

Fixed Time Survival Analysis

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```
# Load the needed packages
library(ggplot2)
library(dplyr)
library(lubridate)
library(survival)
library(ggsurvfit)
library(gtsummary)
library(here)
library(survminer)
library(broom)
library(forestploter)
library(tidyr)
```

```
# Load example data
df <- colon
```

This analysis focus on survival following the chemotherapy treatment for colon cancer.

About the sample data

The data come from the `colon` dataset, available from the *survival* package. These data include information from a clinical trial on the effectiveness of two different types of chemotherapy (levamisole and levamisole+5-fluorouracil) compared to controls (i.e. no chemotherapy treatment) on survival from stage B/C colon cancer.

There are two rows per person in the dataset, one for cancer recurrence and one for death, indicated by the event type (`etype`) variable (`etype==1` corresponds to recurrence and `etype==2` to death). In analysis below, I only focus on analysing death as an outcome.

Note: there is some incomplete values on the `differ` variable, for simplicity, in the below analysis, I drop those incomplete values.

Some important variables:

rx: Treatment - Obs(ervation), Lev(amisole), Lev(amisole)+5-FU **sex:** 1=male **age:** in years **obstruct:** obstruction of colon by tumour **perfor:** perforation of colon **adhere:** adherence to nearby organs **nodes:** number of lymph nodes with detectable cancer **time:** days until event or censoring **status:** censoring status **differ:** differentiation of tumour (1=well, 2=moderate, 3=poor) **extent:** Extent of local spread (1=submucosa, 2=muscle, 3=serosa, 4=contiguous structures) **surg:** time from surgery to registration (0=short, 1=long) **node4:** more than 4 positive lymph nodes **etype:** event type: 1=recurrence,2=death

Data cleaning

- Filter records with death outcome
- Drop incomplete values on the `diff` variable
- Label the `diff` and `extent` variables
- Stratify the `age` variable

```
df1 <- df %>%
  filter(etype == 2) %>% # Filter to deaths
  filter(!is.na(differ)) %>%
  mutate(
    differF = factor(differ, levels = 1:3, labels = c("well","moderate","poor")),
    extentF = factor(extent, levels = 1:4, labels = c("submucosa","muscle","serosa","contiguous"))
```

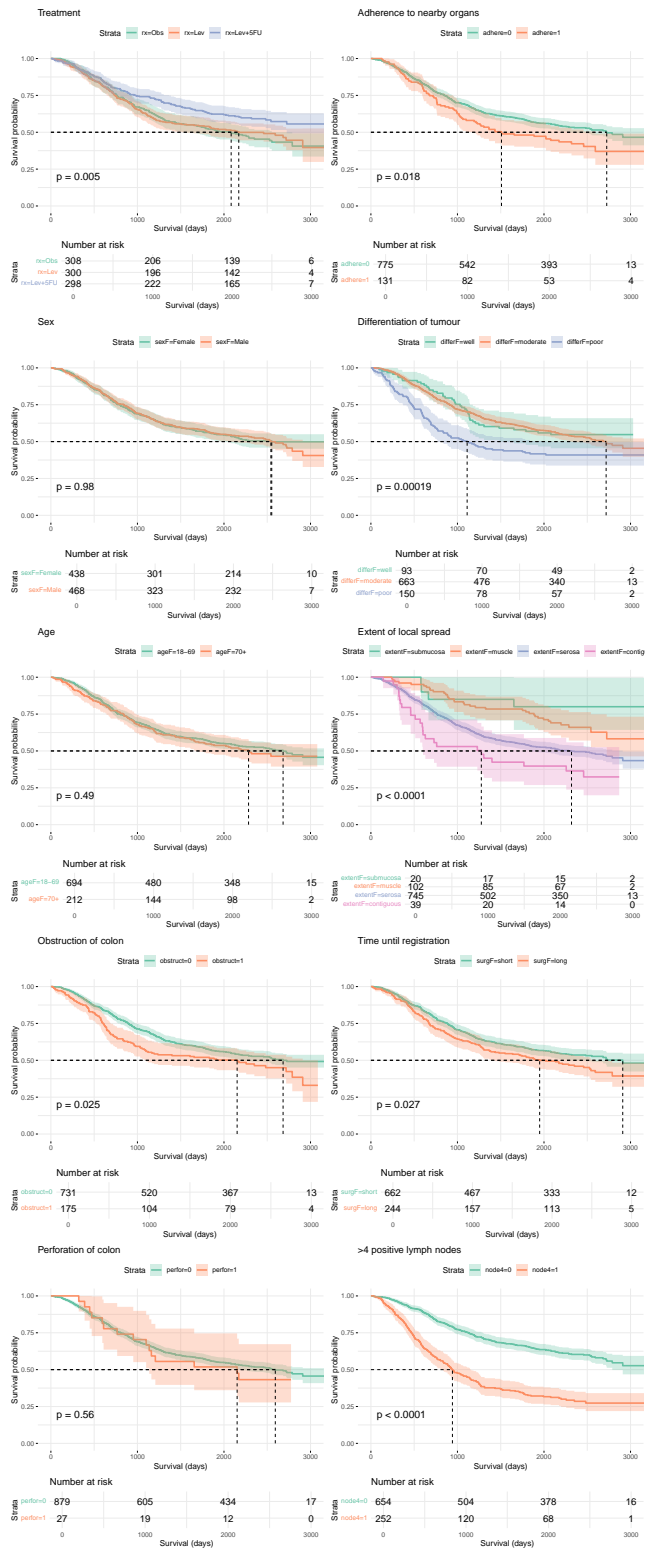
```
ageF = factor(ifelse(age<70, 1, 2), levels = 1:2, labels = c('18-69', '70+')),  
sexF = factor(sex, levels = 0:1, labels = c("Female","Male")),  
