```
csc791sbse:hw4:Fu
Sep 23, 14 11:37
                                                                            Page 1/3
   from __future__ import division
   import sys, random, math
   from models import *
   from sk import *
5 from base import *
   import numpy as np
   from xtile import *
   sys.dont write bytecode = True
   @printlook
10 def sa(model):
     def P(old, new, t):
       prob = math.e**((old - new)/t)
       return prob
     min_energy, max_energy = model.baseline()
     s = model.generate_x()
     e = model.norm(model.getDepen(s))
     sb = s
     eb = e
     k = 1
     icontrol = Control(model)
20
     while k < Settings.sa.kmax:
       stopsign = icontrol.next(k) #true ---stop
       if stopsign:
         break
       sn = model.sa_neighbor(s)
       en = model.norm(model.getDepen(sn))
       icontrol.logxy(sn)
       temp = (k/Settings.sa.kmax)*Settings.sa.cooling
       if en < eb:</pre>
             sb = sn
30
             eb = en
             say('!')
       if en < e:
         s = sn
         e = en
35
          say('+')
        elif P(e, en, temp) < random.random():</pre>
         s = sn
         e = en
         say('?')
       say( '.')
       k = k + 1
       if k % 50 \equiv 0:
         print "\n"
         say(str(round(eb,3)))
45
     print "\n"
     printReport(model)
     print "\n----\n:Normalized Sum of Objectives: ",str(round(eb,3)), "\n:Solution",sn
     lohi=printRange(model)
     return eb, lohi
50
   @printlook
   def mws(model):
     min_energy, max_energy = model.baseline()
     total changes = 0
     total_tries = 0
     norm\_energy = 0
     eraScore = []
     control = Control(model)
     optimalsign = False
     solution = model.generate_x()
     norm_energy = model.norm(model.getDepen(solution))
     for k in range(Settings.mws.max_tries):
       total tries += 1
65
        for _ in range(Settings.mws.max_changes):
          stopsign = control.next(total_changes) #true ---stop
          if stopsign:
           break
          if norm_energy ≤ Settings.mws.threshold:
70
            optimalsign = True
           break
          if random.random()≤Settings.mws.prob:
```

```
csc791sbse:hw4:Fu
Sep 23, 14 11:37
                                                                              Page 2/3
            solution[random.randint(0,model.n-1)] = model.generate_x()[random.randin
   t(0,model.n-1)
            control.logxy(solution)
            sav("+")
          else:
            solution = model.mws neighbor(solution)
            control.logxy(solution)
80
            say("!")
          say(".")
          if total_changes % 50 \equiv 0:
            print "\n"
            say(str(round(model.norm(model.getDepen(solution)), 3)))
          total_changes +=1
85
        if optimalsign v k = Settings.mws.max_tries-1:
          say("\n")
          say(str(round(model.norm(model.getDepen(solution)), 3)))
         print "\n"
          print "total tries: %s" % total_tries
90
          print "total changes: %s" % total_changes
          print "min_energy:{0}, max_energy:{1}".format(min_energy, max_energy)
          print "min_energy_obtained: %s" % model.getDepen(solution)
          printReport(model)
          lohi =printRange(model)
          print "\n---
                       --\n:Normalized Sum of Objectives: ", str(round(norm_energy, 3)), "\n:Solution
   ", solution, "\n"
         return norm_energy, lohi
100 def printReport(m):
     for i, f in enumerate(m.log.y):
        \label{eq:print "} n < \!\! f\%s" \ \%i 
        for era in sorted(m.history.keys()):
          # pdb.set_trace()
          log = m.history[era].log.y[i]
          print str(era).rjust(7), xtile(log._cache, width = 33, show = "%5.2f", lo
   = 0, hi = 1)
   def printRange(m):
     lo = []
     lohi = []
      # print sorted(m.history.keys())
      for i, f in enumerate(m.log.y):
       tlo=10**5
       thi=-10**5
       for era in sorted(m.history.keys()):
115
          # pdb.set_trace()
          if m.history[era].log.y[i].lo < tlo:</pre>
            tlo= m.history[era].log.y[i].lo
          if m.history[era].log.y[i].hi > tlo:
