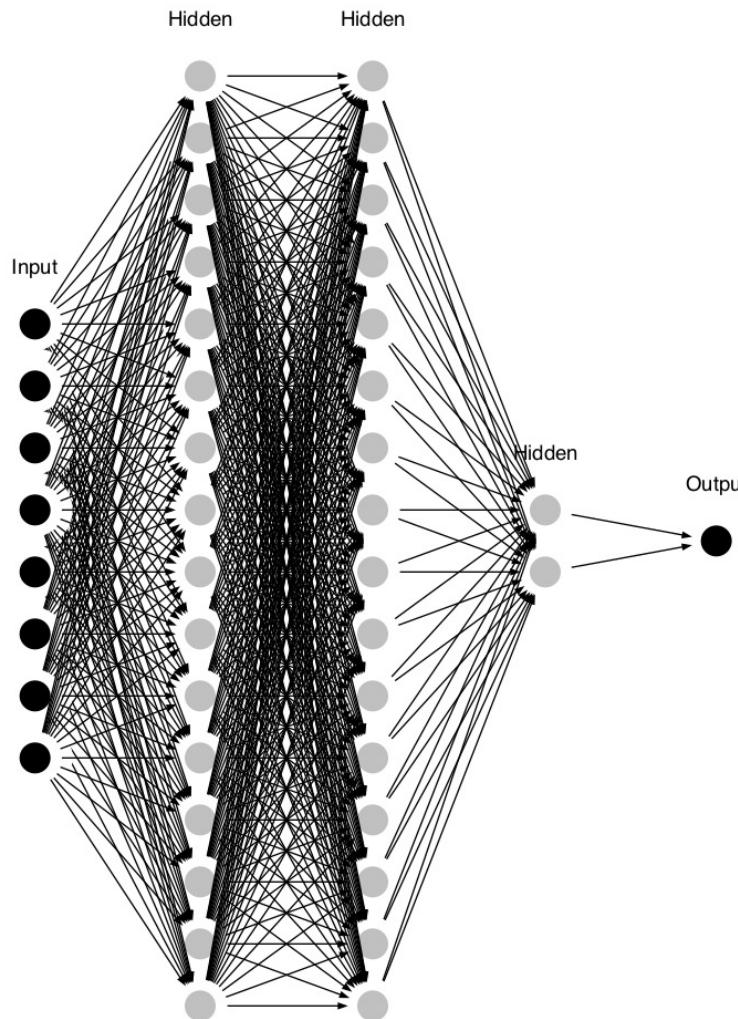
SVM最优结果分析

```
##### linear kernel #####
kernel:linear, C:10, gamma:auto hyper parameters
Train Model accuracy score: 0.9803
Train Model accuracy score: 0.9768
Train Model cross-validation scores:
[0.97835196 0.9825419 0.98218652 0.97659797 0.98113867]
Test Model cross-validation scores :
[0.98463687 0.97765363 0.97206704 0.97346369 0.97486034]
Train Model Average stratified cross-validation scores 0.9802
Test Model Average stratified cross-validation scores: 0.9765
Confusion matrix [[3228 19]
 [ 64 269]]
True Positives(TP) = 3228
True Negatives(TN) = 269
False Positives(FP) = 19
False Negatives(FN) = 64
Classification accuracy : 0.9768
Classification error : 0.0232
Precision : 0.9941
Recall or Sensitivity : 0.9806
False Positive Rate : 0.0660
Specificity : 0.9340
```



在SVM分类中使用线性核函数，C=10时可以达到最好的效果（原始数据中负样本率是90.7%）：
分类精度为97.68%，查准率是99.41%，召回率是98.06%，误判率是6.6%，特异度93.4%。