surgF = factor(surg, levels = 0:1, labels = c("short", "long"))  
)
```

EDA

Table 1: Summary of demographics and disease status by treatment group

Figure 1: Kaplan-Meier survival plots for key predictors

	Obs	Lev	Lev+5FU	
Total (column denominator)	308 (100%)	300 (100%)	298 (100%)	90
Age				
Mean, (SD)	59, (12)	60, (12)	60, (12)	6
Median, (IQR)	61, (53, 68)	61, (53, 69)	62, (52, 70)	61
Range	18, 85	27, 83	26, 81	
Sex				
Female	146 (47%)	131 (44%)	161 (54%)	43
Male	162 (53%)	169 (56%)	137 (46%)	46
Obstruction of colon	62 (20%)	59 (20%)	54 (18%)	17
Perforation of colon	9 (3%)	10 (3%)	8 (3%)	2
Adherence to nearby organs	45 (15%)	47 (16%)	39 (13%)	13
Differentiation of tumour				
well	27 (9%)	37 (12%)	29 (10%)	9
moderate	229 (74%)	219 (73%)	215 (72%)	66
poor	52 (17%)	44 (15%)	54 (18%)	15
Extent of local spread				
submucosa	7 (2%)	3 (1%)	10 (3%)	2
muscle	36 (12%)	35 (12%)	31 (10%)	10
serosa	248 (81%)	251 (84%)	246 (83%)	74
contiguous	17 (6%)	11 (4%)	11 (4%)	3
Time until registration				
short	218 (71%)	222 (74%)	222 (74%)	66
long	90 (29%)	78 (26%)	76 (26%)	24
>4 positive lymph nodes	87 (28%)	87 (29%)	78 (26%)	25
Days until death/censored				
Mean, (SD)	1,599, (857)	1,615, (894)	1,796, (866)	1,6
Median, (IQR)	1,854, (759, 2,274)	1,910, (741, 2,383)	2,092, (977, 2,472)	1,978,
Range	113, 3,214	24, 3,329	23, 3,309	2
Death	165 (54%)	154 (51%)	122 (41%)	44



Characteristic	Univariable			Multivariable		
	HR ¹	95% CI ¹	p-value	HR ¹	95% CI ¹	p-value
Treatment						
Obs	—	—		—	—	
Lev	0.96	0.77, 1.19	0.7	0.98	0.79, 1.23	0.9
Lev+5FU	0.70	0.55, 0.88	0.002	0.70	0.55, 0.88	0.003
Sex	1.00	0.83, 1.21	>0.9			
Age (70+ years)	1.08	0.87, 1.34	0.5			
Obstruction of colon	1.30	1.03, 1.63	0.025	1.29	1.03, 1.63	0.028
Perforation of colon	1.17	0.70, 1.95	0.6			
Adherence to nearby organs	1.35	1.05, 1.73	0.018	1.19	0.92, 1.53	0.2
Differentiation of tumour						
well	—	—		—	—	
moderate	1.05	0.76, 1.45	0.8	0.93	0.67, 1.29	0.7
poor	1.70	1.18, 2.46	0.005	1.36	0.93, 1.97	0.11
Extent of local spread						
submucosa	—	—		—	—	
muscle	1.83	0.65, 5.15	0.3	1.34	0.47, 3.79	0.6
serosa	3.25	1.21, 8.71	0.019	2.18	0.81, 5.87	0.12
contiguous	5.04	1.75, 14.5	0.003	3.07	1.06, 8.94	0.039
Time until registration	1.26	1.03, 1.54	0.027	1.27	1.03, 1.56	0.022
>4 positive lymph nodes	2.58	2.13, 3.12	<0.001	2.49	2.05, 3.02	<0.001

¹HR = Hazard Ratio, CI = Confidence Interval

Key Findings::

Survival following treatment for colon cancer was not differentiated by age (p=0.58), sex (p=0.49) or perforation of colon (p=0.56).

