Structural Explanation and Predictive Analysis of Crime Rates in London

Preparation

- Github link
- Number of words: 1493
- Runtime: 2 m 52 s (*Memory 24 GB, CPU Apple M3*)
- Coding environment: SDS Docker
- License: this notebook is made available under the Creative Commons Attribution license (or other license that you like).
- Additional library *[libraries not included in SDS Docker or not used in this module]*:
  - **watermark**: A Jupyter Notebook extension for printing timestamps, version numbers, and hardware information.
  - **nbformat**: A library for reading, writing, and validating *.ipynb* files in Python.

In [1]:
```
#%pip install nbformat
#%pip install watermark
```

In [2]:
```
# This chunk is for word counting
import nbformat
import os

# get the path of the current notebook file
notebook_path = os.getcwd()
notebook_path = os.path.join(os.getcwd(), "WeiningLI_submission_CASA0006.


# read notebook file
with open(notebook_path, 'r', encoding='utf-8') as f:
    notebook = nbformat.read(f, as_version=4)

# skip the first 3 markdown cells (Title and Preparation)
markdown_cells = [cell for cell in notebook.cells if cell.cell_type == 'm
markdown_cells = markdown_cells[3:-1]
filtered_cells = [cell for cell in markdown_cells if '<div align="center"

# count the number of words in all Markdown cells
total_words = sum(len(cell.source.split()) for cell in filtered_cells)

print(f"Total Markdown word count (excluding Title and Preparation): {tot
```

```
Total Markdown word count (excluding Title and Preparation): 1493
```

In [3]:
```python
# This chunk is for runtime counting

import time
start_time = time.time()
```

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1. Introduction

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Urban crime has long been recognised as a critical social issue affecting residents' sense of safety and quality of life (Cozens, 2008). Understanding the structural and spatial distribution of urban crime is crucial to public safety governance in the UK. Crime rates are shaped not only by individual behaviour but are also deeply embedded in the socio-economic and residential structures of cities. As a representative global metropolis, London presents an ideal context for such analysis. This study adopts the LSOA as the spatial unit of analysis. Its finer spatial resolution enables the detection of neighbourhood-level variation in social and environmental conditions.

A large body of research confirms that crime is spatially patterned and closely tied to socio-economic disadvantage (Freeman, 1999; Finegan et al., 2020; Pazzona, 2024). Education (Lochner & Moretti, 2004), housing conditions (Cheng & Chen, 2021), and public transport access (Gallison & Andresen, 2017) have all been identified as relevant factors. These structural indicators offer critical insight into the geography of urban crime.

2. Research questions

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To what extent can socio-economic and environmental structures explain and predict spatial variation in crime rates across London's LSOAs?

To address this overarching research question, the study is guided by the following sub-questions:

1. Are spatial crime patterns linked to distinctive structural characteristics across neighbourhoods?
2. Which dimensions of deprivation are most strongly associated with crime?
3. Do structural variables contain predictive signals for distinguishing between high- and low-crime areas? If so, which modelling approach provides the best predictive performance?

3. Data

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This study uses structural variables derived from the 2021 London Census at the LSOA level,including indicators such as low education, household language isolation, and unemployment, along with the Public Transport Accessibility Level (PTAL). In total, nine socio-economic and environmental variables are selected. The variables and their sources are listed in **Table 1**.

Table 1. Summary of input variables

Variable	Type	Description	Notes	Source
Total crime rate	Numeric	Crime rate per 1,000 residents, averaged over 2021–2024 [1] and transformed using the Yeo-Johnson method to reduce skewness	Dependent variable	MPS Recorded Crime: Geographic Breakdown
Low-education rate	Numeric	Proportion of residents with no qualifications or only level 1-2 qualifications	Proxy for educational deprivation	2011 Census
Household language isolation rate	Numeric	Proportion of households where no adult speaks English as a main language	Proxy for cultural isolation and communication barriers	Same as above
Unemployment rate	Numeric	Proportion of the economically active population who are unemployed	Proxy for income and labour market deprivation	Same as above
Car or van unavailability rate	Numeric	Proportion of households with no access to a car or van	Reflects both mobility limitations and potential	Same as above

Variable	Type	Description	Notes	Source
			economic disadvantage	
Overcrowding rate	Numeric	Proportion of households with occupancy rating of -1 or less	Reflects living environment	Same as above
Poor health rate	Numeric	Proportion of residents reporting ‘bad’ or ‘very bad’ health	Proxy for general health deprivation	Same as above
Disability rate	Numeric	Proportion of residents with functional limitations legally recognised as disabilities	Captures formally acknowledged structural vulnerability	Same as above
Long-term sickness rate [2]	Numeric	Proportion of residents with long-term physical or mental illness not formally classified as disabled	May indicate hidden vulnerability not captured by formal disability status	Same as above
Public transport accessibility	Numeric	Public transport accessibility index	Measures urban connectivity and mobility	GLA PTAL dataset
Geographical boundary [3]	Shapefile	LSOA-level boundary geometry for mapping and spatial join	Used for visualisation and spatial analysis	ONS Open Geography Portal

> Notes
>
> [1]: The first reason why 2021–2024 period is chosen is because the most recent census was conducted in 2021. Given the short interval, the assumption of stable population characteristics is reasonable. Secondly, 2021 marks the beginning of the post-COVID period, which helps to minimise the confounding effects of the COVID-19 pandemic on crime patterns and socio-demographic variables. Finally, 2024 is the latest year with complete whole-year crime data.
>
> [2]: Criminal behaviour is often associated with physical and psychological vulnerability (Tan and Haining, 2016). One potentially overlooked group is those with long-term illness but no official disability status. While chronic or mental health issues may not limit daily activities, they might reduce social adaptability and, under pressure, relate to behaviours such as violence or defensive theft. To explore this possibility, long-term sickness is included as a variable. Both self-rated general health and legally defined disability are retained to offer a broader view of health-related disadvantage.

> [3]: Of the 4,835 LSOAs in Greater London, only 4,659 contain valid crime data. Missing areas are typically non-residential (e.g. City of London, parks), or show no recorded crime. These are therefore removed.

Data pre-processing

In [4]:
```
# load all the packages first
import pandas as pd
import geopandas as gpd
import requests
import zipfile
from pathlib import Path
import numpy as np
from sklearn.preprocessing import PowerTransformer
import seaborn as sns
import matplotlib.pyplot as plt
from sklearn.preprocessing import StandardScaler
import matplotlib.gridspec as gridspec
from statsmodels.stats.stattools import durbin_watson
from sklearn.decomposition import PCA
from kneed import KneeLocator
import statsmodels.api as sm
from sklearn.cluster import KMeans
from sklearn.metrics import silhouette_score
from sklearn.linear_model import LinearRegression, Lasso
from sklearn.svm import SVR
from sklearn.ensemble import RandomForestRegressor
from sklearn.metrics import mean_squared_error, r2_score
from xgboost import XGBRegressor
from sklearn.model_selection import train_test_split
from sklearn.model_selection import GridSearchCV
```

In [5]:
```
# read in LSOA crime data
df_recent = pd.read_csv("https://raw.githubusercontent.com/Weining5619/DS
df_historical = pd.read_csv("https://raw.githubusercontent.com/Weining561

# read in 2021 census data
df_residents = pd.read_csv("https://raw.githubusercontent.com/Weining5619
df_qualification = pd.read_csv("https://raw.githubusercontent.com/Weining
df_language = pd.read_csv("https://raw.githubusercontent.com/Weining5619/
df_economic_active = pd.read_csv("https://raw.githubusercontent.com/Weini
df_car = pd.read_csv("https://raw.githubusercontent.com/Weining5619/DSSS/
df_bedrooms = pd.read_csv("https://raw.githubusercontent.com/Weining5619/
df_health = pd.read_csv("https://raw.githubusercontent.com/Weining5619/DS
df_disability = pd.read_csv("https://raw.githubusercontent.com/Weining561

# read in PTAI data
df_PTAI = pd.read_csv("https://raw.githubusercontent.com/Weining5619/DSSS
```

In [6]:
```
# download geo boundaries

# first download the zip file to the data folder, and then unzip it to da
# create a "data" folder (if do not exist)
data_dir = "data"
os.makedirs(data_dir, exist_ok=True)
```

```
# download the zip file (if do not exist)
zip_filename = "LSOA_Boundaries_London.zip"
zip_path = os.path.join(data_dir, zip_filename)

if not os.path.exists(zip_path):
    url = "https://github.com/Weining5619/DSSS/raw/main/data/LSOA_Boundar
    response = requests.get(url)
    if response.status_code == 200:
        with open(zip_path, "wb") as f:
            f.write(response.content)
    else:
        raise Exception(f"Download failed. Status code: {response.status_

# unzip the file (if do not exist)
extract_dir = os.path.join(data_dir, "LSOA_Boundaries_London")
if not os.path.exists(extract_dir):
    with zipfile.ZipFile(zip_path, "r") as zip_ref:
        zip_ref.extractall(extract_dir)
```

In [7]:
```
# read in the shapefiles
# (It is a bit complicated here because the LSOA boundaries I found are s

shp_folder = "data/LSOA_Boundaries_London"

# find all .shp files
shp_files = [
    shp for shp in Path(shp_folder).rglob("*.shp")
    if not shp.name.startswith("._") # exclude cache files generated by m
]

# read them all into a gdf
gdf_list = [gpd.read_file(shp) for shp in shp_files]
gdf = gpd.GeoDataFrame(pd.concat(gdf_list, ignore_index=True), crs=gdf_li
```

In [8]:
```
# conver crime data to long table
# first replace spaces in column names with underscores

def clean_columns(df):
    '''
    Unify the format of column names
    '''
    df.columns = df.columns.str.strip().str.replace(" ", "_")
    if "geography_code" in df.columns:
        df.rename(columns={"geography_code": "LSOA_Code"}, inplace=True)
    return df

df_recent = clean_columns(df_recent)

# find all the columns of months
date_cols_rec = [col for col in df_recent.columns if col.isdigit() and co

# conver to long table
df_recent_long = df_recent.melt(
    id_vars=["LSOA_Code", "LSOA_Name", "Borough", "Major_Category", "Mino
    value_vars=date_cols_rec,
    var_name="YearMonth",
    value_name="CrimeCount"
)
```

```
# make it consistent with the number of LSOAs in gdf
df_recent_new = gdf[["LSOA11CD"]].copy()
df_recent_new = df_recent_new.rename(columns={"LSOA11CD": "LSOA_Code"})
df_recent_new = df_recent_new.merge(df_recent_long, on="LSOA_Code", how="
```

