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Image Based Phylogenetic Classification

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Umjesto ove stranice umetnite izvornik Vašeg rada.

Da bi ste uklonili ovu stranicu obrišite naredbu \izvornik.

Thank you...

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1. Introduction

Since the dawn of time, people have tried to explain their surroundings. Life is all around us in many forms, and as such people have tried to categorize it by keen observation, both through its visual and genetic features. Today, it is organised into a taxonomic hierarchy of eight major taxonomic ranks. The number of known species on Earth is in the millions and climbing every year. Great numbers of species make it difficult to classify them only based on images and often requires domain knowledge. Therefore, an algorithm with the capability to classify species on the field or from an image using only the image itself could provide great benefits for field researches.

Machine learning allows computers the ability to learn without being explicitly programmed (Samuel). It, together with an increase in available quality data (cif, ima, kag) has yielded great results in the area of deep learning - a class of machine learning algorithms. Deep learning algorithm's accuracy scales with the amount of data used by the algorithm, that together with the improvements in hardware - mainly general purpose graphic units (GPUs) - has yielded significant performance gains in the last couple of years. One of the most rapidly advancing fields of deep learning is image recognition (Krizhevsky et al.; Simonyan i Zisserman; Szegedy et al.; He et al., a) with new neural network architectures being developed almost at a yearly basis. The performance of deep neural networks on image recognition has achieved results previously thought impossible.

In this thesis I propose a solution for a scalable classification of species from images, based on convolution neural networks and recent modern deep learning techniques.

2. Research context

To fully understand the depth of the image recognition using deep learning, a better understanding of the underlying algorithms and methods in machine learning is needed, as well as fundamental terms and concepts. In the next section, an introduction of basic terms is given, followed by a detailed explanation of fundamental machine learning algorithms.

2.1. Definitions and notation

2.1.1. Image representation

Matrix is a rectangular array of numbers. It is used because some values are naturally represented as matrices. Matrix A with m rows and n columns often written as $m \times n$ has $m * n$ elements and is denoted as $A_{m,n}$. Elements are denoted as $a_{i,j}$ where i and j correspond to the row and column number respectively, as shown in 2.1.

$$A_{m,n} = \begin{bmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m,1} & a_{m,2} & \cdots & a_{m,n} \end{bmatrix} \quad (2.1)$$

Each image is represented as a 3 dimensional matrix. One pixel in the image represent a single element in the matrix and as images have multiple channels (RGB) each channel is a 2 dimensional matrix. Image I denoted as $I_{k,m,n}$ where $k \in [1, 3]$ represent the channel - red, green or blue - and $m, n \in [0, 255]$ represent the pixel intensities in a particular channel as 2 dimensional matrices. Figure 2.1 shows a representation of an image as a 3 dimensional matrix where each pixel is denote as $I_{k,m,n}$.

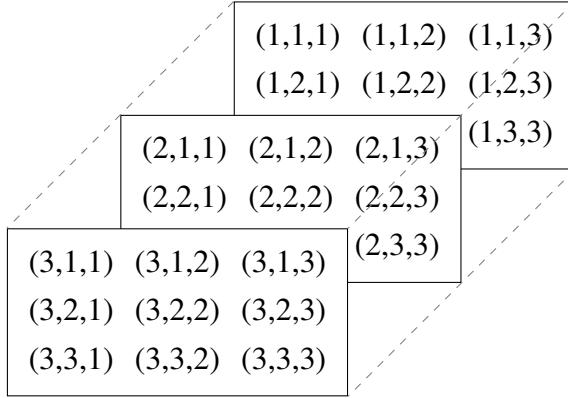


Figure 2.1: RGB image with 9 pixels represented as a 3 dimensional matrix

2.1.2. Gradient

A gradient is a generalization of the derivative in multi-variable space and as such it is represented as a vector. Like the derivative, it represents the slope of the tangent of the graph of the function. Therefore, it points in the direction of the greatest rate of increase of the function. Gradients are widely used in optimization theory as they allow the parameters to shift in a direction which will minimize or maximize a given function. In machine learning the function that is to be minimized is the loss function, which is defined in further chapters in more detail. Gradient of f is denoted as ∇f , where every component of ∇f is a partial derivative of f , denoted as $\frac{\partial f}{\partial x_i} \vec{e}_i$. Notice that gradient components are vectors denoted as \vec{e}_i . Every vector is written with a horizontal arrow above the letter, for example vector a is denoted as \vec{a} . The gradient for a n dimensional space is defined in 2.2.

$$\nabla f = \frac{\partial f}{\partial x_1} \vec{e}_1 + \dots + \frac{\partial f}{\partial x_n} \vec{e}_n \quad (2.2)$$

2.1.3. Activation functions

Machine learning models use nonlinear functions to gain more capacity - expressiveness . The most popular nonlinear functions are *sigmoid*, *tanh* and *relu*. All nonlinear functions have to have easy to compute gradients, as they are computed on parameters in order to reduce loss as explained above.

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}} \quad (2.3)$$

$$\tanh(x) = \frac{1 - e^{-2x}}{1 + e^{-2}} \quad (2.4)$$

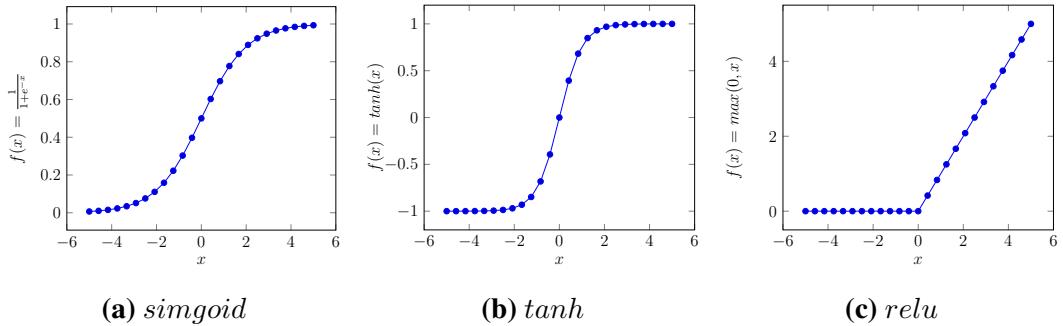


Figure 2.2: Nonlinear activation functions

$$relu(x) = \max(0, x) \quad (2.5)$$

The order of nonlinear functions is given in order of their discoveries. Today *relu* is used the most, since it solves the problem of vanishing gradients (see section 2.3.5 for a detailed explanation of vanishing gradients) for very deep neural networks, this does not apply to all network types. Recurrent neural networks (RNN) are a class of neural networks that often use *tanh* as it is better suited for the particular recurrent architecture.

2.1.4. Metrics

In order to compare different models a set of metrics is employed. Accuracy which gives the accuracy of a model, it is often used on balanced datasets (2.6). The problem with unbalanced datasets can be easily explained with a short example. Imagine having 2 classes $K = \{dog, cat\}$ and there are a total of 100 images in the dataset, of which only 2 are dogs. The model, if optimized for accuracy might say the whole dataset is composed of cats which will yield an accuracy of 98%. To solve the previous problem, additional metrics were introduced for the task of classification; precision (2.7), recall (2.8) and F1 score (2.9). Precision - positive predictive value - is defined as a fraction of retrieved instances that are relevant. Recall - sensitivity - is a fraction of relevant instances that are retrieved. In order to represent the performance of a model as a single variable F1 score was introduced, it represents a harmonic mean of recall and precision.

$$Accuracy = \frac{tp + tn}{tp + tn + fp + fn} \quad (2.6)$$

$$Precision = \frac{tp}{tp + fp} \quad (2.7)$$

Table 2.1: Confusion matrix

	prediciton positive	prediction negative
actual positive	True Positive (TP)	False Negative (FN)
actual negative	False Positive (FP)	True Negative (TN)

$$Recall = \frac{tp}{tp + fn} \quad (2.8)$$

$$F1score = 2 * \frac{precision * recall}{precision + recall} \quad (2.9)$$

Classification results are often represented as a confusion matrix, also known as an error matrix. It is way to visualise the performance of a classification model - classifier. To build the classification matrix, conditions of the experiment must be labelled as positive and negative. Using the cats and dogs example from before and making the cats a positive and dogs a negative class creates a 2×2 matrix of actual and predicted values as shown in table 2.1.

2.1.5. Data

The input data of the machine learning algorithm is labelled as D , and it consists of X and y_t , where X is one input data point (an image in our case) and y_t is the true label of that image - species' name. Written formally the whole input dataset is represented as $D = \{X^i, y^i\}_{i=1}^N$, where i is the i -th data point and N in the number of data points. Prediction of the algorithm is labelled as y_p .

The input data set is usually split into two datasets - called the *training* and the *test* dataset. The training dataset is used to optimize the model's parameters while the test data is used to evaluate the model's performance on previously unseen data - the goal of machine learning is the create models that work well on previously unseen data. Sometimes the training dataset is split further into training and *validation* where the validation dataset is used to tune the models *hyperparameters*. Hyperparameters are parameters that do not belong to the model but non the less effect the model's performance. Depth of the neural network is a type of hyperparameter and will be discussed in later chapters in more detail.

