

Seongil Wi



Notification: Midterm Exam

- Oct. 24 (Thursday)
- Class Time (1h 15m), Closed book

- T/F problems + Computation problems + Descriptive problems
- Scope: everything learned from September 3 to October 17
 - Understanding is important!
 - The MIPS reference card will be provided. Do not memorize the content about it.

 If you are taking Linear Algebra (MTH20401), please send me an email (Those who have already sent an email are excluded)



Q&A Session for Your Midterm Exam

- Today, after the class
 - -45 minutes lecture
 - It is okay to leave the room after the lecture is end
 - -30 minutes Q&A session

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Recap: Floating-point Number

We need a way to represent ...

• Infinite decimal (e.g., 3.1415926535...)



3.1415

 Very small numbers



 0.001×10^{-20}

 Very large numbers



 3.15576×10^{19}

Can be represented with a limited number of bits!

Solution: Floating-point Number Representation

Recap: IEEE 754 Floating-point Standard

• Developed in response to divergence of representations

Divergence of representations

 $0.11_{two} = 1.1_{two} \times 2^{-1} = 11_{two} \times 2^{-2}$

Normalized representation

 $1.1_{\text{two}} \times 2^{-1}$

IEEE 756 representation

S Exponent

Fraction

- Two representations
 - Single precision (32-bit): type float in C
 - Double precision (64-bit): type double in C

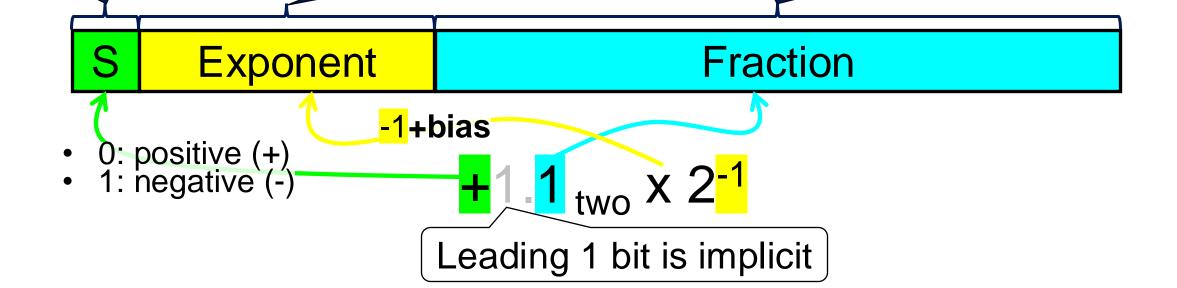
Sign Single: 1 bit Double: 1 bit

Exponent

- Single: 8 bits
- Double: 11 bits

Fractional part of significand

- Single: 23 bits
- Double: 52 bits



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Recap: Special Cases

- Exponent = 00...0, Fraction = 00...0
 - → Not 1.0 x 2^{-127} but **0**
- Exponent = 00...0, Fraction ≠ 00...0
 - \rightarrow Not (1 + fraction) x 2⁻¹²⁷ but (0 + fraction) x 2⁻¹²⁶
 - → Denormalized real numbers (to represent very small numbers)
- Exponent = 11...1, Fraction = 00...0
 - → ±infinity
- Exponent = 11...1, Fraction ≠ 00...0
 - → Not-a-Number (*NaN*)
 - → Indicates illegal or undefined result

How to represent the result of invalid operations (e.g., 0/0)?

