

Object Oriented Scientific Programming in C++ (WI4771TU)

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Numerical Analysis

Overview

- Last lecture we started with template meta programming
 - Implement type-independent functionality
 - Class templates/function templates
 - Generic attributes being able to hold arbitrary data type
 - Generic member function realizing the default behaviour
 - Implement specialised variants of member functions to support special behaviour, e.g., dot product for complex types
 - Instantiate class with concrete types (double, float, etc.)

Overview, cont'd

- Today, advanced template meta programming
 - Template specialisation of complete class or individual functions
 - Partial template specialisation of class templates
 - Type traits
 - SFINAE paradigm

Template specialisation

- Type-independent implementation

```
template<typename T, typename I>
class Demo {
public:
    static void info() {
        std::cout << „Generic info“ << std::endl; }
    static void test() {
        std::cout << „Generic test“ << std::endl; }
};
```

- This implementation is used whenever there is no (partial) specialisation of the class Demo and/or its functions

Class template specialisation

- Task: implement a specialisation of the **entire class** for `T=float` and `I=long`
- Note that template meta programming does not imply inheritance; that is, all attributes/functions that you want to have in a specialised class have to be implemented
- Think of class specialisation as implementing a new independent class `Demo<float,long>` that just has the same name as the generic class `Demo<T,I>`

Class template specialisation, cont'd

- Fully specialised implementation of the entire Demo class

```
template<>
class Demo<float,long> {
public:
    static void info() {
        std::cout << „Fully specialised info“ << std::endl; }
    static void test() {
        std::cout << „Fully specialised test“ << std::endl; }
};
```

- This implementation is used for the special case

Demo<float,long>::info() -> class specialisation

Demo<float,long>::test() -> class specialisation

Class template specialisation, cont'd

- Fully specialised implementation of the entire Demo class but without a function test()

```
template<>
class Demo<float,long> {
public:
    static void info() {
        std::cout << „Fully specialised info“ << std::endl; }
};
```

- This implementation does not provide a function test() and yields a compiler error if the function is used

```
Demo<float,long>::info() -> class specialisation
Demo<float,long>::test() // compiler error
```

Class-function template specialisation

- Task: implement a specialisation of **function info()** for `T=float` and `I=long`
- Since we only implement a specialisation for the individual function `info()`, the implementation of function `test()` from the non-specialised class `Demo` remains available
- Think of class function specialisation as superseding individual member functions by specialised versions

Class-function template specialisation, cont'd

- Fully specialised implementation of function info()

```
template<>
void Demo<double,long>::info() {
    std::cout << „Fully specialised info“ << std::endl; }
}
```

- This implementation provides the specialisation of function info() and the generic implementation of function test()

```
Demo<double,long>::info() -> class-function specialisation
Demo<double,long>::test() -> generic
```

Class template partial specialisation

- Task: implement a specialisation of **entire class** for $T=\text{float}$ and arbitrary I value

Class template partial specialisation, cont'd

- Partially specialised implementation of the Demo class

```
template<typename I>
class Demo<double,I> {
public:
    static void info() {
        std::cout << „Partially specialised info“ << std::endl; }
    static void test() {
        std::cout << „Partially specialised test“ << std::endl; }
};
```

- This implementation is used for the special case

```
Demo<double,int>::info() -> partial class specialisation
Demo<double,int>::test() -> partial class specialisation
```

Class-function template partial specialisation

- Task: implement a specialisation of **function info()** for T=float and arbitrary I value
- Partial (class-)function template specialisation is not possible with C++11/14; hence the following code is invalid

```
template<typename I>
void Demo<float,I>::info() {
    std::cout << „Partially specialised info“ << std::endl; }
}
```

- Partial function template specialisation is also not possible

```
template<typename I>
void info<float,I>() {...}
```

Summary template specialisation

- Given a templated class with member functions
 - Entire class can be fully or partially specialised
 - Individual member functions can fully specialised
 - Individual member functions **cannot** be partially specialised
- Entire class specialisation acts like implementing a new individual class that can be accessed by the same name