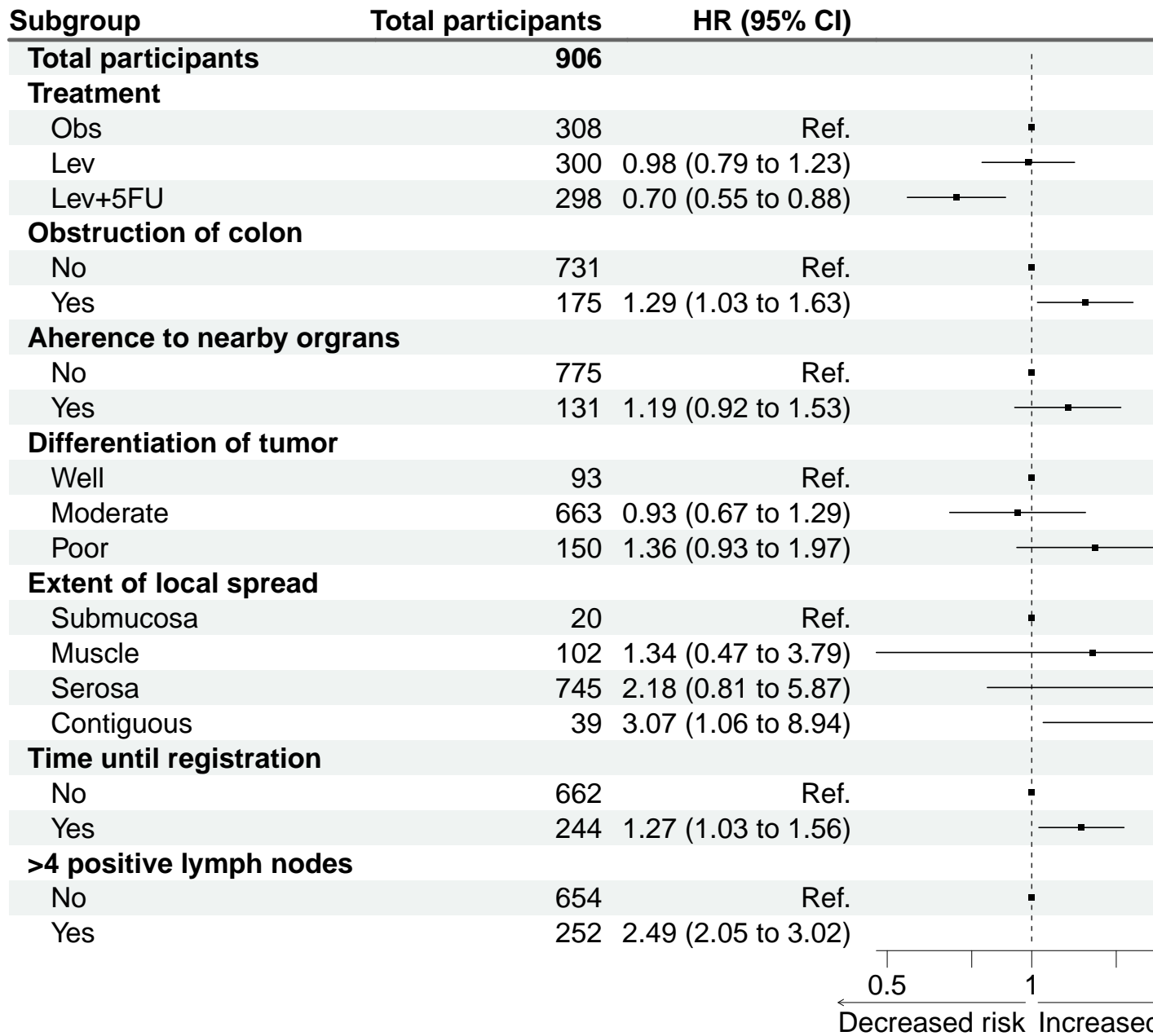
However, survival outcomes did differ across the categories of the remaining variables, with better survival rates associated with the Lev+5FU treatment, unobstructed colon, no adherence to nearby organs, well or moderately differentiated tumour, local spread limited to the submucosa or muscle, shorter time until registration and fewer positive lymph nodes.

Table 2. Hazard ratios and 95% Confidence Intervals for univariable and multivariable Cox regression models

Key Findings:

The estimates confirmed that although treatment with levamisole did not improve outcomes compared to the control group (HR = 0.98, 95% CI = 0.79-1.23), the hazard of death was 30% lower among patients treated with levamisole+5-fluorouracil (HR = 0.70, 95% CI = 0.55-0.88). Other factors significantly associated with increased hazard of death included obstruction of the colon (HR = 1.29, 95% CI = 1.03-1.63), local spread to contiguous regions (HR = 3.07, 95% CI = 1.06-8.94), longer time between surgery and registration (HR = 1.27, 95% CI = 1.03-1.56) and more than 4 positive lymph nodes (HR = 2.49, 95% CI = 2.05-3.02).

Figure 2: Forest plot for hazard ratios and 95% confidence intervals for multivariable Cox regression models



Assessing the proportional hazard assumptions

Using a chi-squared test based on Schoenfeld residuals:

H0: Covariate effect is constant (proportional) over time HA: Covariate effect changes over time

The null hypothesis of proportional hazard is tested for each covariate individually and jointly as well.

If $p < 0.05$ then there is evidence for violation of the proportional hazards assumption.

