

### Aufgabe 1:

$$\text{a) } \int_1^3 x^4 dx = \left[ \frac{x^5}{5} \right]_1^3 = \left( \frac{243}{5} \right) - \left( \frac{1}{5} \right) = 48.4$$

$$\text{b) } \int_{-3}^4 x^6 dx = \left[ \frac{x^7}{7} \right]_{-3}^4 = \left( \frac{16384}{7} \right) - \left( -\frac{2187}{7} \right) = 2653$$

$$\text{c) } \int_{-3}^1 x^3 dx = \left[ \frac{x^4}{4} \right]_{-3}^1 = \left( \frac{1}{4} \right) - \left( \frac{81}{4} \right) = -20$$

### Aufgabe 2:

$$\text{a) } \int_{-1}^2 -x^6 dx = \left[ -\frac{x^7}{7} \right]_{-1}^2 = \left( -\frac{128}{7} \right) - \left( \frac{1}{7} \right) = -18.429$$

$$\text{b) } \int_{-2}^1 x dx = \left[ \frac{x^2}{2} \right]_{-2}^1 = \left( \frac{1}{2} \right) - (2) = -1.5$$

$$\text{c) } \int_{-2}^4 -2x^2 dx = \left[ -\frac{2x^3}{3} \right]_{-2}^4 = \left( -\frac{128}{3} \right) - \left( \frac{16}{3} \right) = -48$$

### Aufgabe 3:

$$\text{a) } \int_{-4}^4 -3x dx = \left[ -\frac{3x^2}{2} \right]_{-4}^4 = (-24) - (-24) = 0$$

$$\text{b) } \int_{-4}^{-2} x^6 + 2x^3 dx = \left[ \frac{x^7}{7} + \frac{x^4}{2} \right]_{-4}^{-2} = \left( -\frac{72}{7} \right) - \left( -\frac{15488}{7} \right) = 2202.3$$

$$\text{c) } \int_0^3 5x^6 - 4x^5 dx = \left[ \frac{5x^7}{7} - \frac{2x^6}{3} \right]_0^3 = \left( \frac{7533}{7} \right) - (0) = 1076.1$$

### Aufgabe 4:

$$\text{a) } \int_{-4}^{-4} 5x^5 + x^4 + x^2 dx = \left[ \frac{5x^6}{6} + \frac{x^5}{5} + \frac{x^3}{3} \right]_{-4}^{-4} = \left( \frac{15936}{5} \right) - \left( \frac{15936}{5} \right) = 0$$

$$\text{b) } \int_2^4 -3x^5 - x^4 - 4x^3 dx = \left[ -\frac{x^6}{2} - \frac{x^5}{5} - x^4 \right]_2^4 = \left( -\frac{12544}{5} \right) - \left( -\frac{272}{5} \right) = -2454.4$$

$$\text{c) } \int_0^3 4x^6 + x^4 dx = \left[ \frac{4x^7}{7} + \frac{x^5}{5} \right]_0^3 = \left( \frac{45441}{35} \right) - (0) = 1298.3$$

### Aufgabe 5:

$$\text{a) } \int_{-3}^1 \frac{1}{x^2} dx = \left[ -\frac{1}{x} \right]_{-3}^1 = (-1) - \left( \frac{1}{3} \right) = -1.3333$$

$$\text{b) } \int_{-1}^0 x dx = \left[ \frac{x^2}{2} \right]_{-1}^0 = (0) - \left( \frac{1}{2} \right) = -0.5$$

$$\text{c) } \int_{-3}^{-2} x^4 dx = \left[ \frac{x^5}{5} \right]_{-3}^{-2} = \left( -\frac{32}{5} \right) - \left( -\frac{243}{5} \right) = 42.2$$

### Aufgabe 6:

$$\text{a) } \int_{-3}^2 2x^5 - 3x + \frac{1}{x^4} dx = \left[ \frac{2x^6}{6} - \frac{3x^2}{2} - \frac{1}{3x^3} \right]_{-3}^2 = \left( \frac{367}{24} \right) - \left( \frac{37181}{162} \right) = -214.22$$

$$\text{b) } \int_{-1}^{-1} -\frac{3}{x^5} dx = \left[ \frac{3}{4x^4} \right]_{-1}^{-1} = \left( \frac{3}{4} \right) - \left( \frac{3}{4} \right) = 0$$

$$\text{c) } \int_0^1 5x^2 dx = \left[ \frac{5x^3}{3} \right]_0^1 = \left( \frac{5}{3} \right) - (0) = 1.6667$$