2.2. Machine learning

As said in the Introduction chapter, machine learning allows computers the ability to learn. Giving data to a machine learning algorithm - model - allows it to find patterns within the dataset. The function that maps the input X to y_p is called a *hypothesis* and is denoted as h (2.10). The hypothesis $h(X; \vec{\theta})$ is parametrized with $\vec{\theta}$ - model's parameters.

$$h(X; \vec{\theta}) : X \rightarrow y \quad (2.10)$$

The model is defined as a set of hypotheses H , $h \in H$. Machine learning can be defined as the search of the best hypothesis h from the hypothesis space H - typical optimization problem. The algorithm tries to minimize the empirical error function $E(h|D)$ - loss function. The error indicates the accuracy of the hypothesis and is called empirical because it is computed on D . Therefore, every machine learning algorithm is defined with the model (2.11), error function (2.12) and the optimization method (2.13).

$$H = \{h(X; \vec{\theta})\}_{\theta} \quad (2.11)$$

$$E(h|D) = \frac{1}{N} \sum_{i=1}^N I\{h(X^i) \neq y^i\} \quad (2.12)$$

$$\theta^* = \operatorname{argmin}_{\theta} E(\theta|D) \quad (2.13)$$

Machine learning algorithms are divided into groups depending on the task, the groups are classification, clustering and regression. Each can be represented as a result of $h(X; \vec{\theta})$. Classification hypothesis takes the input X and returns a class k , example of this method would be image classification. Regression hypothesis takes the input X and returns a number, for example predicting house prices.

$$\text{Regression} - h(X; \vec{\theta}) : X \rightarrow y, y \in \mathbb{R} \quad (2.14)$$

$$\text{Classification} - h(X; \vec{\theta}) : X \rightarrow y, y \in K = \{k_0, \dots, k_n\} \quad (2.15)$$

In this chapter it was mentioned that machine learning algorithms are trained by minimizing the empirical loss, and in the subsection 2.1.5 the idea of having a training and test set was introduced. The goal of the machine learning model is to have good

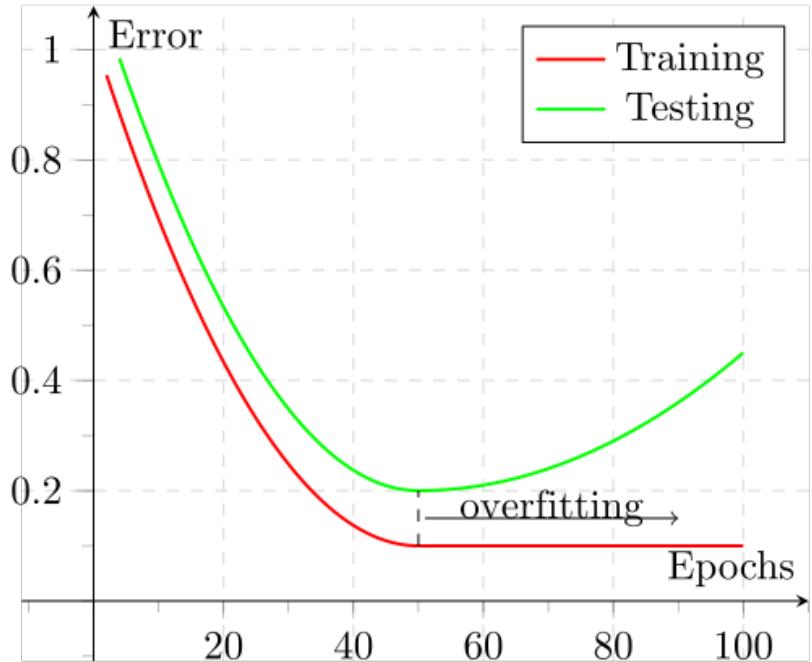


Figure 2.3: Performance of a model by the number of epochs using training and test set

generalization - the ability to perform well on never before seen data X . The training set X_{train} is used by the optimization algorithm to tune the model's parameters, while the test set X_{test} is used to evaluate the generalization performance of the model. If the optimization algorithm does not know when to stop it can learn the whole training set and be able to predict every value, this is called overfitting and it is to be avoided. When the model overfits, it learns to predict based on the data points in X_{train} instead of the learning the underlying patterns in X_{train} , which in turn leads to poor generalization performance. This is commonly seen in models with high capacity. On the other hand, if the model has low capacity, it will under-perform - work below its potential. That is referred to as underfitting. To goal is to find the optimal spot of the model's performance - between underfitting and overfitting. This behaviour can be seen in Figure 2.3. The x-axis shows the number of training epochs - each epoch increases the capacity of the model. We see that the training error E_{train} is falling asymptotically towards zero while the the generalization performance start to fall certain a point (50 epochs). The ideal situation for the model is to stop the training when the model starts to overfit, which is not that easy as we will see in the future chapters.

One way to combat overfitting is by early stopping during training. Another, more popular way is to use regularization. Regularization is a technique for increasing the generalization performance of the model by penalizing high parameter values or reducing the complexity of the model. There is a broad set of regularization techniques used

in machine learning models. Some of the most popular for artificial neural networks are called dropout (Srivastava et al.) and data augmentation, both of which will be explained in more detail in future chapters (subsections 2.3.2 and 2.3.3). Regularization techniques usually add additional components to the loss function in order to prevent the model from learning to map X_{train} to y_{train} directly.

2.2.1. Supervised and unsupervised learning

For the model to be trained it needs data D which is defined as $\{X^i, y^i\}_{i=1}^N$. Unfortunately, y is not always available. In such cases, the model can still use only X to infer and that is called unsupervised learning. When the model uses both the data points X and labels y it is called supervised learning. Classification and regression are both cases of supervised learning. Cluster analysis or more commonly called clustering is a type of unsupervised learning. In clustering the model tries to group a set of objects in such a way that objects in the same group are more similar based on a certain metric. The groups are called clusters, hence the name clustering. Some algorithms need the number of clusters to be predefined, while others discern it by themselves. As the purpose of the task is by itself classification, in following chapters supervised learning methods will be explained in more detail.

2.2.2. Artificial neural network (ANN)

One of the most interesting models in machine learning, with a diverse set of variations are artificial neural network (ANN). The computational model based on mathematics for neural networks was first introduced in 1943 by Warren McCulloch and Walter Pitts (McCulloch i Pitts) called threshold logic. Later on in 1951 a influential paper was published by S. C. Kleene on linking neural networks to finite state automata (Kleene). Artificial neural networks are based on a large collection of small computational units called neurons (figure 2.5). The architecture was inspired by axons (2.4) from our brains. The idea is that even though a single neuron dose not have the capacity to express complicated levels of abstractions - neurons together can. Neurons are connect in order to transfer signals. If a neuron receives a strong enough signal it becomes activated and propagates the received signal toward his output. Just propagating the signal would not be of benefit, as the single would not transform while passing through the network, therefore non linear activation functions, as explained in subsection 2.1.3, are added to each output of a neuron.

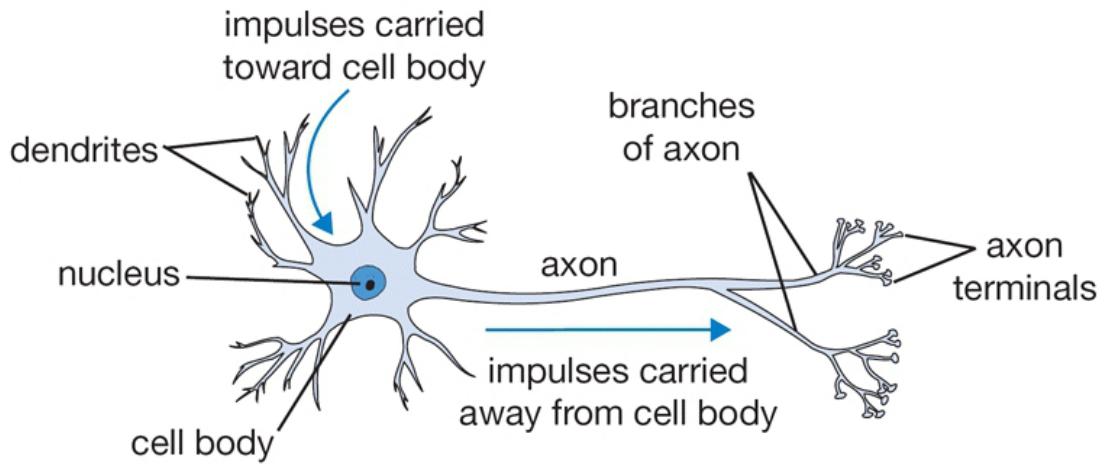


Figure 2.4: Neuron cell in a brain.

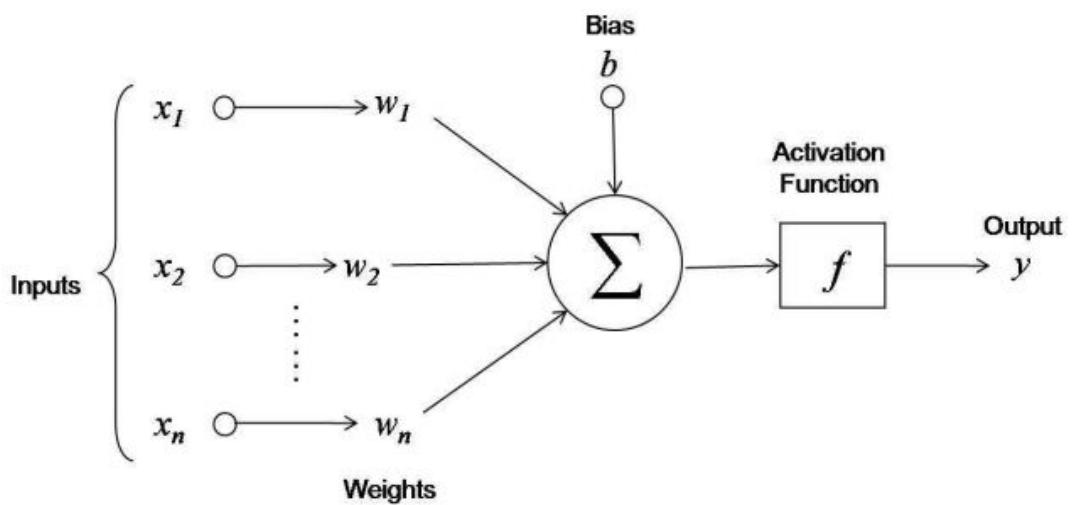


Figure 2.5: Artificial neuron cell.