深度神经网络



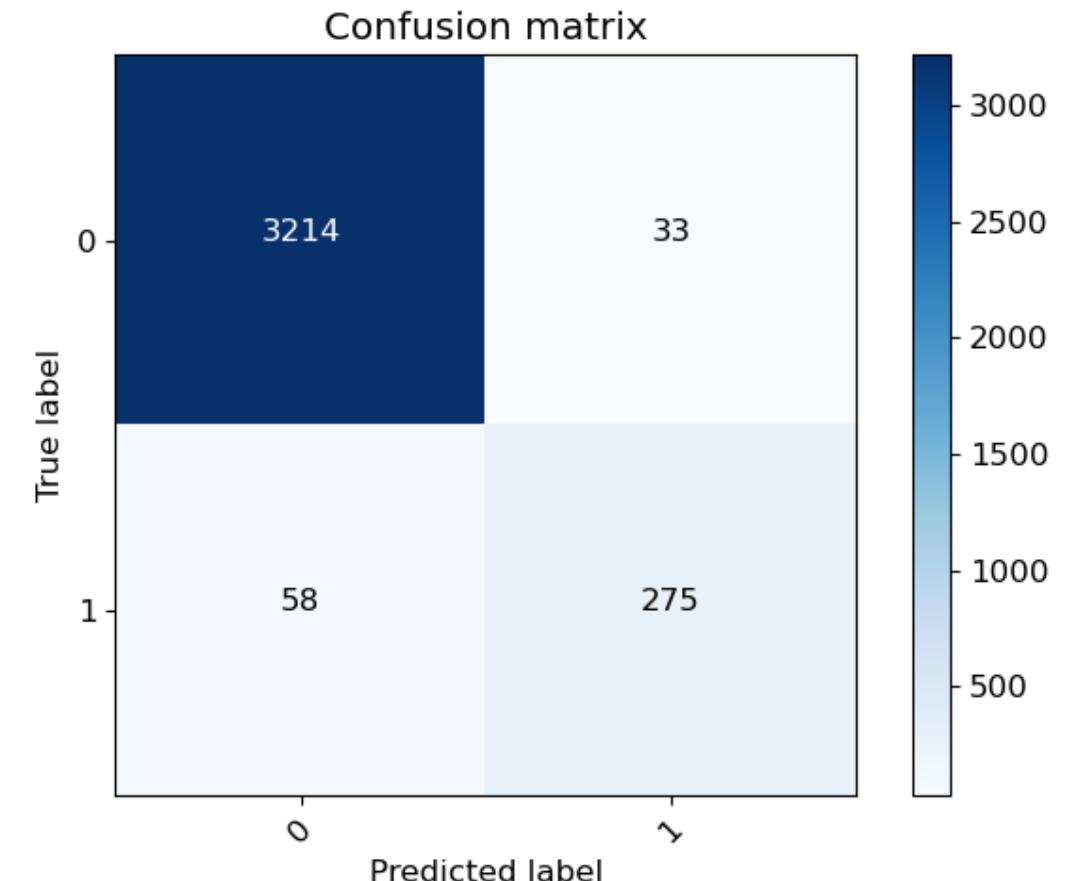
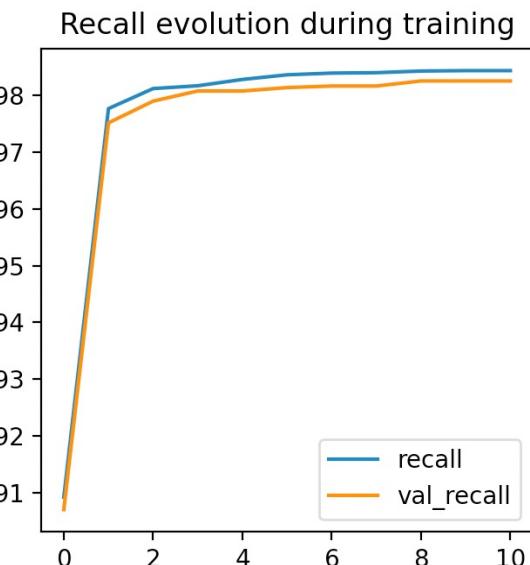
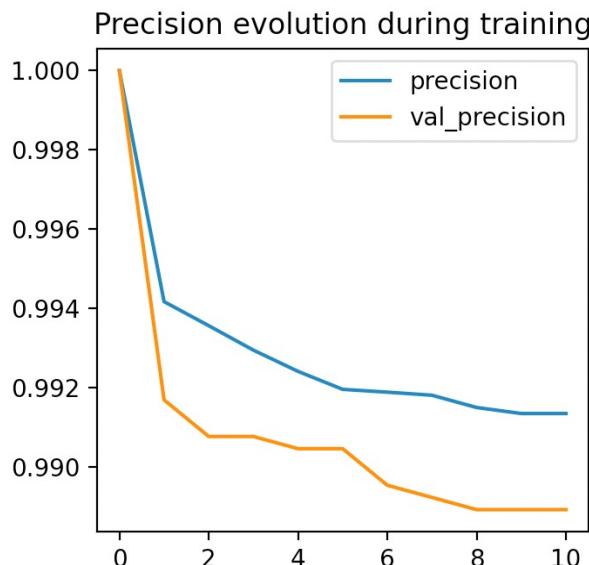
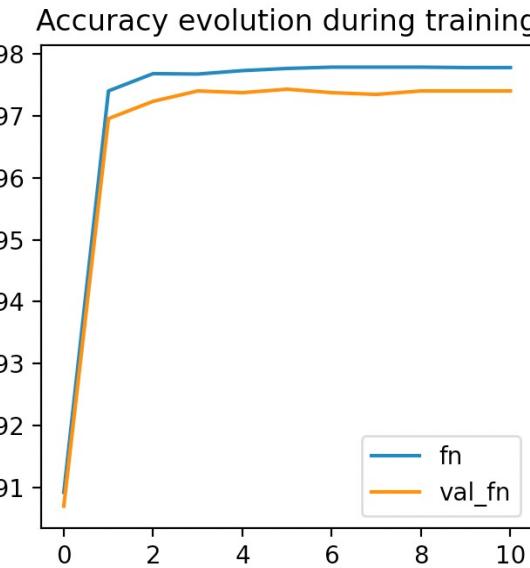
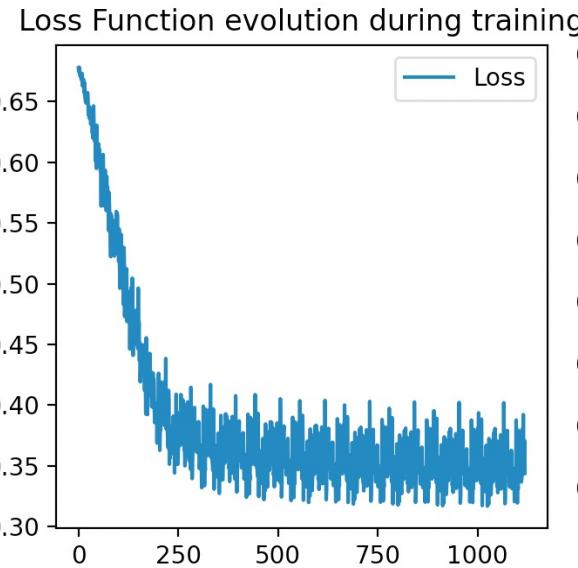
```
class NeuralNetwork(nn.Module):
    def __init__(self, num_classes):
        super(NeuralNetwork, self).__init__()
        self.linear_relu_stack = nn.Sequential(
            nn.Linear(8, 16),
            nn.ReLU(),
            nn.Linear(16, 16),
            nn.ReLU(),
            nn.Linear(16, num_classes),
            nn.Sigmoid()
        )

    def forward(self, x):
        outputs = self.linear_relu_stack(x)
        return outputs
```