Quiz

- Remember the specialised dot product for complex-valued vectors from the previous session, will this work?

```
template<typename S>
std::complex<S>
    Vector<std::complex<S> >::
    dot(const Vector<std::complex<S> > other) const {
        std::complex<S> d=0;
        for (auto i=0; i<n; i++)
            d += data[i]*std::conj(other.data[i]);
        return d;
    }
```

SFINAE paradigm

- C++ allows us to write overloaded functions with different input parameter lists, e.g.,

```
static void info() {...}  
static void info(int i) {...}
```

- It is, however, not allowed to overload functions that only differ in the type of their return parameter, e.g.,

```
static void info() {...}  
static int  info() {...}
```

SFINAE paradigm, cont'd

- C++11 standard states:
„If a substitution results in an invalid type or expression, type deduction fails. An invalid type or expression is one that would be ill-formed if written using the substituted arguments. Only invalid types and expressions in the immediate context of the function type and its template parameter types can result in a deduction failure.“
- SFINAE: **S**ubstitution **F**ailure **I**s **N**ot **A**n **E**rror

SFINAE paradigm, cont'd

- C++11 standard rephrased for our purpose:
„If a template substitution leads to invalid code then the compiler must not throw an error but look for another candidate (i.e. the second templated implementation of our function); an error is just thrown if no other candidate can be found so that the function call remains unresolved“

SFINAE paradigm, cont'd

- SFINAE: **S**ubstitution **F**ailure **I**s **N**ot **A**n **E**rro**r**
 - Write multiple implementations of the same function with
 - the **same name** and
 - the **same input parameters**
 - Ensure – via template meta programming – that only one of them results in valid code upon substitution of template parameters and all other candidates yield invalid expressions

Intermezzo: Traits

- Consider the `is_int` function from the assignment

```
template<typename T>
bool is_int(T a) { return false; }
template<>
bool is_int<int>(int a) { return true; }
```
- This function returns true/false depending on the type of the parameter passed via explicit template specialisation
- We look for an even more elegant solution without the need to pass a parameter at all

Intermezzo: Traits, cont'd

- Consider templated structure with specialisation

```
template<typename T>
struct is_int
{
    const static bool value = false;
};
```

```
template<>
struct is_int<int>
{
    const static bool value = true;
};
```

Intermezzo: Traits, cont'd

- Detect if type is int without passing a parameter

```
std::cout << is_int<int>::value << std::endl;  
std::cout << is_int<double>::value << std::endl;
```

- The is_int trait can be used, e.g., in templated functions

```
template<typename T>  
void test(T a)  
{  
    if (is_int<T>::value)  
        std::cout << „Integer :“ << a << std::endl;  
    else  
        std::cout << „Non-Int :“ << a << std::endl;  
}
```

Intermezzo: Type traits

- C++ brings many type traits via `#include <type_traits>`

<code>is_class<T></code>	Type T is of class type
<code>is_const<T></code>	Type T has const qualifier
<code>is_floating_point<T></code>	Type T is floating point (float, double, long)
<code>is_fundamental<T></code>	Type T is of fundamental type (int, double, ...)
<code>is_integral<T></code>	Type T is of integral type (int, long int, ...)
<code>is_pointer<T></code>	Type T is of pointer type

- For a complete list of standard type traits look at:
http://www.cplusplus.com/reference/type_traits/

Intermezzo: Type traits, cont'd

- The aforementioned C++ standard type traits provide

- Member constants:

- `value` (`=true/false`)

- Member types:

- `value_type` (`=bool`)

- `type` (`=true_type/false_type`)

- Member constants/types can be directly accessed

- `is_fundamental<int>::value` `// true`

- `is_fundamental<int>::value_type` `// bool`

Intermezzo: Type traits, cont'd

- C++ provides type traits that **operator on the type**

```
typedef add_const<int>          A // const int
typedef add_const<const int>    B // const int (unchanged)

typedef add_pointer<int>        C // int*
typedef add_pointer<const int>  D // const int*
typedef add_pointer<int&>       E // int*
typedef add_pointer<int*>       F // int**
typedef add_pointer<int(int)>    G // int(*)int
```


Intermezzo: Type traits, cont'd

- C++ provides type traits that **operator on the type**

```
typedef remove_const<int>           A // int (unchanged)
typedef remove_const<const int>     B // int
```

```
typedef remove_pointer<int>         C // int
typedef remove_pointer<int*>        D // int
typedef remove_pointer<int**>      E // int*
typedef remove_pointer<const int>   F // const int
typedef remove_pointer<const int*>  G // const int
typedef remove_pointer<int* const>  H // int
```