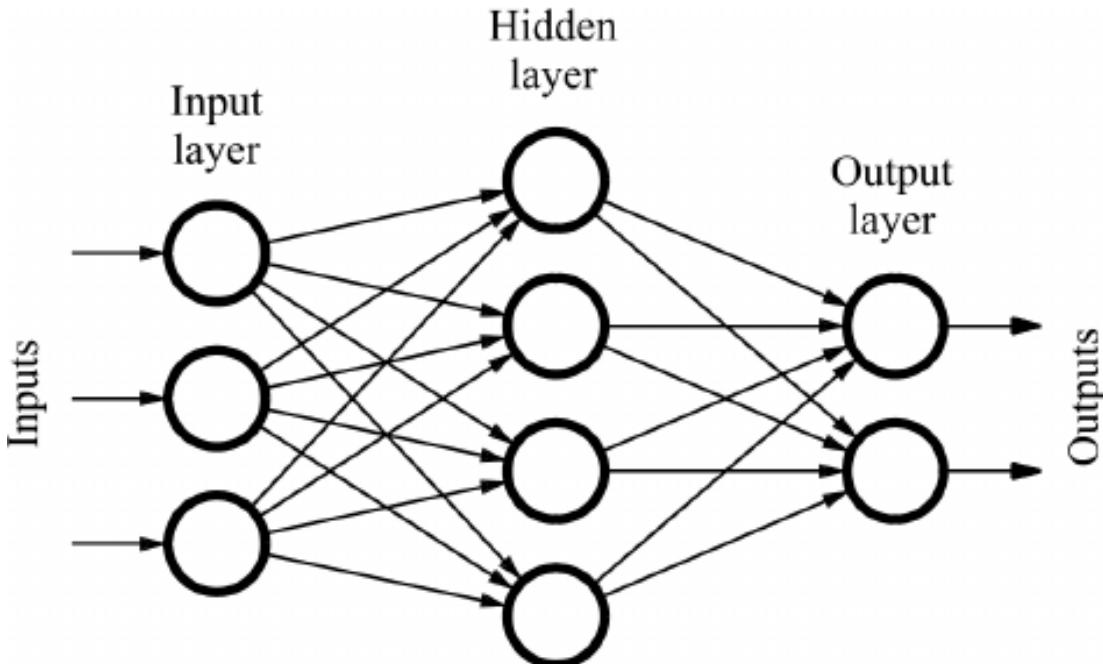


Figure 2.6: Feed-forward neural network

One of the most popular ANN architectures are feed-forward networks (FFN), consisting of fully-connected layers or sometimes also referred to as dense layers. They are called feed-forward because the data X enters at one side of the network (the input layer) and exits at the other end (output layer). Neurons are grouped into layers, and layers make an artificial neural network. The first layer is called an input layer, the last layer is called the output layer and every layer in between is a hidden layer. The network is called fully-connected because each neuron in the hidden and output layers are connected with every neuron of the previous layer as seen in Figure 2.6. Each neuron consists of connections, biases and activation functions. Each connection has a weight that singles the importance of the connection to the neuron. To get the net output of the neuron we multiply the input vector \vec{x} with the weight vector \vec{w} . As the bias (commonly denoted with w_0 or b), does not have an input of its own, we assigned x_0 to 1 so we can do a vector multiplication (2.16). To get the final output y of the neuron, the activation function f is applied to the *net* output, as shown in the expression 2.17). The computational model of the artificial neuron can be seen in the Figure 2.5.

$$net = 1 * w_0 + w_1 * x_1 + \dots + w_n * x_n = \vec{x} * \vec{w} \quad (2.16)$$

$$y = f(net) = f(\vec{x} * \vec{w}) \quad (2.17)$$

Artificial neuron networks have the ability to adjust their capacity to the task. Ad-

justing the number of neurons in a single layer, the number of hidden layers or the type of activation function used in each neuron affects the capacity of the ANN. Such flexibility also leads to a broad number of architectures, and there is no clear way to determine which one suits best. It is often left to the user to test a broad variety of architectures. Figure 2.6 shows that the number of neurons in the input layer matches the input size, this is true also for the output layer. Therefore, when designing an ANN the size of input and output layers are determined by the task and the number of hidden layers by the user.

2.3. Deep learning

Deep learning is a class - subset - of machine learning algorithms. Even though, deep learning may be connected to using "deep" neural networks - neural networks with many layers - it was created as a subset of machine learning that promised the automation of feature extraction task by using unsupervised learning. Unsupervised feature extraction and feature representation is done through a cascade of many non-linear layers, each of which contains artificial neurons.

Visual recognition is one of the fields that is most affected by improvements in deep learning (Krizhevsky et al.; Simonyan i Zisserman; Szegedy et al.; He et al., a). It's difficult and time consuming to build hand crafted features for each visual recognition problem. Deep learning allows the user to use raw images with minimal preprocessing - making it applicable with ease to almost any task.

Deep learning algorithms consist of enormous numbers of parameters (hundreds of millions), therefore training them is computational expensive. Recent breakthroughs in deep learning were driven by advances in hardware - graphics processing unit (GPUs). GPUs are made of a lot of processor unites, making them ideal for highly concurrent tasks. Neural networks are easily trained concurrently because of their composite structure and a special training algorithm called stochastic backpropagation (discussed in detail in subsection 2.3.4), commonly referred to as backprop.

2.3.1. Convolutional neural Network (CNN / ConvNet)

Convolutional neural network is a type of feed-forward network that was inspired by the organization of animal's visual cortex. They are used in recommender systems, natural language processing and image recognition. The architecture was inspired by the works of Hubel and Wiesel in 1950s and 60s (Hubel i Wiesel). Their work showed

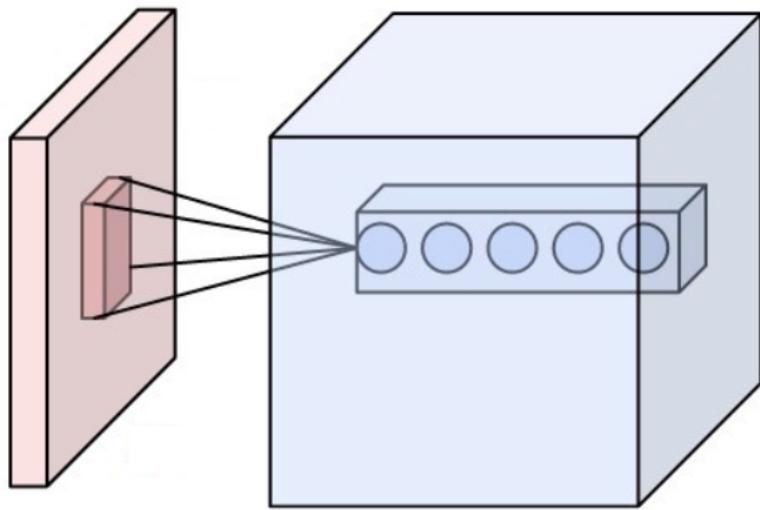


Figure 2.7: 3D structure of a convolutional filter (on the left painted in pink is the input - image - and the blue rectangle with circles is a filter)

that animal's visual cortex contains neurons that individually responds to small regions in the visual field. Their experiments showed that neighbourhood neurons had similar receptive fields.

The necognitron was introduced in 1980s by Kunihiko Fukushima (Fukushima i Miyake; Fukushima) and served as an inspiration for today's modern convolutional neural network architecture. The necognitron is a hierarchical multi-layered artificial neuron network. It was used for handwritten character recognition, which belongs in the domain of image recognition.

Today's modern convolutional neural network architectures, such as: AlexNet, VGG, Inception and ResNet (Krizhevsky et al.; Simonyan i Zisserman; Szegedy et al.; He et al., a) are made mostly of convolution and pooling layers. These architecture have an enormous number of parameters and are trained on powerful GPUs or clusters of servers over a period of days, sometimes even weeks.

The convolution layer is a building block of modern CNNs. The layer's parameters consist of a set of kernels (filters). Each filter has a small receptive field, but extends through the whole depth of the input. During the forward pass of the input through the network, each filter is convolved across the width and height of the input volume. Each time the filter moves to neighbourhood pixels it creates an output pixel (shown in figures 2.7 and 2.8). Each convolution layer consists of multiple filters, each specialized (because of model training) to detect different features in the input. Filters will detect diagonal edges, top edges, corners and other different building blocks of images. Each

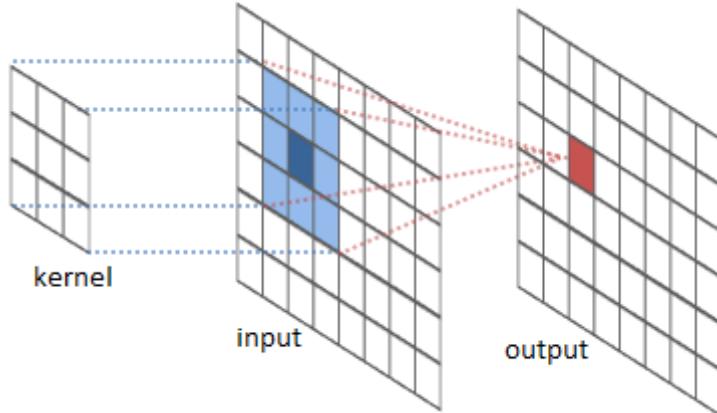


Figure 2.8: A 3x3 kernel (filter) convolving and input to generate an output

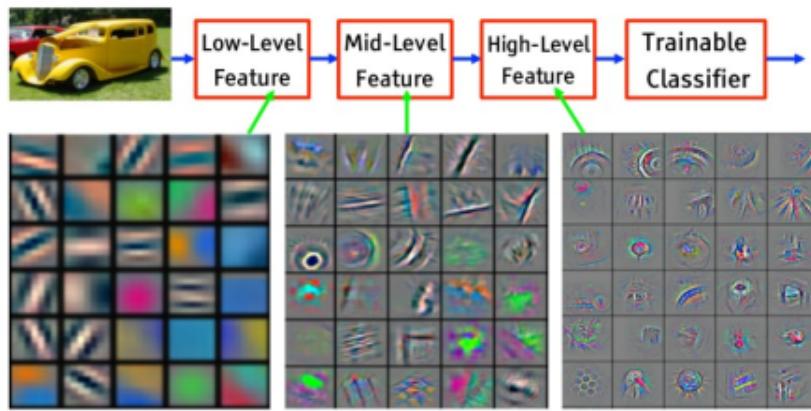


Figure 2.9: Representation of filters through the CNN

filter will use the features of the previous layer to create more abstract features. For example, a filter in the first layer might capture edges, while filters in deeper layers may use the edge filters to create corner and circle detectors (shown in detail in figure 2.9) (Simonyan i Zisserman).

The second core layer of almost every modern CNN is the pooling layer. It, in contrast to the convolution layer, does not have any parameters. The pooling layer takes the input and reduces its dimension. CNNs use max pooling, which maps the input into a reduced output by taking only the max values in the mapping (showed in figure 2.10). Use of pooling layer is a heated topic in today's CNN architectures, unfortunately hardware cannot keep up with the depth of the modern architectures without the use of pooling layers.