In [9]:
```
# do similar processing on historical crime data
df_historical = clean_columns(df_historical)

# drop columns before the year 2021
date_cols_his = [col for col in df_historical.columns if col.isdigit() an
cols_to_keep = ["LSOA_Code", "LSOA_Name", "Borough", "Major_Category", "M
df_historical = df_historical[cols_to_keep]

# conver to long table
df_historical_long = df_historical.melt(
    id_vars=["LSOA_Code", "LSOA_Name", "Borough", "Major_Category", "Mino
    value_vars=date_cols_his,
    var_name="YearMonth",
    value_name="CrimeCount"
)

# make it consistent with the number of LSOAs in gdf
df_historical_new = gdf[["LSOA11CD"]].copy()
df_historical_new = df_historical_new.rename(columns={"LSOA11CD": "LSOA_C
df_historical_new = df_historical_new.merge(df_historical_long, on="LSOA_
```

In [10]:
```
# combine crime data of recent 24 months and historical
df_crime = pd.concat([df_historical_new, df_recent_new], ignore_index=Tru

# count the number of crimes by year
df_crime["Year"] = df_crime["YearMonth"].str[:4] # extract the year
annual_crime_count = df_crime.groupby(["LSOA_Code", "Year"])["CrimeCount"
```

In [11]:
```
# handle column names
df_residents = clean_columns(df_residents)
df_residents = df_residents.rename(columns={"LSOA_code": "LSOA_Code"})
df_population = df_residents[["LSOA_Code", "All_usual_residents"]].copy()

# merge population and crime count
crime_rate = annual_crime_count.merge(df_population, on="LSOA_Code", how=

# calculate the number of cases per 1000 population as the crime rate
crime_rate["Crime_Rate_per_1000"] = crime_rate["CrimeCount"] / crime_rate

df_all = crime_rate[["LSOA_Code", "Year", "Crime_Rate_per_1000"]]
```

In [12]:
```
# process census data
df_qualification = clean_columns(df_qualification)
df_language = clean_columns(df_language)
df_economic_active = clean_columns(df_economic_active)
df_car = clean_columns(df_car)
df_bedrooms = clean_columns(df_bedrooms)
df_health = clean_columns(df_health)
df_disability = clean_columns(df_disability)
df_PTAI = clean_columns(df_PTAI)
df_PTAI = df_PTAI.rename(columns={"LSOA2011": "LSOA_Code"})

# drop all "date", "geography" columns to prevent duplicate columns which
df_language.drop(columns=["date", "geography"], inplace=True, errors="ign
df_economic_active.drop(columns=["date", "geography"], inplace=True, erro
df_car.drop(columns=["date", "geography"], inplace=True, errors="ignore")
df_bedrooms.drop(columns=["date", "geography"], inplace=True, errors="ign
df_health.drop(columns=["date", "geography"], inplace=True, errors="ignor
df_disability.drop(columns=["date", "geography"], inplace=True, errors="i

# merge all census as a combined dataframe
df_var = df_qualification.merge(df_language, on="LSOA_Code", how="left")
df_var = df_var.merge(df_economic_active, on="LSOA_Code", how="left")
df_var = df_var.merge(df_car, on="LSOA_Code", how="left")
df_var = df_var.merge(df_bedrooms, on="LSOA_Code", how="left")
df_var = df_var.merge(df_health, on="LSOA_Code", how="left")
df_var = df_var.merge(df_disability, on="LSOA_Code", how="left")
df_var = df_var.merge(df_PTAI, on="LSOA_Code", how="left")

# Keep only the data of London
London_LOSAs = gdf["LSOA11CD"].tolist()
df_var = df_var[df_var["LSOA_Code"].isin(London_LOSAs)].copy()
```

In [13]:
```
# process all the variables
# Low_Education_Rate = (No qualifications + Level1 + Level2) / All above
df_var["Low_Education_Rate"] = (
    df_var["Highest_level_of_qualification:_No_qualifications"] +
    df_var["Highest_level_of_qualification:_Level_1_and_entry_level_quali
    df_var["Highest_level_of_qualification:_Level_2_qualifications"]
) / df_var["Highest_level_of_qualification:_Total:_All_usual_residents_ag

# Non_English_Household_Rate = (no English + no adults but children) / Al
df_var["Non_English_Household_Rate"] = (
    df_var["Household_language_(English_and_Welsh):_No_people_in_househol
    df_var["Household_language_(English_and_Welsh):_No_adults_in_househol
) / df_var["Household_language_(English_and_Welsh):_Total:_All_households

# Unemployed_Rate = unemployed (students + nonstudents) / All economicall
#   According to the standard definition of unemployment rate used by ONS
#   economically inactive people, such as students, retirees, and those t
df_var["Unemployed_Rate"] = (
    df_var["Economic_activity_status:_Economically_active_(excluding_full
    df_var["Economic_activity_status:_Economically_active_and_a_full-time
) / (df_var["Economic_activity_status:_Total:_All_usual_residents_aged_16
    df_var["Economic_activity_status:_Economically_inactive"])

# No_Car_Rate = No car / All
df_var["No_Car_Rate"] = df_var["Number_of_cars_or_vans:_No_cars_or_vans_i

# Overcrowding_Rate = lack of bedrooms / All
df_var["Overcrowding_Rate"] = (
    df_var["Occupancy_rating_for_bedrooms:_Occupancy_rating_of_bedrooms:_
    df_var["Occupancy_rating_for_bedrooms:_Occupancy_rating_of_bedrooms:_
) / df_var["Occupancy_rating_for_bedrooms:_Total:_All_households"]

# Poor_Health_Rate = bad health + very bad / All
df_var["Poor_Health_Rate"] = (
    df_var["General_health:_Bad_health"] +
    df_var["General_health:_Very_bad_health"]
) / df_var["General_health:_Total:_All_usual_residents"]

# Disability_Rate = disabled / All
df_var["Disabled_Rate"] = df_var["Disability:_Disabled_under_the_Equality
```

```
# Long_Term_Sick_Rate = long-term sick / All
df_var["Long_Term_Sick_Rate"] = df_var["Disability:_Not_disabled_under_th

# Public_Transport_Accessibility_Index
df_var["Public_Transport_Accessibility"] = df_var["AvPTAI2015"]

# merge the data obtained above into crime rate
col_vars = [
    "Low_Education_Rate",
    "Non_English_Household_Rate",
    "Unemployed_Rate",
    "No_Car_Rate",
    "Overcrowding_Rate",
    "Poor_Health_Rate",
    "Disabled_Rate",
    "Long_Term_Sick_Rate",
    "Public_Transport_Accessibility"
]
df_var_only = df_var[["LSOA_Code"] + col_vars]
df_all = df_all.merge(df_var_only, on=["LSOA_Code"], how="left")
```

In [14]:
```
df_all.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 18612 entries, 0 to 18611
Data columns (total 12 columns):
 #   Column                          Non-Null Count  Dtype  
---  ------                          --------------  -----  
 0   LSOA_Code                       18612 non-null  object 
 1   Year                            18612 non-null  object 
 2   Crime_Rate_per_1000             18612 non-null  float64
 3   Low_Education_Rate              18612 non-null  float64
 4   Non_English_Household_Rate      18612 non-null  float64
 5   Unemployed_Rate                 18612 non-null  float64
 6   No_Car_Rate                     18612 non-null  float64
 7   Overcrowding_Rate               18612 non-null  float64
 8   Poor_Health_Rate                18612 non-null  float64
 9   Disabled_Rate                   18612 non-null  float64
 10  Long_Term_Sick_Rate             18612 non-null  float64
 11  Public_Transport_Accessibility  18612 non-null  float64
dtypes: float64(10), object(2)
memory usage: 1.7+ MB
```

Checking Data Distribution

Some variables, such as Public_Transport_Accessibility and Unemployed_Rate, showed heavy skewness. To reduce their impact, log transformations were applied. This helps stabilise the distribution without removing potentially important features. The results, as shown in **Figure 2**, are within an acceptable range.

In [15]:
```
# log transformation
epsilon = 1e-6

df_all["Crime_Rate_log"] = np.log(df_all["Crime_Rate_per_1000"] + epsilon
df_all["PTA_log"] = np.log(df_all["Public_Transport_Accessibility"] + eps
df_all["Unemployed_Rate_log"] = np.log(df_all["Unemployed_Rate"] + epsilo

# Yeo-Johnson
```

```
pt = PowerTransformer(method='yeo-johnson')
df_all['Crime_Rate_yj'] = pt.fit_transform(df_all[['Crime_Rate_per_1000']
```

In [16]:
```
# plot the distribution of all variables
cols_to_plot = [
    "Crime_Rate_yj",
    "Low_Education_Rate",
    "Non_English_Household_Rate",
    "Unemployed_Rate_log",
    "No_Car_Rate",
    "Overcrowding_Rate",
    "Poor_Health_Rate",
    "Disabled_Rate",
    "Long_Term_Sick_Rate",
    "PTA_log"
]

fig = plt.figure(figsize=(20, 6))
gs = gridspec.GridSpec(4, 5, height_ratios=[3, 1, 3, 1], hspace=0.4)

for i, col in enumerate(cols_to_plot):
    col_index = i % 5
    row_base = (i // 5) * 2  # each group occupies two lines

    # Up: Histogram (height*3)
    ax_hist = fig.add_subplot(gs[row_base, col_index])
    sns.histplot(df_all[col], kde=True, bins=50, color='skyblue', ax=ax_h
    ax_hist.set_title(col, fontsize=12)
    ax_hist.set_xlabel("")
    ax_hist.set_ylabel("")
    ax_hist.tick_params(axis='x', labelsize=10)
    ax_hist.tick_params(axis='y', labelsize=10)

    # Down: Box plot (height*1)
    ax_box = fig.add_subplot(gs[row_base + 1, col_index])
    sns.boxplot(x=df_all[col], color='lightgray', ax=ax_box)
    ax_box.set_xlabel("")
    ax_box.set_xticks([]) # remobe x, y axis ticks
    ax_box.set_yticks([])

plt.show()
```

