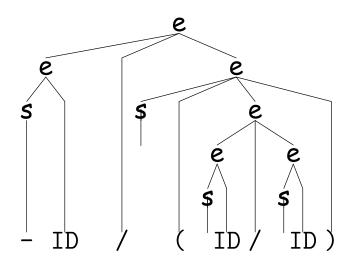
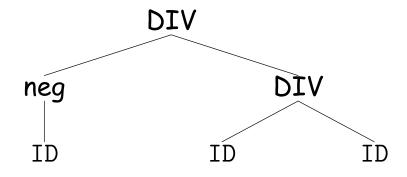
Lecture 5: ASTs, Top-Down Parsing

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Abstract Syntax Trees

- Lecture 4 introduced the concept of a parse tree, such as the one on the left, below.
- However, this contains various artifacts of the concrete syntax: e.g., parentheses and empty sign (s) nodes.
- For the implementer, it is generally more convenient to work with an abstract syntax tree (AST), such as on the right, below.





Making ASTs

- The AST abstracts away the grammar details that are there for parsing, leaving the information needed by the rest of the compiler.
- Rather uniquely, Lisp programs themselves already are ASTs, as one would represent them in Lisp!
- For most languages, some non-trivial translation is needed. Syntaxdirected translation makes this easy.
- Examples (using CUP metasyntax). Semantic values are ASTs:

```
{: RESULT = t; :}
expr ::= term:t
| term:t '/' factor:f {: RESULT = makeTree(DIV, t, f); :}
              {: RESULT = i; :}
factor ::= ID:i
```

