CS 164, Spring 2019 **CS 164: Homework #8** **P. N. Hilfinger**

Due: No submission needed

1. A definition (that is, an assignment) of a simple variable is said to *reach* a point in the program if it *might be* the last assignment to that variable executed before execution reaches that point in the program. So for example, definition A below reaches points B and C, but not D:

```
x = 3       # A
if a < 2:
   x = 2
   pass     # D
else:
   y = 5
   pass     # B
pass        # C
```

Suppose we want to compute $R(p)$, the set of all definitions that reach point p in a program. Give forward rules (in the style of the lecture) for computing the *reaching definitions,* $R_{\text{out}}(s)$ for a statement s (the *set* of definitions that reach the point immediately after the statement) as a function of $R_{\text{in}}(s)$ (the definitions that reach the beginning) for each assignment statement s and give the rules for computing $R_{\text{in}}(s)$ as a function of the R_{out} values of its predecessors.

2. Consider the loop

```
for i := 0 to n-1 do
   for j := 0 to n-1 do
      for k := 0 to n-1 do
         c[i,j] := c[i,j] + a[i,k] * b[k,j]
```

In this nested loop, `a`, `b`, and `c` are two-dimensional arrays of 4-byte integers. Here is a translation into intermediate code (assume that `a`, `b`, and `c` are addresses of static memory, and that all other variables are in registers):

```
Entry:
  i := 0            #1
  goto L6           #2
L1:
  j := 0            #3
  goto L5           #4
L2:
  k := 0            #5
  goto L4           #6
L3:
  t1 := 4 * n       #7
  t2 := t1 * i      #8
  t3 := 4 * j       #9
  t4 := t2 + t3     #10
  t5 := *(t4 + c)   #11
  t6 := 4 * n       #12
  t7 := t6 * i      #13
  t8 := 4 * k       #14
  t9 := t7 + t8     #15
  t10 := *(t9 + a)  #16
  t11 := 4 * n      #17
  t12 := t11 * k    #18
  t13 := 4 * j      #19
  t14 := t12 + t13  #20
  t15 := *(t14 + b) #21
  t16 := t10 * t15  #22
  t17 := t5 + t16   #23
  t18 := 4 * n      #24
  t19 := t18 * i    #25
  t20 := 4 * j      #26
  t21 := t19 + t20  #27
  *(t21+c) := t17   #28
  k := k + 1        #29
L4:
  if k < n: goto L3 #30
  j := j + 1        #31
L5:
  if j < n: goto L2 #32
  i := i + 1        #33
L6:
  if i < n: goto L1 #34
Exit:
```

To notate accesses to memory, we've used C-like notation:

```
r1 := *(r2+K)
*(r1+K) := r2
*K := r3
r3 := *K
```

`K` is an integer literal, and `L` is a static-storage label (a constant address in memory). Unlike C, the additions here are just straight addition: no automatic scaling by word size.

a. According to this code, how are the elements of the three two-dimensional arrays laid out in memory (in what order do the elements of the arrays appear)?

b. Divide the instructions into basic blocks, each headed by a label and with no other labels in the program.

c. The program is almost in SSA form, except for variables `i`, `j`, and `k`. Introduce new variables and ϕ functions as needed to put the program into SSA form (try to minimize ϕ functions).

d. Now optimize this code as best you can, moving assignments of invariant expressions out of loops, eliminating common subexpressions, removing dead statements, performing copy propagation, etc.