```
cox.zph(cox_model)
```

```
#>           chisq df      p
#> rx           2.3509  2 0.30869
#> obstruct     6.2760  1 0.01224
#> adhere       0.0775  1 0.78074
#> differF     16.0442  2 0.00033
#> extentF      7.3605  3 0.06125
#> surg         0.0247  1 0.87521
#> node4        5.8260  1 0.01579
#> GLOBAL      36.5773 11 0.00014
```

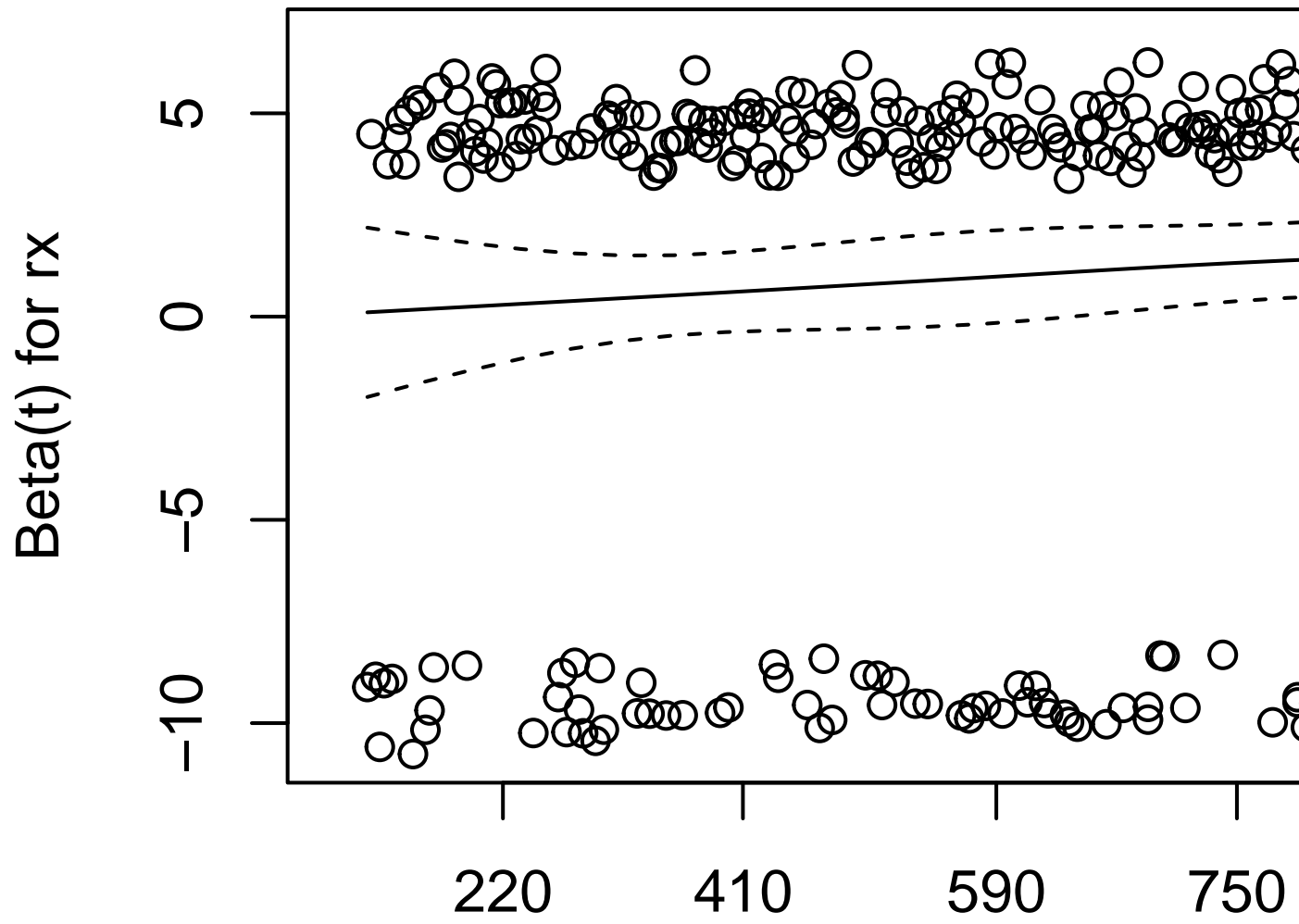
The test confirms that the proportional hazards assumption is violated for obstruction of colon ($p=0.01$), differentiation of tumour ($p < 0.001$) and