Recap: Floating-point Addition

• Now consider a 4-digit binary example $1.000_2 \times 2^{-1} + -1.110_2 \times 2^{-2} (0.5 + -0.4375)$

1. Align binary points

- Shift number with *smaller exponent*
- $-1.000_2 \times 2^{-1} + -0.111_2 \times 2^{-1}$

2. Add significands

$$-0.001_2 \times 2^{-1}$$

3. Normalize result & check for over/underflow

 $-1.000_2 \times 2^{-4}$, with no over/underflow

4. Round

$$-1.000_2 \times 2^{-4} = 0.0625$$

Check $-126 \le -4 \le +127$ in case of a single precision

Recap: Floating-point Multiplication

For biased exponents,

subtract bias from sum

• Now consider a 4-digit binary example $1.000_2 \times 2^{-1} \times -1.110_2 \times 2^{-2} (0.5 \times -0.4375)$

1. Add exponents

- Unbiased: -1 + -2 = -3
- Biased: (-1 + 127) + (-2 + 127) 127 = -3 + 127

2. Multiply significands Typo

$$-1.000_2 \times 1.110_2 = 1.110_2 \implies 1.110_2 \times 2^{-3}$$

3. Normalize result & check for over/underflow

 $-1.110_2 \times 2^{-3}$ (no change) with no over/underflow

4. Round

$$-1.110_2 \times 2^{-3}$$
 (no change)

5. Determine sign: + sign $\times -$ sign $\Rightarrow -$ sign

$$-1.110_2 \times 2^{-3} = -0.21875$$

Today's Topic



- *
- I originally intended to cover logic design
- But I will first address the performance aspect

- Please delete the previous slides on logic design basics
- Your midterm exam scope includes the material covered up to today

Performance

(A review including more detailed information)

We Focus on the Time





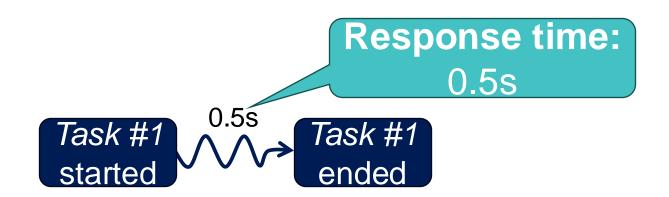
Most important thing: time, time, and time

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Performance Metrics



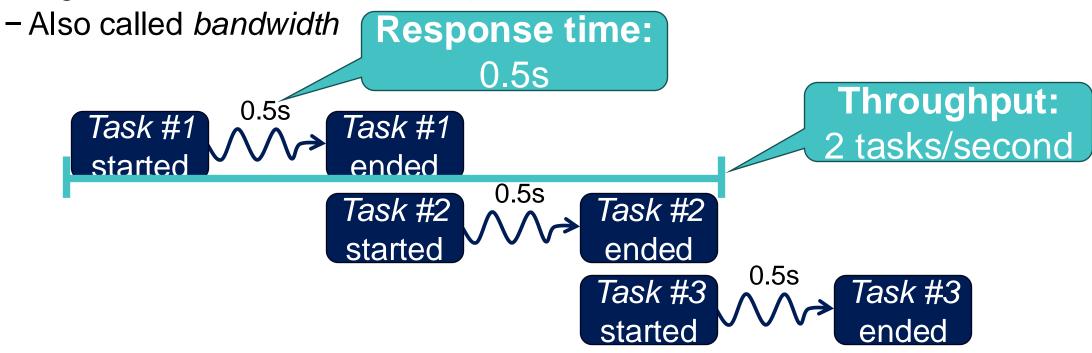
- Response time: the time between the start and completion of a task
 - Also called execution time, latency



Performance Metrics

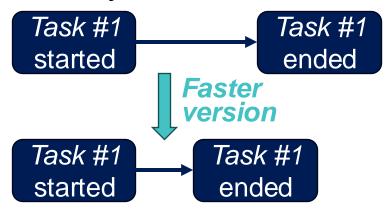


- *
- Response time: the time between the start and completion of a task
 - Also called execution time, latency
- Throughput: total work done per unit time
 - E.g., # of tasks/transactions/... per hour