The typical structure in a CNN network is one or more convolution layers followed by a max pool layer, and that is repeated multiple times to increase the capacity of the model. The most common dimension of convolution filters is 3x3, made popular by

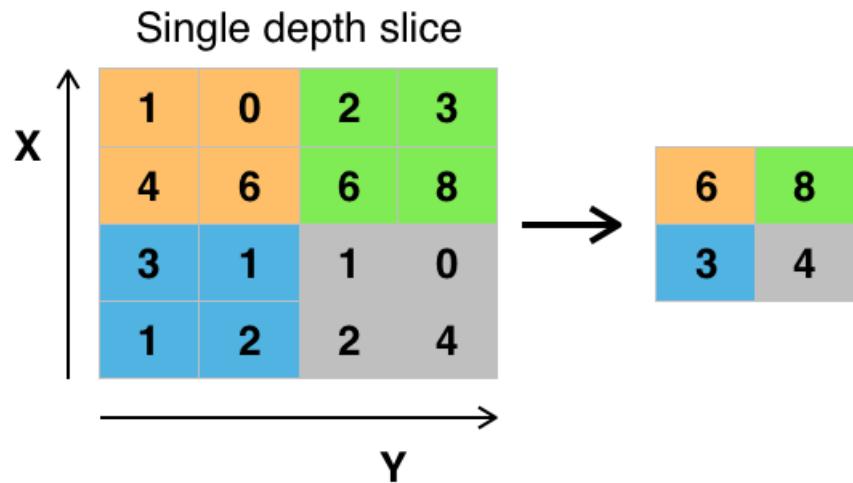


Figure 2.10: Max pooling a 4x4 input to 2x2

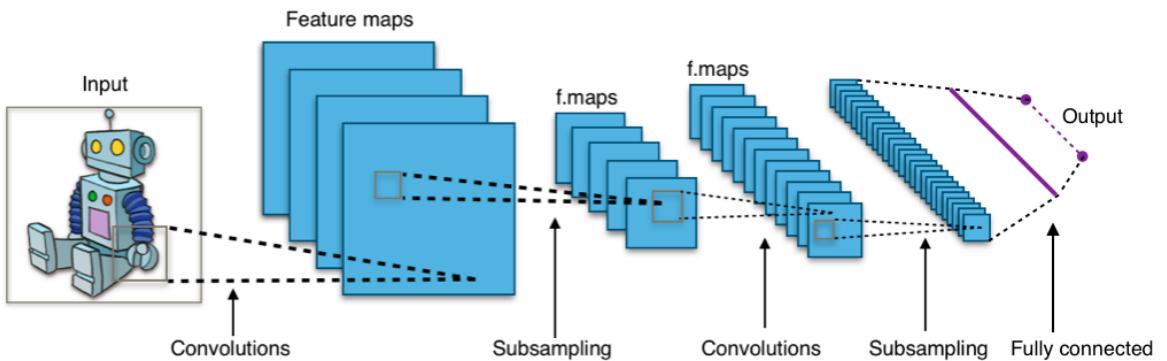


Figure 2.11: Typical modern CNN

the huge success of VGG (Simonyan i Zisserman) CNN architecture. The typical CNN is shown in figure 2.11.

2.3.2. Dropout

One of the most important techniques in machine learning is regularization (subsection 2.2). The modern approach to regularization is called dropout and was introduced in 2014 (Srivastava et al.). Dropout "drops" (removes) a percent of neurons on every forward pass (figure 2.12). The network cannot be sure that the same neurons will always be active and, as a result must not rely on every neuron, therefore increasing the robustness of the model together with its generalization performance. As in every forward pass, the network has a different set of neurons, this technique can be seen as using multiple variations of the same network on the same problem.

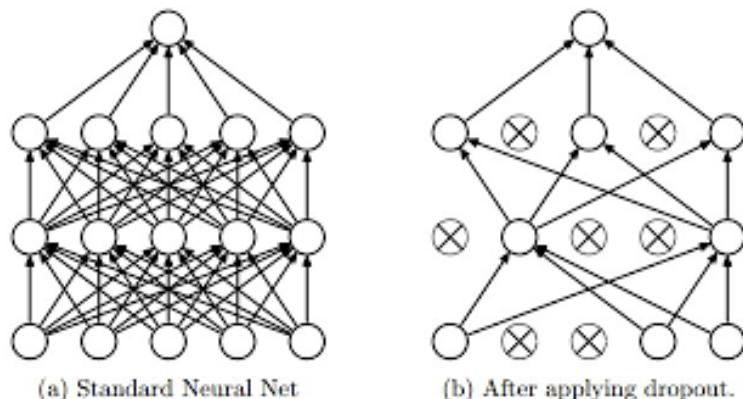


Figure 2.12: An example of the dropout technique

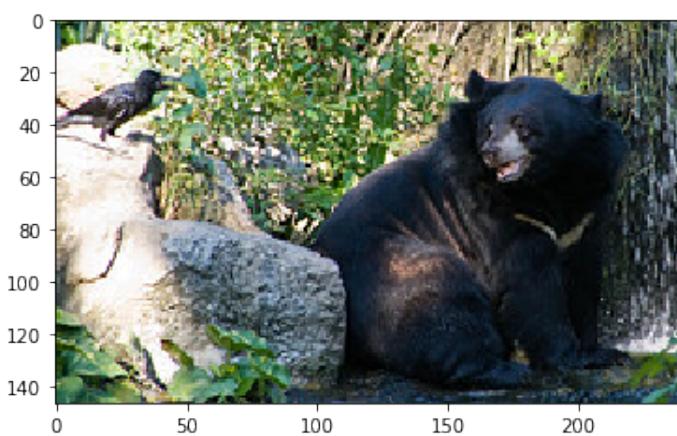


Figure 2.13: An example of the original - unprocessed - image in X_{train}

2.3.3. Data augmentation

Another popular regularization technique is called data augmentation. The model usually trains in tens or even hundreds of epochs - a signal epoch is when the training algorithm uses every data point in X_{train} (one pass over X_{train}). Reusing the same data points can lead to overfitting. One approach to preventing that is to augment X_{train} on every epoch. This approach is commonly called data jittering. Usually the data is augmented with rotation, mirroring, cropping, blurring (all these effects can be seen in figures 2.13 and 2.14). Both, dropout and data augmentation is used in almost every state-of-the-art CNN model today. There are some exceptions due to a new technique called batch normalization (Ioffe i Szegedy).

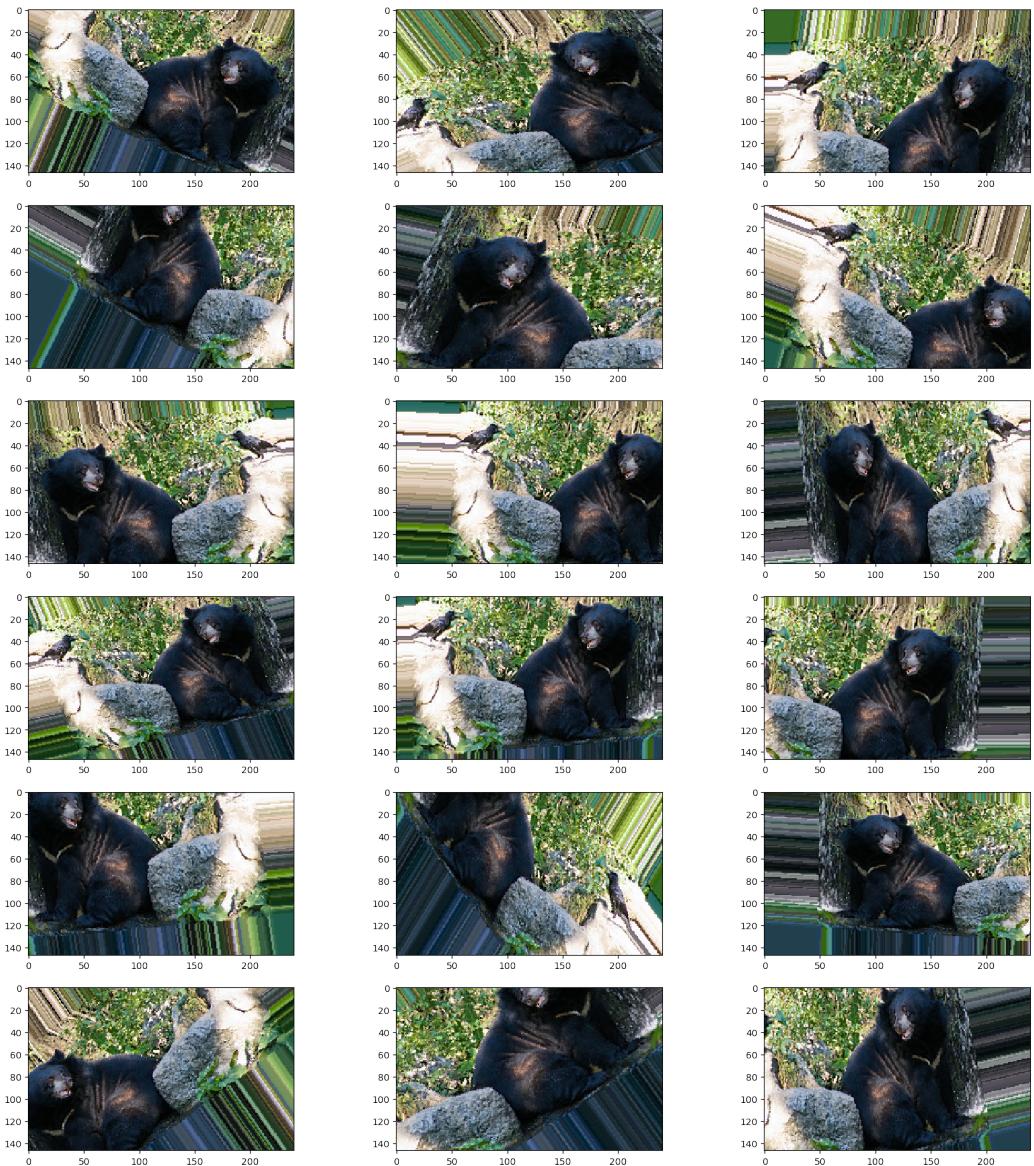


Figure 2.14: Example of data augmented images based on the original image 2.13

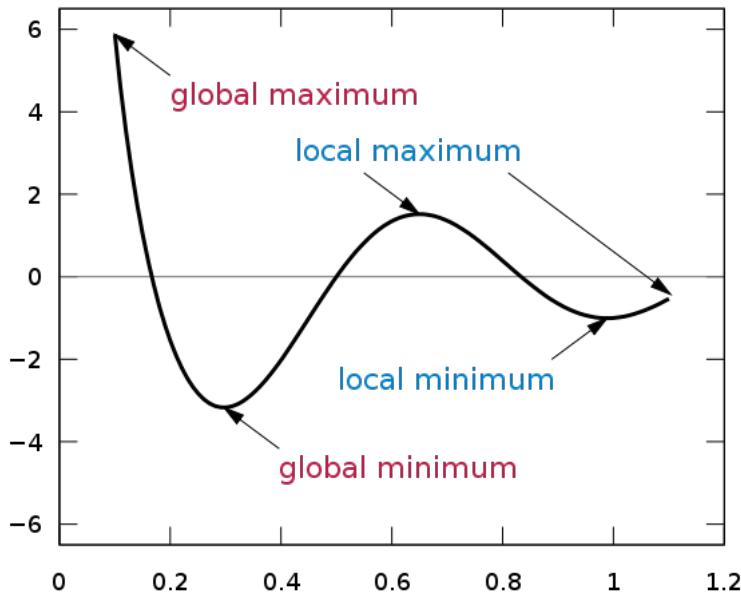


Figure 2.15: An example of local and global maximum and minimum in a function

2.3.4. Backpropagation

To be able to train a convolutional neural network on huge datasets, an algorithm is needed that is able to train the model with a subset of X_{train} . Fitting the whole X_{train} in the GPU memory is not possible for datasets of serious size. Also, the algorithm should be highly concurrent in order to use the structure of neural network to its advantage. The backward propagation of errors or more commonly called backpropagation (backprop) used together with gradient descent is the most popular method for training (most) neural networks.