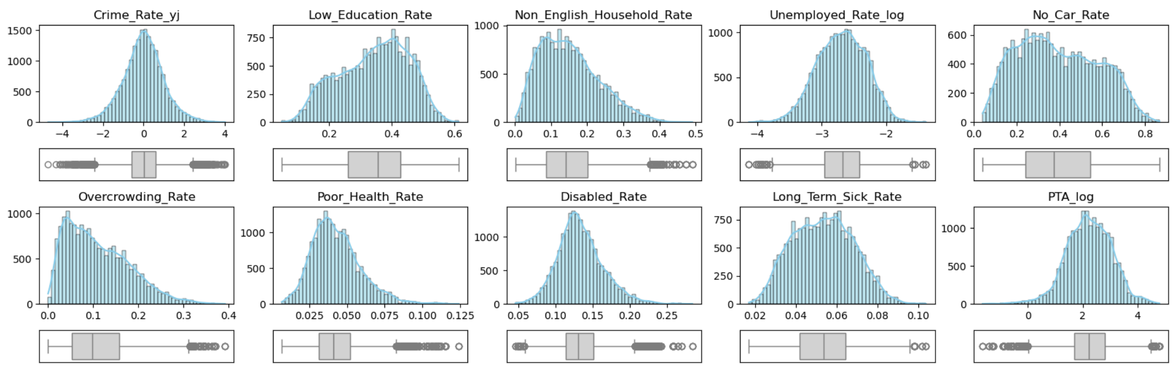

Figure 2. Distribution of variables

4. Methodology

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The workflow of methodology is summarised in **Figure 3**.

Methodology_workflow

Figure 3. Methodology workflow

4.1. PCA

To avoid highly correlated variables dominating the clustering process and skewing results, and to reduce multicollinearity in regression models, the correlation matrix was examine first.

As shown in **Figure 4**, most variables are approximately normally distributed and linearly related. Therefore, Pearson correlation coefficients are calculated to assess pairwise associations (**Figure5**).

In [17]:
```
sns.pairplot(
    df_all[cols_to_plot],
    diag_kind="kde",
    kind="reg", # add reg line on the scatter plot
    corner=True,   # only show the lower triangle
    height=2,
    plot_kws={"line_kws": {"color": "red"},
              "scatter_kws": {"s": 10, "alpha": 0.5}}
)

plt.suptitle("Pairwise Relationships of Selected Variables", fontsize=16,
plt.tight_layout()
plt.show()
```

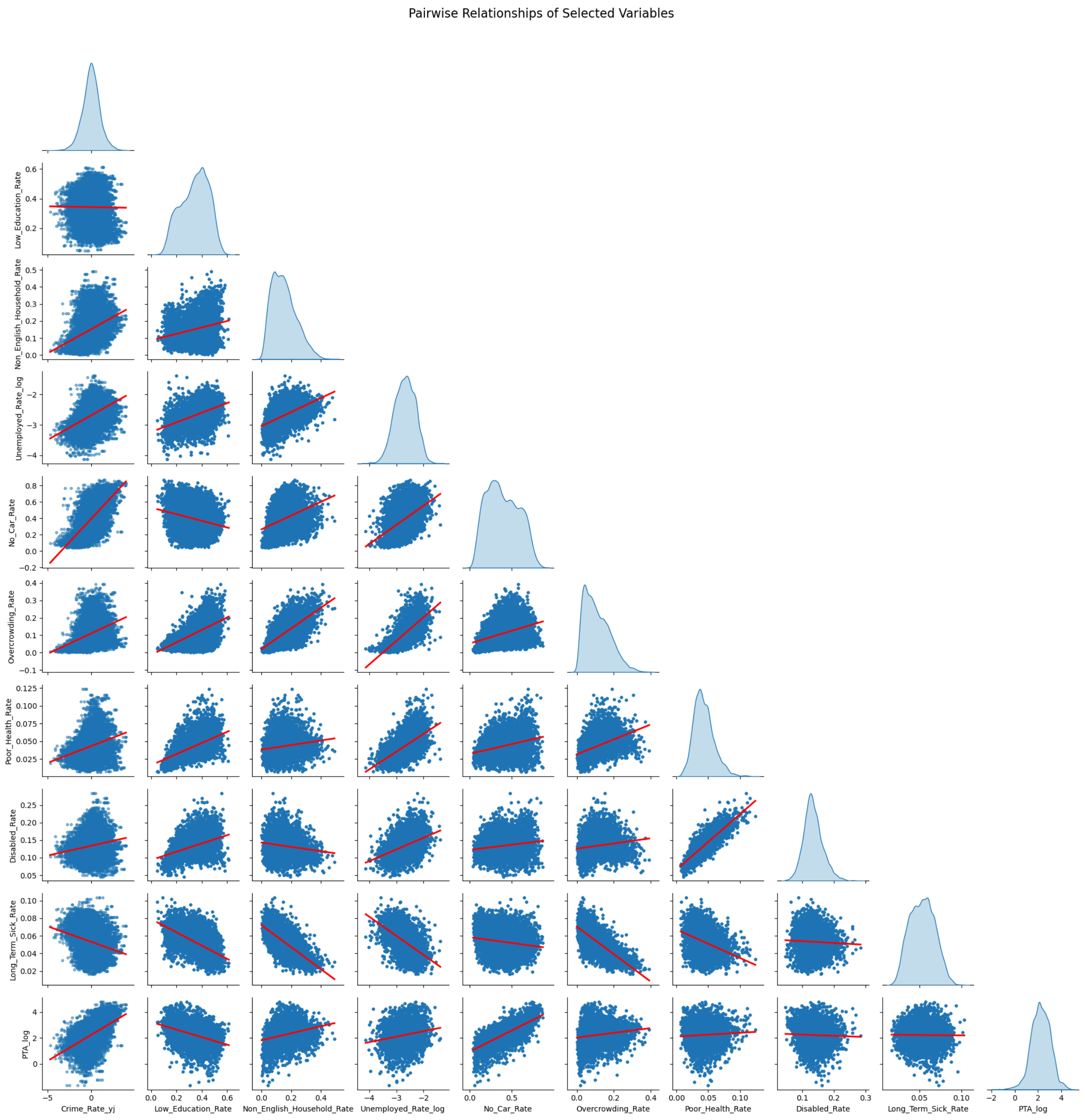


Figure 4. Pairwise Relationships of Selected Variables

In [18]:
```
# calculate the correlation matrix
corr_matrix = df_all[cols_to_plot].corr(method="pearson")

plt.figure(figsize=(10, 8))
sns.heatmap(corr_matrix, annot=True, cmap="coolwarm")
plt.title("Correlation Matrix")
plt.show()
```

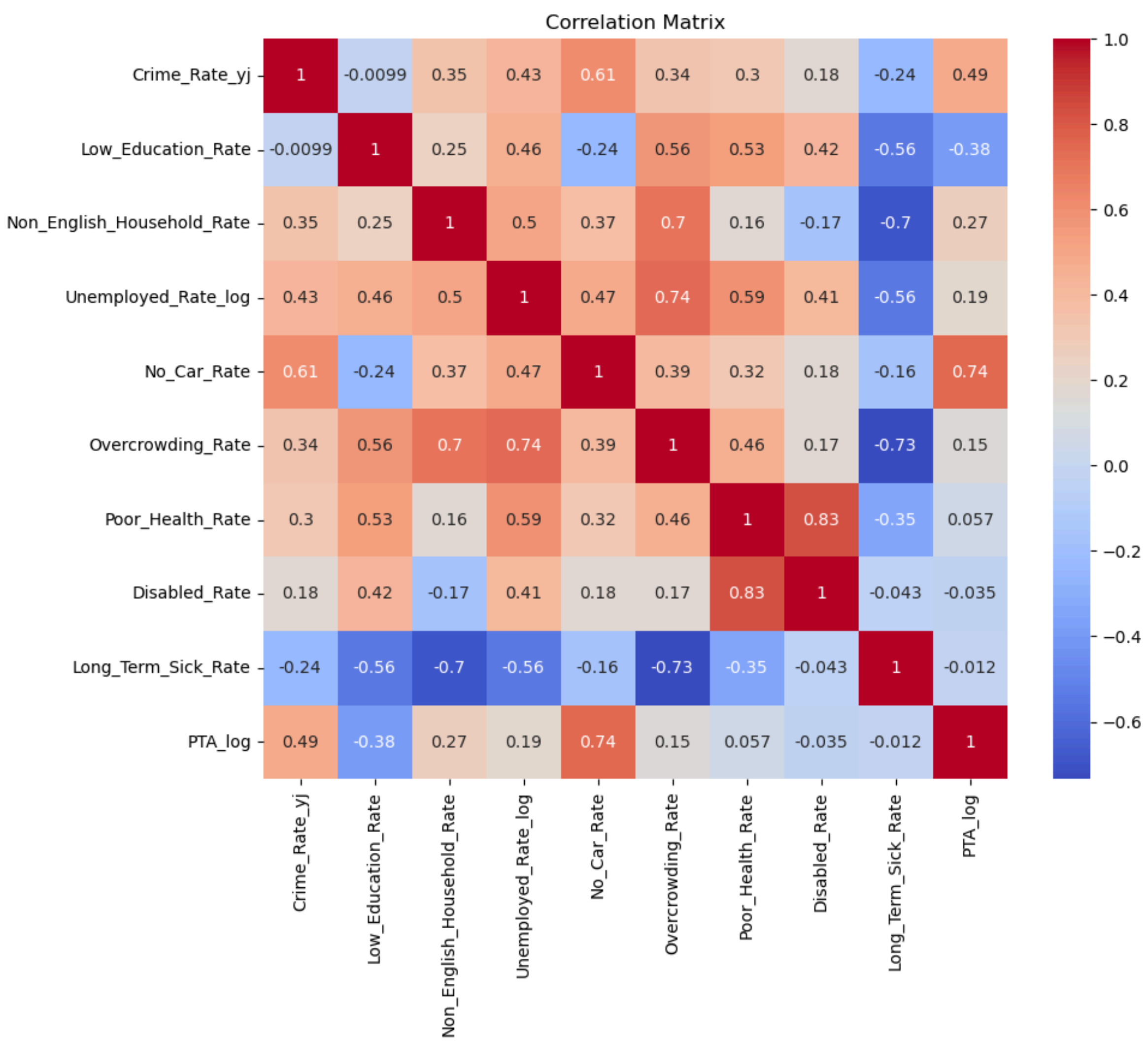


Figure 5. Correlation Matrix

As shown in the correlation matrix (**Figure 5**), several variables are highly correlated. This would lead to unstable regression coefficients, inflated variable effects, and reduced interpretability.