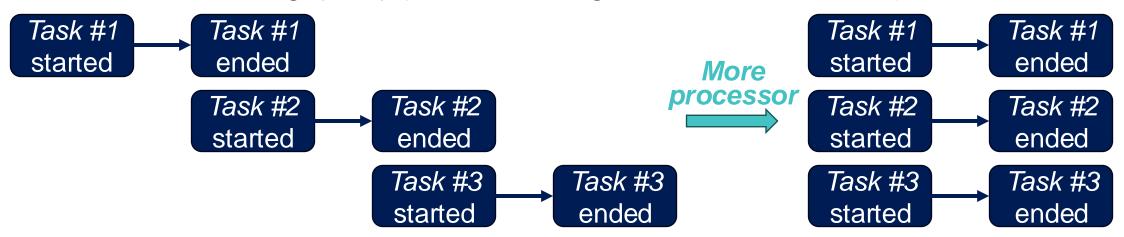


Throughput and Response Time

- How are <u>response time</u> and <u>throughput</u> affected by
 - Replacing the processor with a faster version?
 - → Response time ↑, Throughput ↑



- Adding more processors?
 - → Throughput ↑ (No one task gets work done faster)



Performance Metrics

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- *
- Response time: the time between the start and completion of a task
 - Also called *execution time*, *latency*
- Throughput: total work done per unit time
 - E.g., # of tasks/transactions/... per hour
 - Also called bandwidth

Execution Time



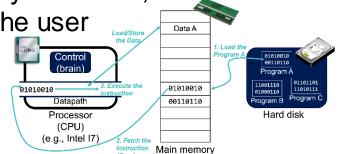




The total time to complete a task

• Counts everything, including disk accesses, memory accesses, ...

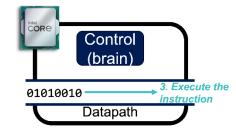
Experienced by the user



CPU Time ___

The actual time the CPU spends

 Doesn't include time spent waiting for I/O or running other programs



time Command in Linux



Elapsed Time

The actual time the CPU spends

CPU Time I

The total time to complete a task

\$ time a.out
real 341m58.124s
user 464m9.282s
sys 13m10.743s

time Command in Linux





CPU Time I

The total time to complete a task

The actual time the CPU spends

\$ time a.out
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Execution Time



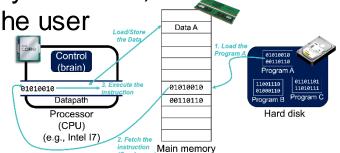




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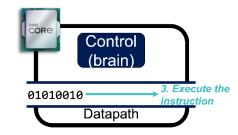
Experienced by the user



CPU Time ___

The actual time the CPU spends

 Doesn't include time spent waiting for I/O or running other programs



Our Focus



We'll focus on CPU time for now!

The total time to complete a task

 Counts everything, including disk accesses, memory accesses, ...

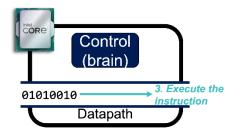
Experienced by the user



CPU Time J

The actual time the CPU spends

 Doesn't include time spent waiting for I/O or running other programs



Performance and Execution Time



Performance =
$$\frac{1}{\text{Execution Time}}$$

• Relative performance: "X is N times faster than Y"

$$N = \frac{\text{Performance}_{x}}{\text{Performance}_{Y}} = \frac{\text{Execution TimeY}}{\text{Execution TimeX}}$$

- Exercise: time taken to run a program
 - -10s on A
 - -15s on B
 - -Q. A is N times faster than B. What is N?