Gradient descent

Gradient descent is an iterative optimization algorithm. It uses the gradient 2.1.2 of a function to find a point on a domain that minimises or maximises the function's value. Gradient descent does not guarantee to find the global maximum or minimum (figure 2.16). There have been several variations of the gradient descent algorithm that deal with the algorithm being stuck in local maximum or minimum, the most famous and most widely used for deep learning is Adam (Kingma i Ba).

$$x_{n+1} = x_n - \eta * \nabla f(x_n) \quad (2.18)$$

Gradient descent uses the gradient of a function to move in a way that minimises or

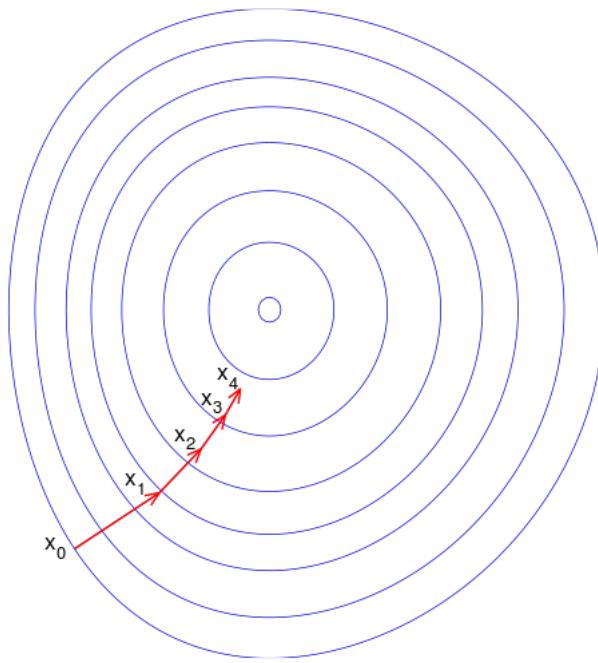


Figure 2.16: An example of gradient descent converging to global minimum in a 2D space (function with two variables)

maximises the given function (2.18). The amount that is used to move the data point - called the step (η) - is crucial for the convergence of the algorithm. If the step is too big the algorithm might diverge or get stuck into a local minimum or maximum, while if the step is too small the algorithm might take too long to converge. Gradient descent, like other optimization algorithms needs to have its parameters properly initialise to achieve good results.

Stochastic gradient descent

The main disadvantage of the gradient descent (2.18) is the need to calculate the gradient on all the dataset, to be able to update the parameter. The gradient has to be calculate on the whole X_{train} . An improvement on the basic gradient descent is the stochastic gradient descent (SGD). It updates the gradient by sampling the dataset in minibatches, usually the size 64, 128 or 256 data points (depending on GPU memory limitations). After every epoch the the whole training dataset X_{train} is shuffled so that different minibatches will be sampled in the next epoch. The rule of thumb is if you can increase the size of minibatch - do it. The more data points are in the minibatch, the more precise is the gradient approximation, also the model trains faster.

Optimization target

The goal of the gradient descent algorithm is to minimise or maximise a function. In deep learning, when training the model, the goal is to minimise the loss function $E(h|D)$ by computing its gradient. In classification (2.15) the goal is for the predicted class y_p to match the true class y_t . Neural networks for classification usually have a softmax layer as their last layer. Softmax (2.19) is a normalization exponential function, which transforms neural network's outputs to probabilities for every class. The sum of the softmax values for all classes is equal to one.

$$\text{softmax}(\vec{z})_j = \frac{e^{z_j}}{\sum_{k=1}^K e^{z_k}} \quad \text{for } j = 1, \dots, K \quad (2.19)$$

For the task of classification, the softmax function is the final layer - the output. Using this information allows us to compute the loss function. The loss of a softmax function is called cross-entropy loss and is computed with negative log likelihood (2.20).

$$L(y_t, y_p) = - \sum_{d=1}^D \sum_{k=1}^K y_t^i * \log(y_p^i) \quad (2.20)$$

To use the cross-entropy loss in the backpropagation we have to calculate its gradient. The gradient for cross-entropy loss is shown in 2.21).

$$\nabla L = \vec{y_t} - \vec{y_p} \quad (2.21)$$

2.3.5. Vanishing gradient

One of the problems in using backpropagation is the propagation of loss gradients in the neural networks. As the neural network is composed of smaller units called neurons, its output is also a function composed of linear combinations and non-linear activation functions of previous layers. The backpropagation algorithm calculates the gradient losses from the output to the front layers of the neural network - hence the name backpropagation. The deeper the network, the more information is lost due to gradient decay - low gradient values. The vanished gradient means that the network is not efficiently training and leads to poor performance. One way to combat that is to use special activation functions (Clevert et al.; Xu et al.; He et al., b) or special architectures (He et al., a) that deal with this problem.

2.3.6. Batch normalization

Normalizing input data before it enters the machine learning algorithm usually increases the performance of the algorithm. It is easier for the model to learn its task when all of its inputs will be in a certain range. Input normalization in CNNs that use images for input will not yield significant performance improvements because the input for images are normalized by nature in the range of 0 to 255 RGB values (2.1.5).

The second problem is the modularity of neural networks. Each layer feeds its outputs into the inputs of the next layer - making any input normalization futile. To combat this a new solution in a form of normalization layer has been introduced in 2015 called batch normalization (Ioffe i Szegedy). It normalizes the data for the whole minibatch that is used in the forward pass of the backpropagation algorithm (2.3.4). As the authors have showed, using batch normalization improves generalization, in some cases removes the need for dropout (2.3.2) and makes the neural network more robust to initial hyperparameter initialization.

3. Model

To make a scalable species classifier that works with specific hardware requirements I had to make a classifier that yields the best performance and could be trained on a GPU with 2GB of RAM in a reasonable time. In this chapter I introduce my solution based on the convolution neural network architecture ResNet (He et al., a).

3.1. Implementation

There are a plethora of computational frameworks to choose to create a deep learning model; TensorFlow (ten), Caffe2 (caf), pyTroc (pyt), Keras (ker), Theano (the), CNTK (cnt) and many more. I have chosen Keras as it has a high level API for creating neural networks and provides pretrained models (more on this in section 3.1.3) which was crucial to train a high accuracy model on a weak GPU. Keras allows the user to choose a backend deep learning framework, at the time of writing this thesis there were two options - TensorFlow and Theano. TensorFlow was chosen as it is newer and has gained a lot of popularity in the past couple of months.

3.1.1. Keras

Keras provides a high level of abstraction when creating neural networks, giving the user a framework for rapid iteration and development. A simple example of the high level API is given below. Using Keras we can create a two layered feed-forward neural network in just a couple of lines of code. The "create_model" function returns a model with two layers the first layer has 32 neurons, the second (also the last) has 10 - this means the classifier has 10 classes (the number of neurons in the last layer should always match the number of classes). The last layer uses the softmax activation function (see section 2.19 for more details) to get class probabilities. The model also defines to type of gradient descent algorithm (2.18) - RMSProp, and the loss function categorical cross entropy (2.20). The "train_model" function takes the created model

and trains it in 10 epochs with a minibatch size of 32 input data points (2.3.4).

```
from keras.layers import Dense

def get_data():
    ...
    return X_train, y_train

def create_model():
    model = Sequential()
    model.add(Dense(32, input_shape=(500,)))
    model.add(Dense(10, activation='softmax'))

    model.compile(optimizer='rmsprop',
                  loss='categorical_crossentropy',
                  metrics=['accuracy'])

    return model

def train_model(model, X_train, y_train):
    model.fit(X_train, y_train,
              batch_size=32, epochs=10)

X_train, y_train = get_data()
model = create_model()
train_model(model, X_train, y_train)
```

Listing 3.1: Keras high level API example

TensorFlow is the backend engine of Keras, and it, same as Keras, allows the user to write computational graphs in Python. Python is a high level language that allows the user for rapid development due to its simplicity. The ease of use of Python comes at the cost of performance, usually Python programs are an order of magnitude slower than programs written in lower abstraction languages such as Rust, C++ or Java. All computational graph frameworks mentioned above work blazingly fast, yet they use (mostly) Python to define the computational graph (neural network). The key to fast performance for these frameworks is that they are written and run in C++, but they offer a high-level API in Python. For this to work the API usually has a "compile" function that builds the graph and the "train" or "fit" function which starts the process of training the neural network.

Table 3.1: CNN architecture performance comparison on ImageNet dataset

Network	Top-1 error	Top-5 error
ResNet-18	30.24	10.92
ResNet-34	26.70	8.58
ResNet-50	23.85	7.13
ResNet-101	22.63	6.44
ResNet-152	21.69	5.94
Inception v3	22.55	6.44
AlexNet	43.45	20.91
VGG-11	30.98	11.37
VGG-13	30.07	10.75
VGG-16	28.41	9.62
VGG-19	27.62	9.12
SqueezeNet 1.0	41.90	19.58
SqueezeNet 1.1	41.81	19.38
Densenet-121	25.35	7.83
Densenet-169	24.00	7.00
Densenet-201	22.80	6.43
Densenet-161	22.35	6.20

3.1.2. Architecture

There are a lot high performance CNN architectures (He et al., a; Simonyan i Zisserman; Szegedy et al.), they offer different performance levels with varying parameter sizes, as shown in 3.1. To classify species on a 2GB GPU I needed a powerful yet small neural network. ResNet and Inception v3 are perfect for the task as they give a competitive performance per parameter ratio, especially the ResNet-50. Obviously, one can create its own architecture but doing that removes the performance boost of pretrained models, this is explained in more detail in a future section ???. The final architecture consisted of a base pretrained model with a feed-forward neural network on top of it. Two main candidates for the base network were the ResNet-50 and Inception v3 CNN architectures.

