

## List 04. AR with GARCH effects

Nikita V. Artamonov

November 22, 2024

#1. Consider historical data on log-return of US GDP (quarterly data) from 1990 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?

#2. Consider historical data on log-return of US M2 (monthly data) from 1995 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?

#3. Consider historical data on log-return of US M2 (weekly data) from 2000 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?

#4. Consider monthly data on first difference of 10-years rate from 1995 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?

#5. Consider weekly data on first difference of 10-years rate from 1995 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

- Which model is preferable due to information criterions?
- Perform cross-validation for the models. Which one is preferable?

#6. Consider monthly data on first difference on 3-month treasury bill from 1995 to nowadays.

- Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

- Which model is preferable due to information criterions?
- Perform cross-validation for the models. Which one is preferable?

#7. Consider weekly data on first difference on 3-month treasury bill from 1995 to nowadays.

- Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?

#8. Consider log-return of daily observations on S&P500 from 2010 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?

#9. Consider log-return of monthly data (end of month) on S&P500 from 2010 to nowadays.

1. Fit the following AR-GARCH(p,o,q) models

Model	$\lambda$
AR(1)-GARCH(1,0,1)	2
AR(1)-GARCH(1,0,1)	1
AR(2)-GARCH(1,0,1)	2
AR(2)-GARCH(1,0,1)	1

and evaluate 10 periods forward forecasts for  $y$  and for its volatilities.

2. Which model is preferable due to information criterions?
3. Perform cross-validation for the models. Which one is preferable?