To address this while retaining most of the underlying information, PCA was applied to compress them into a smaller number of uncorrelated components.

PCA

In [19]:
```
# select variable columns for dimensionality reduction
cols_for_pca = [
    "Low_Education_Rate",
    "Non_English_Household_Rate",
    "Unemployed_Rate_log",
    "No_Car_Rate",
    "Overcrowding_Rate",
    "Poor_Health_Rate",
    "Disabled_Rate",
    "Long_Term_Sick_Rate",
    "PTA_log"
]
# Here, I still choose the logarithmically transformed Crime_Rate and Pub
# that are more inclined to a normal distribution.
# This is because if the original variable is highly skewed (especially s
# a few extreme values will dominate the variance explanation. Therefore,

# standardization
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
X_scaled = scaler.fit_transform(df_all[cols_for_pca])

# Initialize PCA
rand_st_int = 5525
pca = PCA(random_state=rand_st_int)

X_pca = pca.fit_transform(X_scaled)

print(f"Number of PCs retained: {pca.n_components_}")
print(f"Explained variance ratio of each component: {pca.explained_varian

# add the principal component results to the original table
for i in range(pca.n_components_):
    df_all[f"PCA_{i+1}"] = X_pca[:, i]
```

```
Number of PCs retained: 9
Explained variance ratio of each component: [0.44484783 0.23071704 0.18342
958 0.03959046 0.03083549 0.02533328
 0.02180343 0.01267983 0.01076306]
```

In [20]:
```
# show the PCA Loadings Matrix
loadings = pd.DataFrame(
    pca.components_.T,
    columns=[f"PC{i+1}" for i in range(pca.n_components_)],
    index=cols_for_pca
)
display(loadings.round(2))
```

	PC1	PC2	PC3	PC4	PC5	PC6	PC7	PC8
Low_Education_Rate	0.31	-0.46	-0.14	-0.12	0.57	0.19	0.00	0.53
Non_English_Household_Rate	0.34	0.25	-0.39	-0.22	-0.42	0.57	-0.31	0.14
Unemployed_Rate_log	0.43	0.03	0.07	0.71	-0.01	-0.21	-0.50	0.01
No_Car_Rate	0.24	0.50	0.30	0.11	-0.14	-0.07	0.50	0.56
Overcrowding_Rate	0.44	0.05	-0.21	0.22	0.25	0.23	0.52	-0.54
Poor_Health_Rate	0.36	-0.22	0.41	-0.29	-0.24	0.06	0.04	-0.27
Disabled_Rate	0.23	-0.30	0.57	-0.14	-0.13	0.07	-0.10	-0.00
Long_Term_Sick_Rate	-0.38	0.03	0.37	0.38	0.13	0.73	-0.02	0.00
PTA_log	0.11	0.58	0.24	-0.35	0.57	-0.02	-0.35	-0.17

Table 2. PCA Loadings Matrix

In [21]:
```
# extract the scores of the first two PCs and draw Biplot
# The figures drawn by 'bioinfokit' are not easy to modify, so use matplo
plt.figure(figsize=(6, 4))
xs = X_pca[:, 0]
ys = X_pca[:, 1]
plt.scatter(xs, ys, alpha=0.2, color="coral", s=8)
```

```
for i, var in enumerate(cols_for_pca):
    plt.arrow(0, 0,
              pca.components_[0, i]*7,
              pca.components_[1, i]*7,
              color='deepskyblue', alpha=0.6, head_width=0.02)
    plt.text(pca.components_[0, i]*8,
             pca.components_[1, i]*8,
             var, fontsize=10, ha="center", va="center")

plt.axhline(0, color="gray", linestyle="--")
plt.axvline(0, color="gray", linestyle="--")
plt.xlabel(f"PC1 ({pca.explained_variance_ratio_[0]*100:.2f}%)")
plt.ylabel(f"PC2 ({pca.explained_variance_ratio_[1]*100:.2f}%)")
plt.title("PCA Biplot")
plt.grid(True)
plt.tight_layout()
plt.show()
```

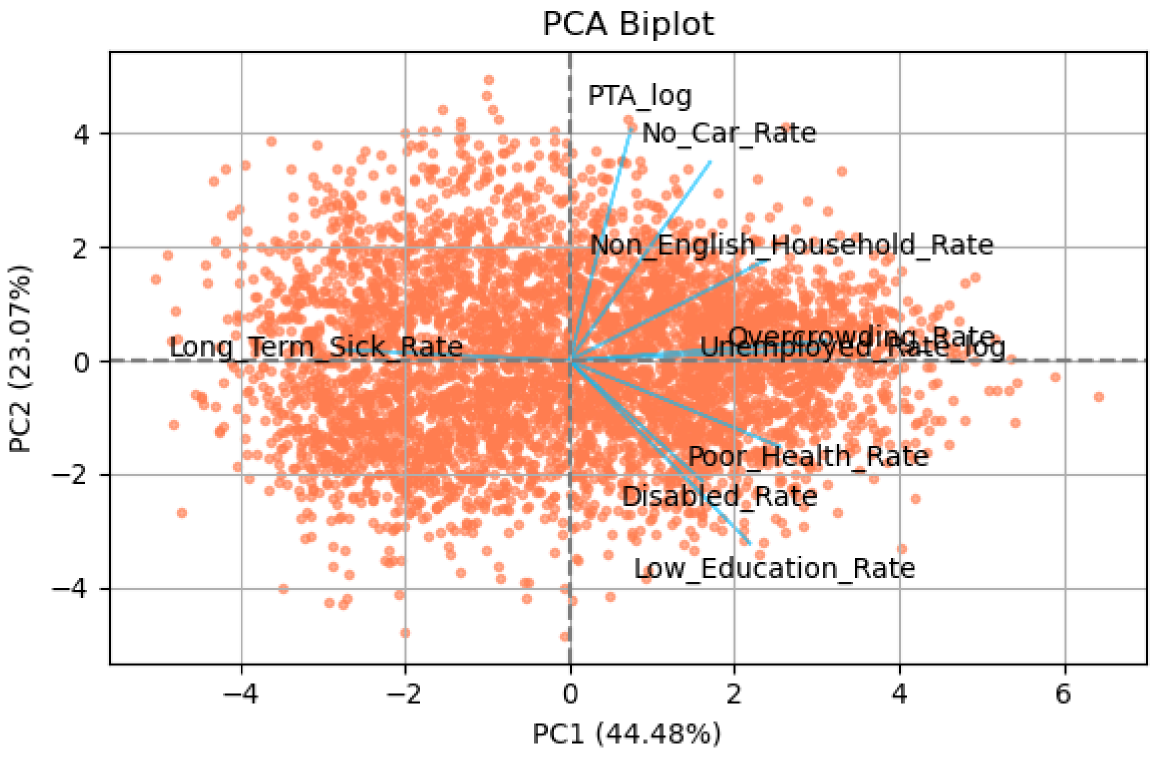


Figure 6. PCA Biplot

In [22]:
```
# use Scree plot to locate a point that occurs just before the Scree plot
eigenvalues = pca.explained_variance_
pcs = list(range(1, len(eigenvalues) + 1))

# use KneeLocator to find the elbow.
knee = KneeLocator(pcs, eigenvalues, curve='convex', direction='decreasin

plt.figure(figsize=(6, 4))
plt.plot(pcs, eigenvalues, marker='o', label='Eigenvalue')
plt.axvline(x=knee.knee, color='red', linestyle='--', label=f'Elbow at PC
plt.title("Scree Plot with Elbow Point of PCA")
plt.xlabel("Number of Principal Components")
plt.ylabel("Eigenvalue")
plt.legend()
plt.grid(True)
plt.tight_layout()
plt.show()
```