ResNet's performance comes from a unique way in which it builds layers. ResNet is short from residual neural network - residual is the input of a layer that is being summed to the layers output, giving input information a path for input to circumvent the layer's transformation. This method allows for very deep neural networks to con-

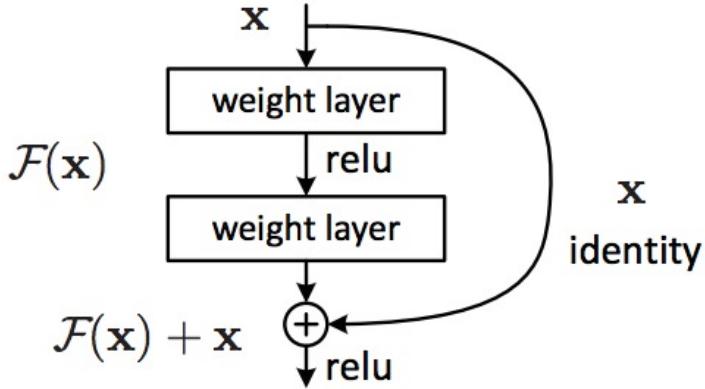


Figure 3.1: The residual layer (module) - the core building block of the ResNet

verge when trained. The residual can pass one layer or more, the architecture in the paper uses two convolution layers between each residual (figures 3.1 and 3.2).

Figure 3.2 shows a direct comparison between VGG and ResNet architectures. One of the main benefits of using ResNet is a lower memory consumption on the GPU because of the lack of fully-connected (dense) layers at the end of the network. The fully-connected layers contain the most parameters, and removing them increases the number of convolution layers while lowering the number of parameters.

Another mentioned CNN architecture is Inception v3. It uses an inception module (see figure 3.3) to increase the performance of the convolution layers in the neural network. The inception v3 architecture is composed of inception modules. The inception module consists of multiple convolution blocks, each with a different kernel size. This allows the inception module to gather multiple layers of abstraction in each module. The performance of ResNet-50 and Inception v3 is similar and after testing both, Inception v3 provided better results by a slight margin on this task. The full result are shown in section 5.

3.1.3. Pretrained parameters

As seen in figure 2.9, each convolution layer learns a specific level of abstraction. Those abstractions are general building blocks of images (boxes, circles, edges, etc.). This implies that if you train a CNN on one set of images, the parameters in the front convolution layers can be reused on a different task. Using this, higher accuracy can be achieved when working on small datasets. This is called pretraining or fine-tuning the model.

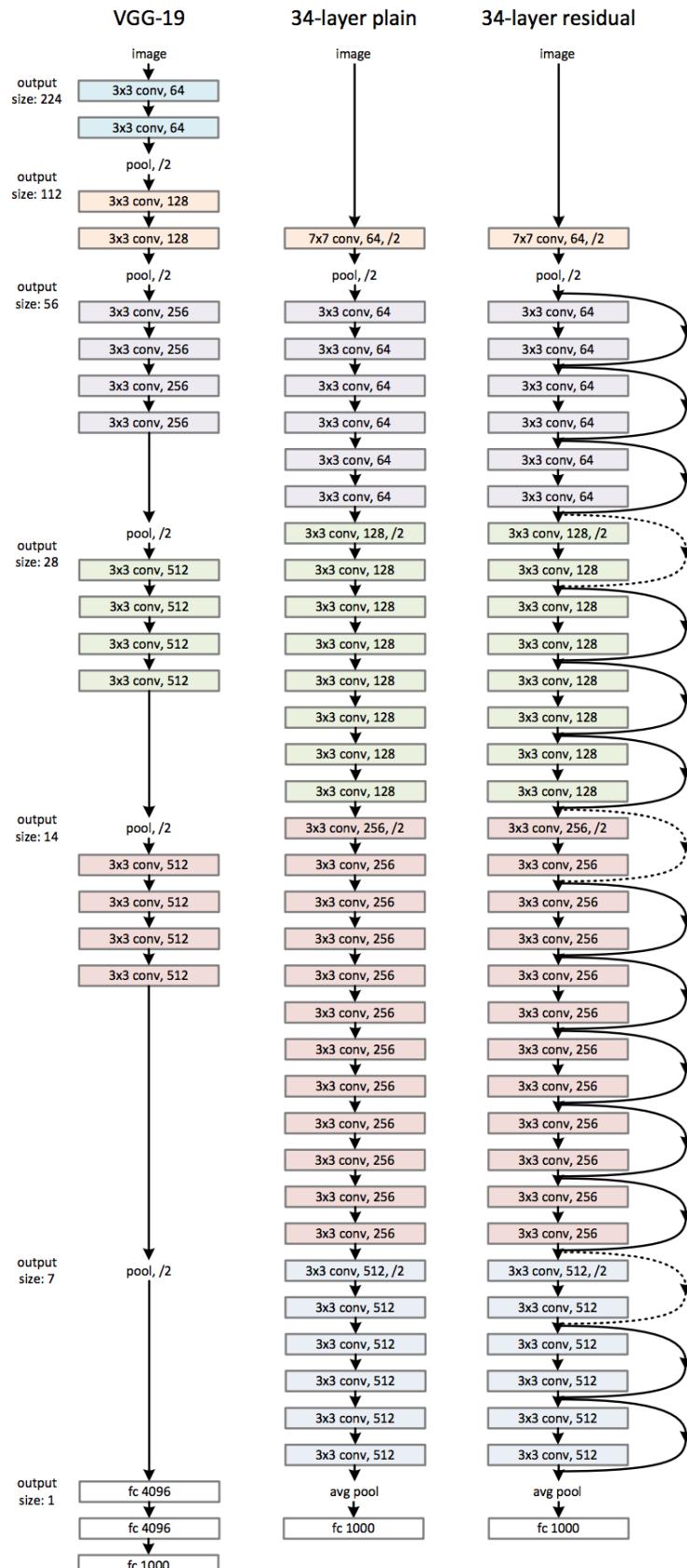


Figure 3.2: A comparison of two popular CNN architectures - ResNet and VGG

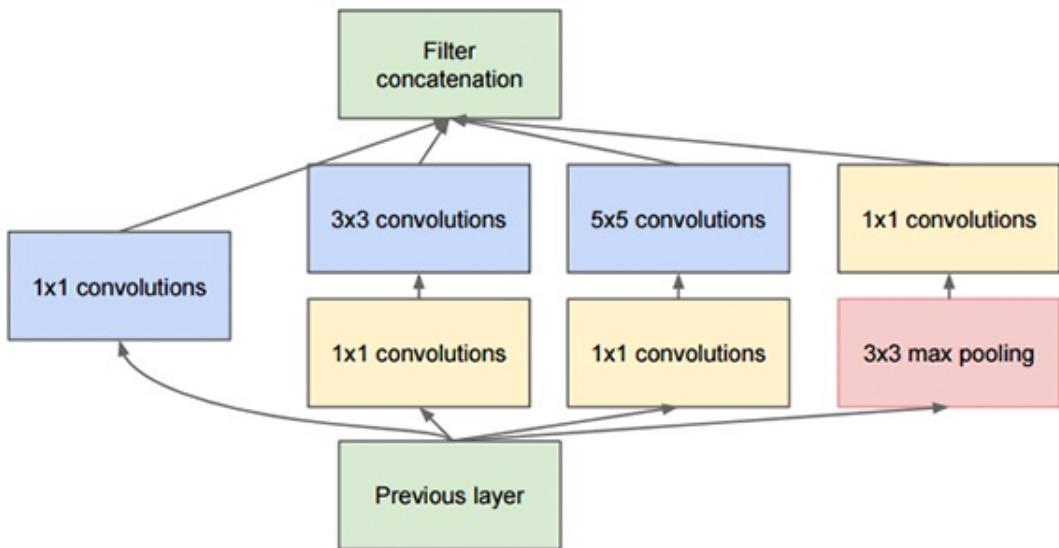


Figure 3.3: Inception v3’s inception module

One of the biggest labeled image databases is ImageNet (ima) and is the go to dataset for image classification research. Almost every modern CNN architecture was evaluated and trained on it. Downloading the parameters from those trained neural networks and initialising the model with them gives us state of the art performance even on small datasets. The only needed step is to fine-tune the neural network by training it on our dataset, after it was initialised with the pretrained values - fine tuning.

Below is the Keras code for creating a pretrained model from the ImageNet dataset. First, the pretrained model is loaded without the top layer (the top layer is not important as it is a fully-connected layer which was build for 1000 classes, the convolution layers are only needed for this task). The second step is to create a small feed-forward network and append it to the end of the network. Set the pretrained convolution layers to not train and compile to model. The final softmax layer has 15 neurons as the model was tested on a dataset of 15 classes that is 2GB in size. The model was trained with backpropagation using the Adam optimizer (Kingma i Ba).

```

from keras.applications import ResNet50

IMG_DIM = 224
INPUT_TENSOR = Input(shape=(IMG_DIM, IMG_DIM, 3))

base_model = ResNet50(input_tensor=INPUT_TENSOR, include_top=False)

```

```

top_model = Sequential()
top_model.add(Flatten(input_shape=base_model.output_shape[1:]))

top_model.add(Dense(32))
top_model.add(BatchNormalization())
top_model.add(Activation('relu'))

top_model.add(Dense(64))
top_model.add(BatchNormalization())
top_model.add(Activation('relu'))

top_model.add(Dense(15, activation='softmax'))


model = Model(input= base_model.input, output= top_model(
    base_model.output))

for layer in model.layers[:-8]:
    layer.trainable = False

model.compile(loss='categorical_crossentropy',
              optimizer='adam',
              metrics=['accuracy'])

```

Listing 3.2: Creating a custom pretrained ResNet on the ImageNet dataset

3.1.4. Improving generalization

To improve the generalization of the model, batch normalization was added after every fully-connected layer in the network. Also, the input images were augmented (2.3.3). The X_{test} had its images only rescaled, while X_{train} and $X_{validation}$ were more aggressively augmented (random zoom, horizontal flip, rescale and sheered), this is show in detail in the figure 2.14.

```

batch_size = 16

train_datagen = ImageDataGenerator(
    rescale=1./255,
    shear_range=0.2,
    zoom_range=0.2,

```

```
    horizontal_flip=True)

test_datagen = ImageDataGenerator(rescale=1./255)

train_generator = train_datagen.flow_from_directory(
    '../input/train',
    target_size=(150, 150),
    batch_size=batch_size,
    class_mode='categorical')

validation_generator = test_datagen.flow_from_directory(
    '../input/validation',
    target_size=(150, 150),
    batch_size=batch_size,
    class_mode='categorical')
```

Listing 3.3: Data augmentation of the input dataset (images)

4. Data

Many would argue that the data is the most important part of the machine learning system. If the training data does not represent the real world input of the system in production (as a product) the machine learning algorithm is good as useless. Furthermore, the quantity of data is crucial for deep learning algorithms. Compared to traditional machine learning algorithms, deep learning algorithms gain more performance scale from the dataset size. Therefore, data collection for this problem is a crucial step in the machine learning pipeline and impacts the whole solution.