marginally for extent of local spread ($p=0.06$). The test also suggests that the variable indicating more than 4 positive lymph nodes also violates the assumption ($p=0.016$); the global test also indicates the assumption is invalid ($p<0.001$).

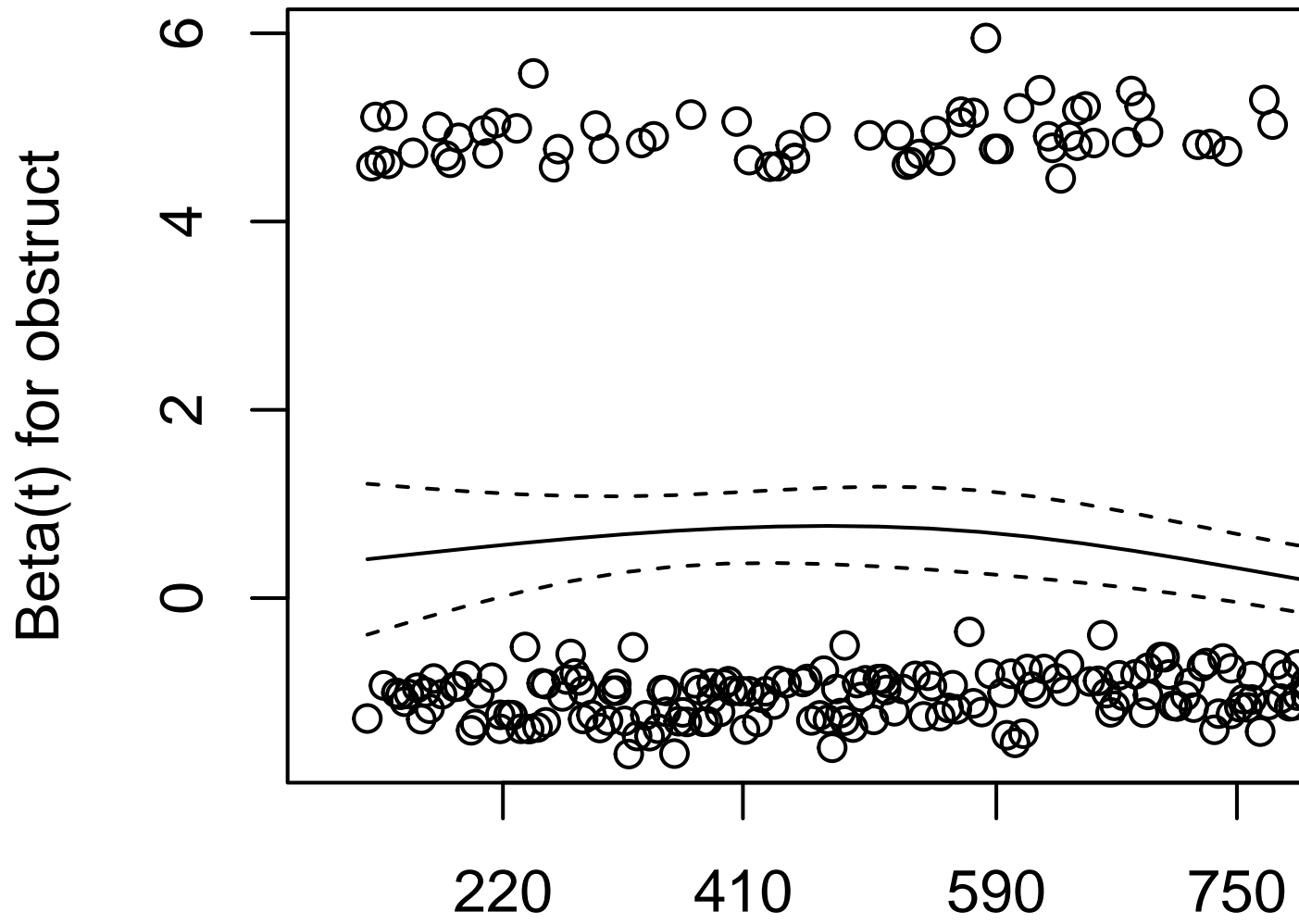
A plot of a smoothed curve over the Schoenfeld residuals

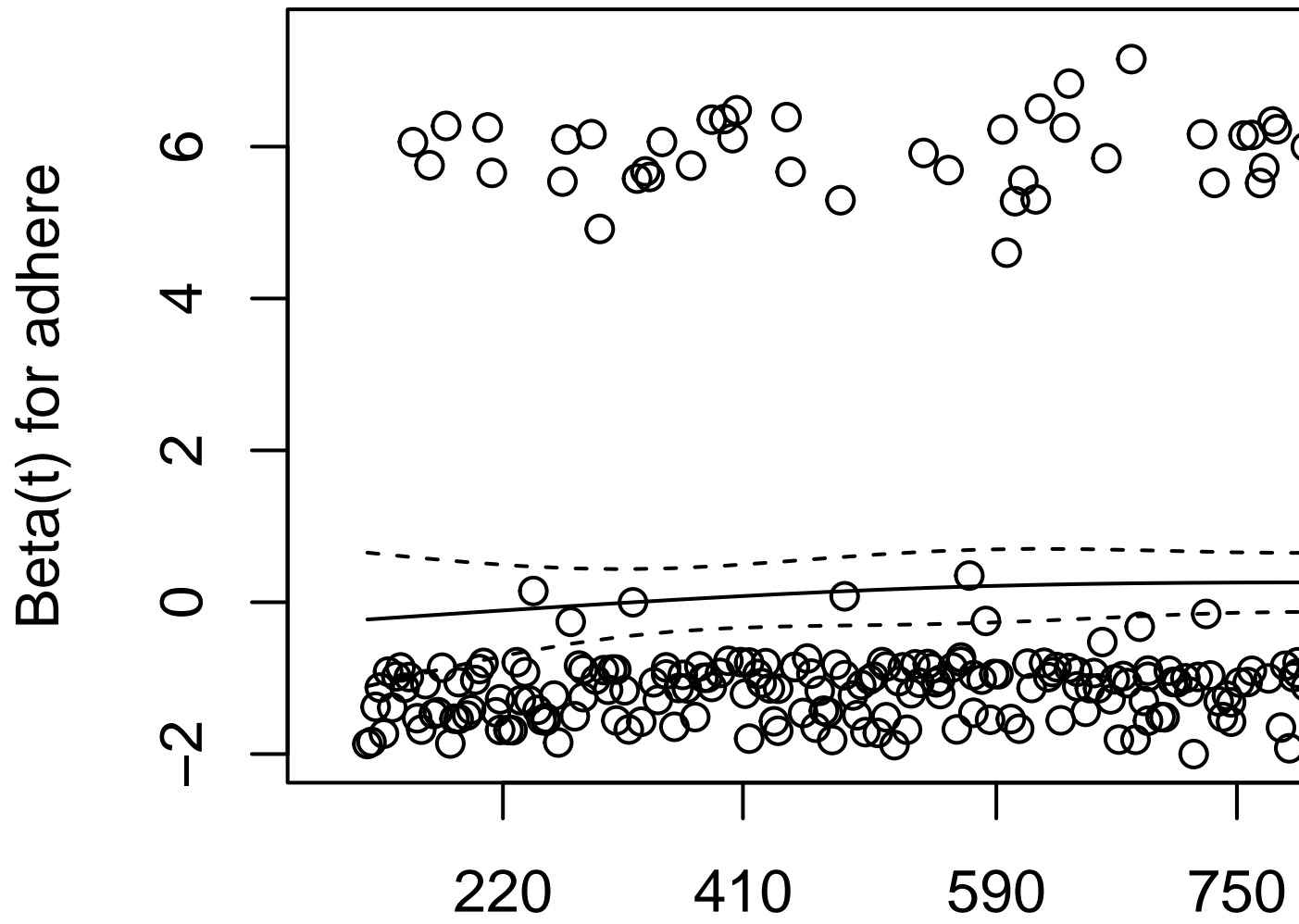
Note: It is actually plotting the coefficient for each predictor at each time point over time). We want to see a flat line over time.