Intermezzo: Type traits, cont'd

- C++ provides type traits that **operator on two types**:
Check if two types are ***exactly*** the same (including qualifiers)

```
bool is_same<A,B>::value
```

```
bool is_same<int,int>::value           // true
```

```
bool is_same<int,const int>::value     // false
```

```
bool is_same<remove_const<int>,  
             remove_const<const int> >::value // true
```

Intermezzo: Type traits, cont'd

- C++ provides type traits that **operator on two types**:
Check if type B is derived from type A

```
struct A {};  
struct B : A {};  
bool is_base_of<A,B>::value
```

```
bool is_base_of<A,A>::value // true  
bool is_base_of<A,B>::value // true  
bool is_base_of<B,A>::value // false  
bool is_base_of<B,B>::value // true
```

Intermezzo: Type traits, cont'd

- C++ provides type trait to enable types conditionally

```
template<typename T>
typename std::enable_if<std::is_integral<T>::value,
                        bool>::type
is_odd(T i) { return bool(i%2); }
```

```
int i=2;
cout << „i is odd :“ << is_odd(i) << endl;
```

- If `is_odd` is called with an **integral type** (e.g., `int`) the compiler expands the above templated function as follows

```
bool is_odd(int i) { return bool(i%2); }
```

Intermezzo: Type traits, cont'd

- C++ provides type trait to enable types conditionally

```
template<typename T>
typename std::enable_if<std::is_integral<T>::value,
                        bool>::type
is_odd(T i) { return bool(i%2); }
```

```
float i=2;
cout << „i is odd :“ << is_odd(i) << endl;
```

- If `is_odd` is called with a **non-integral type** (e.g., `float`) the compiler expands the above templated function as follows
`is_odd(float i) { return bool(i%2); } // compiler error`

SFINAE revisited

- SFINAE: **S**ubstitution **F**ailure **I**s **N**ot **A**n **E**rror
 - Write multiple implementations of the same function with
 - the **same name** and
 - the **same input parameters**
 - Ensure using the **enable_if type trait** that only one of them results in valid code upon substitution of template parameters and all other candidates yield invalid expressions

SFINAE revisited, cont'd

- Consider the info() member function

```
template<typename T, typename I>
class Demo {
    static void info() { ... };
};
```

- Let's try to enable „void“ in case that I=int so that info has no return type if I!=int (which means that it is invalid code)

```
bool v = std::is_same<I, int>::value // either true or false
std::enable_if<v, void>::type        // either void or empty
```

SFINAE revisited, cont'd

- First attempt of partially specialised info() member function

```
template<typename T, typename I>
class Demo {
    // partial specialisation for I=int
    std::enable_if<std::is_same<I, int>::value, void>::type
    static info() { ... };
    // partial specialisation for I!=int
    std::enable_if<!std::is_same<I, int>::value, void>::type
    static info() { ... };
};
```

- This code will not compile; we need to introduce an extra function template parameter for the info() function

SFINAE revisited, cont'd

- Partially specialised info() member function (working!)

```
template<typename T, typename I>
class Demo {
    template<typename J=I>
    typename std::enable_if<std::is_same<J, int>::value,
                            void>::type
    static info() { ... };

    template<typename J=I>
    typename std::enable_if<!std::is_same<J, int>::value,
                            void>::type
    static info() { ... };
};
```

SFINAE revisited, cont'd

- In words...
 - Introduce function template parameter that by default takes the value of the class template parameter (`template<typename J=I>`)
 - Make type traits depend on artificial template parameter
`typename std::enable_if<std::is_same<J, int>::value,
void>::type`
 - Make sure that exactly one member function leads to valid source code that can be compiled without errors
`typename std::enable_if<!std::is_same<J, int>::value,
void>::type`

SFINAE revisited, cont'd

- Let us reconsider the dot-product for complex-valued vectors
- Use SFINAE paradigm to realise alternative implementations of the dot product for real- and complex-valued types
- Strategy:
 1. Write **type trait** `is_complex<T>` that has value=true if T is of type `std::complex<U>` and value=false otherwise
 2. Use **enable_if trait** to distinguish between real-valued and complex-values implementation of the dot-product

