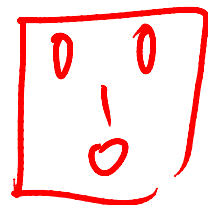


Some instructions on
assignment 4

Reference dataset



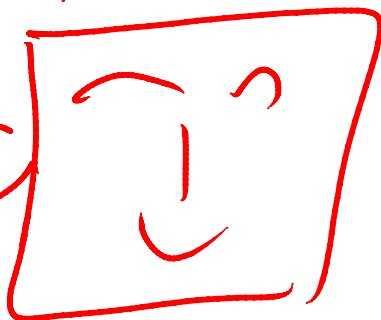
person A



person B

⋮

Test



$$\|V\|_1 = |v_1| + |v_2| + \dots + |v_D|$$

• Simplest way ^{NV} — template match

distance metrics

$$\|I_{\text{test}} - I_{\text{training}_i}\|_2^2$$

$\|I_{\text{test}} - I_{\text{training}_i}\|_1$
similarity metric

$$I_{\text{test}} \times I_{\text{training}_i}$$

$$\|V\|_2^2 = v_1^2 + v_2^2 + \dots + v_D^2$$

$$V = \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_D \end{bmatrix}$$

$$\{I_m\}_{m=1 \dots M}$$

$$\bar{I} = \frac{\sum_{m=1}^M I_m}{M}$$

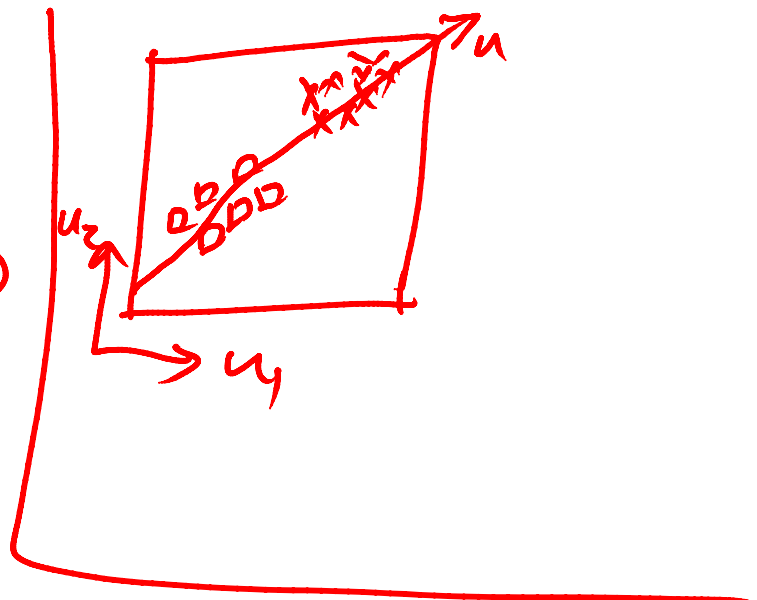
$$I_m \leftarrow I_m - \bar{I}$$

$I_{30 \times 40 \times 3}$ $D \approx 3600$

$$I = d_1 \cdot u_1 + d_2 u_2 + \dots + d_k \cdot u_k \quad k \ll D$$

$$\begin{bmatrix} I \end{bmatrix} = \underset{\uparrow}{d_1} \cdot \begin{bmatrix} u_1 \end{bmatrix} + \underset{\uparrow}{d_2} \cdot \begin{bmatrix} u_2 \end{bmatrix} + \dots + \underset{\uparrow}{d_k} \cdot \begin{bmatrix} u_k \end{bmatrix} \quad \text{e.g. } K=30$$

$$I \leftarrow \underline{[d_1, d_2, \dots, d_k]^T}$$



$\{I_i\}_{i=1 \dots M}$ training images.