New Topic: Beating Grammars into Programs

- A BNF grammar looks like a recursive program. Sometimes it works to treat it that way.
- Assume the existence of
 - A function 'next' that returns the syntactic category of the next token (without side-effects);
 - A function 'scan(C)' that checks that the next syntactic category is C and then reads another token into next(). Returns the previous value of next().
 - A function ERROR for reporting errors.
- \bullet Strategy: Translate each nonterminal, A, into a function that reads an A according to one of its productions and returns the semantic value computed by the corresponding action.
- Result is a recursive-descent parser.

```
def prog ():
                       def sexp ():
prog ::= sexp '⊢'
                          elif _____ :
sexp ::= atom
      | '(' elist ')'
                          else:
      | '\'' sexp
elist ::= \epsilon
       | sexp elist
                       def atom ():
atom ::= SYM
                          if :
       l NUM
       | STRING
                          else:
                       def elist ():
                          if :
```

```
def prog ():
                           sexp(); scan(\dashv)
                         def sexp ():
prog ::= sexp '⊢'
                           elif _____ :
sexp ::= atom
      | '(' elist ')'
                           else:
      | '\', sexp
elist ::= \epsilon
        | sexp elist
                         def atom ():
atom ::= SYM
                           if :
       l NUM
       | STRING
                           else:
                         def elist ():
                           if ____:
```

```
def prog ():
                           sexp(); scan(\dashv)
                        def sexp ():
                           if next() in [SYM, NUM, STRING]:
prog ::= sexp '⊢'
                            atom()
sexp ::= atom
                           elif :
      | '(' elist ')'
                           else:
      | '\', sexp
elist ::= \epsilon
        | sexp elist
                        def atom ():
atom ::= SYM
                           if :
       l NUM
       | STRING
                           else:
                        def elist ():
                           if :
```

```
def prog ():
                              sexp(); scan(\dashv)
                           def sexp ():
                              if next() in [SYM, NUM, STRING]:
prog ::= sexp '⊢'
                                 atom()
                              elif \underline{next()} == '('):
sexp ::= atom
                                 scan('('); elist(); scan(')')
       | '(' elist ')'
                              else:
       | '\'' sexp
elist ::= \epsilon
         | sexp elist
                           def atom ():
atom ::= SYM
                              if :
        l NUM
        | STRING
                              else:
                           def elist ():
                              if :
```

```
def prog ():
                               sexp(); scan(\dashv)
                            def sexp ():
                               if next() in [SYM, NUM, STRING]:
prog ::= sexp '⊢'
                                  atom()
                               elif \underline{\text{next}()} == '('):
sexp ::= atom
                                  scan('('); elist(); scan(')')
       | '(' elist ')'
                               else:
       | '\', sexp
                                  scan('\','); sexp()
elist ::= \epsilon
         | sexp elist
                            def atom ():
atom ::= SYM
                               if :
        l NUM
        | STRING
                               else:
                            def elist ():
                               if :
```

```
def prog ():
                                sexp(); scan(\dashv)
                             def sexp ():
                                if next() in [SYM, NUM, STRING]:
prog ::= sexp '⊢'
                                   atom()
                                elif \underline{next()} == '('):
sexp := atom
                                   scan('('); elist(); scan(')')
       | '(' elist ')'
                                else:
        | '\'' sexp
                                   scan('\''); sexp()
elist ::= \epsilon
          | sexp elist
                             def atom ():
atom ::= SYM
                                if next() in [SYM, NUM, STRING]:
         NUM
                                   scan(next())
         I STRING
                                else:
                             def elist ():
                                if :
```

```
def prog ():
                                sexp(); scan(\dashv)
                             def sexp ():
                                if next() in [SYM, NUM, STRING]:
prog ::= sexp '⊢'
                                   atom()
                                elif \underline{next()} == '('):
sexp ::= atom
                                   scan('('); elist(); scan(')')
       | '(' elist ')'
                                else:
        | '\'' sexp
                                   scan('\''); sexp()
elist ::= \epsilon
          | sexp elist
                             def atom ():
atom ::= SYM
                                if next() in [SYM, NUM, STRING]:
         NUM
                                   scan(next())
        | STRING
                                else:
                                   ERROR()
                             def elist ():
                                if :
```

```
def prog ():
                                 sexp(); scan(\dashv)
                              def sexp ():
                                 if next() in [SYM, NUM, STRING]:
prog ::= sexp '⊢'
                                    atom()
                                 elif next() == '(':
sexp ::= atom
                                    scan('('); elist(); scan(')')
        | '(' elist ')'
                                 else:
        | '\', sexp
                                    scan('\''); sexp()
elist ::= \epsilon
          | sexp elist
                              def atom ():
atom ::= SYM
                                 if next() in [SYM, NUM, STRING]:
         l NUM
                                    scan(next())
                                 else:
         | STRING
                                    ERROR()
                              def elist ():
                                 if next() in [SYM, NUM, STRING, '(', "'"]:
                                    sexp(); elist();
```

Expression Recognizer with Actions

- Can make the nonterminal functions return semantic values.
- Assume lexer somehow supplies semantic values for tokens, if needed

```
{: RESULT = emptyList; :}
elist ::= \epsilon
         | sexp:head elist:tail {: RESULT = cons(head, tail); :}
def elist ():
   if next() in [SYM, NUM, STRING, '(', "'"]:
   else:
       return emptyList
```

Expression Recognizer with Actions

- Can make the nonterminal functions return semantic values.
- Assume lexer somehow supplies semantic values for tokens, if needed

Grammar Problems I

In a recursive-descent parser, what goes wrong here?

Grammar Problems I

In a recursive-descent parser, what goes wrong here?

If we choose the second or third alternative for e, we'll get an infinite recursion ("left recursion problem"). If we choose the first, we'll miss '/' and '*' cases.

Grammar Problems II

Well then: What goes wrong here?

```
p ::= e '⊢'
e ::= t:t1
                    {: RESULT = t1; :}
    | t:lft '/' e:rgt {: RESULT = makeTree(DIV, lft, rgt); :}
    | t:lft '*' e:rgt {: RESULT = makeTree(MULT, lft, rgt); :}
```

Grammar Problems II

Well then: What goes wrong here?

```
p ::= e '⊢'
e ::= t:t1
                    {: RESULT = t1; :}
    | t:lft '/' e:rgt {: RESULT = makeTree(DIV, lft, rgt); :}
    | t:lft '*' e:rgt {: RESULT = makeTree(MULT, lft, rgt); :}
```

No infinite recursion, but we still don't know whether to use the second or third case until after parsing the 't' nonterminal (potentially a lot of text).