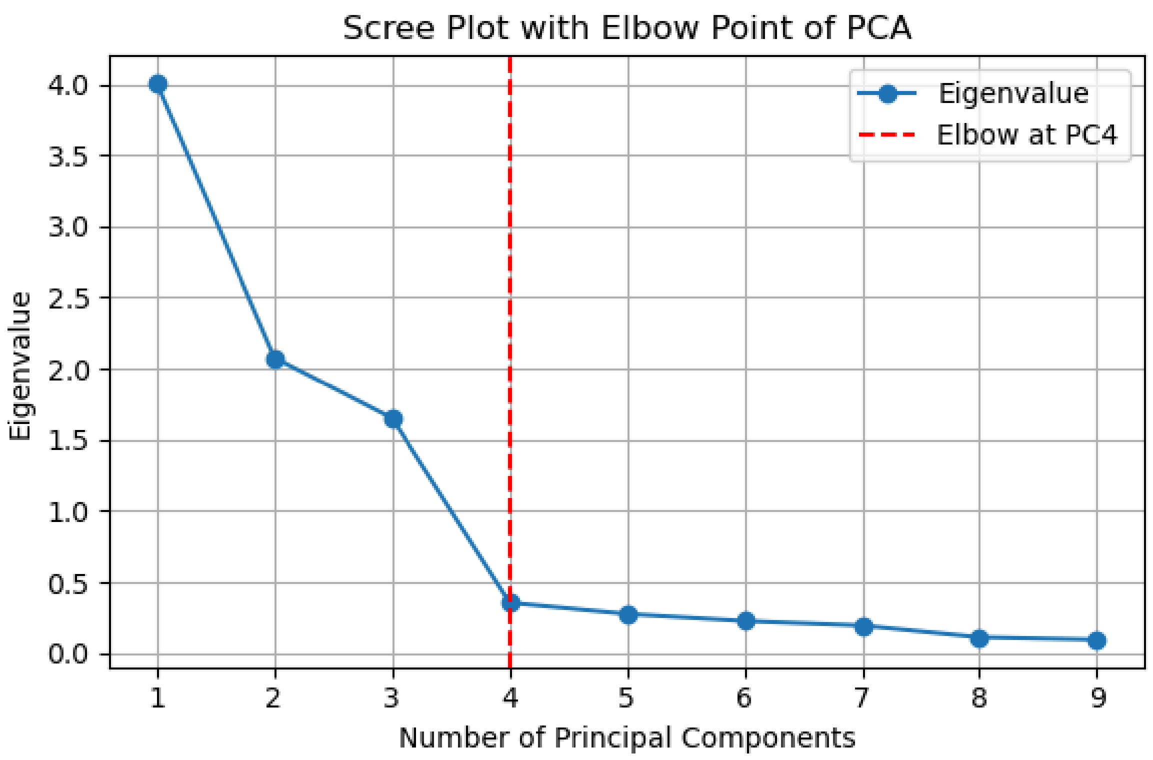


Figure 7. Scree Plot with Elbow Point of PCA

In [23]:
```
variance_explained = pca.explained_variance_ratio_[0] + pca.explained_var
print(f"Proportion of variance explained by PC1 to PC4: {variance_explain
```

```
Proportion of variance explained by PC1 to PC4: 89.86%
```

Based on the elbow point in the scree plot (**Figure**), the first 4 principal components were retained, explaining 89.86% of the total variance.

- PC1 reflects general socioeconomic disadvantage, with high scores in areas of low education, unemployment, poor health, overcrowding, and limited transport access.
- PC2 captures urban connectivity, positively associated with public transport access, education, and vehicle ownership.
- PC3 represents language isolation, driven mainly by the proportion of non-English-speaking households.
- PC4 relates to health conditions, influenced by poor health and long-term sickness rates.

PCA effectively reduced dimensionality while preserving key structural information, supporting more stable clustering and regression analyses.

4.2. Clustering

In [24]:
```
X = df_all[['PCA_1', 'PCA_2', 'PCA_3', 'PCA_4']]

k_range = range(2, 11)
sse = []
```

```
silhouette = []

for k in k_range:
    kmeans = KMeans(n_clusters=k, random_state=5525, n_init=10)
    labels = kmeans.fit_predict(X)
    sse.append(kmeans.inertia_)
    silhouette.append(silhouette_score(X, labels))

# find elbow
kl = KneeLocator(k_range, sse, curve='convex', direction='decreasing')
elbow_k = kl.elbow

# plot
fig, ax1 = plt.subplots(figsize=(8, 5))
ax2 = ax1.twinx()

ax1.plot(k_range, sse, marker='o', color='royalblue', label='SSE (Distort
ax1.axvline(elbow_k, linestyle='--', color='black', label=f'Elbow at k={e
ax1.set_xlabel("k")
ax1.set_ylabel("SSE", color='royalblue')
ax1.tick_params(axis='y', labelcolor='royalblue')

ax2.plot(k_range, silhouette, marker='x', linestyle='--', color='darkoran
ax2.set_ylabel("Silhouette Score", color='darkorange')
ax2.tick_params(axis='y', labelcolor='darkorange')

plt.title(f"Elbow & Silhouette Analysis (Elbow at k={elbow_k})")
plt.tight_layout()
plt.show()
```

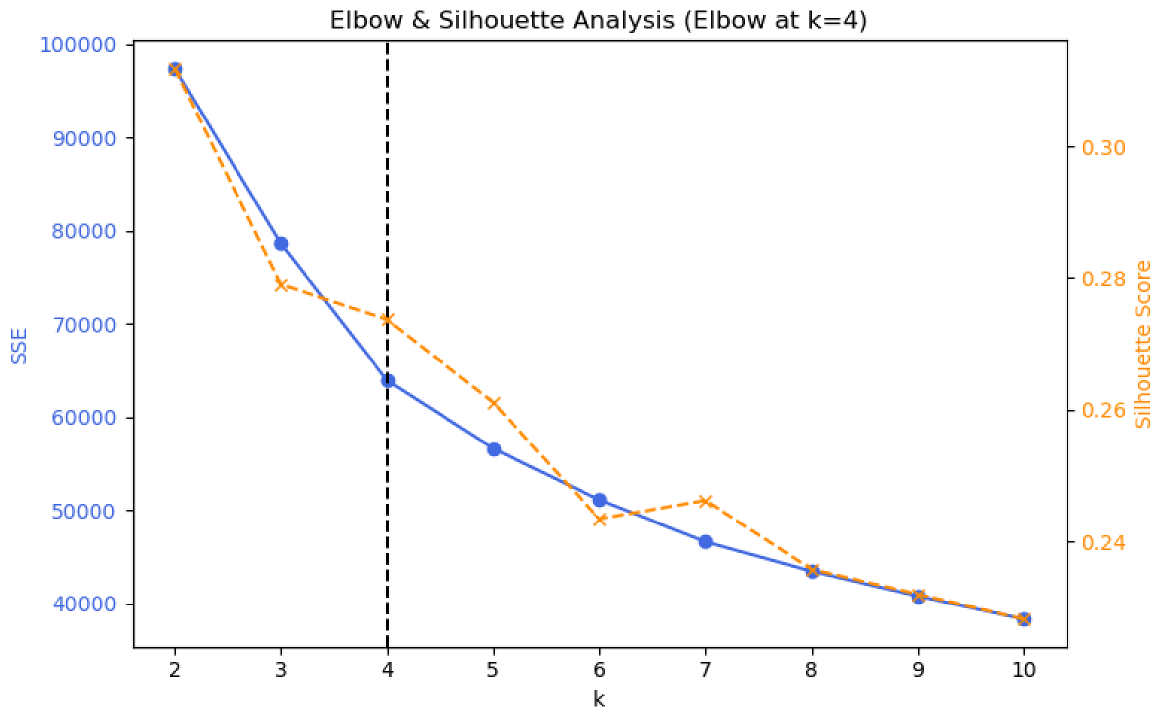


Figure 8. Elbow & Silhouette Analysis

As vividly shown in **Figure 8** the elbow method suggests k = 4, and the silhouette scores are relatively high at this point.

```
In [25]: gdf_c_plot = gdf.copy()
gdf_c_plot = gdf_c_plot.rename(columns={"LSOA11CD": "LSOA_Code"})
```

```
X = df_all[['PCA_1', 'PCA_2', 'PCA_3', 'PCA_4']]
lsoa_codes = df_all["LSOA_Code"].values

# KMeans clustering
kmeans = KMeans(n_clusters=4, random_state=5525, n_init=10)
labels = kmeans.fit_predict(X)

# merge the cluster labels with the gdf
df_clustered = pd.DataFrame({"LSOA_Code": lsoa_codes, "cluster": labels})
gdf_plot = gdf_c_plot.merge(df_clustered, on="LSOA_Code", how="left")

fig, ax = plt.subplots(figsize=(10, 8))
gdf_plot.plot(
    column="cluster",
    categorical=True,
    legend=True,
    cmap="Set2",
    linewidth=0.1,
    edgecolor="grey",
    ax=ax
)
ax.set_title("2021-2024: KMeans Clusters (k=4)", fontsize=14)
ax.axis("off")

plt.tight_layout()
plt.show()
```

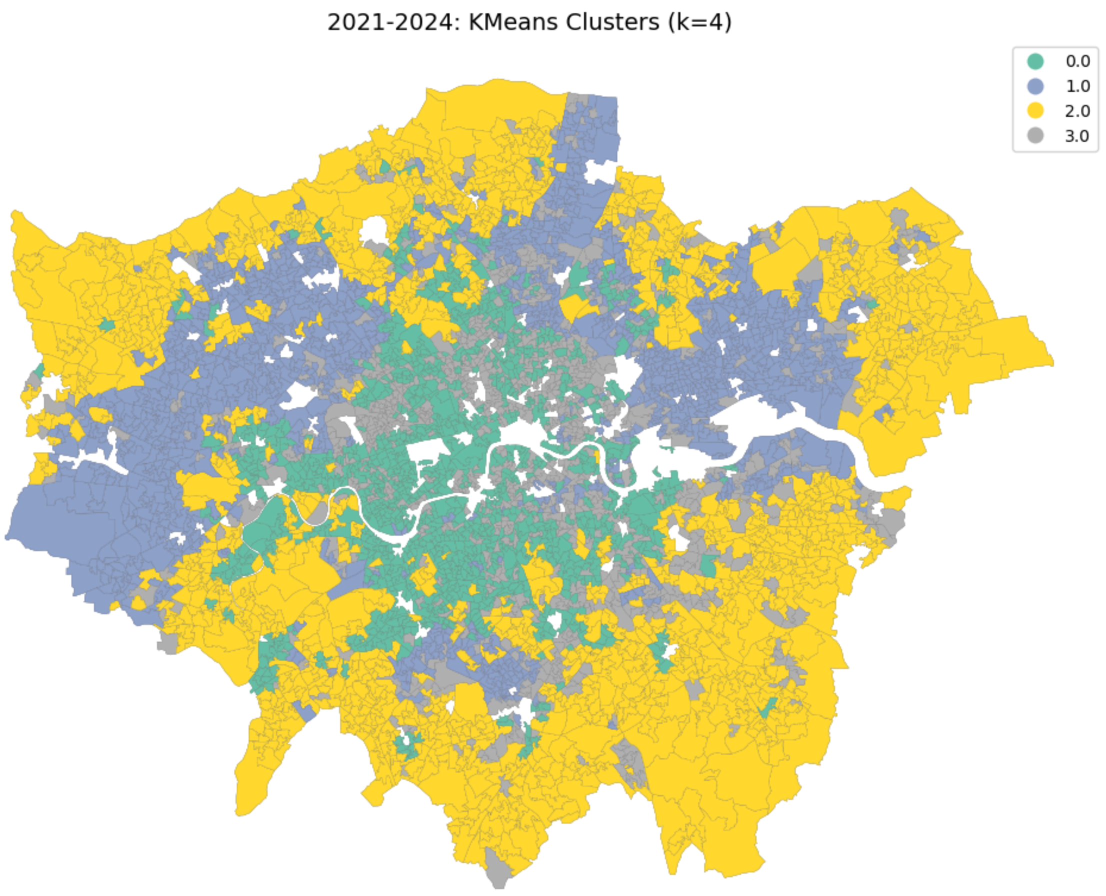


Figure 9. KMeans Clusters

In [26]:
```
# print the average PC score of each cluster
df_all['cluster'] = labels
print(df_all.groupby('cluster')[['PCA_1', 'PCA_2', 'PCA_3', 'PCA_4']].mea
```

```
            PCA_1     PCA_2     PCA_3     PCA_4
cluster
0       -1.396080  1.621061  0.239188  0.025322
1        1.661418 -0.081466 -1.289811  0.005961
2       -1.773209 -1.184461 -0.048706 -0.013704
3        1.769938 -0.126356  1.389657 -0.017086
```