           thi= m.history[era].log.y[i].hi
120
       lohi.append(tlo)
       lohi.append(thi)
     return lohi
       # print "\n the range of f%s is %s to %s " % (i, str(tlo), str(thi))
125
   def start(): #part 5 with part 3 and part4
     r = Settings.other.repeats
     rlohi=[] # stupid codes here, to be fixed
     f1lo = []
     f1hi = []
     f0lo = []
     f0hi =[]
      f2lo =[]
     f2hi =[]
      for klass in [Schaffer, Fonseca, Kursawe, ZDT1, ZDT3, Viennet3]:
       print "\n!!!!", klass.__name__
        for searcher in [sa, mws]:
         name = klass.__name__
         n = 0.0
140
          reseed()
          # scorelist = []
          for in range(r):
```

```
csc791sbse:hw4:Fu
Sep 23, 14 11:37
                                                                              Page 3/3
            x, lohi=searcher(klass()) # lohi is a list containing [lo,hi] paris of f
   1&£2
           #=====part 5======
145
            rlohi.append(lohi)
          for i in range(0, r):
            f0lo.append(rlohi[i][0])
            f0hi.append(rlohi[i][1])
            fllo.append(rlohi[i][2])
150
            flhi.append(rlohi[i][3])
            if name \equiv "Viennet3": # f1, f2, f3
              f2lo.append(rlohi[i][4])
              f2hi.append(rlohi[i][5])
          print "\n # The range of f0 during %s repeats is from %s to %s " \
155
                 % (r, str(round(sorted(f0lo)[0], 3)), str( round(sorted(f0hi)[-1]))
          print "\n # The range of f1 during %s repeats is from %s to %s " \
                 % (r, str(round(sorted(f1lo)[0],3)), str(round(sorted(f1hi)[-1])))
          if name ≡"Viennet3":
160
            print "\n # The range of f1 during %s repeats is from %s to %s "\
                 % (r, str(round(sorted(f2lo)[0],3)), str(round(sorted(f2hi)[-1])))
          rlohi = []
          #====part 5 ends======
165
          #the following codes for hw3
          \# n += float(x)
          # scorelist +=[float(x)]
          # print xtile(scorelist,lo=0, hi=1.0,width = 25)
          # print "# {0}:{1}".format(name, n/r)
170 @demo
   def part6():
     r = 5
      lastera = []
      searchcount = 0
     for klass in [ZDT1]:
print "\n!!!!", klass.__name__
        for searcher in [sa, mws]:
          reseed()
          for k in range(r):
            Settings.sa.cooling = rand() # get variants of sa, mws
180
            Settings.mws.prob = rand()
            Settings.mws.max_changes = int(1000*rand())
            model = klass()
            x, lohi = searcher(model)
            for i, f in enumerate(model.log.y):
185
              searchername = "mws" if searchcount else "sa"
              label = searchername + str(k) + "f%s" %i
              temp = (model.history[sorted(model.history.keys())[-1]].log.y[i]._cach
   e)
              temp = [ float(i) for i in temp]
190
              temp.insert(0,str(label))
              lastera.append(temp)
          rdivDemo(lastera)
          searchcount +=1
195
          lastera = []
   @demo
   def testmodel():
     # model = ZDT3()
      model = Schaffer()
     depen = model.getDepen(model.generate_x())
     print depen
   if __name__ = "__main__": eval(cmd())
205
210
```

```
csc791sbse:hw4:Fu
Sep 22, 14 23:50
                                                                             Page 1/4
    from __future__ import division
   from log import *
   import sys, random, math, datetime, time, re, pdb
   sys.dont write bytecode = True
   exp = math.e
   sgrt = math.sgrt
   sin = math.sin
10 pi = math.pi
   class Model:
     def name(i):
      return i.__class__.__name__
     def setup(i):
       i.xy = Options(x = [i.generate_x()], y = [i.f1, i.f2])
       i.log = Options(x = [ Num() for _ in range(i.n)], y = [ Num() for _ in range
    (i.fn)]) # hardcode 2
       i.history = {} # hold all logs for eras
     def generate_x(i):
       x= [i.lo + (i.hi-i.lo)*random.random() for _ in range(i.n)]
       return x
     def getDepen(i, xlst):
       # y = [i.f1, i.f2]
       return sum([f(xlst) for f in i.xy.y])
     def getDepenlst(i, xlst):