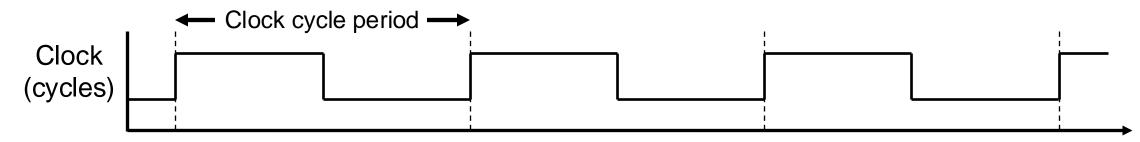
$$\frac{\text{Execution TimeB}}{\text{Execution TimeA}} = \frac{15s}{10s} = 1.5$$

Recap: CPU Clocking





Operation of digital hardware governed by a constant-rate clock



Clock cycle (period): duration of a clock cycle

$$-e.g.$$
, $250ps = 0.25ns = 250 \times 10^{-12}s$

Clock rate (frequency): # of cycles per second

$$-e.g.$$
, $4.0GHz = 4000MHz = 4.0 \times 10^{9}Hz$

Frequency (Hz) = $\frac{1}{\text{Clock Cycle Period}}$

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Background: Metric Prefixes

peta	Р	10 ¹⁵		1 000 000 000 000 000
tera	Т	10 ¹²		1 000 000 000 000
giga	G	10 ⁹		1 000 000 000
mega	М	10 ⁶		1 000 000
kilo	k	10 ³		1 000
hecto	h	10 ²		100
deka	da	10¹		10
base unit		10°		1
deci	d	10-1	1/10	0.1
centi	С	10-2	1/100	0.01
milli	m	10-3	1/1 000	0.001
micro	μ	10-6	1/1 000 000	0.000 001
nano	n	10-9	1/1 000 000 000	0.000 000 001
Ångström	Å	10-10	1/10 000 000 000	0.000 000 000 1
pico	р	10-12	1/1 000 000 000 000	0.000 000 000 001

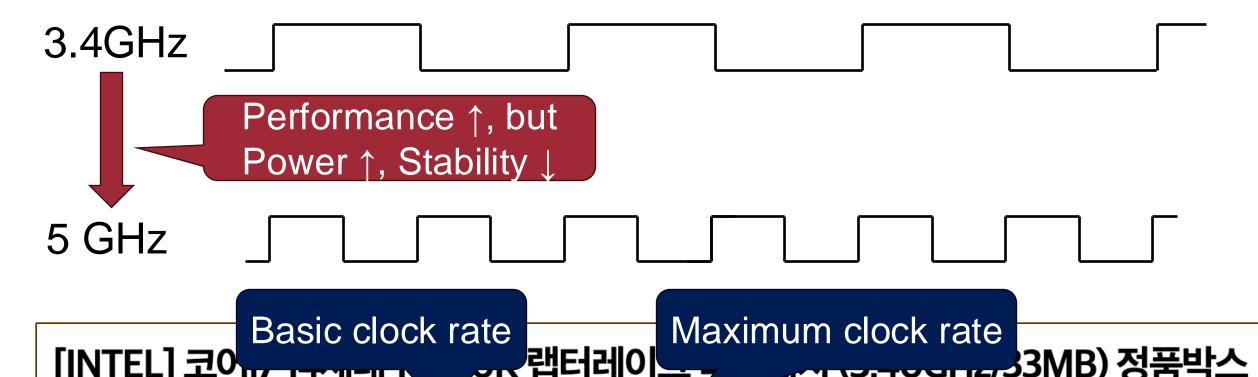
This information will be provided in your midterm exam!

FYI: CPU Overclocking





 The practice of increasing the clock rate of a computer to exceed that certified by the manufacturer



인텔(소켓1700) / 8+12코어 / 16+12쓰레드 / 기본 클럭: 3.4GHz / 최대 클럭: 5.6GHz / L3 캐시: 33MB / PBP : 125W / PCle5.0 , 4.0 / 메모리 규격: DD 픽: 탑재 / 인텔 UHD 770 / 기술 지원: 하이퍼스레닝 / 굴러: 미포함