4.1. ImageNet

One of the largest labeled image datasets freely opened to the public is ImageNet (ima). It contains more than 14 million images, detailed statistics of the dataset can be found in table 4.1. To train the model for species recognition I have used a subset of images found on ImageNet. Using every class that represents a species in ImageNet is not doable on a single 2GB GPU (atleast not in reasonable time), therefore I have manually picked 15 classes which represent the whole problem. The idea is to have some species that are similar to others, for example multiple species of ladybugs while still having a wide variate of species that represent the diverse form of life (typical example of an image from the ImageNet dataset can be seen in figure 4.1).

4.1.1. Dataset

As mentioned in the previous section, the dataset - X - consists of 15 species of images from the ImageNet dataset. Each species has a different number of samples, the distribution of X_{train} can be seen in detail in figure 4.2. We can see that some classes (Mexican bean beetle and Black-footed albatross) have below average number of images, this will yield a lower classification performance for these classes. Also, we can expect the classifier to work best for the classes with above average number of

Table 4.1: ImageNet statistics

High level category	synset (subcategories)	Avg images per synset	Total images
amphibian	94	591	56K
animal	3822	732	2799K
appliance	51	1164	59K
bird	856	949	812K
covering	946	819	774K
device	2385	675	1610K
fabric	262	690	181K
fish	566	494	280K
flower	462	735	339K
food	1495	670	1001K
fruit	309	607	188K
fungus	303	453	137K
furniture	187	1043	195K
geological formation	151	838	127K
invertebrate	728	573	417K
mammal	1138	821	934K
musical instrument	157	891	140K
plant	1666	600	999K
reptile	268	707	190K
sport	166	1207	200K
structure	1239	763	946K
tool	316	551	174K
tree	993	568	564K
utensil	86	912	78K
vegetable	176	764	135K
vehicle	481	778	374K
person	2035	468	952K



Figure 4.1: Typical ImageNet image, class herbivore

Table 4.2: Dataset statistics

Size [GB]	1.6
Class number	15
Type	RGB Images
Train size	14929
Validation size	1649

images like the Ice bear species. A deeper analysis on classification performance for certain classes will be shown in further sections.

The convolution network expects a fixed size input, therefore every image in the dataset - X - has to be scaled to a fixed size. Lowering the dimensions of the input image will result in a performance decrease. Therefore, after experimenting with the hyperparameter I have picked $224 * 224$ image dimensions in order to have the optimal classification and speed performance (this dimension is also the original ResNet input which is convenient).

4.1.2. Preprocessing

Preprocessing of data is an essential part of the machine learning pipeline. As stated in the previous section 4.1.1, every image has to be a fixed size in order to be able to serve as an input into the deep learning model. The fixed size that ended up working best with the pretrained Inception v3 was $224 * 224$. When scaling images to a fixed size sometimes because of the aspect ratio of the image we need to fill a part of the image with a constant pixel value.

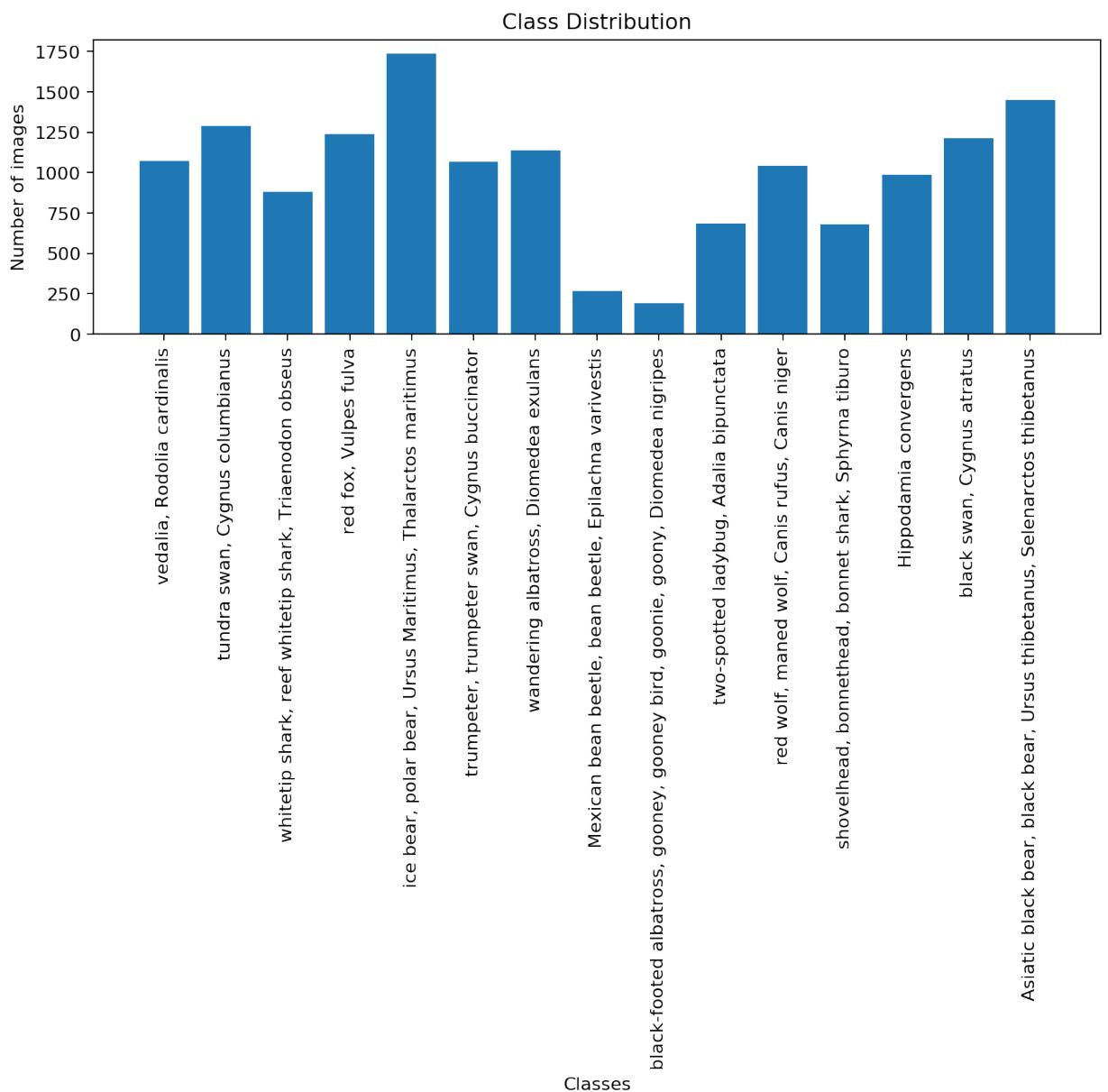


Figure 4.2: Class distribution of training data

Table 4.3: List of all 15 species used to train the model

Species (common name)	Species (Latin name)
whitetip shark, reef whitetip shark	Triaenodon obesus
shovelhead, bonnethead, bonnet shark	Sphyrna tiburo
tundra swan	Cygnus columbianus
trumpeter, trumpeter swan	Cygnus buccinator
black swan	Cygnus atratus
wandering albatross	Diomedea exulans
black-footed albatross, gooney, goonie, goony	Diomedea nigripes
red wolf, maned wolf	Canis rufus, Canis niger
red fox	Vulpes fulva
Asiatic black bear, black bear	Ursus thibetanus
ice bear, polar bear	Ursus Maritimus
two-spotted ladybug	Adalia bipunctata
Mexican bean beetle, bean beetle	Epilachna varivestis
convergent lady beetle	Hippodamia convergens
vedalia	Rodolia cardinalis

Also, another important part of the preprocessing is the generation of the validation dataset. For the validation to be efficient the validation dataset has to represent the training dataset. Keeping that in mind, the validation set - $X_{validation}$ - was created by taking 10% of images from each class (species).

4.2. Species

This chapter shows typical images found in the ImageNet dataset that were used as input for the model. The list of all 15 species used for model training is found in table 4.3.

Some of the species are shown in figure 4.3. Some species seem so similar that expert knowledge is needed (see figures 4.3g and 4.3h). These images can seem almost identical to an untrained eye while being different species, or not even close in the evolutionary tree. Neural networks with enough capacity have the ability to distinguish these traits on a level that is hard to interpret.

There is a lot of noise in the images found in X , animals are usually found in their habitat which makes them hard to be distinguished from their surroundings. This

can be seen in figure 4.3k, the *Canis rufus* is hidden and hard to see because of the color of his fur in regard to his surrounding.



Figure 4.3: Examples of species with a randomly picked image from the input dataset

5. Results

5.1. Hardware and software

The model is implemented in Keras 2.0.4 with Python 3.5. All the results were computed on my personal laptop with the following hardware and software specifications (see tables 5.1 and 5.4). All the software was chosen to support the given hardware specifications and to be able to efficiently build and train a deep learning model, explained in detail in chapter 3. Python is currently the leading language for deep learning, as well as TensorFlow and its higher-level framework Keras. All the programs were run inside Docker (doc) containers specifically made for the previously mentioned technology stack.