The clustering maps (**Figure 9**) reveal some spatial variation over time, particularly in central and edge areas, highlighting the socio-economic heterogeneity across London's LSOAs. Based on the scores of four PCs above, the KMeans algorithm identifies four distinct residential types:

- **Cluster 0** represents relatively affluent areas with good public transport access and a high proportion of non-English-speaking households.
- **Cluster 1** includes socioeconomically disadvantaged but lower-density zones, often located at the urban–suburban fringe.
- **Cluster 2** shows the most advantaged profile—higher income, better education, and stable housing—but with weaker transport connectivity.
- **Cluster 3** captures areas with severe deprivation, overcrowding, and cultural isolation, likely reflecting high-density social housing.

The spatial pattern of clusters broadly aligns with the crime rate heatmaps (**Figure 10**), especially in inner and outer LSOAs. Clusters 1 and 3 are associated with higher crime, while Clusters 0 and 2 tend to show lower crime rates. The contrast in crime levels across clusters supports the reason for further regression analysis.

In [27]:
```
df_year = df_all.groupby('LSOA_Code')['Crime_Rate_per_1000'].mean().reset

pt = PowerTransformer(method='yeo-johnson')
df_year['Crime_Rate_yj'] = scaler.fit_transform(df_year[['Crime_Rate_per_

fig, ax = plt.subplots(figsize=(10, 8))

gdf_crime = gdf_c_plot.copy()
gdf_crime = gdf_crime.merge(df_year, on="LSOA_Code", how="left")

gdf_crime['Crime_Quartile'] = pd.qcut(gdf_crime['Crime_Rate_yj'], q=4, la

gdf_crime.plot(
    column='Crime_Quartile',
    cmap='viridis',
    categorical=True,
    legend=True,
    linewidth=0.1,
    edgecolor='grey',
    ax=ax
)

ax.set_title("London Crime Rate Heatmap", fontsize=14)
ax.axis("off")
```

```
plt.tight_layout()
plt.show()
```

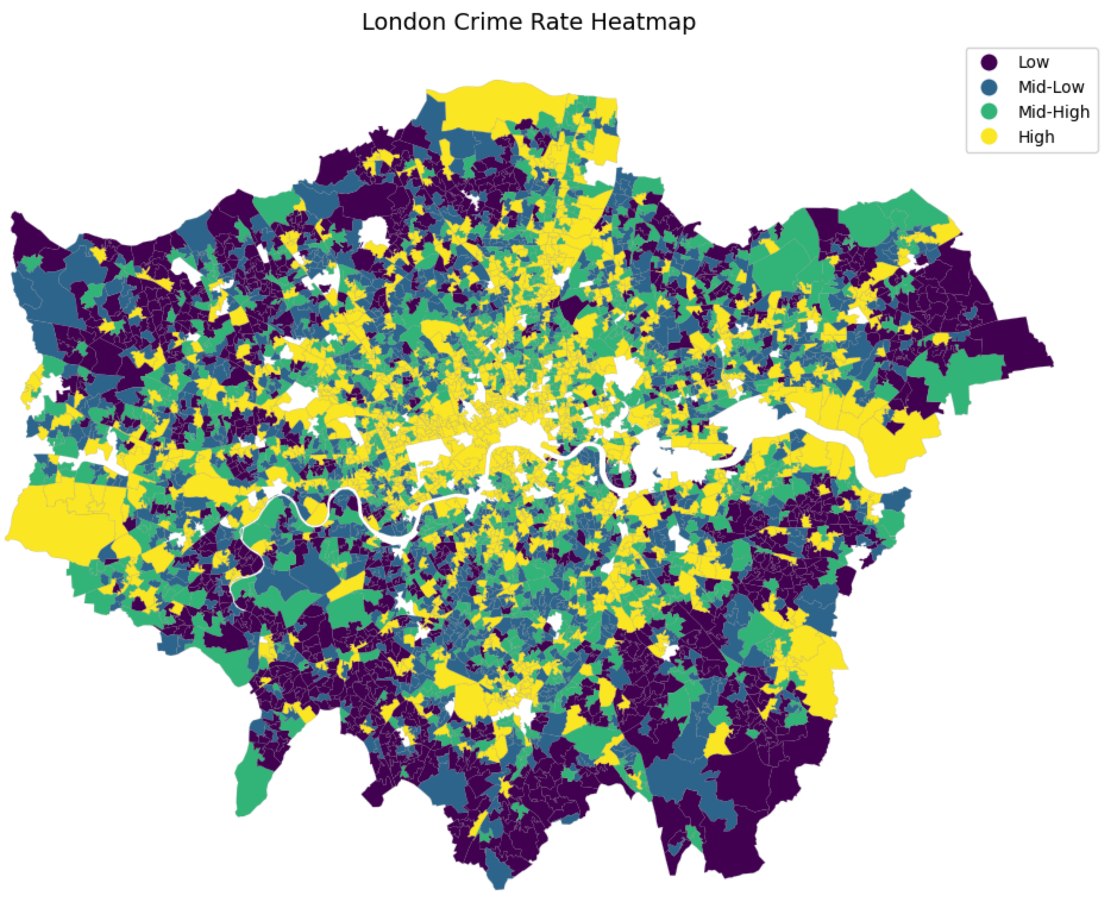


Figure 10. London Crime Rate Heatmap

4.2. Liner Regression

Check Assumptions

In [28]:
```
# A. Linearity
plt.figure(figsize=(6, 4))

sns.pairplot(
    df_all[["Crime_Rate_yj", "PCA_1", "PCA_2", "PCA_3", "PCA_4"]],
    diag_kind="kde",
    kind="reg",
    corner=True,
    height=2,
    aspect=2, #the picture is compressed here for typesetting
    plot_kws={"line_kws": {"color": "red"},
              "scatter_kws": {"alpha": 0.3, "s": 10}}
)

plt.suptitle("Pairwise Relationships of PCA and Crime Rate", fontsize=12)
plt.tight_layout()
plt.show()
```

```
<Figure size 600x400 with 0 Axes>
```

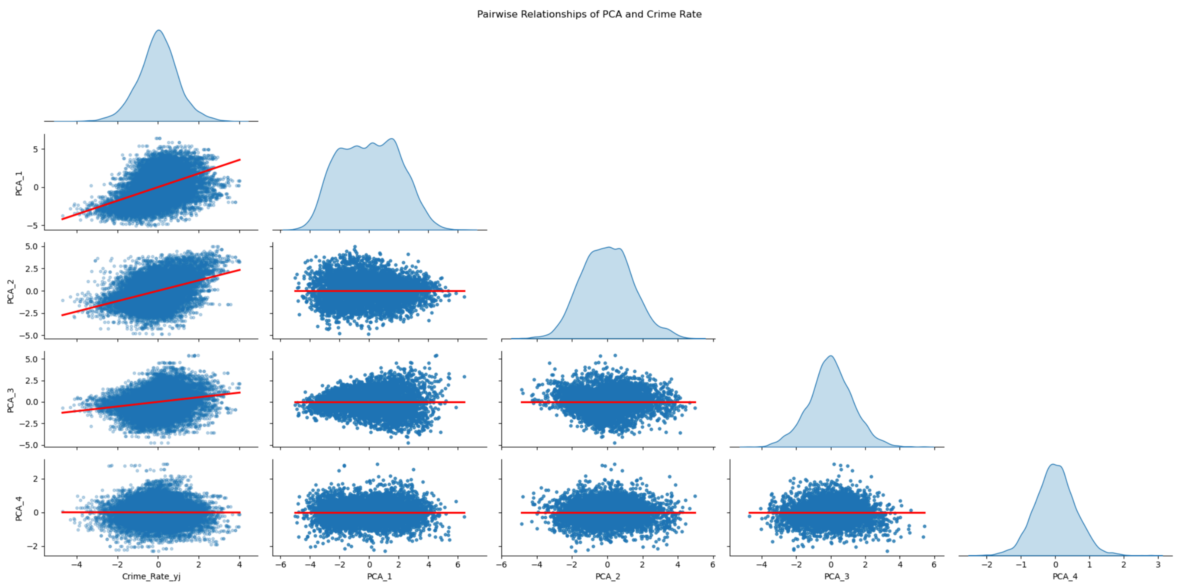
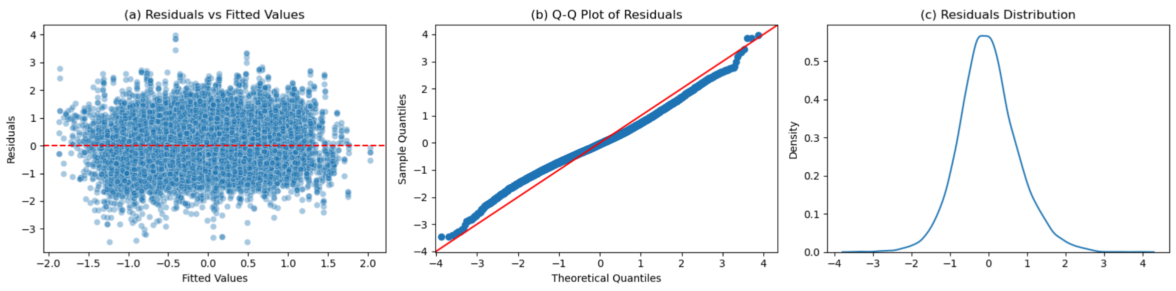