Type trait `is_complex`

- First implementation of type trait `is_complex` (will suffice for our purpose but is not really in line with standard traits)

```
template<typename T>
struct is_complex {
    static const bool value = false;
};
template<>
struct is_complex<std::complex<float> > {
    static const bool value = true; }
struct is_complex<std::complex<double> > {
    static const bool value = true; }
...
```

Type trait `is_complex`, cont'd

- C++ standard way to implement type traits by deriving from structure `std::integral_constant<T>`

```
template<typename T>
struct is_complex
: std::integral_constant<bool, // type bool
    std::is_same<T, std::complex<float>>::value ||
    std::is_same<T, std::complex<double>>::value ||
    ...
> {}
```

- Logical or (`||`) combination of all `std::complex<S>` that should be supported by the `is_complex` type trait

Type trait `is_complex`, cont'd

- Implementation of dot-product for **complex-valued types**

```
template<typename T>
class Vector {
    ...
    template<typename U=T>
    typename std::enable_if<is_complex<U>::value, U>::type
    dot(const Vector<T>& other) const {
        T d=0;
        for (auto i=0; i<n; i++)
            d += data[i]*std::conj(other.data[i]);
        return d;
    }
};
```

Type trait `is_complex`, cont'd

- Implementation of dot-product for **real-valued types**

```
template<typename T>
class Vector {
    ...
    template<typename U=T>
    typename std::enable_if<!is_complex<U>::value, U>::type
    dot(const Vector<T>& other) const {
        T d=0;
        for (auto i=0; i<n; i++)
            d += data[i]*other.data[i];
        return d;
    }
};
```

Summary SFINAE paradigm

- General approach to circumvent the limitations of C++ to not allow **partial specialisation of (class-)function templates**
 - Use `std::enable_if` type trait and `std::is_XXX` or self-written type trait to switch between different implementations of a function
- Code gets less readable due to dummy function template
- Default template arguments for function templates (`template<typename J=I>`) are a new feature in C++11
- For a complete list of standard type traits look at: http://www.cplusplus.com/reference/type_traits/

SFINAE Quiz

- What does this code do?

```
struct A {  
    A() {}  
    A(const A& a) {}  
};  
struct B : A {  
    B() {}  
    B(const B& b) {}  
};  
struct C {  
    C() {}  
    C(const C& c) {}  
};
```

```
template<typename T>  
typename std::conditional<  
    std::is_base_of<A,T>::value,  
    A,T>::type  
get_base_type(T t)  
{  
    typename std::conditional<  
        std::is_base_of<A,T>::value,  
        A,T>::type ReturnType;  
    return ReturnType(t);  
}
```

SFINAE Quiz, cont'd

- See `get_base_type` in action

```
A a; B b; C c;
```

```
typeid(a).name()    // -> 1A
```

```
typeid(b).name()    // -> 1B
```

```
typeid(c).name()    // -> 1C
```

```
typeid(get_base_type(a)).name()    // -> 1A
```

```
typeid(get_base_type(b)).name()    // -> 1A
```

```
typeid(get_base_type(c)).name()    // -> 1C
```

Final word on SFINAE

- Recall that we started the SFINAE-journey since we needed partial specialisation of the dot-product member function
- How would you implement the function `std::conj(...)`?

Final word on SFINAE, cont'd

- Viable implementation of the function `std::conj(...)` that uses the self-written `is_complex` type trait

```
template<typename T>
typename std::enable_if<is_complex<T>::value, T>::type
static conj(T t)
{ return T(t.real(), t.imag()); }
```

```
template<typename T>
typename std::enable_if<!is_complex<T>::value, T>::type
static conj(T t)
{ return T(t); }
```

Final word on SFINAE, cont'd

- Return value of function `std::conj(...)` is of `std::complex` type

```
template<typename T>
typename std::enable_if<is_complex<T>::value, T>::type
static conj(T t)
{ return T(t.real(), t.imag()); }
```

```
template<typename T>
typename std::enable_if<!is_complex<T>::value,
                        std::complex<T>>::type
static conj(T t)
{ return T(t); }
```