FIRST and FOLLOW

• If α is any string of terminals and nonterminals (like the right side of a production) then FIRST(α) is the set of terminal symbols that start some string that α produces, plus ϵ if α can produce the empty string. For example:

```
p ::= e '⊢'
e ::= s t
s ::= ε | '+' | '-'
t ::= ID | '(' e ')'
```

Since $e \Rightarrow s t \Rightarrow (e) \Rightarrow \ldots$, we know that '(' \in FIRST(e). Since $s \Rightarrow \epsilon$, we know that $\epsilon \in$ FIRST(s).

Using FIRST

 In our previous recursive-descent Lisp-expression recognizer, we converted

into a function.

• Using FIRST, we can reformulate that function as

```
def sexp ():
    if next() in FIRST(atom):
        atom()
    elif next() in FIRST('(' elist ')'):
        scan('('); elist(); scan(')')
    elif next() in FIRST('\'' sexp):
        scan('\''); sexp()
```

Using FOLLOW

• Likewise, for

```
\texttt{elist} ::= \epsilon \\ | \texttt{sexp elist}
```

ullet By observing that the first choice for elist produces ϵ , we can translate this into

```
def elist():
    if next() in FIRST(\epsilon) or next() in FOLLOW(elist):
        pass
    elif next() in FIRST(sexp elist):
        sexp(); elist()
```

(I've included next() in $FIRST(\epsilon)$ just to be general. Since a token can never be ϵ , that term really isn't needed in this case. However, FIRST sets that contain ϵ can also contain real terminal symbols).

The General Idea

- To summarize,
 - In a recursive-descent compiler where we have a choice of right-hand side for a non-terminal, X, look at the FIRST set of each choice and use that right-hand side it if the set contains the next input symbol...
 - ... and if a right-hand side's FIRST set contains ϵ , use that right-hand side if the next input symbol is in FOLLOW(X).

Grammar Problems III

What actions?

What are FIRST and FOLLOW?

Grammar Problems III

What actions?

```
p::= e',-' Here, we don't have the previous e::= t et \{:?1:\} problems, but how do we build a et ::= \epsilon \{:?2:\} tree that associates properly (left | ',' e \{:?3:\} to right), so that we don't interpret | '*' e \{:?4:\} I/I/I as if it were I/(I/I)? t ::= I:i1 \{:RESULT = i1;:\}
```

What are FIRST and FOLLOW?

Grammar Problems III

What actions?

```
p::= e',-' Here, we don't have the previous e::= t et \{:?1:\} problems, but how do we build a et ::= \epsilon \{:?2:\} tree that associates properly (left | ',' e \ \{:?3:\} to right), so that we don't interpret | '*, e \ \{:?4:\} I/I/I as if it were I/(I/I)? t ::= I:i1 \{:RESULT = i1;:\}
```

What are FIRST and FOLLOW?

```
FIRST(p) = FIRST(e) = FIRST(t) = { I }

FIRST(et) = { \epsilon, '/', '*' }

FIRST('/' e) = { '/' } (when to use ?3)

FIRST('*' e) = { '*' } (when to use ?4)

FOLLOW(e) = { '-|' }

FOLLOW(et) = FOLLOW(e) (when to use ?2)

FOLLOW(t) = { '-|', '/', '*' }
```

- There are ways to deal with the left-association problem in last slide within the pure framework, but why bother?
- Implement the 'e' procedure with a loop, instead:

def	e():		
	while _ if _		:
	else	:	
	return		

- There are ways to deal with the left-association problem in last slide within the pure framework, but why bother?
- Implement the 'e' procedure with a loop, instead:

def	e():		
	r = t()		
	while _		:
	if _		:
	else	:	
	return		

- There are ways to deal with the left-association problem in last slide within the pure framework, but why bother?
- Implement the 'e' procedure with a loop, instead:

def	e():				
	r = t(()			
	while	next()	in	['/',	,* ,]
	if				
	els	se:			
	returr	າ			