模型参数

Layer (type:depth-idx)	Output Shape	Param #	
NeuralNetwork	[1, 2]	--	
└ Sequential: 1-1	[1, 2]	--	$144 = 16 * 8 + 16$
└ Linear: 2-1	[1, 16]	144	
└ ReLU: 2-2	[1, 16]	--	$271 = 16 * 16 + 16$
└ Linear: 2-3	[1, 16]	272	
└ ReLU: 2-4	[1, 16]	--	
└ Linear: 2-5	[1, 2]	34	$34 = 2 * 16 + 2$
└ Sigmoid: 2-6	[1, 2]	--	
Total params: 450			
Trainable params: 450			
Non-trainable params: 0			
Total mult-adds (M): 0.00			

实验结果



残差网络

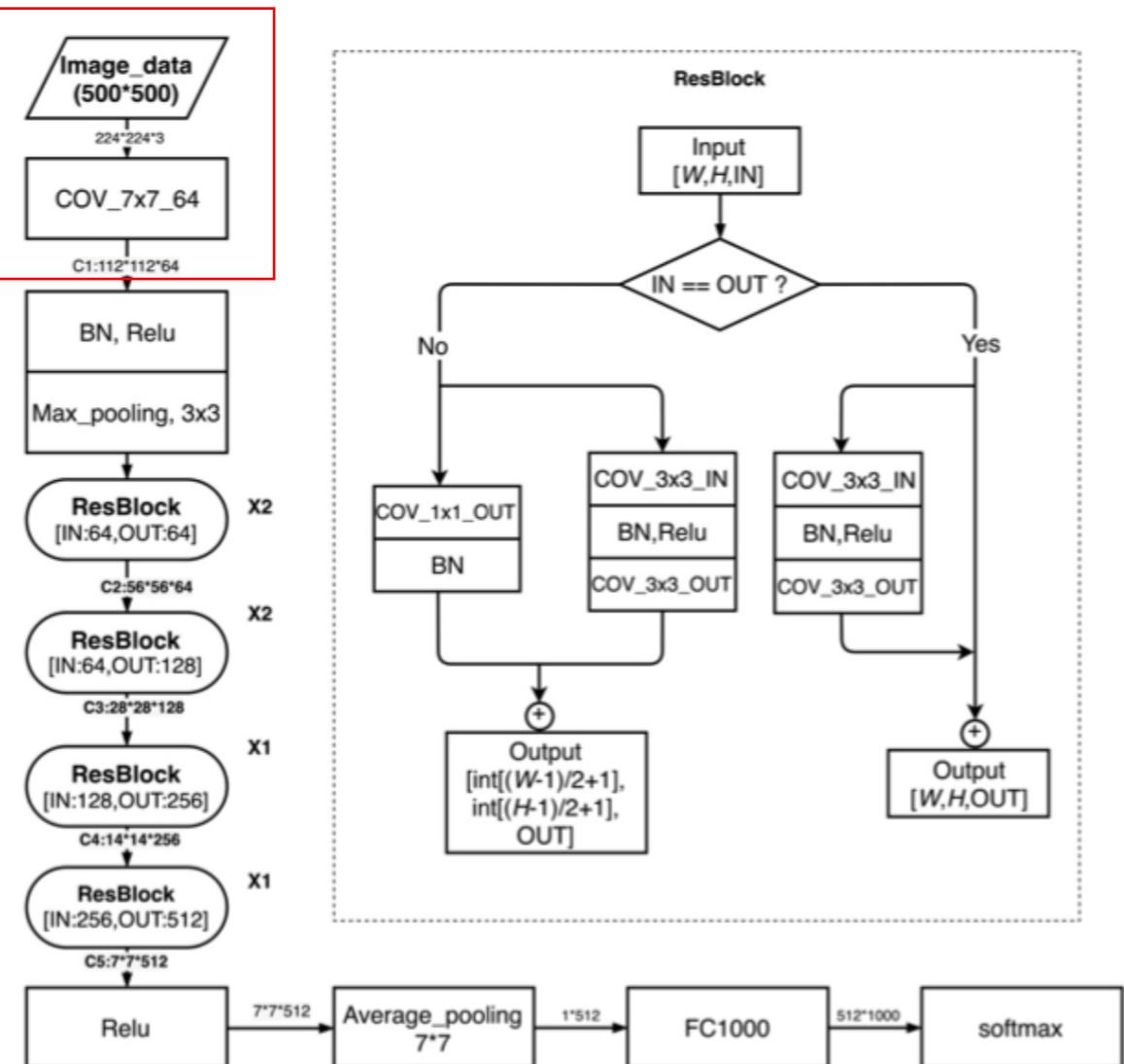


图 3 模型架构^[30]

Layer (type:depth-idx)	Output Shape	Param #
ResNet	[1, 2]	--
└ Sequential: 1-1	[1, 8, 1]	--
└ ResidualBlock: 2-1	[1, 8, 1]	--
└ Sequential: 3-1	[1, 8, 1]	416
└ Sequential: 3-2	[1, 8, 1]	--
└ ResidualBlock: 2-2	[1, 8, 1]	--
└ Sequential: 3-3	[1, 8, 1]	416
└ Sequential: 3-4	[1, 8, 1]	--
└ Sequential: 1-2	[1, 16, 1]	--
└ ResidualBlock: 2-3	[1, 16, 1]	--
└ Sequential: 3-5	[1, 16, 1]	1,216
└ Sequential: 3-6	[1, 16, 1]	160
└ ResidualBlock: 2-4	[1, 16, 1]	--
└ Sequential: 3-7	[1, 16, 1]	1,600
└ Sequential: 3-8	[1, 16, 1]	--
└ Sequential: 1-3	[1, 16, 1]	--
└ ResidualBlock: 2-5	[1, 16, 1]	--
└ Sequential: 3-9	[1, 16, 1]	1,600
└ Sequential: 3-10	[1, 16, 1]	288
└ Sequential: 1-4	[1, 16, 1]	--
└ ResidualBlock: 2-6	[1, 16, 1]	--
└ Sequential: 3-11	[1, 16, 1]	1,600
└ Sequential: 3-12	[1, 16, 1]	288
└ Linear: 1-5	[1, 2]	34
Total params:	7,618	
Trainable params:	7,618	
Non-trainable params:	0	
Total mult-adds (M):	0.01	