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FYI: CPU Overclocking

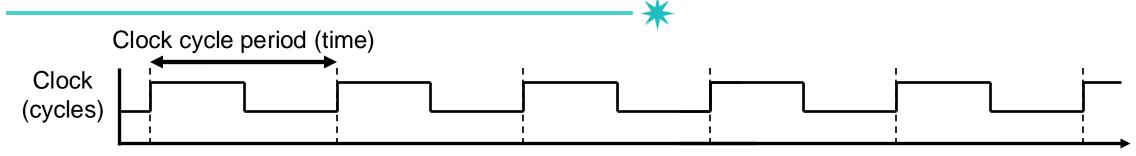




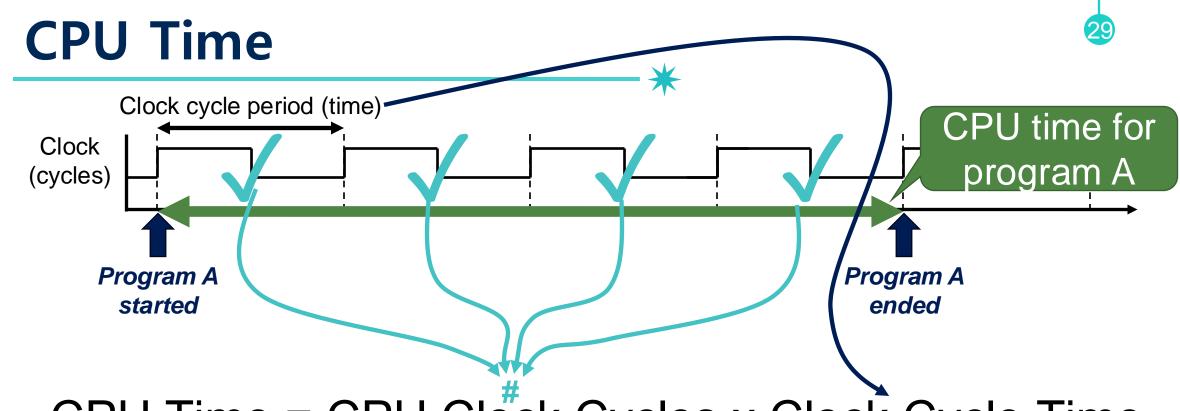


CPU Time

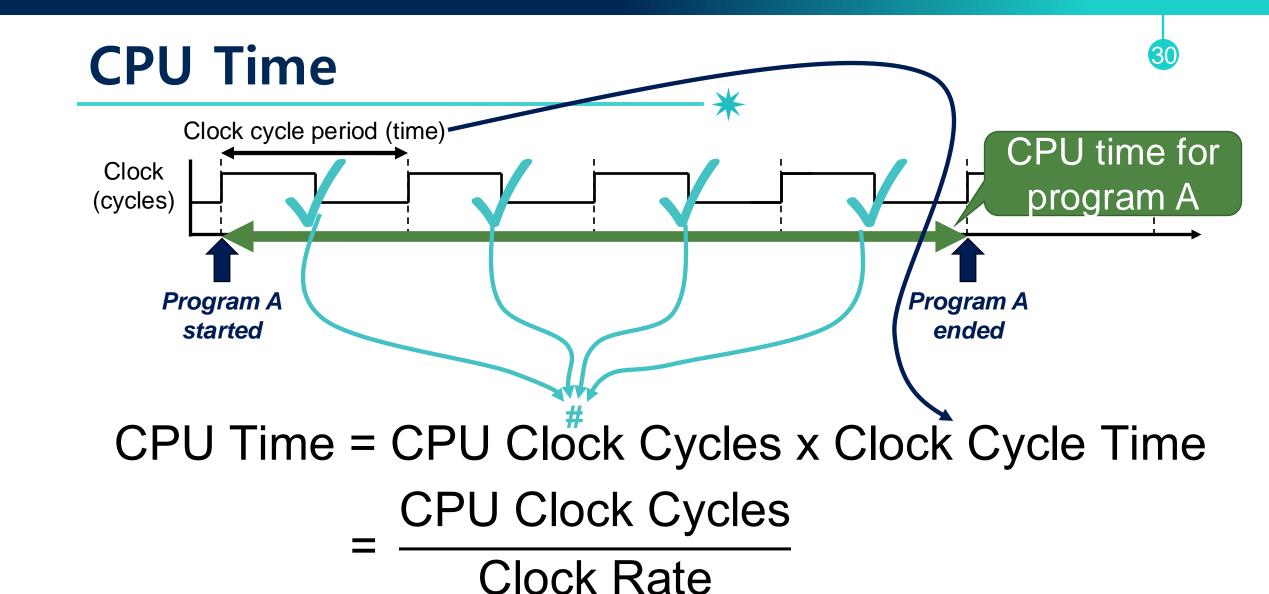




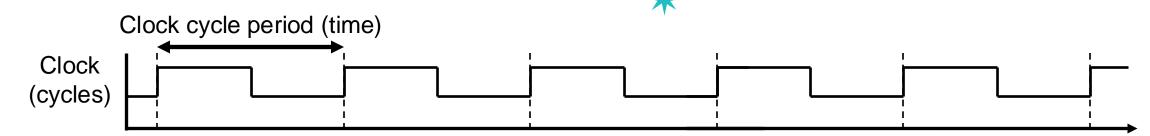
CPU Time = CPU Clock Cycles x Clock Cycle Time



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Performance Improvement



Performance improved by

- Reducing number of clock cycles
- Increasing clock rate

Reducing clock cycles requires **more operations per cycle**, which lowers the clock rate

CPU Time





CPU Time = CPU Clock Cycles x Clock Cycle Time