Figure 11. Pairwise Relationships of PCA and Crime Rate

```
In [29]: # fit the model
X = df_all[["PCA_1", "PCA_2", "PCA_3", "PCA_4"]]
X = sm.add_constant(X)
y = df_all["Crime_Rate_yj"]

model = sm.OLS(y, X).fit()


fig, axs = plt.subplots(1, 3, figsize=(16, 4))

# B. Homoscedasticity
# left: Residuals vs Fitted
fitted_vals = model.fittedvalues
residuals = model.resid
sns.scatterplot(x=fitted_vals, y=residuals, alpha=0.4, ax=axs[0])
axs[0].axhline(0, color='red', linestyle='--')
axs[0].set_xlabel("Fitted Values")
axs[0].set_ylabel("Residuals")
axs[0].set_title("(a) Residuals vs Fitted Values")

# C. Normality of residuals
# middle: Q-Q plot
sm.qqplot(residuals, line='45', ax=axs[1])
axs[1].set_title("(b) Q-Q Plot of Residuals")

# right: KDE plot
sns.kdeplot(residuals, ax=axs[2])
axs[2].set_title("(c) Residuals Distribution")

plt.tight_layout()
plt.show()


# D. Independence of errors
dw_stat = durbin_watson(model.resid)
print("Durbin-Watson statistic:", dw_stat)
```



```
Durbin-Watson statistic: 0.6487436928814837
```

Figure 12. Homoscedasticity and Normality of residuals test

Model assumptions were checked across five aspects.

A. Linearity: Scatterplots and fitted lines from **Figure 11** suggest a roughly linear relationship between most PCs and crime rate.

B. Homoscedasticity: The residuals vs. fitted plot (**Figure 12 - a**) shows a cloud-like pattern without funnel shapes, indicating fairly constant variance.

C. Normality of residuals: The QQ plot (**Figure 12 - b**) and KDE plot (**Figure 12 - c**) show residuals are approximately normal.

D. Independence of errors: The Durbin–Watson statistic is below 2 suggests positive autocorrelation, possibly due to the static nature of census-based variables across 2021–2024.

E. Multicollinearity: Addressed through PCA.

The model is specified as follows.

Linear Regression Results

```
In [30]: print(model.summary())
```

```
                            OLS Regression Results
==========================================================================
====
Dep. Variable:          Crime_Rate_yj   R-squared:
0.406
Model:                            OLS   Adj. R-squared:
0.406
Method:                 Least Squares   F-statistic:                     3
181.
Date:                Mon, 21 Apr 2025   Prob (F-statistic):
0.00
Time:                        11:46:59   Log-Likelihood:                -21
560.
No. Observations:               18612   AIC:                         4.313
e+04
Df Residuals:                   18607   BIC:                         4.317
e+04
Df Model:                           4
Covariance Type:            nonrobust
==========================================================================
====
                 coef    std err          t      P>|t|      [0.025      0.
975]
--------------------------------------------------------------------------
----
const       2.254e-15      0.006   3.99e-13      1.000      -0.011
0.011
PCA_1          0.2230      0.003     78.980      0.000       0.217
0.229
PCA_2          0.2804      0.004     71.518      0.000       0.273
0.288
PCA_3          0.1629      0.004     37.038      0.000       0.154
0.171
PCA_4         -0.0036      0.009     -0.375      0.707      -0.022
0.015
==========================================================================
====
Omnibus:                      386.964   Durbin-Watson:
0.649
Prob(Omnibus):                  0.000   Jarque-Bera (JB):               61
2.369
Skew:                           0.208   Prob(JB):                    1.06e
-133
Kurtosis:                       3.785   Cond. No.
3.35
==========================================================================
====

Notes:
[1] Standard Errors assume that the covariance matrix of the errors is cor
rectly specified.
```

The PCA-based OLS regression explains approximately 40.6% of the variance in crime rate ($R^2 = 0.406$). All components included in the model are statistically significant ($p < 0.001$) except for PC4, suggesting that the retained socio-economic structural variables are relevant, but not fully explanatory.

The fitted model:

Crime_Rate_yj = 0.2230 × PC1 + 0.2804 × PC2 + 0.1629 × PC3

In [31]:
```
# extract the loading matrix W (variables × PC) of the first four princip
W = loadings.iloc[:, :3].values  # shape: (num_vars, 3)

# extract their regression coefficients β
beta_vector = np.array([0.2230, 0.2804, 0.1629])  # shape: (3,)

# Calculate the coefficient θ of the restored variable.
theta = W @ beta_vector  # shape: (num_vars,)

original_coef = pd.DataFrame({
    'variable': loadings.index,
    'coefficient': theta
}).sort_values(by='coefficient', ascending=False)

print(original_coef.round(4))
```

```
                     variable  coefficient
3                 No_Car_Rate       0.2433
8                     PTA_log       0.2258
2          Unemployed_Rate_log       0.1164
5            Poor_Health_Rate       0.0870
1  Non_English_Household_Rate       0.0821
4          Overcrowding_Rate       0.0793
6              Disabled_Rate       0.0593
7          Long_Term_Sick_Rate      -0.0179
0          Low_Education_Rate      -0.0823
```

To enhance interpretability, the original variable-level coefficients were recovered using the formula:

Crime_Rate_yj = X · θ = X · (W × β)

where:

- X is matrix of original (standardised) variables;
- W is the loadings matrix from PCA;
- θ represents recovered coefficients for the original variables;
- β represents the regression coefficients for retained components.

This back-transformation allows for estimating the individual effect of each original feature on the crime rate and better understand the structural drivers behind it: transport access, car ownership and Unemployment are among the strongest predictors of crime rate, followed by health-related and culture isolation (non-english) indicators.

4.4. Machine Learning

Based on this, a set of predictive models was implemented to further assess the explanatory power of structural variables. Linear Regression, Lasso, Support Vector Regression (SVR), Random Forest, and XGBoost were applied and compared under consistent settings, including the same train-test split, standardised inputs, and evaluation metrics (R^2 and RMSE).

In [32]:
```
# separate features and targets
features = [
    "Low_Education_Rate",
    "Non_English_Household_Rate",
    "Unemployed_Rate_log",
    "No_Car_Rate",
    "Overcrowding_Rate",
    "Poor_Health_Rate",
    "Disabled_Rate",
    "Long_Term_Sick_Rate",
    "PTA_log"
]
X = df_all[features]
y = df_all["Crime_Rate_yj"]

# split training/testing
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,

#standardization (only fit on the training set)
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)

# set up models
models = {
    "LinearRegression": LinearRegression(),
    "Lasso": Lasso(alpha=0.1, random_state=5525),
    "SVR": SVR(kernel='rbf'),
    "RandomForest": RandomForestRegressor(n_estimators=100, random_state=
    "XGBoost": XGBRegressor(n_estimators=100, learning_rate=0.1, max_dept
}

# training and evaluation
results = []
for name, model in models.items():
    model.fit(X_train_scaled, y_train)
    y_pred = model.predict(X_test_scaled)
    results.append({
        "Model": name,
        "R²": r2_score(y_test, y_pred),
        "RMSE": np.sqrt(mean_squared_error(y_test, y_pred))
    })

results_df = pd.DataFrame(results)
print(results_df)
```

```
               Model        R²      RMSE
0  LinearRegression  0.409688  0.765884
1             Lasso  0.386709  0.780648
2               SVR  0.537408  0.677986
3      RandomForest  0.855679  0.378692
4           XGBoost  0.529260  0.683931
```

In [33]:
```
fig, axes = plt.subplots(2, 3, figsize=(18, 10))
axes = axes.flatten()

for i, (name, model) in enumerate(models.items()):
    y_pred = model.predict(X_test_scaled)
    ax = axes[i]
    ax.scatter(y_test, y_pred, alpha=0.3)
    ax.plot([y_test.min(), y_test.max()], [y_test.min(), y_test.max()], '
    ax.set_title(f"{name}: Predicted vs Actual")
    ax.set_xlabel("True Crime Rate")
    ax.set_ylabel("Predicted Crime Rate")
    ax.grid(True)

fig.delaxes(axes[-1])

plt.suptitle("Model Performance Comparison: Predicted vs True Values", fo
plt.tight_layout(rect=[0, 0.03, 1, 0.95])
plt.show()
```