       return [f(xlst) for f in i.xy.y]
     def cloneModel(i): # from Dr.Menzies'
     return i.__class__()
def logxy(i, x):
       for val, log in zip(x, i.log.x): log += val
       y = i.getDepenlst(x)
     for val, log in zip(y, i.log.y): log += val
def better(news,olds): # from Dr.Menzies'
       def worsed():
                            ∧ ¬ betterIqr) ∨
         return ((same
                   (¬ same ∧ ¬ betterMed))
       def bettered():
         return ¬ same ∧ betterMed
40
       out = False
       for new,old in zip(news.log.y, olds.log.y):
         betterMed, same, betterIgr = new.better(old)
          # print betterMed, same, betterIqr
          # pdb.set_trace()
         if worsed() : return False # never any worsed
45
         if bettered(): out= out v True # at least one bettered
       return out
     def sa_neighbor(i, old):
       p = \overline{1}/i.n
       new = old
       for j in range(len(old)):
         if random.random() < p:</pre>
            new gen = i.generate x()
            old[j] = new_gen[random.randint(0, i.n-1)]
55
       return old
     def mws_neighbor(i,solution):
       optimized_index = random.randint(0, len(solution)-1)
        increment = (i.hi - i.lo)/10
       temp_min = 10*(5)
60 # print "old solution : %s" % solution
        for _ in range(10):
         solution[optimized_index] = i.lo + increment
          temp = i.norm(i.getDepen(solution))
         if temp < temp min:</pre>
            temp_min = temp
       print "new solution : %s" % solution
       return solution
     def baseline(i):
     # model = eval(model+"()")
       i.min = 10**(5)
70
       i.max = -10**(5)
       for in xrange(100000):
```

```
csc791sbse:hw4:Fu
Sep 22, 14 23:50
                                                                              Page 2/4
          temp = i.getDepen(i.generate_x())
          if temp > i.max:
           i.max = temp
          if temp < i.min:</pre>
                i.min = temp
        return i.min, i.max
     def norm(i, x):
            e = (x - i.min)/(i.max - i.min)
            return max(0, min(e,1)) #avoid values <0 or >1
   class Control(object): # based on Dr. Menzies' codes
     def __init__(i, model):
       i.kmax = Settings.sa.kmax
       i.era = Settings.other.era
       i.lives = Settings.other.lives
       i.logAll = \{\}
       i.model = model
     def __call__(i, k):
        i.next(k)
     def logxy(i, results):
       both = [i.model.history, i.logAll]
        for log in both:
          if ¬ i.era in i.logAll:
            log[i.era] = i.model.cloneModel()
        for log in both:
          log[i.era].logxy(results)
     def checkimprove(i):
          if len(i.logAll) ≥ 2:
100
            current = i.era
           before = i.era - Settings.other.era
currentLog = i.logAll[current]
            beforeLog = i.logAll[before]
            # pdb.set_trace()
105
            if ¬ currentLog.better(beforeLog):
             pass
            else:
              i.lives += 1
     def next(i, k):
       if k ≥ i.era:
          i.checkimprove()
          i.era +=Settings.other.era
          if i.lives \equiv 0:
           return True
115
          else:
            i.lives -=1
            return False
120
   '' Schaffer''
   class Schaffer(Model):
     def __init__(i):
       i.lo = -2
       i.hi = 2
       i n = 1
       i.fn = 2
       i.setup()
     def f1(i, x):
       return x[0] * x[0]
     def f2(i, x):
       return (x[0]-2) ** 2
135 ' ' ' Fonseca' ' '
   class Fonseca(Model):
     def __init__(i):
       i.lo = -4
       i.hi = 4
       i.n = 3
140
       i.fn = 2
       i.setup()
       return (1 - \exp^{**}(-1 * sum([(xlst[k] - 1/sqrt(i.n)))**2 for k in xrange(i.n)]
```

models.py

```
csc791sbse:hw4:Fu
Sep 22, 14 23:50
                                                                                  Page 3/4
      def f2(i, xlst):
        return (1 - \exp^{**}(-1 * \operatorname{sum}([(\operatorname{xlst}[k] + 1/\operatorname{sqrt}(i.n))^{**}2 \text{ for } k \text{ in } \operatorname{xrange}(i.n)]
   ))))
    ''' Kusarvs'''
   class Kursawe(Model):
     def __init__(i):