$$= \frac{Instructions}{Program} \times \frac{Clock\ cycles}{Instruction} \times \frac{Seconds}{Clock\ cycle}$$

of Instructions per Program (Instruction Count)

Instruction Count

of Instructions per Program (Instruction Count)

$$CPU Time = \frac{Instructions}{Program} \times \frac{Clock cycles}{Instruction} \times \frac{Seconds}{Clock cycle}$$

```
swap:
  multi $2, $5, 4 add $2, $4, $2
```

of instructions per program

Affected by:

- Compiler
- Algorithm
- Programming language
- ISA

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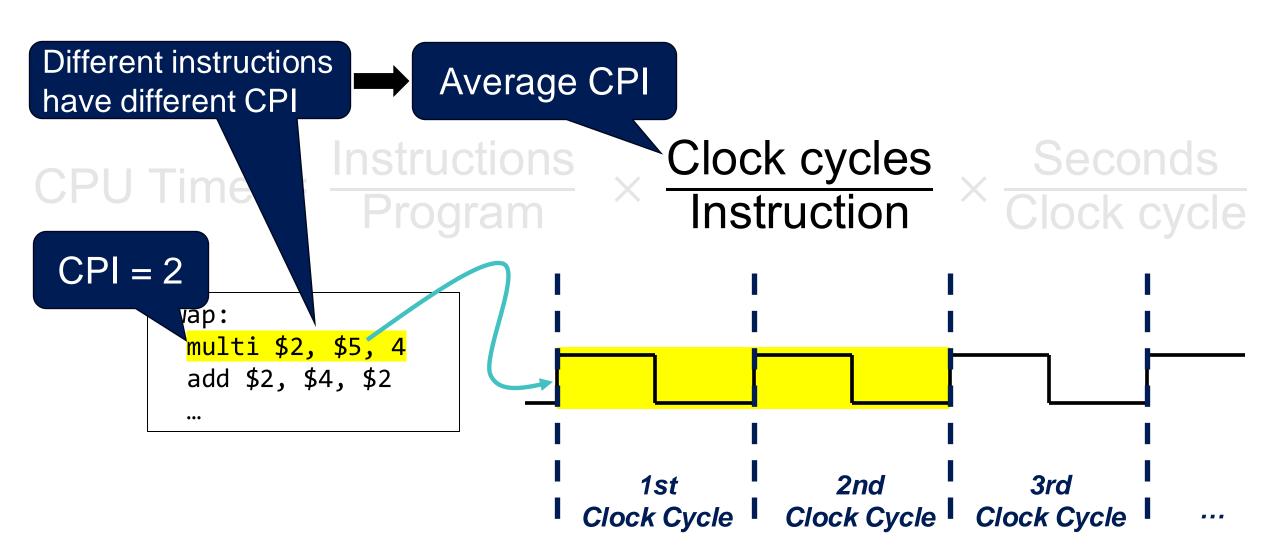
Clock Cycles per Instruction (CPI)

