Aufgabe 1:

a)
$$\int_{1}^{1} x \, dx = \left[\frac{x^{2}}{2}\right]_{1}^{1} = \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) = 0$$

b)
$$\int_{-4}^{-2} x^6 dx = c) \int_{-2}^{5} x^3 dx = [\frac{x^7}{7}]_{-4}^{-2} = (-\frac{128}{7}) - (-\frac{16384}{7}) = [\frac{x^4}{4}]_{-2}^{5} = (\frac{625}{4}) - (4) = 152.25$$
2322.3

c)
$$\int_{-2}^{5} x^3 dx = \left[\frac{x^4}{4}\right]_{-2}^{5} = \left(\frac{625}{4}\right) - (4) = 152.25$$

Aufgabe 2:

a)
$$\int_0^1 -4x^7 dx =$$
 b) $\int_1^5 x^5 dx =$ c) $\int_{-2}^1 x^4 dx =$ $\left[-\frac{x^8}{2}\right]_0^1 = \left(-\frac{1}{2}\right) - (0) = -0.5$ $\left[\frac{x^6}{6}\right]_1^5 = \left(\frac{15625}{6}\right) - \left(\frac{1}{6}\right) = 2604$ $\left[\frac{x^5}{5}\right]_{-2}^1 = \left(\frac{1}{5}\right) - \left(-\frac{32}{5}\right) = 6.6$

b)
$$\int_{1}^{5} x^{5} dx = \left[\frac{x^{6}}{6}\right]_{1}^{5} = \left(\frac{15625}{6}\right) - \left(\frac{1}{6}\right) = 2604$$

c)
$$\int_{-2}^{1} x^4 dx = \frac{x^5}{5}\Big|_{-2}^{1} = \left(\frac{1}{5}\right) - \left(-\frac{32}{5}\right) = 6.6$$

Aufgabe 3:

a)
$$\int_{-1}^{5} 5x^{2} + 2x \, dx =$$

$$[\frac{5x^{3}}{3} + x^{2}]_{-1}^{5} = (\frac{700}{3}) - (-\frac{2}{3}) =$$

$$234$$
b)
$$\int_{-4}^{-1} -3x^{4} - x^{2} \, dx =$$

$$[-\frac{3x^{5}}{5} - \frac{x^{3}}{3}]_{-4}^{-1} =$$

$$(\frac{14}{15}) - (\frac{9136}{15}) = -634.8$$
c)
$$\int_{4}^{4} -x^{5} + 4x^{3} \, dx =$$

$$[-\frac{x^{6}}{6} + x^{4}]_{4}^{4} =$$

$$(-\frac{1280}{3}) - (-\frac{1280}{3}) = 0$$

b)
$$\int_{-4}^{-1} -3x^4 - x^2 dx = \left[-\frac{3x^5}{5} - \frac{x^3}{3} \right]_{-4}^{-1} = \left(\frac{14}{15} \right) - \left(\frac{9536}{15} \right) = -634.8$$

c)
$$\int_{4}^{4} -x^{5} + 4x^{3} dx =$$
$$\left[-\frac{x^{6}}{6} + x^{4} \right]_{4}^{4} =$$
$$\left(-\frac{1280}{3} \right) - \left(-\frac{1280}{3} \right) = 0$$

Aufgabe 4:

a)
$$\int_{1}^{5} x^{2} dx = \left[\frac{x^{3}}{3}\right]_{1}^{5} = \left(\frac{125}{3}\right) - \left(\frac{1}{3}\right) = 41.333$$

b)
$$\int_{-1}^{3} -2x \, dx =$$
 $[-x^2]_{-1}^{3} = (-9) - (-1) = -8$

a)
$$\int_{1}^{5} x^{2} dx =$$
 b) $\int_{-1}^{3} -2x dx =$ c) $\int_{-2}^{0} -4x^{3} - 2x^{2} + 3x dx =$ $[-x^{2}]_{-1}^{3} = (-9) - (-1) = -8$ c) $\int_{-2}^{0} -4x^{3} - 2x^{2} + 3x dx =$ $[-x^{4} - \frac{2x^{3}}{3} + \frac{3x^{2}}{2}]_{-2}^{0} =$ $(0) - (-\frac{14}{3}) = 4.6667$

Aufgabe 5:

a)
$$5x - 3 = 4$$

b)
$$-3x + 1 = -4$$

c)
$$3x = 2$$

Aufgabe 6:

a)
$$-x^2 + 5x - 1 = 0$$

b)
$$x^2 - 2x + 3 = 0$$

c)
$$-2x^2 + 5x + 3 = 0$$

Aufgabe 7:

a)
$$4x^2 + 2x + 5 = 0$$

b)
$$3x^2 + 5x + 2 = 0$$

 $x_1 = -1.0, x_2 = -0.67$

c)
$$x^2 + x + 4 = 0$$