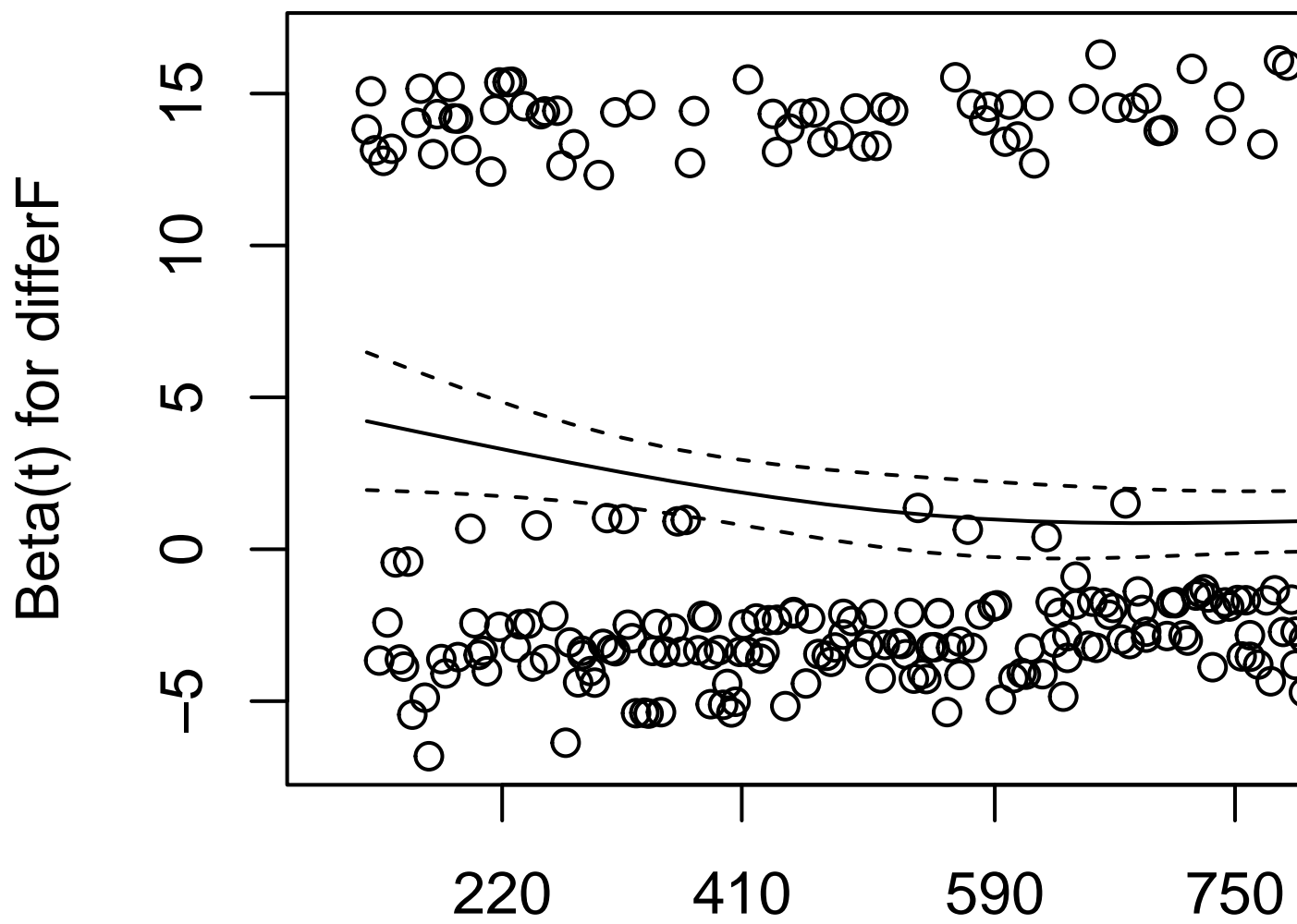
(Side note: If we have a large data, we will be able to detect very small changes of coefficients over time. So if the change in the coefficient is not large enough to be clinically meaningful, it can perhaps be ignored as well).