网络定义

```
class ResidualBlock(nn.Module):
    def __init__(self, inchannel, outchannel, stride=1):
        super(ResidualBlock, self).__init__()
        self.left = nn.Sequential(
            nn.Conv1d(inchannel, outchannel, kernel_size=3,
                      stride=stride, padding=1, bias=False),
            nn.BatchNorm1d(outchannel),
            nn.ReLU(inplace=True),
            nn.Conv1d(outchannel, outchannel, kernel_size=3,
                      stride=1, padding=1, bias=False),
            nn.BatchNorm1d(outchannel)
        )
        self.shortcut = nn.Sequential()
        if stride != 1 or inchannel != outchannel:
            self.shortcut = nn.Sequential(
                nn.Conv1d(inchannel, outchannel, kernel_size=1,
                          stride=stride, bias=False),
                nn.BatchNorm1d(outchannel)
            )
    def forward(self, x):
        out = self.left(x)
        out = out + self.shortcut(x)
        out = F.relu(out)
        return out
```

```
class ResNet(nn.Module):
    def __init__(self, ResidualBlock, num_classes=10):
        super(ResNet, self).__init__()
        self.inchannel = 8
        self.layer1 = self.make_layer(ResidualBlock, 8, 2, stride=1)
        self.layer2 = self.make_layer(ResidualBlock, 16, 2, stride=2)
        self.layer3 = self.make_layer(ResidualBlock, 16, 1, stride=2)
        self.layer4 = self.make_layer(ResidualBlock, 16, 1, stride=2)
        self.fc = nn.Linear(16, num_classes)

    def make_layer(self, block, channels, num_blocks, stride):
        strides = [stride] + [1] * (num_blocks - 1)
        layers = []
        for stride in strides:
            layers.append(block(self.inchannel, channels, stride))
            self.inchannel = channels
        return nn.Sequential(*layers)

    def forward(self, x):
        out = x[:, None, :]
        out = out.permute(0, 2, 1)
        out = self.layer1(out)
        out = self.layer2(out)
        out = self.layer3(out)
        out = self.layer4(out)
        out = F.avg_pool1d(out, 1)
        out = out.view(out.size(0), -1)
        out = self.fc(out)
        return out
```