Instruction Count

Average CPI

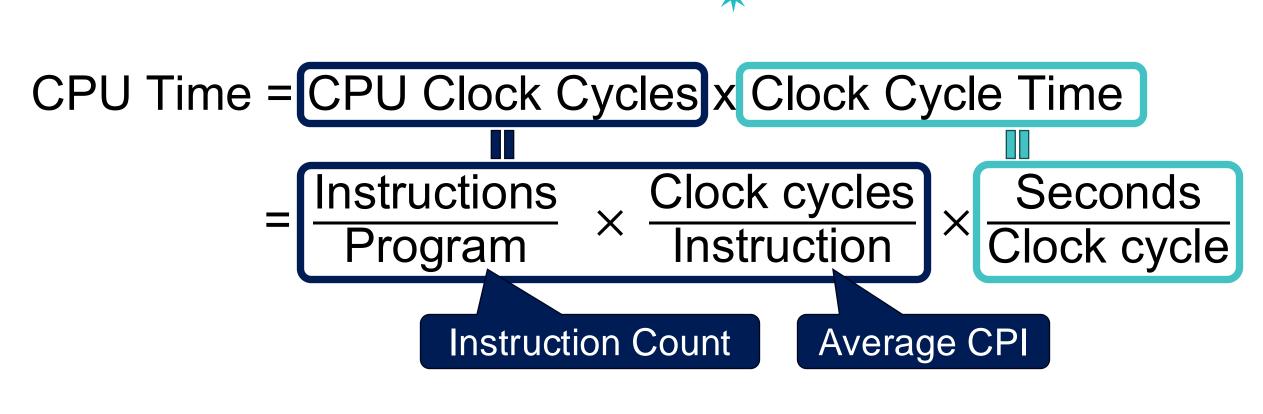
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Clock Cycles per Instruction (CPI)