$$A = \begin{bmatrix} | & | & \dots & | \\ I_1 & I_2 & & I_M \end{bmatrix}_{D \times M} \quad \text{e.g. } \begin{matrix} D=3600 \\ M=184 \end{matrix}$$

$$G_V = A A^T \quad \begin{matrix} D \times M & M \times D \\ \hline D \times D \end{matrix}$$

$$A^T A \quad \begin{matrix} M \times M \\ M \times D & D \times M \end{matrix}$$

$$B u = \lambda u$$

\uparrow eigenvalue \nwarrow eigenvector

$$[V, D] = \text{eig}(A A^T)$$

$\begin{bmatrix} | & \dots & | \\ \hline \end{bmatrix}_{D \times M} [V]$

$$(A A^T) u = \lambda u$$

(2)

$$u = A v$$

$$D \times M \quad M \times 1$$

$$\begin{bmatrix} | & \dots & | \\ \hline \end{bmatrix}_{D \times 1} = \begin{bmatrix} | & | & \dots & | \\ \hline \end{bmatrix}_{D \times M} \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_M \end{bmatrix}_{M \times 1}$$

$$\textcircled{1} (A^T A) v = \lambda' v$$

$m \times m$ ✓

$$(A A^T) A v = \lambda' A v$$

$$\underline{I = \alpha_1 u_1 + \alpha_2 u_2 + \dots + \alpha_k u_k + 0(\epsilon)}$$

$$u_i^T I = \alpha_1 \underbrace{u_i^T u_1}_{\substack{1 \\ |}} + \alpha_2 \underbrace{u_i^T u_2}_{\substack{0 \\ |}} + \dots + \alpha_k \underbrace{u_i^T u_k}_{\substack{0 \\ |}} = \alpha_i$$

$$\boxed{u_k^T I = \alpha_k}$$

$$I \leftarrow \underline{[\alpha_1, \alpha_2, \dots, \alpha_k]^T}$$

$$u_1^T u_1 = 1$$

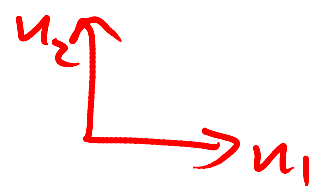
$$u_1^T u_2 = 0$$

\vdots

$$u_i^T u_j = \begin{cases} 1 & \text{if } i=j \\ 0 & \text{otherwise} \end{cases}$$

$$u_1 = (1, 0)$$

$$u_2 = (0, 1)$$



$$u_1^T u_1$$

$n_{\text{subject}} = 33$ in training data

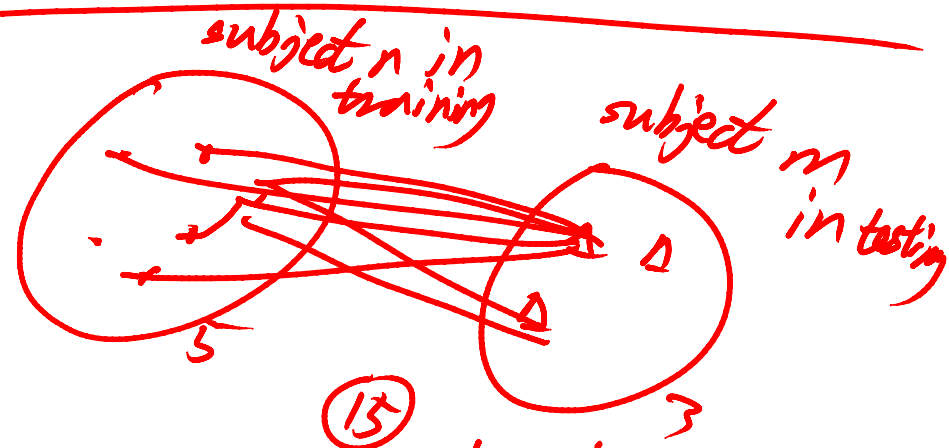
$n_{\text{Image}} = 184$

$n_{\text{subject}} = 27$ in testing data

$n_{\text{Image}} = \underline{249}$

•
$$\text{Accuracy} = \frac{\# \text{ matched image}}{\# \text{ test image}}$$

•
$$\text{Accuracy} = \frac{\# \text{ matched subjects}}{\# \text{ test subject}}$$



$$\text{dist}(m, n) = \min_{i \in I_m, j \in I_n} \text{dist}(i, j)$$