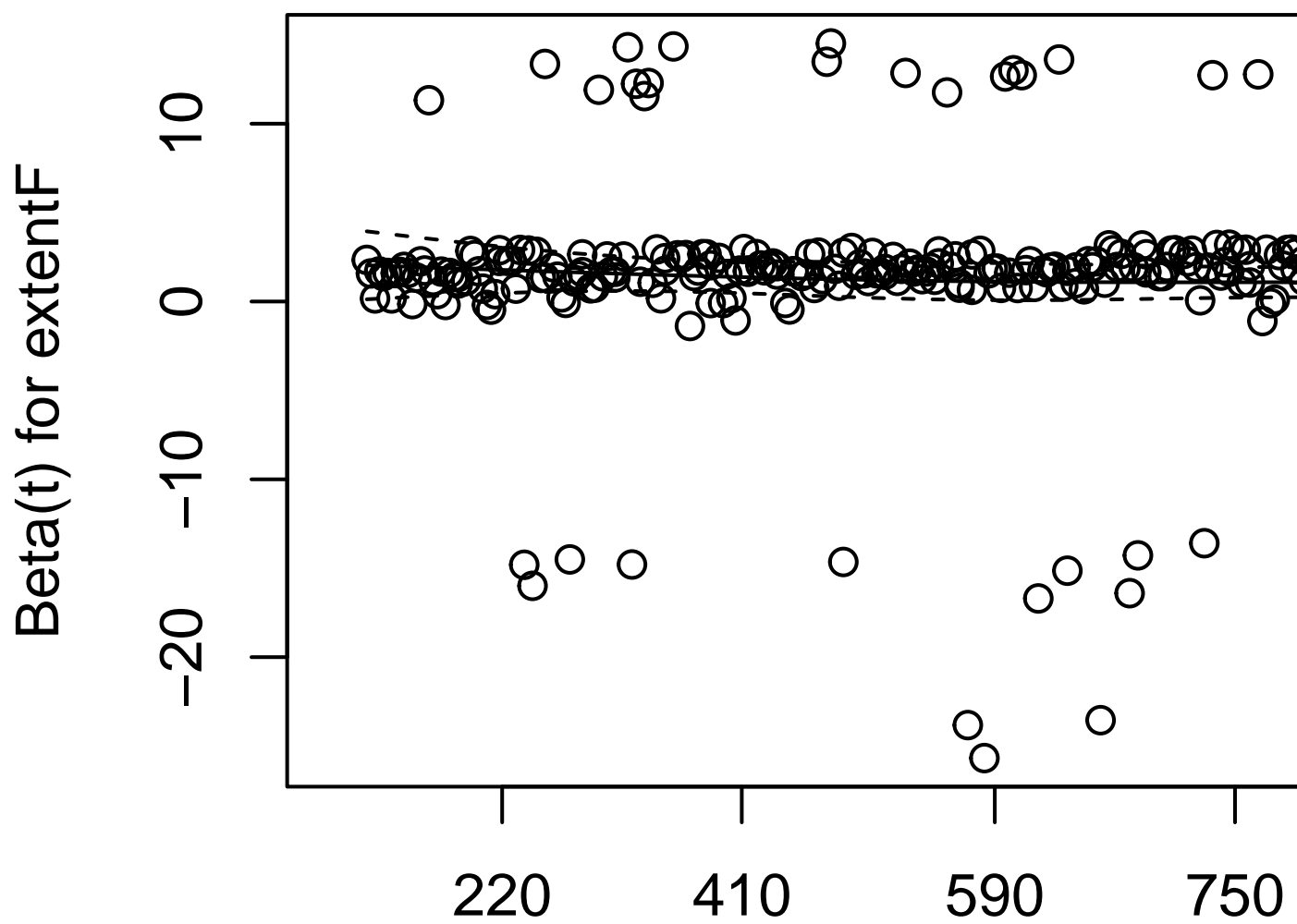
```
plot(cox.zph(cox_model))
```

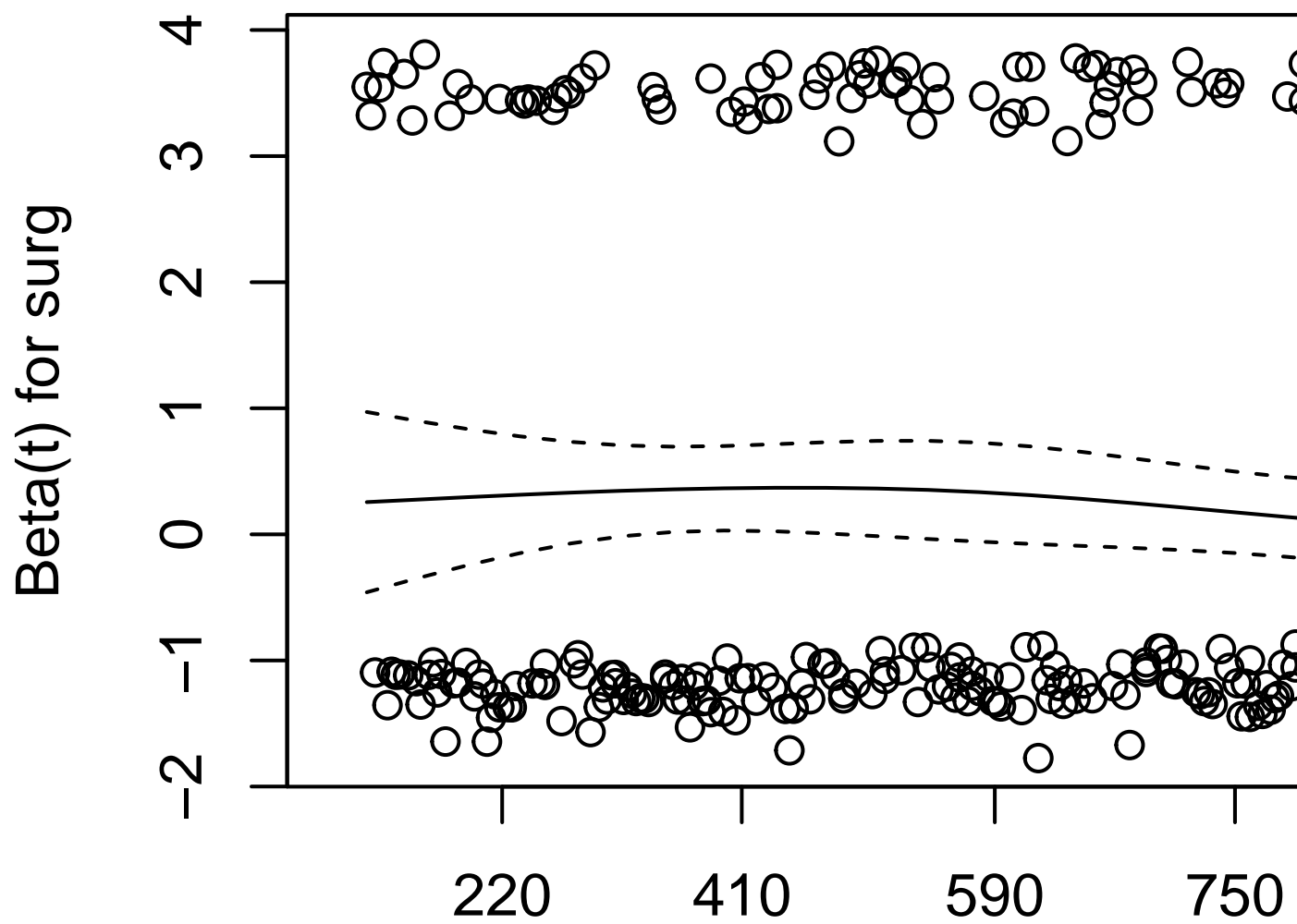


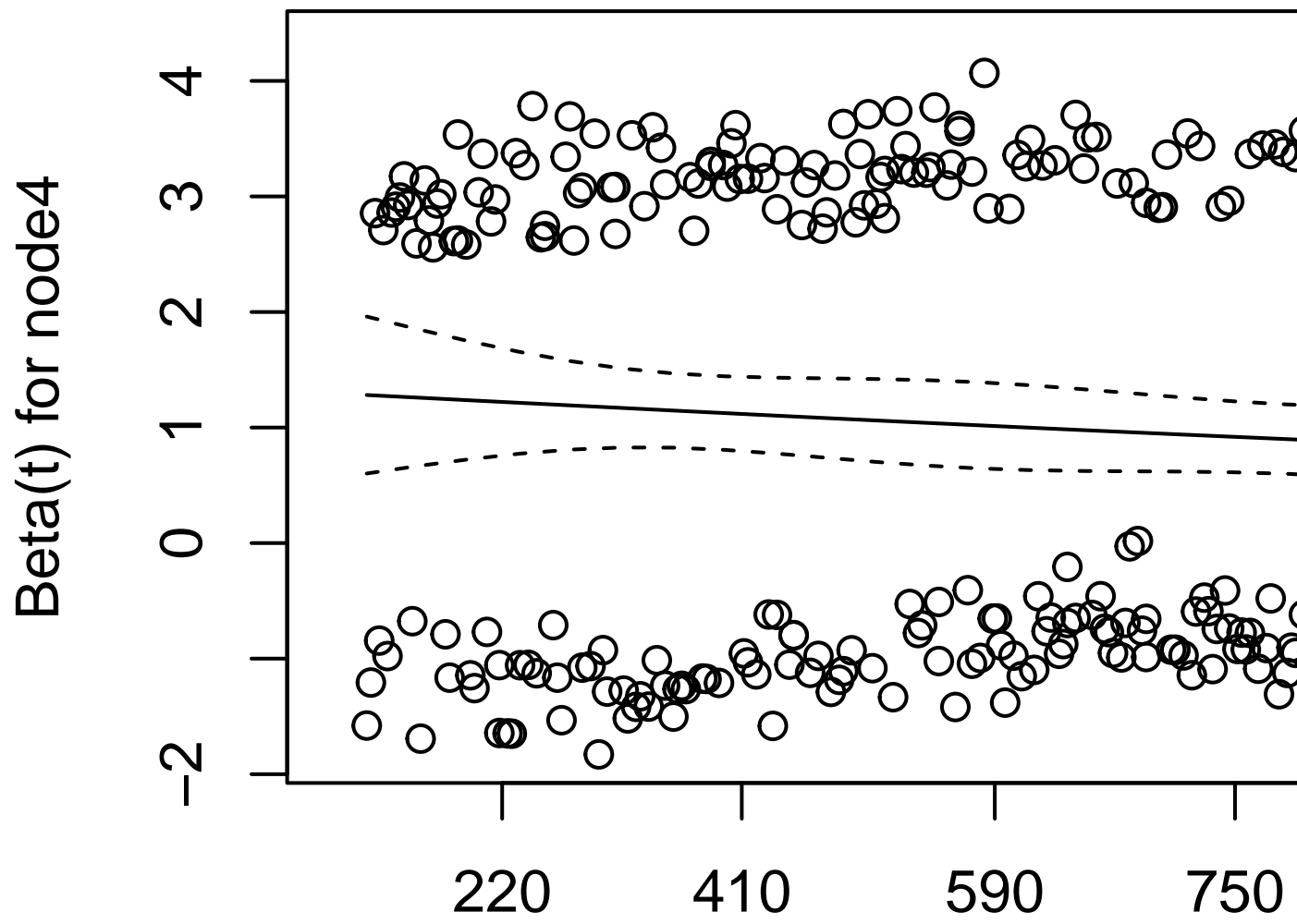












Dealing with proportional hazards violation as a sensitivity Analysis

Stratify by the non-PH variable

In the stratified Cox model: - The cox model is estimated separately in each stratum - Draw-back: we cannot quantify the effect of the stratification variable on survival (i.e., no coefficient will be estimated).

Because these variables are not primary factors of interest we can control for them using stratification. The resulting estimated hazard ratios and 95% confidence intervals are presented in Table 3. As can be seen, the proportional hazards assumption is met in this model.

```
mvModelStratified <- coxph(Surv(time, status) ~ rx + strata(obstruct) + adhere + strata(diff  
cox.zph(mvModelStratified)
```

```
#>          chisq df    p  
#> rx          2.24767  2 0.33  
#> adhere      1.50847  1 0.22  
#> surg         0.00211  1 0.96  
#> GLOBAL      3.87358  4 0.42
```