实验结果

True Positives(TP) = 3232

True Negatives(TN) = 262

False Positives(FP) = 15

False Negatives(FN) = 71

	precision	recall	f1-score	support
--	-----------	--------	----------	---------

0	0.98	1.00	0.99	3247
1	0.95	0.79	0.86	333

accuracy			0.98	3580
----------	--	--	------	------

macro avg	0.96	0.89	0.92	3580
-----------	------	------	------	------

weighted avg	0.98	0.98	0.97	3580
--------------	------	------	------	------

Classification accuracy : 0.9760

Classification error : 0.0240

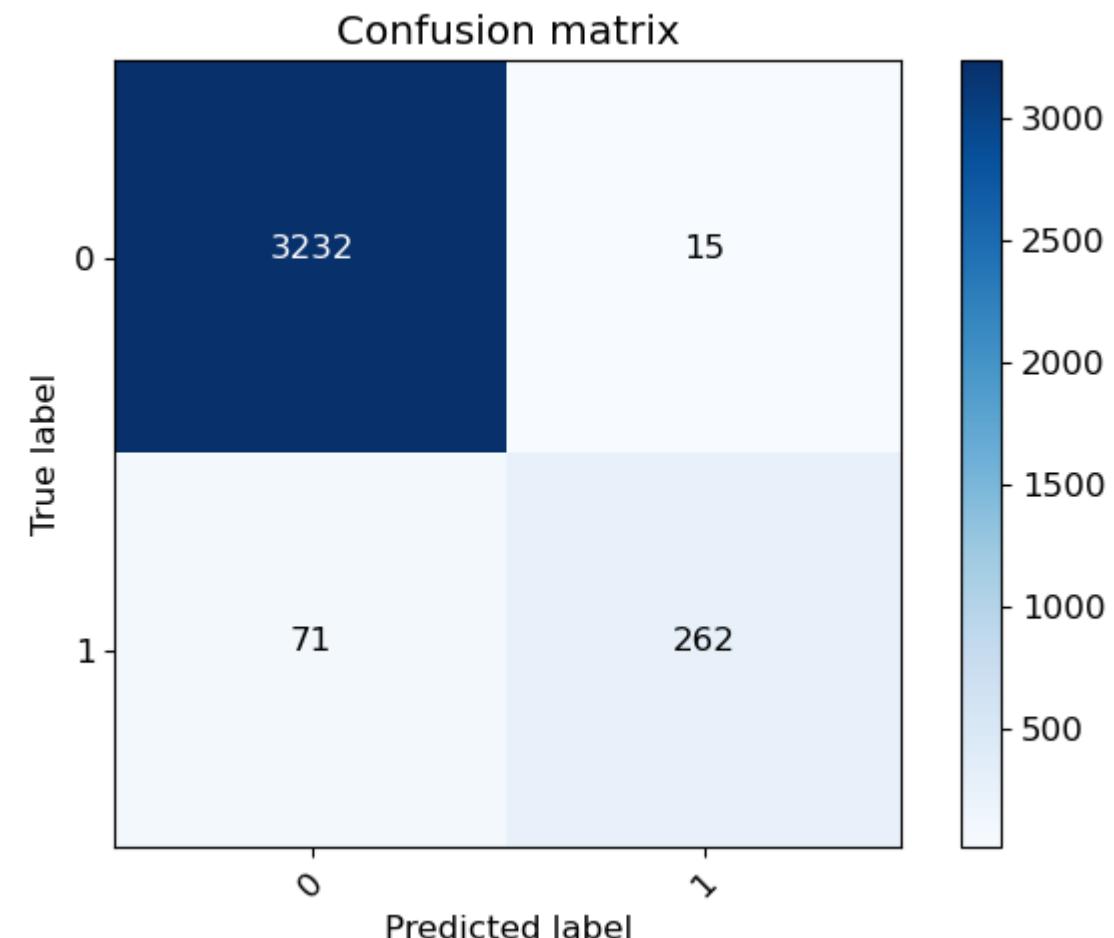
Precision : 0.9954

Recall or Sensitivity : 0.9785

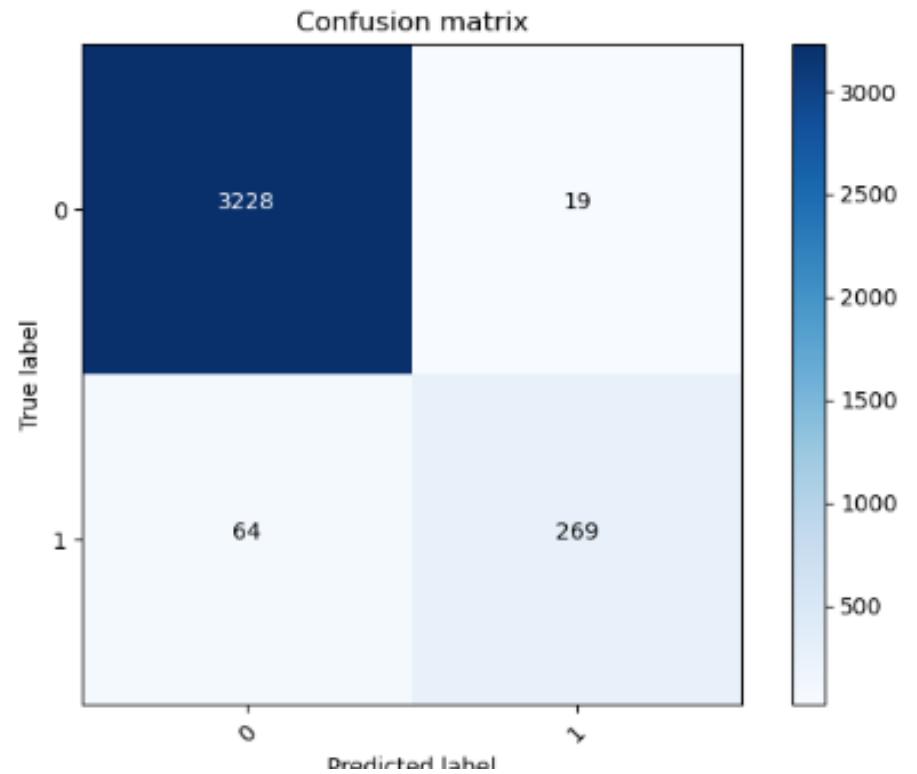
False Positive Rate : 0.0542

Specificity : 0.9458

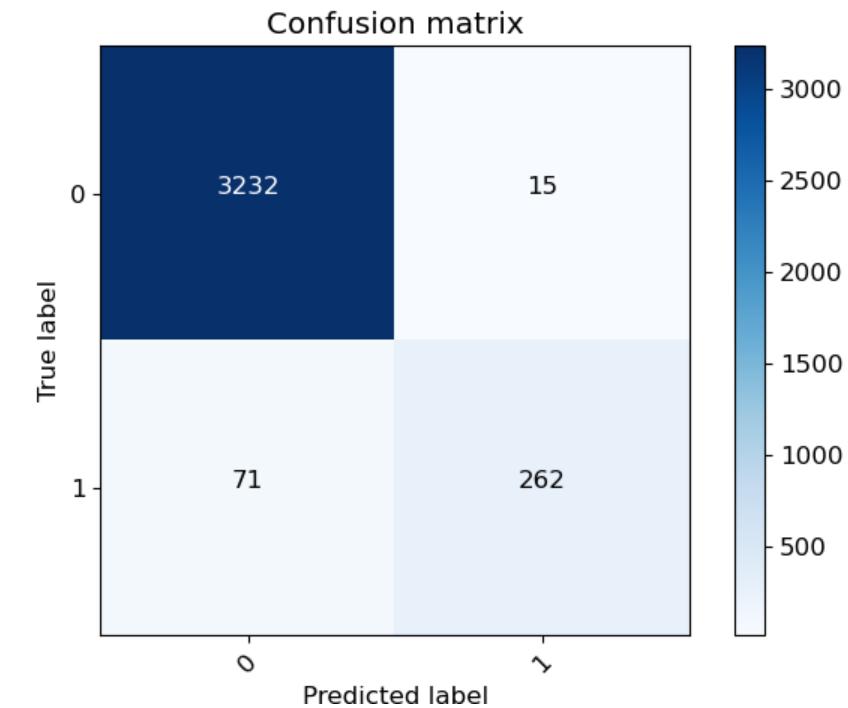
Test's ac is: 97.598%



对比结果



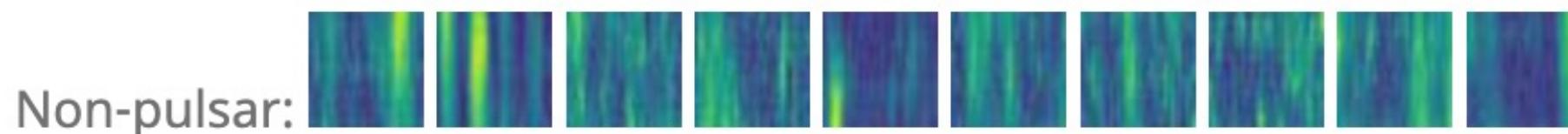
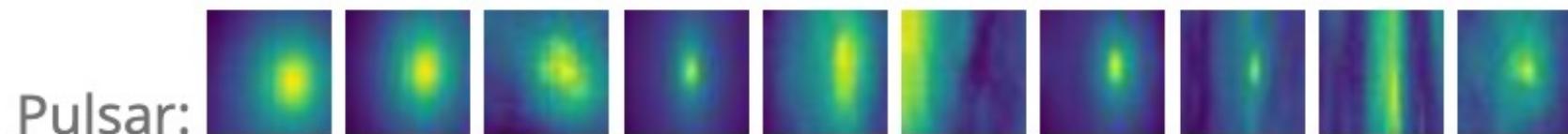
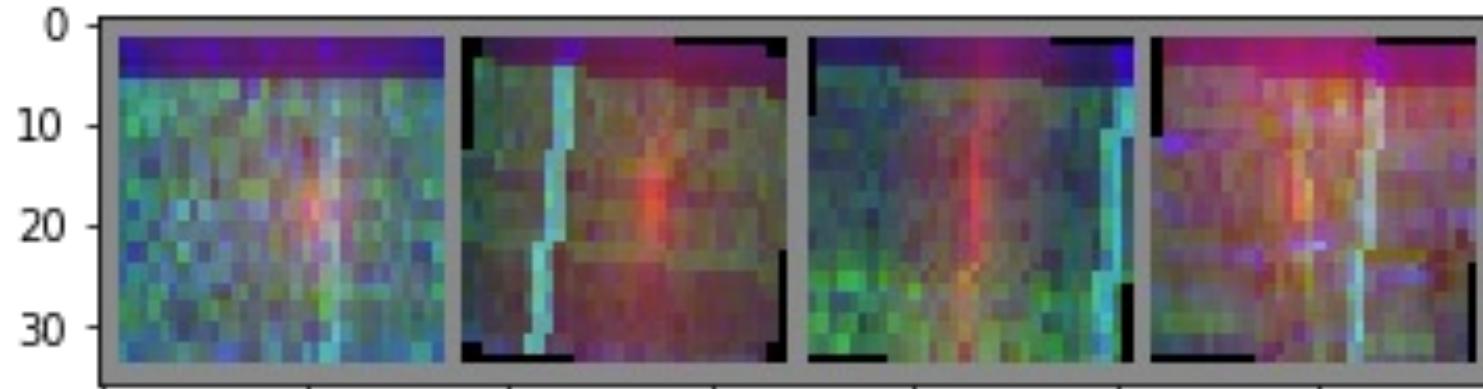
在SVM分类中使用线性核函数，C=10时可以达到最好的效果（原始数据中负样本率是90.7%）：
分类精度为97.68%，查准率是99.41%，召回率是98.06%，误判率是6.6%，特异度93.4%。



在CNN/ResNet分类中，最好的效果（原始数据中负样本率是90.7%）：
分类精度为97.60%，查准率是99.54%，召回率是97.85%，误判率是5.42%，特异度94.58%。

And More

如果直接处理图像数据呢？



图片数据集: <https://as595.github.io/HTRU1/>

处理图片的残差网络

```
class ResidualBlock(nn.Module):
    def __init__(self, inchannel, outchannel, stride=1):
        super(ResidualBlock, self).__init__()
        # 这里定义了残差块内连续的2个卷积层
        self.left = nn.Sequential(
            nn.Conv2d(inchannel, outchannel, kernel_size=3, stride=stride, padding=1, bias=False),
            nn.BatchNorm2d(outchannel),
            nn.ReLU(inplace=True),
            nn.Conv2d(outchannel, outchannel, kernel_size=3, stride=1, padding=1, bias=False),