CPU Time



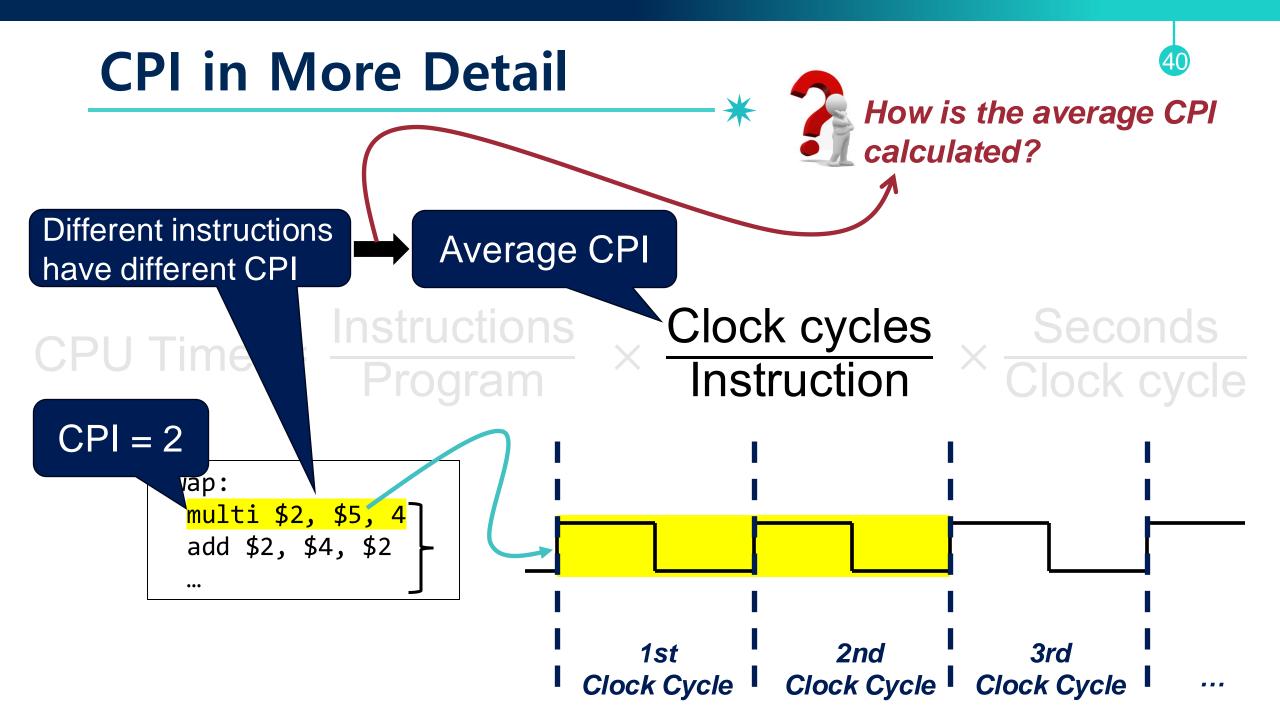


CPI Example



- Computer A: Cycle Time = 250ps, CPI = 2.0
- Computer B: Cycle Time = 500ps, CPI = 1.2
- Same ISA
- Which is faster, and by how much?

A and B consists of the same instructions



CPI in More Detail

of instruction classes



Clock Cycles =
$$\sum_{i=1}^{11}$$
 (CPI_i × Instructio n Count_i)

$$CPU Time = \frac{Instructions}{Program}$$

Clock cycles
Instruction

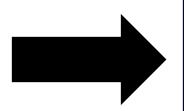
Seconds
Clock cycle

```
CPI = 2
```

CPI = 1

CPI = 2

Program A: multi \$2, \$5, 4 -add \$2, \$4, \$2 _multi \$3, \$4, 6



Clock Cycles = $(2 \times 2) + (1 \times 1) =$

CPI in More Detail

of instruction classes



Clock Cycles =
$$\sum_{i=1}^{n}$$
 (CPI_i×Instructio n Count_i)

(Weighted average)
$$CPI = \frac{Clock\ Cycles}{Instructio\ n\ Count} = \sum_{i=1}^{n} \left(CPI_i \times \frac{Instructio\ n\ Count_i}{Instructio\ n\ Count_i}\right)$$

Relative frequency

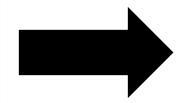
Clock cycles Instruction

```
CPI = 2
```

CPI = 1

CPI = 2

Program A: multi \$2, \$5, 4 -add \$2, \$4, \$2 _multi \$3, \$4, 6

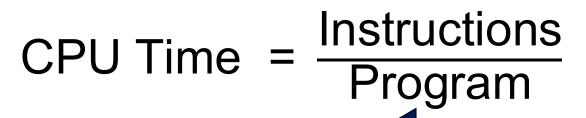


Average CPI = $(2 \times 2/3) + (1 \times 1/3) =$ 5/3

Clock cycle

Performance Summary





× Clock cycles
Instruction

× Seconds
Clock cycle

Instruction Count

Average CPI

Clock Cycle Period

- Performance depends on
 - Algorithm: affects IC, CPI
 - Programming language: affects IC, CPI
 - Compiler: affects IC, CPI
 - Instruction set architecture (ISA): affects IC, CPI, Clock Cycle Period

Question?