

Datamodelling and Databases [2ID50]: Homework Assignment Week 6

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1. We can derive $\beta \twoheadrightarrow \gamma$, since $\beta \rightarrow \gamma$ and by using the replication rule. And from $\beta \twoheadrightarrow \gamma$ and $\alpha \twoheadrightarrow \beta$ we derive $\alpha \twoheadrightarrow \gamma - \beta$ by multivalued transitivity. And since it is the case that $\gamma - \beta = \gamma$, we obtain $\alpha \twoheadrightarrow \gamma$.

2. Consider the shopping database with the purchase table:

purchase(tID, cID, sID, pID, date, quantity, price)

In this table the following constraints hold:

tID, pID \rightarrow cID, sID, date, quantity, price (in other words tID, pID is a superkey)

tID \rightarrow cID, sID, date (every transaction is done by one customer, in one store, on one date)

sID, pID, date, quantity \rightarrow price (for the same quantity of a product, on a certain date, in a certain store, everyone pays the same price)

Note that when we do not have multivalued dependencies in a relation, then when it is in BCNF, it will also be in 4NF. Hence it suffices to decompose the relation purchase in BCNF. This is exactly what I will do. We start by calculating purchase⁺

tID \rightarrow cID, sID, date, quantity, price, tID, pID

cID \rightarrow cID

sID \rightarrow sID, price

pID \rightarrow pID, tID, cID, sID, date, quantity, price

date \rightarrow date, price

quantity \rightarrow quantity, price

price \rightarrow price

We see that tID and pID are candidate keys, sID, date and quantity are not however. From this we conclude that sID \rightarrow sID, price, date \rightarrow date, price and also quantity \rightarrow quantity, price are not allowed in the BCNF. So we can decompose purchase into purchase_1 (tID, pID, price, cID), purchase_2(date, price), purchase_3(sID, price) and purchase_4(quantity, price). In the first result of our decomposition, purchase_1, tID and pID are superkeys. In purchase_2 date is a candidate key and price only determines itself. In purchase_3 sID is a candidate key and price again only determines itself and

finally in purchase_4 quantity is a candidate key and price again determines itself.
So we have 4 relations in BCNF.

3.

cust (cID, cName) :- customer(cID, cName, street, city)
st(sID, sName):- store(sID, "Albert Heijn", street, city)
purch(sID, cID):- purchase(tID, pID, sID, cID, date, quantity, price)
ah(cName):- cust(cID,cName), st(sID, sName), purch(cID,sID)
?ah(cName)

4.

st(sName, sID):- store (sID, sName, street, city)
stcity(sName):- store (sID, sName, street, "Eindhoven")
chain(sName):- st(sName, A), st(sName, B), A≠B
notehv(sName):- chain(sName), not stcity(sName)
?notehv(sName)

5. The meaning of the query in plain English is: List all the customer names who have made a purchase in all the stores in their city.