            nn.BatchNorm2d(outchannel)
        )
        self.shortcut = nn.Sequential()
        if stride != 1 or inchannel != outchannel:
            # shortcut, 这里为了跟2个卷积层的结果结构一致, 要做处理
            self.shortcut = nn.Sequential(
                nn.Conv2d(inchannel, outchannel, kernel_size=1, stride=stride, bias=False),
                nn.BatchNorm2d(outchannel)
            )
    def forward(self, x):
        out = self.left(x)
        # 将2个卷积层的输出跟处理过的x相加, 实现ResNet的基本结构
        out = out + self.shortcut(x)
        out = F.relu(out)
        return out
```

网络参数

Layer (type:depth-idx)	Output Shape	Param #
<hr/>		
ResNet	[1, 2]	--
└ Sequential: 1-1	[1, 64, 56, 56]	--
└ Conv2d: 2-1	[1, 64, 56, 56]	1,728
└ BatchNorm2d: 2-2	[1, 64, 56, 56]	128
└ ReLU: 2-3	[1, 64, 56, 56]	--
└ Sequential: 1-2	[1, 64, 56, 56]	--
└ ResidualBlock: 2-4	[1, 64, 56, 56]	--
└ Sequential: 3-1	[1, 64, 56, 56]	73,984
└ Sequential: 3-2	[1, 64, 56, 56]	--
└ ResidualBlock: 2-5	[1, 64, 56, 56]	--
└ Sequential: 3-3	[1, 64, 56, 56]	73,984
└ Sequential: 3-4	[1, 64, 56, 56]	--
└ Sequential: 1-3	[1, 64, 28, 28]	--
└ ResidualBlock: 2-6	[1, 64, 28, 28]	--
└ Sequential: 3-5	[1, 64, 28, 28]	73,984
└ Sequential: 3-6	[1, 64, 28, 28]	4,224
└ Sequential: 1-4	[1, 128, 14, 14]	--
└ ResidualBlock: 2-8	[1, 128, 14, 14]	--
└ Sequential: 3-9	[1, 128, 14, 14]	221,696
└ Sequential: 3-10	[1, 128, 14, 14]	8,448
└ Sequential: 1-5	[1, 256, 7, 7]	--
└ ResidualBlock: 2-9	[1, 256, 7, 7]	--
└ Sequential: 3-11	[1, 256, 7, 7]	885,760
└ Sequential: 3-12	[1, 256, 7, 7]	33,280
└ Linear: 1-6	[1, 2]	514
<hr/>		

