

1. Exercise 3.

$$\|e\|_s \leq Ch^{\beta} \|u\|_{k+1}$$

$$\beta = \min(k+1-s, z(k+1-m))$$

$$m=1 \text{ and } k=2, \quad \beta = \min(3-s, 4)$$

$$\because 0 \leq s \leq m \quad \rightarrow \quad 0 \leq s \leq 1 \quad \therefore 3-s < 4$$

$$\beta = 3-s$$

$$\text{for } e \text{ in } L_2, \quad s=0 \quad \beta=3 \quad \|e\|_0 \leq Ch^3 \|u\|_3$$

$$\text{for } e \text{ in } H^1, \quad s=1 \quad \beta=2 \quad \|e\|_1 \leq Ch^2 \|u\|_3$$

Exercise 4.

$$m=2, k=3, \quad \beta = \min(4-s, 4)$$

$$0 \leq s \leq 2 \quad \therefore 4-s \leq 4 \quad \therefore \beta = 4-s$$

$$\text{for } e \text{ in } L_2, \quad s=0 \quad \beta=4 \quad \|e\|_0 \leq Ch^4 \|u\|_4$$

$$\text{for } e \text{ in } H^1, \quad s=1 \quad \beta=3 \quad \|e\|_1 \leq Ch^3 \|u\|_4$$

$$\text{for } e \text{ in } H^2, \quad s=2 \quad \beta=2 \quad \|e\|_2 \leq Ch^2 \|u\|_4$$