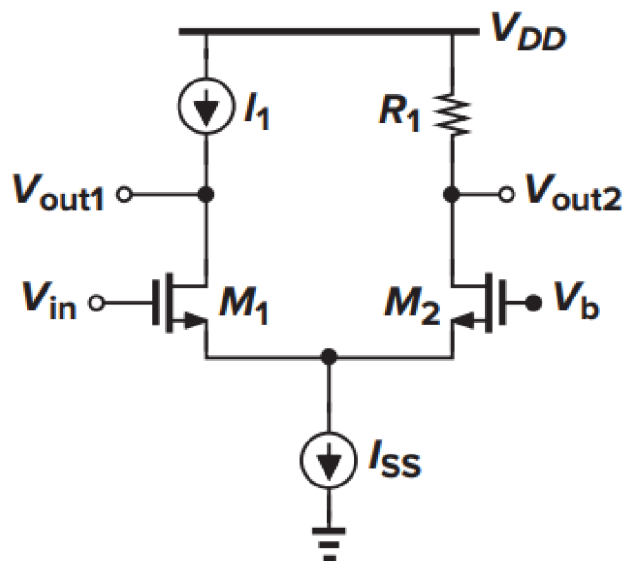


Due: **December 6th**

- 1) Please use A4 size paper or page.
- 2) Please clearly state out your final result for each question.
- 3) Please attach the screenshot of Pspice simulation result if necessary.

[20pts] For a differential amplifier circuits shown below, assume that I_1 and I_{SS} are ideal and $\lambda, \gamma > 0$, determine the value of V_{out1}/V_{in} and V_{out2}/V_{in} .



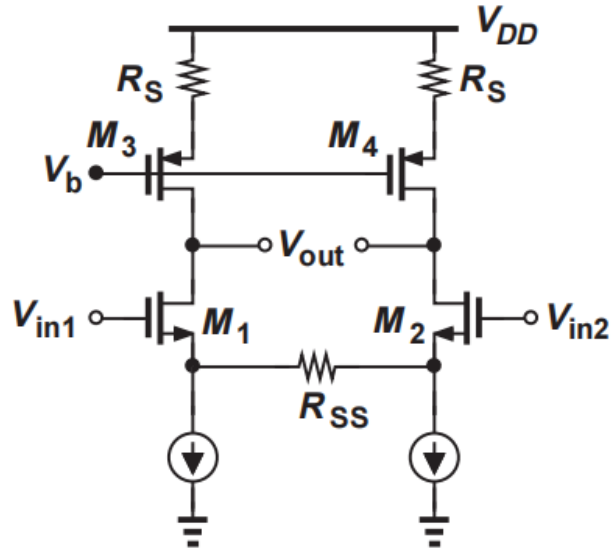
As for M_1 , the following equation could be established using small signal analysis:

$$\frac{V_{out1}}{r_{o1}} + g_{m1}V_{in1} = 0$$

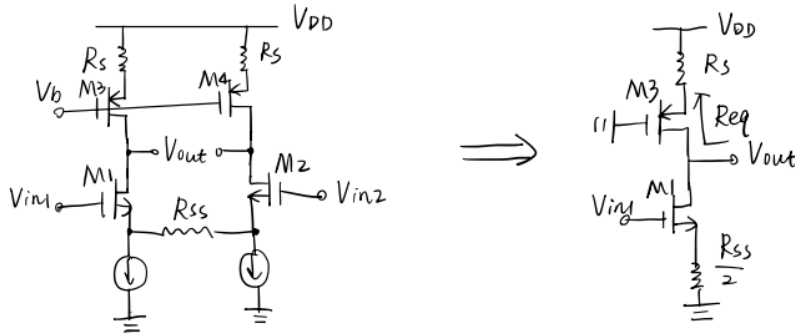
$$\frac{V_{out1}}{V_{in}} = -g_{m1}r_{o1}$$

Question 2. Differential Amplifier Circuits 2

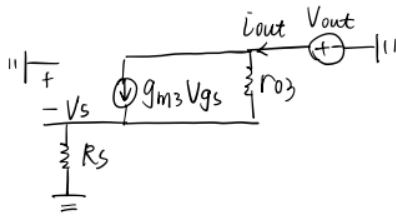
[40pts] Calculate the differential voltage gain of the circuits shown below. Assume perfect symmetry and $\lambda > 0$. You may need to compute the gain as $A_v = -G_m R_{out}$. Hint: use half circuit and R_{SS} can be divided into $\frac{R_{SS}}{2}$ in your half circuit.