        i.lo = -5
        i.hi = 5
        i.n = 3
        i fn = 2
        i.setup()
      def f1(i, xlst):
        return sum([-10*exp**(-0.2 * sqrt(xlst[k]**2 + xlst[k+1]**2))) for k in xrang
   e(i.n -1)])
      def f2(i, xlst):
        a = 0.8
        b = 3
160
        return sum([abs(x)**a + 5*sin(x)**b for x in xlst])
    '''ZDT1'''
   class ZDT1(Model):
     def __init__(i):
       i.lo = 0
        i.hi = 1
        i.n = 30
        i.fn = 2
        i.setup()
170
      def f1(i, xlst):
        return xlst[0]
      def g(i, xlst):
        return (1 + 9 * (sum(xlst[1:]))/(i.n-1))
      def f2(i,xlst):
        q1 = i.q(xlst)
        return g1*(1-sqrt(xlst[0]/g1))
    '''ZDT3'''
180 class ZDT3(Model):
      def ___init___(i):
        i.lo = 0
        i.hi = 1
        i.n = 30
       i.fn = 2
185
        i.setup()
      def f1(i, xlst):
       return xlst[0]
      def g(i, xlst):
       return (1 + (9/(i.n-1)) * sum(xlst[1:]))
190
      def h(i,f1,g):
       return (1 - sqrt(f1/g) - f1/g) * sin(10 * pi * f1)
      def f2(i, xlst):
        return i.g(xlst) * i.h(i.f1(xlst),i.g(xlst))
195
    ''' Viennet3'''
   class Viennet3(Model):
      def __init__(i):
       i.lo = -3
        i.hi = 3
        i.n = 2
        i.fn = 3
        i.setup1()
      def setup1(i):
       i.xy = Options(x = [i.generate_x()], y = [i.f1, i.f2, i.f3])
i.log = Options(x = [ Num() for _ in range(i.n)], y = [ Num() for _ in range
    (i.fn)]) # hardcode 2
        i.history = {} # hold all logs for eras
      def fl(i, xlst):
        xy2 = xlst[0]**2 + xlst[1]**2
        return 0.5* (xy2) + sin(xy2)
      def f2(i, xlst):
        x = xlst[0]
        y = xlst[1]
        return ((3*x -2*y +4)**2/8 + (x-y+1)**2/27 + 15)
```

```
Printed by Wei Fu
                               csc791sbse:hw4:Fu
Sep 22, 14 23:50
                                                                       Page 4/4
     def f3(i, xlst):
      xy2 = xlst[0]**2 + xlst[1]**2
       return (1/(xy2+1) - 1.1* exp**(-xy2))
```

```
csc791sbse:hw4:Fu
Sep 23, 14 11:37
                                                                                                          Page 1/2
     from __future__ import division
     import sys, random, math
     from base import *
     from al2 import *
5 sys.dont_write_bytecode = True
     '''All these are based on Dr.Menzies' tricks A sample codes'''
10 class Log():
      def __init__(i, tolog = []):
i._cache, i.n, i._report = [], 0, None
       i.setup()
       map(i.__iadd__, tolog)
      def __iadd__(i, tolog):
       if tolog == None: return tolog
       i.n += 1
       updated = False
       if len(i._cache) < Settings.other.keep:
       i._cache +=[tolog]
20
        updated = True
       else:
        if rand() <= Settings.other.keep/i.n:
  i._cache[int(rand()*Settings.other.keep)] = tolog
          updated = True
       if updated:
        i._report = None
        i.updateLoHi(tolog)
       return i
      def has(i):
       if i._report == None:
        i._report = i.report()
       return i._report
    class Num(Log):
      def setup(i):
       i.lo = 10**5
       i.hi = -10**5
      def updateLoHi(i,x):
       i.lo = min (i.lo, x)
       i.hi = max(i.hi, x)
      def median(i):
       n = len(i\_cache)
       p = n//2
      if (n % 2) : return i._cache[p]
       q = p + 1
       q = max(0, min(q,n))
       return (i._cache[p] + i._cache[q])/2
      def better(new,old):
       "better if (1)less median or (2)same and less igr"
       t = Settings.other.a12
       betterIqr = new.has().iqr < old.has().iqr
       new.lessp = False
       if new.lessp:
        betterMed = new.has().median >= old.has().median
        same = a12(old._cache, new._cache) <= t
       else:
        betterMed = new.has().median <= old.has().median
        same = a12(new._cache, old._cache) <= t
       return betterMed, same, betterIqr
      def report(i):
       sortedCache = sorted(i._cache)
       n = len (sortedCache)
       return Options(
           median = i.median(),
65
           iqr = sortedCache[int(n*0.75) - int(n*0.5)],
           10 = i.10.
