

F14076083 魏湧致

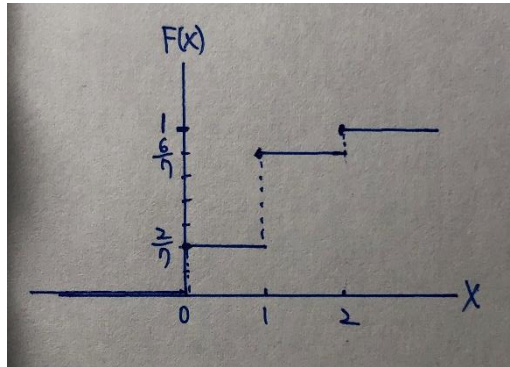
3.6

$$(a) P(X > 200) = \int_{200}^{\infty} \frac{20000}{(x+100)^3} dx = -\frac{10000}{(x+100)^2} \Big|_{200}^{\infty} = \frac{10000}{90000} = \frac{1}{9}$$

$$(b) P(80 < X < 120) = \int_{80}^{120} \frac{20000}{(x+100)^3} dx = -\frac{10000}{(x+100)^2} \Big|_{80}^{120} = \frac{10000}{180^2} - \frac{10000}{220^2} \approx 0.10203$$

3.16

$$F(x) = \begin{cases} 0, & \text{when } x < 0 \\ 2/7, & \text{when } 0 \leq x < 1 \\ 6/7, & \text{when } 1 \leq x < 2 \\ 1, & \text{when } x \geq 2 \end{cases}$$



3.24

$$f(x) = \frac{\binom{5}{x} \binom{2+3}{4-x}}{\binom{5+2+3}{4}} = \frac{\binom{5}{x} \binom{5}{4-x}}{\binom{10}{4}}, \quad x=0,1,2,3,4$$

3.36

$$(a) P(X < 0.5) = \int_0^{0.5} 2(1-x) dx = 2x - x^2 \Big|_0^{0.5} = 0.75$$

$$(b) P(X > 0.4) = 2x - x^2 \Big|_{0.4}^1 = 0.36$$

$$(c) P(X < 0.7 \mid X \geq 0.5) = \frac{P(0.5 \leq X < 0.7)}{P(X \geq 0.5)} = \frac{2x - x^2 \Big|_{0.5}^{0.7}}{2x - x^2 \Big|_{0.5}^1} = \frac{0.16}{0.25} = \frac{16}{25}$$

3.40

$$(a) g(x) = \int_0^{1/2} \frac{2}{3} (x + 2y) dy = \frac{2}{3} (xy + y^2) \Big|_{y=0}^{y=1/2} = \frac{2}{3} (x + 1), \text{ for } 0 \leq x \leq 1,$$

and  $g(x) = 0$  elsewhere

$$(b) h(y) = \int_0^{1/2} \frac{2}{3} (x + 2y) dx = \frac{2}{3} \left( \frac{x^2}{2} + 2xy \right) \Big|_{x=0}^{x=1/2} = \frac{2}{3} \left( \frac{1}{2} + 2y \right), \text{ for } 0 \leq y \leq 1,$$

and  $h(y) = 0$  elsewhere

$$(c) P(X < \frac{1}{2}) = \int_0^{1/2} \frac{2}{3} (x + 1) dx = \frac{2}{3} \left( \frac{x^2}{2} + x \right) \Big|_{x=0}^{x=1/2} = \frac{5}{12}$$

3.50

(a)

x	2	4
g(x)	$0.1+0.2+0.1 = 0.4$	$0.15+0.3+0.15 = 0.6$

(b)

Y	1	3	5
h(y)	$0.1+0.15 = 0.25$	$0.2+0.3 = 0.5$	$0.1+0.15 = 0.25$