First, apply half circuit method:



For R_{eq} :

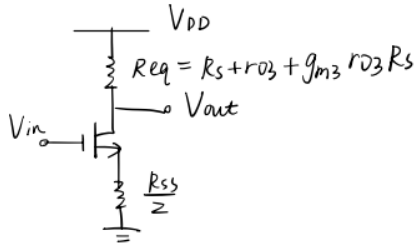


by KCL: $i_{out} = \frac{V_s}{R_s} = g_{m3}V_{gs} + \frac{V_{out} - V_s}{r_{o3}}$

by KVL: $V_{gs} = -V_s$

$$\Rightarrow R_{eq} = \frac{V_{out}}{i_{out}} = R_s + r_{o3} + g_{m3}r_{o3}R_s$$

\therefore the circuit can be simplify as a CS stage with source degeneration:



$$\therefore R_{out} = (R_s + r_{o3} + g_{m3}r_{o3}R_s) \parallel \left(\frac{R_{ss}}{2} + r_{o1} + g_{m1}r_{o1}\frac{R_{ss}}{2} \right)$$

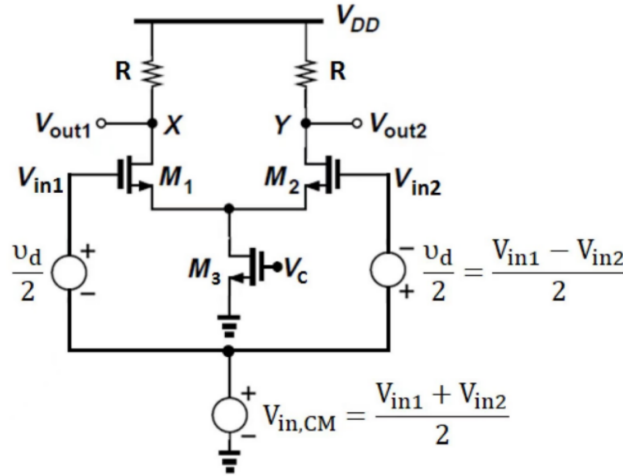
$$G_m = \frac{2g_{m1}}{R_{ss}} \left(\frac{1}{g_{m1}} \parallel r_{o1} \parallel \frac{R_{ss}}{2} \right)$$

$$\therefore A_v = -G_m \cdot R_{out} = \frac{-2g_{m1}}{R_{ss}} \left(\frac{1}{g_{m1}} \parallel r_{o1} \parallel \frac{R_{ss}}{2} \right) \cdot (R_s + r_{o3} + g_{m3}r_{o3}R_s) \parallel \left(\frac{R_{ss}}{2} + r_{o1} + g_{m1}r_{o1}\frac{R_{ss}}{2} \right)$$

Question 3. Differential Amplifier with PSPICE Simulation

[40pts] For the circuit shown below, use NMOS SPICE model except for $\lambda = 0$, $\eta = 0$

- For $V_{DD} = 5V$, $V_{in,CM} = 2.2V$, $V_C = 1.2V$, $R = 5k\Omega$, $(\frac{W}{L})_1 = (\frac{W}{L})_2 = \frac{50\mu m}{2\mu m}$, $(\frac{W}{L})_3 = \frac{100\mu m}{2\mu m}$, what are the values for A_{DM} and A_{CM} ?
- Plot $(V_{out1} - V_{out2})$ as a function of $(V_{in1} - V_{in2})$ from $-4V$ to $4V$ (i.e. $\frac{v_d}{2}$ from $-2V$ to $2V$). Confirm whether A_{DM} in (a) is consistent with the simulation result here. (Hint: To generate both $\frac{v_d}{2}$ and $-\frac{v_d}{2}$, you may need to use a Voltage Controlled Voltage Source(VCVS). You can find it in Pspice component)
- Plot $V_{out,CM}$ as a function of $V_{in,CM}$ from $0V$ to $5V$, while $v_d = 0$. Confirm whether A_{CM} in (a) is consistent with the simulation result here.



NMOS Model

LEVEL = 1	VTO = 0.7	GAMMA = 0.45	PHI = 0.9
NSUB = 9e+14	LD = 0.08e-6	UO = 350	LAMBDA = 0.1
TOX = 9e-9	PB = 0.9	CJ = 0.56e-3	CJSW = 0.35e-11
MJ = 0.45	MJSW = 0.2	CGDO = 0.4e-9	JS = 1.0e-8

(a). Since M_3 could be treat as an ideal current source in this case,

$$I_{SS} = \frac{1}{2}\mu_n C_{ox} \left(\frac{W}{L_{eff}}\right)_3 (V_c - V_{th})^2 = 9.12 \times 10^{-4} A$$

Then,

$$A_{DM} = -g_{m1,2} R_D = -9.12, A_{CM} = 0$$

Simulation for (b) and (c) are shown below.