- There are ways to deal with the left-association problem in last slide within the pure framework, but why bother?
- Implement the 'e' procedure with a loop, instead:

```
def e():
    r = t()
    while <u>next() in ['/', '*']</u>:
       if next() == '/':
            scan('/'); t1 = t()
            r = makeTree (DIV, r, t1)
       else:
    return
```

- There are ways to deal with the left-association problem in last slide within the pure framework, but why bother?
- Implement the 'e' procedure with a loop, instead:

```
def e():
    r = t()
    while <u>next() in ['/', '*']</u>:
       if next() == '/':
           scan('/'); t1 = t()
           r = makeTree (DIV, r, t1)
       else:
           scan('*'); t1 = t()
           r = makeTree (MULT, r, t1)
    return _____
```

- There are ways to deal with the left-association problem in last slide within the pure framework, but why bother?
- Implement the 'e' procedure with a loop, instead:

```
def e():
    r = t()
    while \underline{\text{next}()} in ['/', '*']:
        if next() == '/':
            scan('/'); t1 = t()
            r = makeTree (DIV, r, t1)
        else:
            scan('*'); t1 = t()
            r = makeTree (MULT, r, t1)
    return r
```

From Recursive Descent to Table Driven

• Our recursive descent parsers have a very regular structure.

Definition of nonterminal A:

$A ::= \alpha_1$ $\mid \alpha_2$ $\mid \ldots$ $\mid \alpha_3$

Program for A:

```
def A(): if next() in S_1: translation of \alpha_1 elif next() in S_2: translation of \alpha_2
```

. .

• Here,

$$S_i = \left\{ \begin{aligned} & \mathsf{FIRST}(\alpha_i), & \text{if } \epsilon \not\in \mathsf{FIRST}(\alpha_i) \\ & \mathsf{FIRST}(\alpha_i) \cup \mathsf{FOLLOW}(A), & \text{otherwise.} \end{aligned} \right\}$$

- ullet and the translation of α_i simply converts each nonterminal into a call and each terminal into a scan.
- If the S_i do not overlap, we say the grammar is LL(1): input can be processed from Left to right, producing a Leftmost derivation, and checking 1 symbol of input ahead to see which branch to take.

Table-Driven LL(1)

- Because of this regular structure, we can represent the program as a table, and can write a general LL(1) parser that interprets any such table.
- Consider a previous example:

1. prog	: :=	sexp '⊢'								
2. sexp	: :=	atom		Lookahead symbol						
3.		'(' elist ')'	Nonterminal	()	,	SYM	NUM	STRING	\dashv
4.		'\', sexp	prog	(1)		(1)	(1)	(1)	(1)	
5. elist	: :=	ϵ	sexp	(3)		(4)	(2)	(2)	(2)	
6.		sexp elist	elist	(6)	(5)	(6)	(6)	(6)	(6)	(5)
7. atom	: :=	SYM	atom				(7)	(8)	(9)	
8.		NUM								
9.		STRING								

- The table shows nonterminal symbols in the left column and the other columns show which production to use for each possible lookahead symbol.
- Grammar is LL(1) when this table has at most one production per entry.

A General LL(1) Algorithm

Given a fixed table T and grammar G, the function LLparse(X), where parameter X is a grammar symbol, may be defined

```
\label{eq:def-LLparse} \begin{array}{lll} \text{def LLparse(X):} \\ & \text{if X is a terminal symbol:} \\ & \text{scan(X)} \\ & \text{else:} \\ & \text{prod = T[X][next()]} \\ & \text{Let } p_1 p_2 \cdots p_n \text{ be the right-hand side of production prod} \\ & \text{for i in range(n):} \\ & \text{LLparse}(p_i) \end{array}
```