Total params: 1,451,714

Trainable params: 1,451,714

Non-trainable params: 0

Total mult-adds (M): 676.58

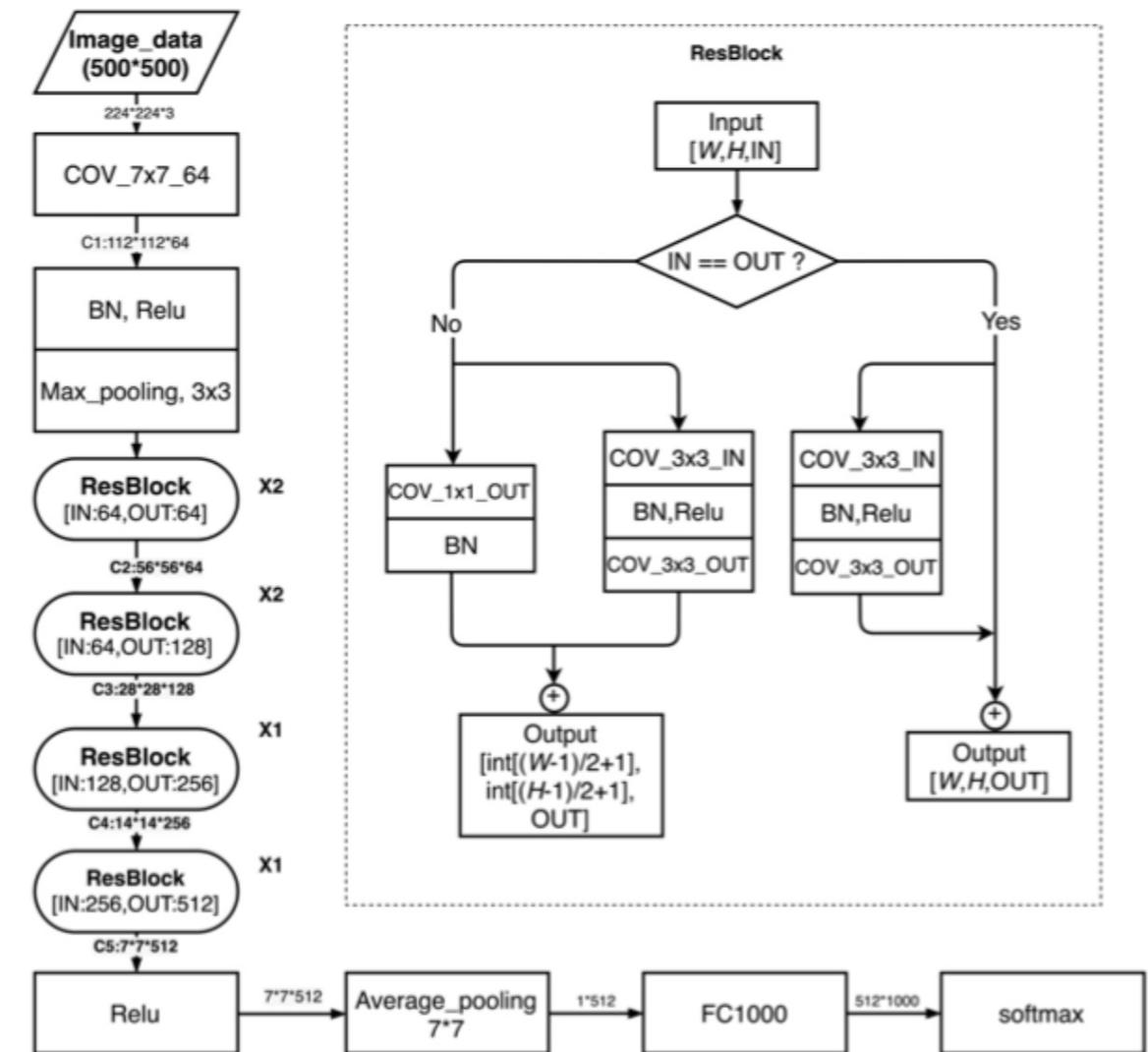
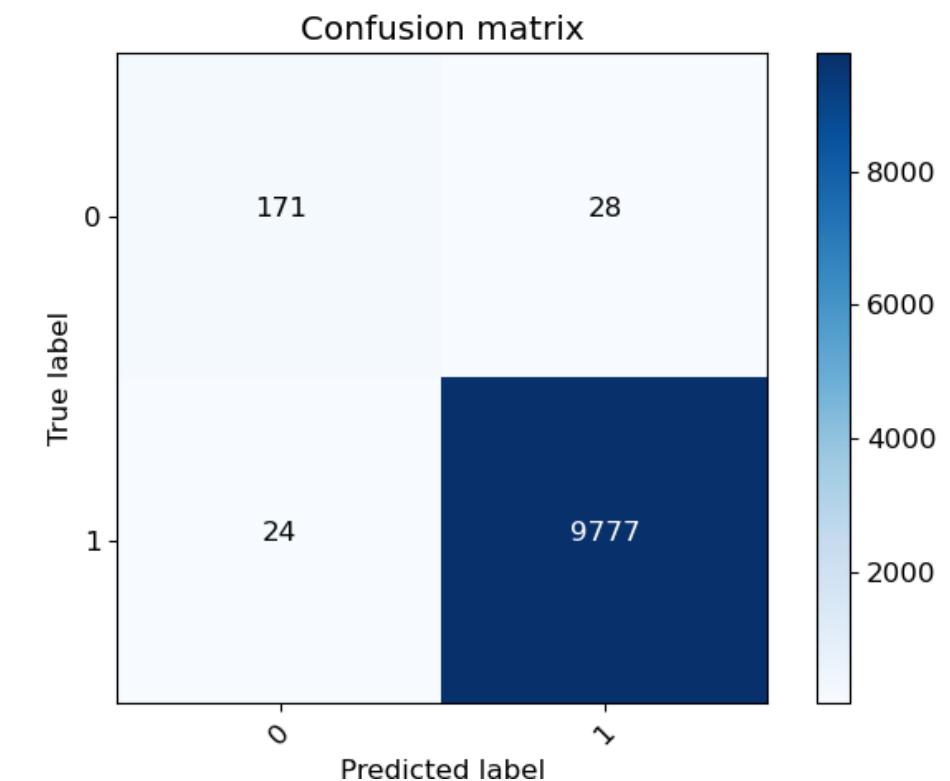
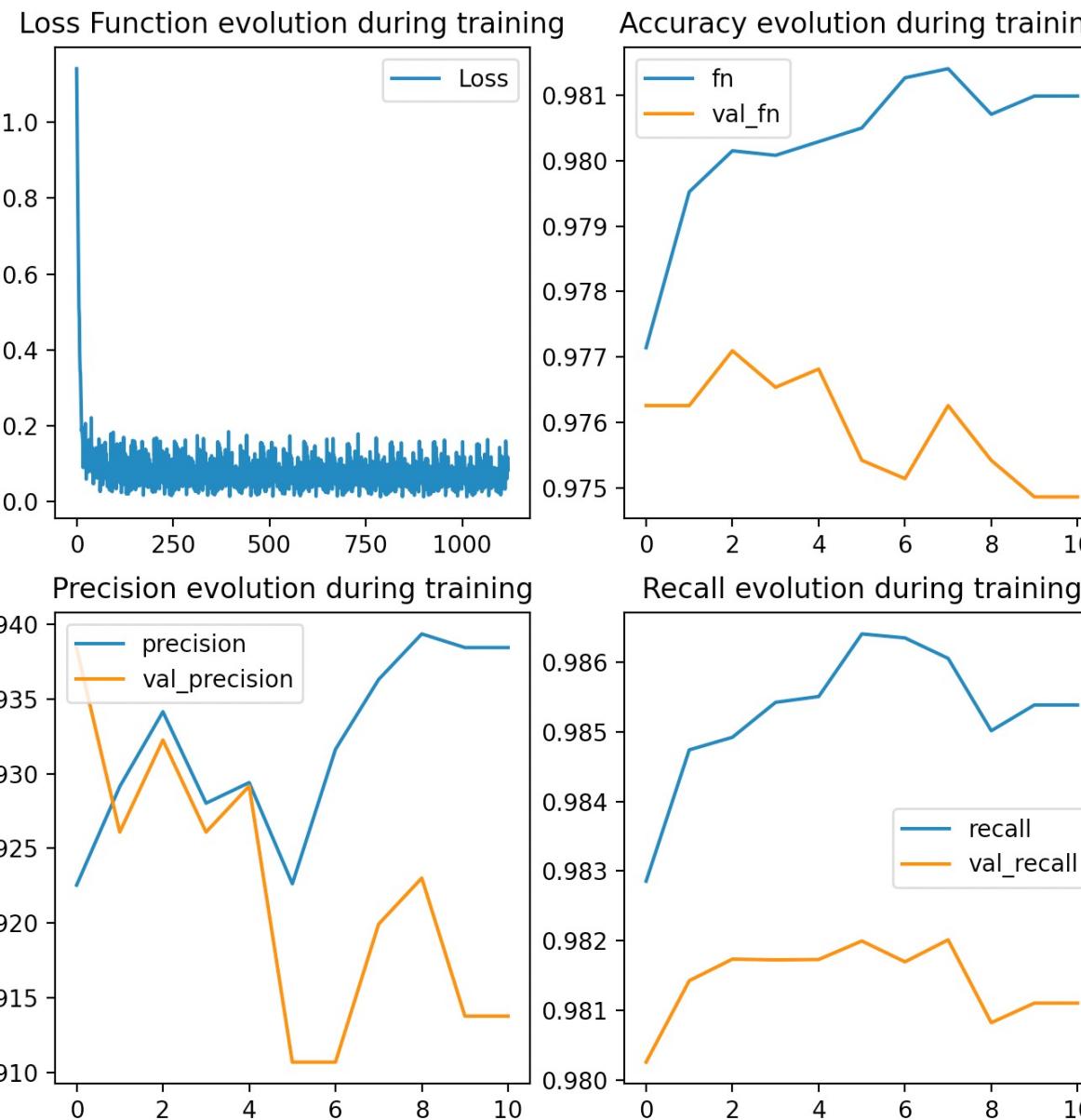