           hi = i.hi
70 @demo
     def demoNum():
      for size in [16,32, 64,128, 256]:
       Settings.other.keep = size
```

```
csc791sbse:hw4:Fu
Sep 23, 14 11:37
                                                                                         Page 2/2
      log = Num()
      for x in xrange(100000): log +=x
      print size, ":", log.has().median
80 if __name__ == "__main__": eval(cmd())
```

6/9

```
csc791sbse:hw4:Fu
Sep 22, 14 23:59
                                                                                 Page 1/2
    from __future__ import division
    import sys, random, math, datetime, time, re
    sys.dont_write_bytecode = True
5 rand= random.random
    class Options: #"Thanks for Peter Norvig's trick"
      def __init__(i, **d): i.__dict__.update(d)
    Settings = Options(sa = Options(kmax = 1000,
                                             baseline = 1000,
                                      score = {},
                                      cooling = 0.5),
15
                        mws = Options(threshold = 0.0001,
                                      max\_tries = 20,
                                      max changes = 1000,
                                      prob = 0.25,
                                      score = {}
20
                        other = Options(keep = 128,
                                          era = 50,
                                          lives = 3,
                                          a12 = [0.56, 0.64, 0.71][0],
                                          repeats = 1))
   def atom(x):
      try : return int(x)
      except ValueError:
        try : return float(x)
        except ValueError : return x
30
    def cmd(com="demo('-h')"):
      "Convert command line to a function call."
      if len(sys.argv) < 2: return com</pre>
     def strp(x): return isinstance(x,basestring)
def wrap(x): return "'%s'"%x if strp(x) else str(x)
      words = map(wrap,map(atom,sys.argv[2:]))
return sys.argv[1] + '(' + ','.join(words) + ')'
40 def demo(f=None,cache=[]):
      def doc(d):
        return '#'+d.__doc__ if d.__doc__ else ""
      if f \equiv '-h':
        print '# sample demos'
        for n,d in enumerate(cache):
          print '%3s)' %(n+1),d.func_name,doc(d)
      elif f:
        cache.append(f);
      else:
        s='|'+'='*40 + ' n'
50
        for d in cache:
          print '\n==|',d.func_name,s,doc(d),d()
      return f
55 def reseed():
            seed = 1
            return random.seed(seed)
    def say(mark):
      sys.stdout.write(mark)
      sys.stdout.flush()
   def printlook(f):
      def wrapper(*lst): #tricks from Dr.Menzies
        ShowDate = datetime.datetime.now().strftime
65
        print "\n###", f.__name__, "#" * 50
        print "#", ShowDate("%Y-%m-%d%H:%M:%S")
        beginTime = time.time()
        x = f(*lst)
        endTime = time.time()
70
        print "\n" +("-"*60)
        dump(Settings, f.__name__)
        print "\n# Runtime: %.3f secs" % (endTime-beginTime)
```

csc791sbse:hw4:Fu Sep 22, 14 23:59 Page 2/2 return x # return the searcher name and the results return wrapper def dump(d, searchname, lvl = 0): # tricks from Dr. Menzies d = d if isinstance(d, dict) else d.__dict_ callableKey, line, gap = [], "", " "*lvl for k in sorted(d.keys()): val= d[k] if isinstance(val, (dict, Options)): callableKey += [k] else: #if callable(val): # val = val.__name line $+=(" \{0\}:\{1\}".format(k, val))$ print gap + line for k in callableKey: **if** $k \equiv \text{searchname} \lor k \equiv "\text{other}"$: print gap + (":{0} {1}".format(k, "options")) dump(d[k], lvl+1)

```
csc791sbse:hw4:Fu
Sep 22, 14 23:50
                                                                               Page 1/1
   from __future__ import division
   import sys, random, math, datetime, time, re, pdb
   sys.dont_write_bytecode = True
   def pairs(lst):
      last=lst[0]
      for i in lst[1:]:
       vield last,i
       last = i
   def xtile(lst,lo=0,hi=0.001, width = 50,
                 chops=[0.1 ,0.3,0.5,0.7,0.9],
                 marks=["-" ," "," ","-"," "],
bar="|",star="*",show="%3s"):
15
      " " "The function _xtile_ takes a list of (possibly)
    unsorted numbers and presents them as a horizontal
    xtile chart (in ascii format). The default is a
    contracted _quintile_ that shows the
    10,30,50,70,90 breaks in the data (but this can be
    changed- see the optional flags of the function).