5.2. ResNet-50 and Inception v3 comparison

After deciding that ResNet-50 and Inception v3 were the best base CNN architectures for this task, testing was done to decide which one performed better. ResNet-50 had the better performance and was used as the final model, all the performance metrics are shown below (table 5.3)

Table 5.1: Hardware specifications

Hardware component	Specification
RAM	8GB DDR3
Dedicated GPU	Nvidia GTX 650m
Processor	Intel Core i7-3632QM 2.2GHz \ Turbo Boost 3.2GHz
Cuda cores	384
GPU Memory Bandwidth	80.0 GB/sec
Graphics Clock	Up to 900 MHz
Memory Interface	DDR3 \ GDDR5

Table 5.2: Software specifications

Software	Version
Operating System	Ubuntu 16.04 LTS
Python	64-bit version 3.5
Keras	2.0.4
TensorFlow	1.1

Table 5.3: ResNet-50 and Inception v3 architectures comparison

Metric	ResNet-50	Inception v3
Accuracy	0.83505	0.81807
Precision	0.80856	0.77996
Recall	0.80211	0.78006
F1	0.80311	0.77810

Table 5.4: Software specifications

Software	Version
Operating System	Ubuntu 16.04 LTS
Python	64-bit version 3.5
Keras	2.0.4
TensorFlow	1.1

5.3. Performance

In this section, different metrics and their impact on the performance of the model, as well as a detailed insight into the performance of the model is shown. The model is evaluated on a validation dataset that is created from 10% images of every class from the whole input dataset. The distribution of the data with more informations can be find the chapter 2.1.5.

Classification performance is shown in table 5.5 with metrics described in detail in section 2.1.4. This table shows a detailed outline of the overall classification performance of the model, but it fails to give insight into the classification performance on a class by class level. To resolve this problem, a confusion matrix is shown in figure 5.1. The confusion matrix shows that certain species are less likely to be confused with certain other species. The confusion matrix has a couple of clusters, the clusters appear to form near similar looking species. All the images of lady bug species look almost the same and it is natural to expect the classifier to have worst performance with these species, a potential method for increasing the performance for these species is giving the section 5.5.

This algorithm is designed so it should scale to thousands of species. To do so it must keep its accuracy even with different subsets of the original input dataset. To test this, the model was evaluated for different subsets of species - the result is shown in figure 5.2. The accuracy falls and raises for lower class numbers meaning that the model works well but the number of images per class has the biggest effect to the model performance. Building an ingestion platform for data collection, for example with web scraping, would significantly increase the performance of the model as most of the classes have around 1000 images which is considered relatively small for deep learning.

Quality of the dataset is also crucial for the model's performance as images that do not represent the class will lower the performance and make the training phase difficult. Collecting images that represent a class is difficult, collection high-quality images is even harder. Big companies usually have team's that annotate and collect data for machine learning algorithms and products.

5.4. Memory footprint

Using a pretrained model allows for faster training as the only parameters that change are the ones int he last layer of the network. Number of trainable and non-

Table 5.5: Classifier performance

Metrics	Value
Accuracy	0.83505
Precision	0.80856
Recall	0.80211
F1	0.80311

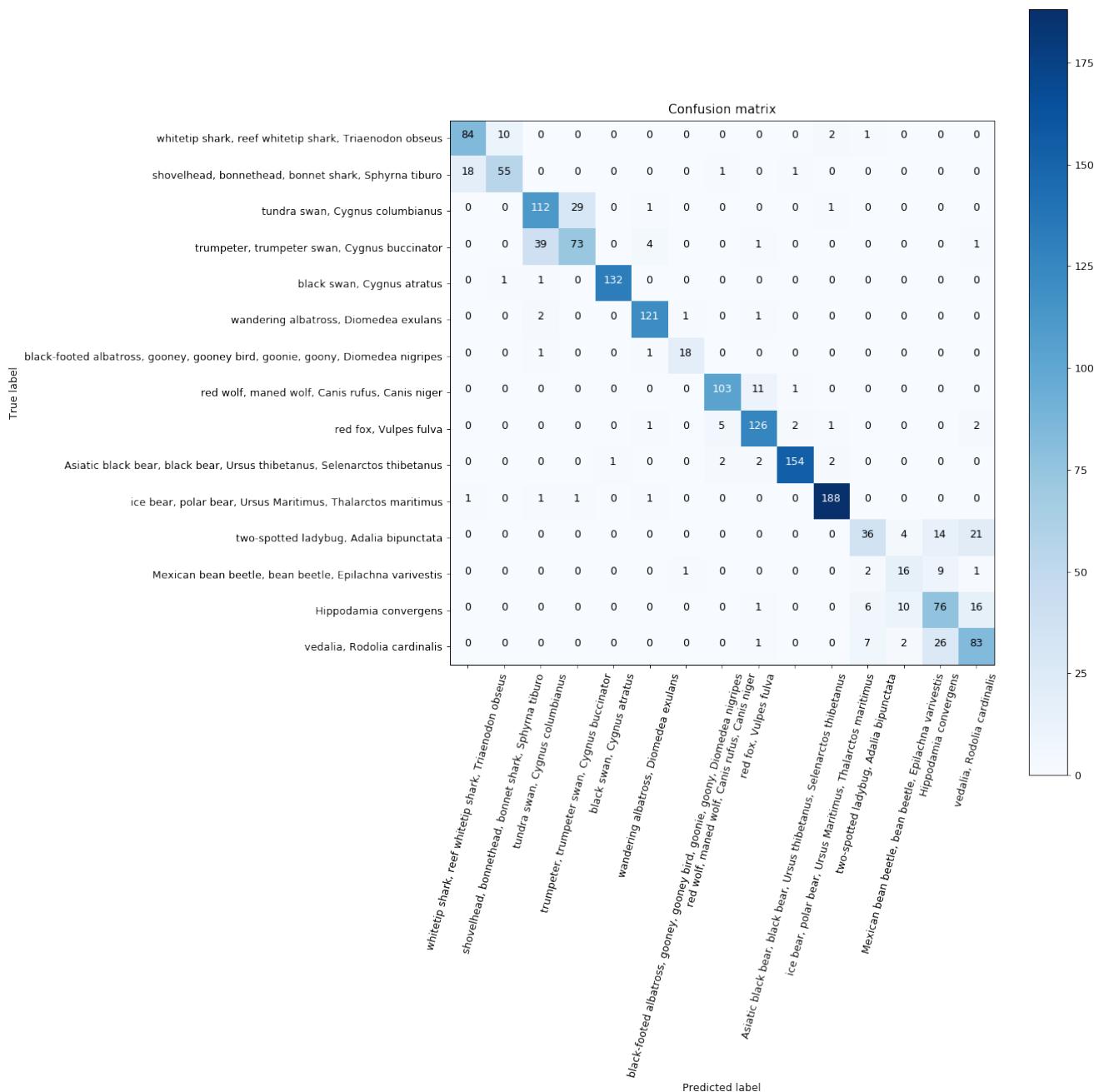


Figure 5.1: Confusion matrix generated on $X_{validation}$

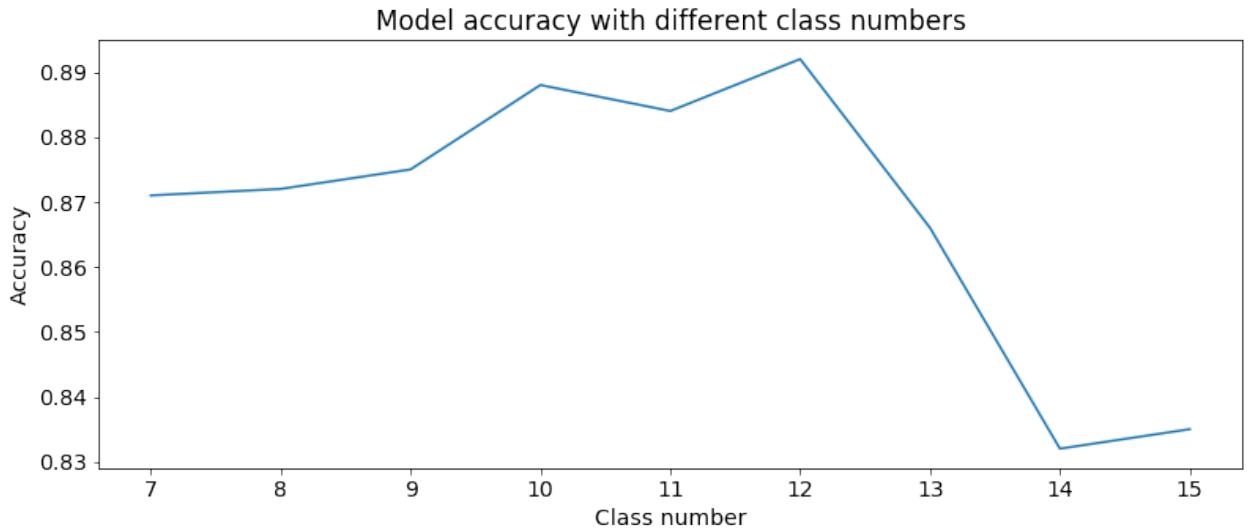


Figure 5.2: Model accuracy compared with different number of classes in $X_{validation}$

Table 5.6: Number of parameters

Parameters	Number
Trainable	23,534,592
Non-trainable	53,120
Total	23,587,712

trainable parameters can be found in table 5.6. TODO FIX THE NUMBER OF PARAMS IN THIS TABLE

Each parameter is a weight - 32-bit float number.

5.5. Future work

Firstly, getting better hardware and scaling the model to more than a thousand species is crucial for a reasonable product. Currently results give the information that the model is scalable and that the current flaw is in species that look similar.

The confusion matrix is able to give insight into which classes confuse the model. Using this information an algorithm can be made that combats those deficiencies. For example, building separate classifiers for each cluster in confusion matrix could yield better model performance. This is called a hierarchical convolution neural network (HD-CNN) as is a topic that is being currently research (Yan et al., b,a).

6. Conclusion

With the increase in high quality annotated data, and both, hardware and software improvements - deep learning model's will only get better. Also, with the abundance of high-level deep learning framework, the barrier to enter in the deep learning field is lowering each day. This will over time spur even more innovation and progress in the field. This can be seen already today - with new models, architectures, techniques being developed on a monthly basis.

It is expected for deep learning models to gain even higher accuracy on tasks that were previously considered difficult for computers - like visual recognition and natural language processing.

Keeping up with the pace of deep learning research is crucial as using and exploring new techniques usually yields the most competitive model performance. Also, with the increase of new techniques, a framework for rapid iteration and exploring is necessary for development of competitive performance models. Therefore, using Keras and similar frameworks allows a significant performance boost.

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Image Based Phylogenetic Classification

Sažetak

Sažetak na hrvatskom jeziku.

Ključne riječi: Ključne riječi, odvojene zarezima.

Title

Abstract

Abstract.

Keywords: Keywords.