图 3 模型架构^[30]

实验结果



在图片ResNet分类中，2轮训练后的效果（原始数据中负样本率是90.7%）：
分类精度为99.48%，查准率是85.93%，召回率是87.69%，误判率是0.29%，特异度99.71%。

总结

SVM分类办法：

优点：

1. 逻辑清晰，实现简单，内部逻辑解释性强
2. 训练、测试时间短，资源消耗少
3. 精确度相对比较高

缺点：

1. 针对不同的数据集需要多次调整比较不同参数的效果
2. 算法效果达到最好后难以继续提升
3. 无法很好地处理图片数据

深度神经网络分类办法：

优点：

1. 准确度高，可探索改进空间大
2. 算法复用及泛化能力强
3. 可通过卷积方式有效处理图片数据

缺点：

1. 逻辑模糊，实现复杂，内部逻辑解释性差
2. 训练、测试时间长，资源消耗多

参考链接

- [SVM Classifier Tutorial](#)
- [天眼科学目标：脉冲星的观测与研究意义](#)
- [脉冲星候选样本分类方法综述：中国科学院 天文大数据中心](#)
- [脉冲星数据比对分析和可视化系统设计与实现](#)
- [Undersampling and oversampling imbalanced data](#)
- [HTRU1 Pulsar Star](#)
- [HTRU2 Pulsar Star](#)
- [ResNet](#)