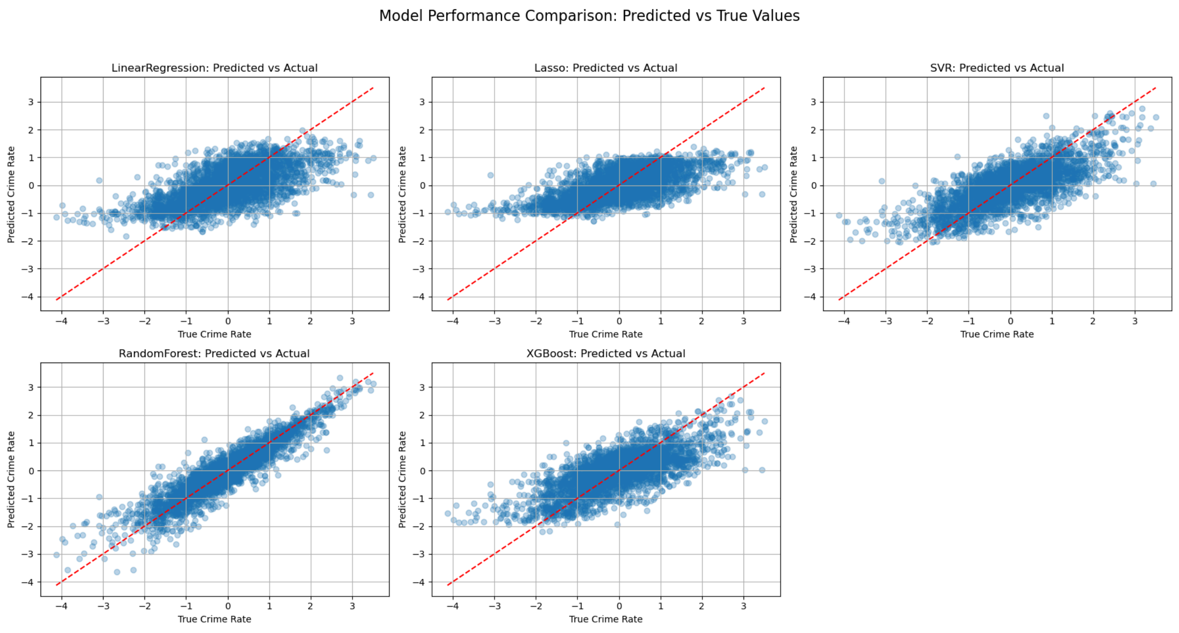


Figure 13. Predictions vs True Values

In [34]:
```
# Extract R² of linear regression as baseline
baseline_r2 = results_df[results_df["Model"] == "LinearRegression"]["R²"]

sns.set(style="whitegrid")
palette = sns.color_palette("pastel")

fig, ax1 = plt.subplots(figsize=(10, 6))

# R²  bar plot
palette = sns.color_palette("pastel")[:5]
sns.barplot(x="Model", y="R²", hue="Model", data=results_df, ax=ax1, pale
ax1.set_ylabel("R² Score", color="blue")
ax1.set_ylim(0, 1.0)

# add baseline
ax1.axhline(baseline_r2, color='gray', linestyle='--', linewidth=1.5, lab
ax1.legend(loc='upper left')

# RMSE line plot
ax2 = ax1.twinx()
sns.lineplot(x="Model", y="RMSE", data=results_df, ax=ax2, color="red", m
ax2.set_ylabel("RMSE", color="red")

plt.title("Model Performance Comparison: R² and RMSE", fontsize=14)
plt.tight_layout()
plt.show()
```

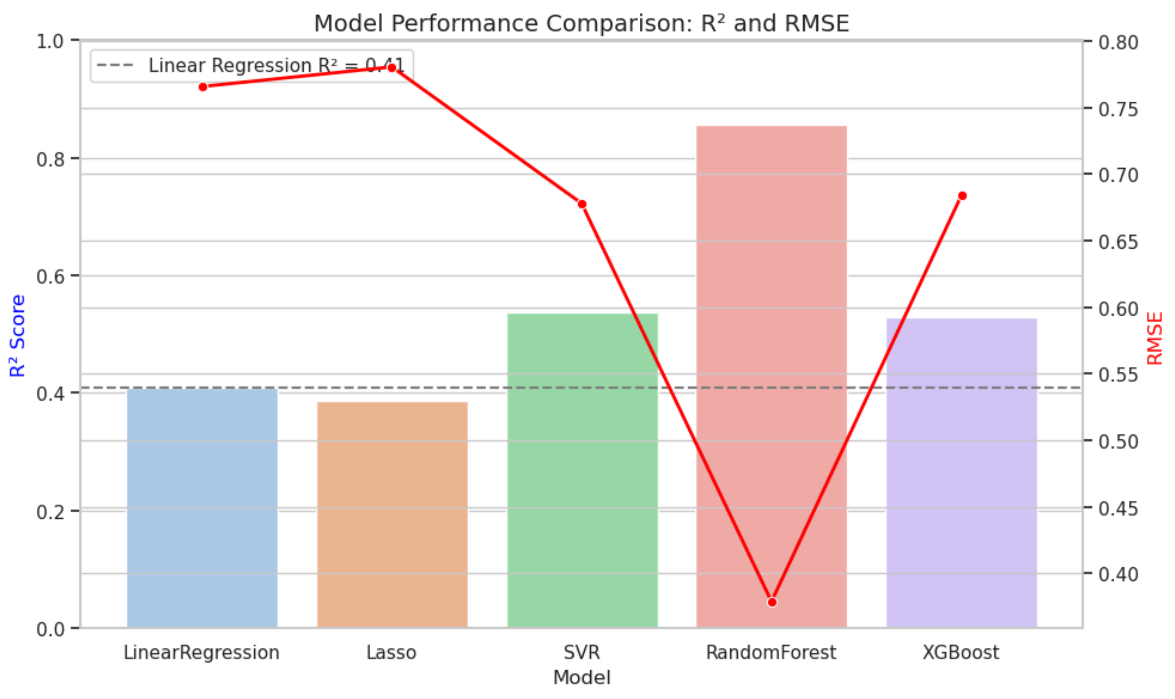


Figure 14. Model Performance Comparison: R^2 and RMSE

The results reveal that:

1. **Linear models** offer limited explanatory power ($R^2 \approx 0.4$), suggesting that while structural variables are relevant to crime rate, many non-linear effects and interactions remain uncaptured.
2. Non-linear models, particularly **Random Forest**, show substantial performance gains, highlighting the need to account for more complex patterns when modelling crime.
3. **Lasso** performs worst in this context, likely due to the lack of sparsity in the selected features.
4. **SVR** and **XGBoost** show moderate performance between Linear models and Random Forest.

Overall, Random Forest or XGBoost is recommended when predicting.

Test Generalization Ability of Random Forest and XGBoost

In [35]:
```
param_grid_rf = {
    'n_estimators': [100, 200],
    'max_depth': [10, 20, None],
    'min_samples_split': [2, 5],
    'min_samples_leaf': [1, 2],
    'max_features': ['sqrt', 'log2']
}

grid_rf = GridSearchCV(
    RandomForestRegressor(random_state=5525),
    param_grid_rf,
    cv=3, scoring='r2', n_jobs=-1
)

grid_rf.fit(X_train_scaled, y_train)
print("Best RF params:", grid_rf.best_params_)
print("Best RF R² on CV:", grid_rf.best_score_)
```

```
Best RF params: {'max_depth': None, 'max_features': 'sqrt', 'min_samples_l
eaf': 1, 'min_samples_split': 2, 'n_estimators': 200}
Best RF R² on CV: 0.8048535824517881
```

Although the Random Forest model achieved a high R^2 (0.8557) when refitted on the full dataset, the cross-validated score from GridSearchCV ($R^2 = 0.8049$) is more reliable, as it reflects the model's average generalisation performance.

In [36]:
```
param_grid_xgb = {
    'n_estimators': [100, 200],
    'max_depth': [3, 6],
    'learning_rate': [0.05, 0.1],
    'subsample': [0.8, 1.0],
    'colsample_bytree': [0.8, 1.0],
    'gamma': [0, 1]
}

grid_xgb = GridSearchCV(
    XGBRegressor(random_state=5525, verbosity=0),
    param_grid_xgb,
    cv=3, scoring='r2', n_jobs=-1
)

grid_xgb.fit(X_train_scaled, y_train)
print("Best XGB params:", grid_xgb.best_params_)
print("Best XGB R² on CV:", grid_xgb.best_score_)
```

```
Best XGB params: {'colsample_bytree': 1.0, 'gamma': 0, 'learning_rate': 0.
1, 'max_depth': 6, 'n_estimators': 200, 'subsample': 0.8}
Best XGB R² on CV: 0.7358687085463188
```

The best XGBoost R^2 on cross-validation was 0.7359, indicating that structural variables offer strong predictive power for crime rate, even though performance is slightly lower than that of Random Forest.

5. Results and discussion

[go back to the top]

PC1 reflects broad socio-economic deprivation and is positively associated with crime. PC2 indicates urban connectivity, PC3 captures language isolation, and PC4 relates to health—each contributing differently to spatial crime variation.

Clustering results further reveal spatially distinct neighbourhood types, with high-crime areas concentrated in central London, suggesting persistent structural patterns.

While linear models show limited explanatory power, non-linear predictive models—especially Random Forest—perform substantially better.This performance difference highlights the complex non-linear relationship between structural characteristics and crime.

6. Conclusion

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This study shows that socio-economic structures shape crime patterns across London's LSOAs to some extent. While linear models offer limited explanatory power—possibly due to non-linearity or missing variables—machine learning models achieve strong predictive performance, highlighting the value of structural data in forecasting crime.

However, the use of static 2021 census variables may limit temporal generalisability.

Future work may incorporate longitudinal data, geographically weighted regression (GWR), or non-linear interaction modelling to further enhance explanatory power.

7.References

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In [37]:
```
end_time = time.time()
total_time = end_time - start_time

mins, secs = divmod(total_time, 60)
print(f"🕒 Notebook running time: {int(mins)} m {secs:.2f} s")
```

```
🕒 Notebook running time: 2 m 51.52 s
```

In [38]:
```
%load_ext watermark
%watermark
%watermark -iv
```

```
Last updated: 2025-04-21T11:48:18.261440+00:00

Python implementation: CPython
Python version       : 3.11.9
IPython version      : 8.27.0

Compiler    : GCC 12.3.0
OS          : Linux
Release     : 6.10.14-linuxkit
Machine     : aarch64
Processor   : aarch64
CPU cores   : 8
Architecture: 64bit

xgboost    : 2.1.1
sklearn    : 1.5.2
matplotlib : 3.8.4
json       : 2.0.9
nbformat   : 5.10.4
geopandas  : 1.0.1
requests   : 2.32.3
statsmodels: 0.14.3
seaborn    : 0.13.2
numpy      : 1.26.4
sys        : 3.11.9 | packaged by conda-forge | (main, Apr 19 2024, 18:25:
01) [GCC 12.3.0]
pandas     : 2.2.2
IPython    : 8.27.0
kneed      : 0.8.5
```

```
In [ ]:
```