      # ordered_list = sorted(lst) # Dr.Menzies tricks
     # lo = min(lo, ordered_list[0])
     # hi = max(hi, ordered_list[-1])
      # showNumbers = [ ordered_list[int(percent * len(lst))] for percent in chops]
      # # print showNumbers
      # showMarks = [" "] * width
      # def find_index (x):
     # return int(width*float((x-lo))/(hi-lo))
      # markIndex = [find_index(i) for i in showNumbers]
      # for i in range(width):
      # if i in range(markIndex[0],markIndex[1]+1) or i in range(markIndex[-2],mar
   kIndex[-1]+1):
           showMarks[i] = "-"
      # #print showMarks
      # showMarks[int(width * 0.5)] = "|"
      # showMarks[find_index(ordered_list[int(len(lst)*0.5)])] = "*"
      # return " ".join(showMarks) + ", ".join([show %str(round(i,3)) for i in showN
   umbers])
      def pos(p)
                  : return ordered[int(len(lst)*p)]
     def place(x) :
       return int(width*float((x - lo))/(hi - lo+0.00001))
      def pretty(lst) :
       return ', '.join([show % x for x in lst])
      ordered = sorted(lst)
            = min(lo,ordered[0])
     hi
             = max(hi,ordered[-1])
      what
             = [pos(p) for p in chops]
     where = [place(n) for n in what]
             = [""] * width
     for one, two in pairs (where):
       for i in range(one, two):
          out[i] = marks[0]
       marks = marks[1:]
      out[int(width/2)]
                            = bar
     out[place(pos(0.5))] = star
      return ''.join(out) + "," + pretty(what)
60 def Demo():
      import random
      random.seed(1)
      # nums = [random.random()**2 for _ in range(100)]
      \#nums = [0.011, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01]
     nums = [0,0.1,0.1,0.6,0.4,0.1,0.9,0.1,0.1,3]
      line = ' '*26+'='*23
      print ('%29s, %3s, %3s, %3s, %3s' % ('10%', '30%', '50%', '70%', '90%'))+'\n'+line
      print xtile(nums, lo=0, hi=1.0, width=25,)
   if name = " main ": Demo()
```

```
csc791sbse:hw4:Fu
Sep 23, 14 11:37
                                                                               Page 1/1
   from __future__ import division
   import sys
   sys.dont_write_bytecode = True
   from base import *
   def ab12():
     def a12slow(lst1.lst2):
       more = same = 0.0
       for x in sorted(lst1):
          for y in sorted(lst2):
            if x≡y :
              same += 1
            elif x > y:
             more += 1
15
       return (more + 0.5*same) / (len(lst1)*len(lst2))
      random.seed(1)
     11 = [random.random() for x in range(5000)]
more = [random.random()*2 for x in range(5000)]
      12 = [random.random() for x in range(5000)]
     less = [random.random()/2.0 for x in range(5000)]
      for tag, one,two in [("lless",l1,more),
                            ("lmore", more, less), ("same", 11, 12)]:
        t1 = msecs(lambda : a12(11,less))
       t2 = msecs(lambda : a12slow(l1,less))
       print "\n",tag,"\n",t1,a12(one,two)
25
       print t2, a12slow(one, two)
   def a12(lst1,lst2):
      " " "how often is lst1 often more than y in lst2?
30 assumes lst1 nums are meant to be greater than lst2 " " "
     def loop(t,t1,t2):
        while t1.m < t1.n \wedge t2.m < t2.n:
         h1 = t1.1[t1.m]
          h2 = t2.1[t2.m]
         h3 = t2.1[t2.m+1] if t2.m+1 < t2.n else None
35
          if h1 > h2:
           t1.m += 1; t1.gt += t2.n - t2.m
          elif h1 \equiv h2:
            #if h3 and gt(h1,h3) < 0: original bugs
            if h3 ∧ h1 > h3:
               t1.gt += t2.n - t2.m - 1
            t1.m += 1; t1.eq += 1; t2.eq += 1
          else:
            t2,t1 = t1,t2
       return t.gt*1.0, t.eq*1.0
45
      lst1 = sorted(lst1,reverse=True)
     lst2 = sorted(lst2,reverse=True)
     n1 = len(lst1)
     n2 = len(lst2)
      t1 = Options(l=lst1,m=0,eq=0,gt=0,n=n1)
      t2 = Options(l=1st2, m=0, eq=0, gt=0, n=n2)
     gt,eq=loop(t1, t1, t2)
      return gt/(n1*n2) + eq/2/(n1*n2)
55
   if __name__ = "__main__": eval(cmd())
```